An Investigation of the Thermal Expansion Coefficient for Resin Concrete with ZrW$_2$O$_8$

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Abstract: This paper presents a novel resin concrete obtained by adding cubic zirconium tungstate (ZrW$_2$O$_8$) as filler. A prediction algorithm on the thermal expansion coefficient (CTE) of resin concrete (including filler) was established on the basis of the meso-mechanics method and a three-phase model for concrete. The concept of twice mixing was also proposed for prediction accuracy. Then, a 2D and 3D irregular polygon aggregate particles packing model was set up by Matlab and the properties of the packing model were simulated by finite element analysis. Finally, resin concrete samples were made and their CTE were measured. Mix proportion and addition of ZrW$_2$O$_8$ as influencing factors were considered in this experiment. The CTE of resin concrete was verified by comparing results of the prediction model, simulation model and experiment. The optimum CTE obtained from the experiment was 1.504 × 10$^{-6}$/K. Compared with 6.817 × 10$^{-6}$/K without ZrW$_2$O$_8$, it was found that the addition of ZrW$_2$O$_8$ to resin concrete can make it perform significantly better in thermal expansion.

Keywords: resin concrete; ZrW$_2$O$_8$ powder; thermal expansion coefficient; prediction model; irregular polygon model
1. Introduction

Nowadays, ultra-precision machining technology is developing towards the scales of micron, submicron and nano. Therefore, traditional cast iron machine tools can hardly satisfy the needs of actual application. The idea of using resin concrete as a bed material emerges for solving this problem. It is a kind of composite material that is mainly composed of aggregates of different sizes and liquid organic resin which hardens through polymerization reaction. Due to its outstanding properties such as high strength, excellent vibration attenuation and thermal stability, resin concrete attracts considerable attention.

Thermal deformation plays a vital role in the appearances of manufacturing errors. Aiming at special demand of ultra-precision computer numerical control (CNC) machine tool for high thermal stability, negative thermal expansion (NTE) material is urgently needed. It contracts upon heating within a certain range of temperature rises and adding NTE material can make the composite in CTE change. Cubic Zirconium Tungstate (ZrW$_2$O$_8$) exhibits strong, isotropic NTE behavior in a wide temperature scope from 0.3 K to 1050 K. Kofteros [1] conducted an experiment of CTE of cement by adding ZrW$_2$O$_8$. The experiment results showed addition of ZrW$_2$O$_8$ played a vital role in reduction of CTE. By finite element analysis, Yilmaz [2] studied thermal mismatch stresses of a Cu-ZrW$_2$O$_8$ composite. Hence, we consider that the addition of ZrW$_2$O$_8$ can have a great effect on the thermal ability of resin concrete. The use of ZrW$_2$O$_8$ in concrete contributes in providing new advanced composites.

Numerous analytical approaches aiming at effective CTE prediction has been studied extensively in the literature. Turner [3] assumed that inner material does not exhibit internal stress at initial temperature and the CTE has no relation with the shape and size of the inclusions. It is also assumed that the components only bear isostatic pressure and the dimensional changes of the components and the macro composite material in terms of temperature occur at the same rate. In this model, the CTE of composites depends on volume fraction and bulk modulus of each component. Although this model is in accord with experimental results on some composite systems, deviations can also be observed because of the model assumption [4]. Considering internal boundaries of composites and shear effects between phase boundaries, Kerner’s model is widely applied for CTE prediction [5]. The derivation process is based on self-consistent algorithms. In this model, shear modulus of the matrix has an effect on the CTE of composites. This model completely accords with a linear correlation between the CTE of the components and volume fraction of each component [6]. Schapery [7] further developed the prediction model and studied bounds on effective CTE of composite materials made up of isotropic phases based on thermo-elastic principles. Upper and lower bounds can be obtained based on the Hashin-Shtrikman [8] model.

