Recent Advances in Ultrafast Structural Techniques

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Abstract: A review that summarizes the most recent technological developments in the field of ultrafast structural dynamics with focus on the use of ultrashort X-ray and electron pulses follows. Atomistic views of chemical processes and phase transformations have long been the exclusive domain of computer simulators. The advent of femtosecond (fs) hard X-ray and fs-electron diffraction techniques made it possible to bring such a level of scrutiny to the experimental area. The following review article provides a summary of the main ultrafast techniques that enabled the generation of atomically resolved movies utilizing ultrashort X-ray and electron pulses. Recent advances are discussed with emphasis on synchrotron-based methods, tabletop fs-X-ray plasma sources, ultrabright fs-electron diffractometers, and timing techniques developed to further improve the temporal resolution and fully exploit the use of intense and ultrashort X-ray free electron laser (XFEL) pulses.

Keywords: femtosecond X-ray diffraction; femtosecond electron diffraction; synchrotron radiation; laser slicing; X-ray plasma sources; X-ray free electron lasers; XFEL; ultrafast structural dynamics; ultrafast imaging; ultrafast diffraction

1. Introduction

The present review article summarizes some of the key advances in the development of ultrafast structural techniques over the last decade. Pioneering experiments including a historical compilation can be found elsewhere [1–7]. After more than 30 years of continuous improvements in femtosecond (fs, 1 fs = 10\(^{-15}\) s) hard X-ray and fs-electron sources, ultrafast diffractometers confer the prerequisite spatial and temporal resolutions to capture atoms in motion. The characteristic length-scale that such ultrafast cameras had to resolve is evident—this is the size of an atom or a bond length \((d_c) \approx 1 \text{ Å} = 10^{-10} \text{ m} = 0.1 \text{ nm}\). In order to determine their necessary shutter speed or temporal resolution, however, one must assume a characteristic speed \((v_c)\) for atomic motion. There are faster and slower processes in nature but as a general rule of thumb, \(v_c \approx 10^3 \text{ m/s} = 1 \text{ nm ps}^{-1}\) (1 ps = 10\(^{-12}\) s), which is roughly the speed of sound in most solid-state organic materials and liquids results a good estimate [8]. Note that structural chemists, biologists, and condensed matter physicists are usually interested in rather low-frequency, high-amplitude atomic displacements. Soft vibrational modes are those that govern chemical reactivity through the anharmonicities encountered along the potential energy landscape as we approach the bond dissociation threshold or the transition state [9]. Protein function, on the other hand, seems to rely on collective low-frequency vibrational modes that couple to large amplitude protein motions for which thermal bath fluctuations and entropic factors play key roles (vide infra examples in Sections 2.4.2 and 2.4.3). In addition, very interesting condensed matter physics arises from low-frequency collective excitations (vide infra examples in Sections 2.1, 3.5 and 3.6). Two examples are the famous amplitude phonon mode (known as amplitudon) that modulates the charge density wave (CWD) gap in Peierls distorted systems, [10] and the lattice...
vibrations responsible for the formation of Cooper pairs that lead to the foundation of the BCS theory for superconductivity [11]. Thus, a characteristic time ($\Delta t_c$) or temporal resolution of about $\Delta t_c = d_c v_c^{-1} = 0.1 \text{ nm} \cdot (1 \text{ nm ps}^{-1})^{-1} = 0.1 \text{ ps} = 100 \text{ fs}$ suffices to monitor a vast variety of structurally relevant phenomena.

Ultrafast diffraction belongs to a family of techniques known as pump-probe in which two well-synchronized pulses, a pump and a probe, are implemented. The pump is a fs-optical pulse coming from a master fs-laser and is responsible for initiating structural changes by bringing the system out of equilibrium. The probe is an ultrashort X-ray or electron pulse, which scatters off the irradiated sample volume to generate a diffraction pattern downstream. A series of diffraction patterns obtained for different time delays ($t$) between these two pulses is then recorded in a stroboscopic fashion. Structural refinement finally brings time-dependent changes in diffracted intensities to real-space information to render a “molecular movie” that unveils details about electron density and nuclear reorganization. The success of ultrafast structural dynamics, therefore, relies on the ability of producing ultrashort hard X-ray pulses or electron bursts as well as maintaining an outstanding synchronization between probe and pump pulses. Recall these are repetitive stroboscopic experiments so both the durations of the pump and probe pulses and their relative timing are vital factors in addition to source brightness. The synchronization noise is referred to as timing jitter and has been one of the key issues when radio frequency (RF) fields are utilized for accelerating or compressing electron bunches.

It should be noted that a good source of intense electron bursts is not only the heart of any time-resolved electron diffractometer, but also the first component required to generate hard X-ray pulses at synchrotron and X-ray free electron laser (XFEL) facilities. Furthermore, RF technology is fundamental to operate electron injectors, linacs (linear accelerators), boosters, and storage rings. Thus, circumventing the problem of the timing jitter between the driving fs-laser and RF fields has been essential to the success of ultrafast structural experiments performed with both RF-based fs-electron diffraction (FED) setups (vide infra Sections 3.6 and 3.7) and XFELs (vide infra Section 2.5). A brief description of the main techniques that enabled monitoring atomic motion with the aforementioned time resolution of ~100 fs is highlighted in the application-based examples which follow.

2. Structural Techniques Involving Ultrashort X-ray Pulses

2.1. Laser Slicing at Third-Generation Synchrotron Facilities

Synchrotron radiation continues to be one of the most powerful sources of polychromatic light capable of covering a wide spectral range that extends from THz to hard X-rays [12]. Depending on the facility, type of insertion device, beam optics, and required degree of monochromaticity; X-ray fluxes at synchrotrons typically range from about $10^4$ to $10^8$ photons/pulse (at the sample position). Moreover, photon energies >6 keV (photon wavelengths <2.1 Å) are often required in order to attain atomic spatial resolution. The temporal resolution of synchrotron sources is dictated by the length (duration) of the stored electron bunch, which commonly ranges from 50 ps to 200 ps (fwhm, full width at half maximum) [13,14].

Laser slicing techniques [15–22] enabled the