There are also many studies related to the CTE of concrete. Hulsey [9] investigated the effect of age, moisture content and mix proportion on concrete CTE. Venecanin [10] explored the influence of aggregate of low CTE to the whole CTE. Sellevold [11] held that moisture has a big impact on the CTE and proved it. Wyrzykowski [12] considered that superabsorbent polymers (SAP) can suppress the negative effect of self-desiccation which leads to increase of the CTE. In recent years, some scholars [13–15] have developed prediction models for CTE of concrete. Many aspects, such as volume fractions of aggregate, elastic moduli of components, and aggregate type, were investigated to analyze their effects on concrete CTE. However, up to now there is no special model or theory for the
CTE of resin concrete. Experiments of the CTE of resin concrete were conducted by Kim [16] and Haddad [17]. Nonetheless, adding ZrW2O8 as filler to resin concrete has never been taken into account.

In order to reduce the CTE of resin concrete, we have tried to conduct research from three aspects: the first, making a prediction model; the second, establishing an irregular polygon aggregate particles packing model; the last, conducting experiments.

2. Prediction of the CTE of Resin Concrete Made by Adding ZrW2O8 Powders

The fillers used in the paper are $\alpha$-phase of ZrW2O8 powders and the average particle size is 250 mesh. Mesh is the number of meshes per unit length (1 inch in Tyler standard screen scale), which can indicate mesh size. Two hundred and fifty mesh is about 58 $\mu$m. There is obvious difference between quartz sand and ZrW2O8 powders in aggregate gradation. Therefore, ZrW2O8 powders (fillers) are mixed with resin binder initially (first mixing). Then, the mixtures generated in the previous step are mixed with quartz sand (aggregates) (second mixing). Through the process of “first mixing” and “second mixing”, the finished product can be obtained. Cement particle size of common cement mortar is rarely more than 80 $\mu$m. Because the maximum particle size of ZrW2O8 powders is 61 $\mu$m, the mixing process of resin binder and ZrW2O8 powders is just similar to that of water and cement flour. The descriptions of resin binder, ZrW2O8 and quartz sand are shown in the following sections.

2.1. First Mixing

ZrW2O8 powders and resin binder are mixed. Denoting $c_1$ and $(1-c_1)$ are the volume fractions of ZrW2O8 and resin binder in concrete, respectively. Let $E_\alpha$, $\mu_\alpha$, $\alpha_0$ be the Young’s modulus, Poisson’s ratio and CTE of the resin binder as matrix and $E_i$, $\mu_i$, $\alpha_i$ those of the ZrW2O8 powders as fillers. Model-A and Model-B are two different computing methods of CTE for determining the interactions between components of resin concrete. Filler strain is approximately equal to the CTE $\alpha_i$ of isolated filler embedded in an infinite matrix under the constraint of matrix without considering the interactions between ZrW2O8 powders and between matrix and ZrW2O8 powders. It is named Model-A of “first mixing”. Thus, the CTE $\alpha_i^*$ of the mixtures can be given by [18]:

$$\alpha_i^* = c_i \alpha_i + (1-c_i) \alpha_0$$  \hspace{1cm} (1)

where

$$\alpha_i = \frac{2E_0 - \alpha_0 + E_i}{(1+\mu_0)(1-2\mu_i)}$$  \hspace{1cm} (2)

Due to the dense distribution of fillers, the correlations and interactions between fillers and between the matrix and the filler are under consideration. It is named Model-B of “first mixing”. $G$ represents the macro effective shear modulus of the mixture. Thus, the CTE $\alpha_2^*$ of the mixtures can be given by [18]:

...
\[
\alpha_2^* = \frac{(4\overline{G} + \frac{E_i}{1-2\mu_i})(1-c_1)}{3(1-2\mu_i)} \left( \frac{E_0\alpha_0}{3(1-2\mu_i)} + (4\overline{G} + \frac{E_i}{1-2\mu_i}) \left( \frac{E_0\alpha_1}{3(1-2\mu_i)} \right) \right)
\]

where

\[
\overline{G} = \frac{E_0}{2(1+\mu)} \left[ 1 + \frac{c_1 \left( \frac{E_0E_i}{(1+\mu_0)(1+\mu_i)} - 1 \right)}{1 + (1-c_1) \frac{2(4-5\mu_0)}{15(1-\mu_0)} \left( \frac{E_0E_i}{(1+\mu_0)(1+\mu_i)} - 1 \right) - 1} \right]
\]

As pointed out in [19], a three-phase model is presented for the prediction of Young’s modulus of concrete. The three phases are inclusion, Interfacial Transition Zone (ITZ) and matrix, as shown in Figure 1. The Poisson’s ratio of concrete experiences a smaller change than the shear modulus. Hence, in order to simplify the calculation process and be convenient for engineering applications, the transverse series model is used [20]. Thus, the Poisson’s ratio \( \mu^*_t \) of concrete is approximated by:

\[
\mu^*_t = c_a\mu_a + c_b\mu_b + c_c\mu_c
\]

Where, \( E_a, \mu_a, c_a \) are the Young's modulus, Poisson's ratio and CTE of matrix phase and \( E_b, \mu_b, c_b \) those of ITZ layer and \( E_c, \mu_c, c_c \) those of inclusion. According to [20], \( E_b = 0.3E_a, \mu_b = 0.30 \).

![Figure 1. Three-phase model for concrete with Interfacial Transition Zone (ITZ).](image)

According to the inference result in [19], the Young’s modulus \( E_t^* \) after mixing can be given by:

\[
E_t^* = \frac{k_{11}^a k_{11}^b k_{11}^c + k_{21}^a k_{21}^b k_{21}^c + k_{12}^a k_{12}^b k_{12}^c + k_{22}^a k_{22}^b k_{22}^c}{k_{11}^a k_{11}^b k_{11}^c + k_{12}^a k_{12}^b k_{12}^c + k_{11}^b k_{12}^b k_{12}^c + k_{22}^b k_{22}^b k_{22}^c} (1-2\nu_t)
\]

where

\[
k_{11}^a = 1 - \frac{(1+\mu_a)}{3(1-\mu_a)} c_a, k_{12}^a = \frac{(1+\mu_a)(1-2\mu_a)}{3(1-\mu_a)} c_a, k_{21}^a = \frac{2E_a c_a}{3(1-2\mu_a)}, k_{22}^a = 1 - \frac{2(1-2\mu_a)c_a}{3(1-2\mu_a)}
\]
\[ k_{11}^b = 1 - \frac{(1 + \mu_b) c_b}{3(1 - \mu_b)(c_b + c_c)} \], \[ k_{12}^b = \frac{(1 + \mu_b)(1 - 2 \mu_b) c_b}{3(1 - \mu_b) E_b (c_b + c_c)} \], \[ k_{21}^b = \frac{2 E_b c_b}{3(1 - \mu_b)(c_b + c_c)} \], \[ k_{22}^b = 1 - \frac{2(1 - 2 \mu_b) c_b}{3(1 - 2 \mu_b)(c_b + c_c)} \]

\[ k_i^* = 1, k_2^* = \frac{E}{1 - 2 \mu_c} \] (8)

Therefore, \( \alpha_1^*, \alpha_2^*, E_i^* \) and \( \mu_* \) of the mixture can be solved by Equations (5) and (6).

### 2.2. Second Mixing

Quartz sand and the mixtures after the first mixing process are mixed. Let \( E_2, \mu_2, \alpha_2 \) be the Young's modulus, Poisson's ratio and CTE of the quartz sand as aggregates. Denoting \( c_2 \) and \( 1 - c_2 \) are the volume fractions of quartz sand and resin binder in concrete, respectively. \( \bar{\alpha}_i^{(1)} \) and \( \bar{\alpha}_i^{(2)} \) are the restraint CTE of isolated aggregate embedded in an infinite matrix in “Model-A + Model-A” and “Model-B + Model-A” model, respectively. \( \bar{G}^{(i)} \) is the macro effective shear modulus of the final mixture. Due to the prediction models that are presented in the previous paper, Model-A and Model-B are also available in “second mixing” while replacing ZrW2O8 powders with quartz sand. They are named Model-A of “second mixing” and Model-B of “second mixing”, respectively. Thus, we also have two choices in the second mixing process, so there are four prediction results in all. For instance, “Model-B + Model-A” means that Model-B is used in “first mixing” and Model-A is applied to “second mixing”. These results can be obtained from \( \alpha_i^*, \bar{\alpha}_i, \alpha_i^*, \bar{G} \) by the replacement as shown in Table 1.

### Table 1. Substitution table.

<table>
<thead>
<tr>
<th>Model</th>
<th>Substitute</th>
<th>For</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model-A + Model-A</td>
<td>( \alpha_1^{<em>,(1)}, \alpha_1^{</em>,(1)} )</td>
<td>( \bar{\alpha}_1^{(1)}, \alpha_1^{<em>,(1)}, \alpha_2^{</em>,(1)}, \alpha_2^{*,(1)}, E_0, E_1, \mu_0, \mu_1 )</td>
</tr>
<tr>
<td>Model-B + Model-A</td>
<td>( \alpha_1^{<em>,(1)}, \alpha_1^{</em>,(1)} )</td>
<td>( \bar{\alpha}_1^{(1)}, \alpha_1^{<em>,(1)}, \alpha_2^{</em>,(1)}, E_0, E_1, \mu_0, \mu_1 )</td>
</tr>
<tr>
<td>Model-A + Model-B</td>
<td>( \alpha_2^{*,(1)}, \bar{G}^{(1)} )</td>
<td>( \bar{\alpha}_1^{(1)}, \alpha_1^{<em>,(1)}, \alpha_2^{</em>,(1)}, E_0, E_1, \mu_0, \mu_1 )</td>
</tr>
<tr>
<td>Model-B + Model-B</td>
<td>( \alpha_1^{*,(1)}, \bar{G}^{(1)} )</td>
<td>( \bar{\alpha}_1^{(1)}, \alpha_2^{<em>,(1)}, \alpha_2^{</em>,(1)}, E_0, E_1, \mu_0, \mu_1 )</td>
</tr>
</tbody>
</table>

According to optimum proportion of resin binder to the sum of fillers and aggregates provided by the manufacturer, three mixing compositions used in this study are outlined in Table 2. Results of the prediction formula are shown in Table 3. Sample No.1 is a mixture of resin binder and quartz sand without ZrW2O8 powder. Hence, the mixing process cannot be divided into “first mixing” and “second mixing”. So, “Model-A + Model-B” and “Model-B + Model-A” do not exist. For Sample No.1, “Model-A + Model-A” means that Model-A is used in whole mixing process. Similarly, “Model-B + Model-B” means that Model-B is applied.
Table 2. Comparison of the proportions of three mixing compositions.

<table>
<thead>
<tr>
<th>No.</th>
<th>Subject</th>
<th>Mass ratio</th>
<th>Volume ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Resin binder:quartz</td>
<td>0.073:0.927</td>
<td>0.148:0.852</td>
</tr>
<tr>
<td>2</td>
<td>Resin binder:quartz:ZrW₂O₈</td>
<td>0.066:0.742:0.192</td>
<td>0.148:0.767:0.085</td>
</tr>
<tr>
<td>3</td>
<td>Resin binder:quartz:ZrW₂O₈</td>
<td>0.059:0.597:0.344</td>
<td>0.148:0.682:0.170</td>
</tr>
</tbody>
</table>

Table 3. Results of the prediction formula.

<table>
<thead>
<tr>
<th>No.</th>
<th>CTE ($\times 10^{-6}$/K)</th>
<th>Model A + A</th>
<th>Model A + B</th>
<th>Model B + A</th>
<th>Model B + B</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>9.161</td>
<td>---</td>
<td>---</td>
<td>6.598</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>8.777</td>
<td>3.512</td>
<td>6.158</td>
<td>2.768</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>7.577</td>
<td>2.909</td>
<td>3.403</td>
<td>1.536</td>
<td></td>
</tr>
</tbody>
</table>

---: Result does not exist.

3. Packing Model and Property Simulation

3.1. Establishment of Packing Model

The 2D/3D packing model of resin concrete was established based on relevant knowledge of material meso-structure and meso-mechanics. At least millions of particles exist in a granular pack. Hence, computer performance analysis of powder material is mainly applied to 2D packing models [21]. We consider that 3D model can be obtained by random arbitrary distribution, and then the 2D model is one slice directly captured from the 3D model.

Based on gradation results that we determine, related settings used to simulate packing model of resin concrete are as follows: According to Japan national standard JIS G5901-1974 [22], the aggregate size distribution is 0.076–0.15 mm, 0.15–0.22 mm, 0.22–0.5 mm, 0.5–0.9 mm, 0.9–1.6 mm, 1.6–2.5 mm and 2.5–4 mm, respectively. According to mass fractions of aggregate, the number of all kinds of aggregate is calculated for precision improvement. Detailed aggregates ratio and particle number of each grade are shown in Table 4. Aggregates are packed from the largest to the smallest size in a cube with an $h$ side and $h = 12$ mm. Pores represent resin binder. In order to improve the reality and accuracy of the packing model, this paper adopts the polygonal aggregates model, not the spherical one. The process of establishing 3D microstructure is as follows: (1) Coordinate of sphere center $x(i), y(i), z(i)$ and radius $r(i)$ of each random aggregate are determined for be completely inside the cube and can be given by in Matlab:

$$
\begin{align}
    x(i) &= r(i) + (h - 2 \times r(i)) \times \text{rand()} \\
    y(i) &= r(i) + (h - 2 \times r(i)) \times \text{rand()} \\
    z(i) &= r(i) + (h - 2 \times r(i)) \times \text{rand()} \tag{10}
\end{align}
$$

The generated aggregate is reserved; (2) For newly generated sphere, intersection with other spheres might exist. Hence, interference calculation with generated spheres is carried out in order to determine whether interference exists or not. If it exists, the sphere is deleted; (3) According to the above rules, particles are accumulated grade by grade. For each grade, the volume should meet the need of
aggregate ratio mentioned above; (4) We take \( n \) \((n > 3)\) random points in one sphere. Then, planes are drawn by using three arbitrary points. After drawing, overlapped planes are deleted by Boolean Operation and polygonal aggregate is obtained. To avoid sharp aggregates, all points should not be placed in the same half spherical region.

The filling rate of the 3D model is higher than 85% which satisfies the condition of high density packing, and polygonal aggregates occupy the square area of 85.2% in the 2D model. Therefore, the generated 2D/3D models are given in Figure 2.

### Table 4. Aggregates’ ratio of resin concrete.

<table>
<thead>
<tr>
<th>Particle size (mm)</th>
<th>Mass ratio (%)</th>
<th>Particle number (without ZrW(_2)O(_8))</th>
<th>Particle number (Volume ratio of aggregate: ZrW(_2)O(_8) = 9:1)</th>
<th>Particle number (Volume ratio of aggregate: ZrW(_2)O(_8) = 8:2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.076–0.15</td>
<td>10.586%</td>
<td>117304</td>
<td>105571</td>
<td>93837</td>
</tr>
<tr>
<td>0.15–0.22</td>
<td>9.064%</td>
<td>16088</td>
<td>14478</td>
<td>12871</td>
</tr>
<tr>
<td>0.22–0.5</td>
<td>16.075%</td>
<td>3248</td>
<td>2923</td>
<td>2598</td>
</tr>
<tr>
<td>0.5–0.9</td>
<td>5.891%</td>
<td>424</td>
<td>381</td>
<td>339</td>
</tr>
<tr>
<td>0.9–1.6</td>
<td>19.626%</td>
<td>320</td>
<td>288</td>
<td>256</td>
</tr>
<tr>
<td>1.6–2.5</td>
<td>16.871%</td>
<td>40</td>
<td>36</td>
<td>32</td>
</tr>
<tr>
<td>2.5–4</td>
<td>21.887%</td>
<td>16</td>
<td>14</td>
<td>12</td>
</tr>
</tbody>
</table>

**Figure 2.** 3D and 2D particles packing model in Matlab.

### 3.2. Finite Element Analysis on CTE

Ansys Mechanical APDL 14.5 is used to analyze CTE of 2D packing model with the side length of 12 mm. We import data of aggregate particles from Matlab R2012a and select plane13 element. The material parameters of resin concrete in the model are listed in Table 5. The mesh generation is automatic and sparse degree of mesh is controlled by SMRTSIZE function. Considering accuracy and precision of calculating, parameter SMRTSIZE is set at 3. A mesh convergence study is performed. As for boundary condition, as thermal deformation belongs to 2D nonlinear analysis, it is necessary to restrain X-direction freedom of all points on the bottom line for ensuring full deformation of the entire material in the Y-direction. Simulating the ambient temperature range from 20 °C to 140 °C, the CTE of the 2D model through the change of temperature can be obtained.
Table 5. Properties of constituents.

<table>
<thead>
<tr>
<th></th>
<th>Density ($\times 10^3$Kg/m$^3$)</th>
<th>Young’s modulus (GPa)</th>
<th>Poisson’s ratio</th>
<th>CTE ($\times 10^{-6}$/K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Resin binder</td>
<td>1.0</td>
<td>3.5</td>
<td>0.38</td>
<td>55</td>
</tr>
<tr>
<td>Granite</td>
<td>2.65</td>
<td>31</td>
<td>0.22</td>
<td>4.6</td>
</tr>
<tr>
<td>Quartz sand</td>
<td>2.20</td>
<td>79</td>
<td>0.17</td>
<td>0.55</td>
</tr>
<tr>
<td>ZrW$_2$O$_8$</td>
<td>5.09</td>
<td>82</td>
<td>0.342</td>
<td>$-8.6$</td>
</tr>
</tbody>
</table>

With reference to Figure 3, the displacements of C relative to A and D relative to B are 0.0197 mm and 0.0164 mm at Y-direction, respectively. According to constraint load conditions and formulas of CTE, the ratio of distance change of AC/BD to length of AC/BD is CTE of resin concrete owing to change in unit temperature. The aggregate uses granite. Due to the simulated temperature range from 20 °C to 140 °C, $\frac{0.0197-0}{12} \times \frac{1}{140-20} = 1.36 \times 10^{-5}$/K, $\frac{0.0164-0}{12} \times \frac{1}{140-20} = 1.17 \times 10^{-5}$/K. Therefore, the average CTE of resin concrete is $12.7 \times 10^{-6}$/K and approximate closely to $12 \times 10^{-6}$/K in [16]. It indicates that this model has high accuracy.

Figure 3. Thermal deformation of resin concrete under constraint condition. AC and BD are dimensions of left side and right side of model, respectively.

The filler of resin concrete is ZrW$_2$O$_8$ and the aggregates constitute quartz sand in this paper. According to three situations of experimental design in Table 2, thermal deformation and the simulation results are shown in Table 6.

Table 6. Simulation results of three samples.

<table>
<thead>
<tr>
<th>No.</th>
<th>AC(mm)</th>
<th>BD(mm)</th>
<th>CTE($\times 10^{-6}$/K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.0102</td>
<td>0.0085</td>
<td>6.493</td>
</tr>
<tr>
<td>2</td>
<td>0.00424</td>
<td>0.00366</td>
<td>2.743</td>
</tr>
<tr>
<td>3</td>
<td>0.00306</td>
<td>0.00272</td>
<td>2.007</td>
</tr>
</tbody>
</table>
4. Experimental Program

4.1. Materials

Epoxy resin and curing agent used in this experiment were supplied by The Huntsman Corporation. ZrW$_2$O$_8$ powders were supplied by Kunming Titan Advanced Materials Co., ltd. GY 250 is typical bisphenol A epoxy resin with high viscosity. ARADUR 3225 was applied as curing agent that is suitable to GY 250. There is no need for adding diluent because GY 250 has been diluted before it is sold. The aggregate is high grade quartz sand with a purity of 99.5%. The aggregate size distribution and aggregates ratio is the same as the packing model aforementioned. ZrW$_2$O$_8$ with a purity of 99.5% was used as filler to improve the thermal stability of resin concrete.

The moulds were 1000 mL beakers. Release agent was coated on the surface of the beakers beforehand in order to demould easily. First, each grade of aggregates was put in successively and mixed evenly. Second, resin and curing agent were measured with measuring cylinder and stirred uniformly, then resin binder was mixed with aggregates thoroughly and stirred in a plastic bucket manually. If ZrW$_2$O$_8$ was added to resin concrete, there were some changes in the manufacturing process. ZrW$_2$O$_8$ powders after measuring and resin binder were mixed first. Then, after stirring for 5 min by hand, the mixture and aggregates were mixed and stirred in the plastic bucket. The mixture was rolled in the rotary mixer (motor model: Y90L-6; speed: 910 r/min) for about 0.5 hour so that it blended well and compacted in the moulds. Finally, we placed it under indoor temperature conditions for 24 hours and demoulded it after curing. The production process diagram is shown in Figure 4. Test samples of 50 × 25 × 10 mm$^3$ were obtained after finished products were machined on a machine tool.

![Figure 4. The production process of resin concrete.](image)

4.2. Experimental Technique

A strain gauge was attached to a measured sample that is connected to a bridge arm of a Wheatstone bridge. The entire circuitry is shown in Figure 5.
As the gauge produces expansion because of temperature change, the resistance of the gauge is changed accordingly [23]. The output voltage \( V_{\text{out}} \) between points a and b of the bridge can be given by:

\[
V_{\text{out}} = \left[ \frac{V_{\text{in}}}{(R + R_g)} \right] R_g - \left[ \frac{V_{\text{in}}}{(2R)} \right] R
\]

where \( V_{\text{in}} \) is the voltage applied to the bridge, \( R_g \) is the resistance of the strain gauge, \( R_k = R_s = R \). When \( R_g = R \), the output voltage of the bridge is zero.

The CTE of the sensitive gate \( \alpha_e \) can be given by:

\[
\alpha_e = 4V_{\text{out}} / (KV_{\text{in}} \Delta T) + \alpha_g'
\]

where \( K \) is the sensitivity coefficient of the strain gauge, \( \Delta T \) is the temperature change of the sample, \( \alpha_g' \) is the CTE of the gauge material.

The strain gauge BX120-30AA consists of constantan foil as sensitive gate material and phenolic as substrate material. It was supplied by Taizhou Huangyan Juxing Testing Instrument Factory. The other two bridge arms were fixed resistance value and \( R = 120 \Omega \). The variable one consisted of a 1000-\( \Omega \) potentiometer in series with a 2400-\( \Omega \) resistor and a 160-\( \Omega \) resistor in parallel for zero adjustment. The temperature coefficient of resistance of these resistors is less than 25 ppm and their accuracy is no more than 0.05%. According to error analysis, the error is very little and can be ignored. With the temperature increases, the output voltage can be measured by a digital multimeter HP34401A. The sample and the Platinum resistance of temperature measurement equipment LS-1100 produced by Tianjin Overblue Technology Development Co., ltd were placed in incubator.

4.3. Experimental Results

Quartz glass sample was attached to the strain gauge in order to get \( \alpha_g' \). The CTE of quartz glass \( \alpha_e \) is \( 0.5 \times 10^{-6}/\text{K} \) and \( V_{\text{in}} = 1.400V \). When the temperature rose from \( T_1 = 18 \degree \text{C} \) to \( T_2 = 60 \degree \text{C} \) and the output voltage was stable, \( V_{\text{out}} = -0.342\text{mV} \),

\[
\alpha_g' = \alpha_e - 4V_{\text{out}} / (KV_{\text{in}} \Delta T) = 11.579 \times 10^{-6} / \text{K}
\]
where the sensitivity coefficient of the gauge $K=2.10$.

The three different samples were measured in turn. $V_{out}$, $\Delta T$ obtained and $\alpha_g$ were substituted in Equation (11), respectively, and the results are outlined in Table 7.

<table>
<thead>
<tr>
<th>Sample number</th>
<th>$V_{out}$ (mV)</th>
<th>$\alpha_g \times 10^{-6}$/K</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>−0.147</td>
<td>6.817</td>
</tr>
<tr>
<td>2</td>
<td>−0.269</td>
<td>2.885</td>
</tr>
<tr>
<td>3</td>
<td>−0.311</td>
<td>1.504</td>
</tr>
</tbody>
</table>

5. Results and Discussion

In order to facilitate the discussion, the experimental data of Table 3, Table 6 and Table 7 are all shown in Figure 6. As seen in Figure 6, it might be concluded that the prediction equation of “Model-B + Model-B” and the irregular polygon model has higher accuracy because the broken lines of “Model-B + Model-B”, simulation and experiment match well with each other. For “Model-A + Model-A”, “Model-A + Model-B” and “Model-B + Model-A”, there are obvious deviations due to neglecting interactions between components. The addition of ZrW$_2$O$_8$ can significantly reduce the CTE of resin concrete. Sample No.3 has lower CTE than the other two samples. The volume ratio of aggregate to ZrW$_2$O$_8$ powders is an important factor which influences the concrete CTE.

![Figure 6. Comparison between prediction, simulation and experimental results.](image)

6. Conclusions

In this paper, the influence of addition of ZrW$_2$O$_8$ to resin concrete was investigated. A prediction algorithm on CTE of resin concrete (including filler) was established on the basis of the meso-mechanics method and a three-phase model for concrete. Four CTE computational models were deduced based on the consideration of interactions between inclusions and the effect, if any, of...
inclusions on the matrix and the twice mixing method. A 2D and 3D irregular polygon aggregate particles packing model was set up and the concrete CTE was analyzed by the finite element method. From the experiment, it was found that the addition of ZrW$_2$O$_8$ to resin concrete showed appreciable reduction in thermal expansion and mix proportion had an effect on CTE. By comparing all the results, the irregular polygon model was found to have very high simulation precision. The computational model of “Model-B + Model-B” has higher precision than the other three models. It proves that the accuracy of models can be improved effectively when considering interactions between components of resin concrete. The optimum CTE obtained was $1.504 \times 10^{-6}/\text{K}$ when the volume ratio of aggregate to ZrW$_2$O$_8$ powder was 8:2.

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Author Contributions

Establishment of models and simulation: Shuang Qiu; Performing the experiment: Kuangzhe Lin; Drafting of manuscript: Kuangzhe Lin, Shuang Qiu; Critical revision: Bin Lin, Yuguo Wang; Planning and supervision of the research: Bin Lin.

Conflicts of Interest

The authors declare no conflict of interest.

References


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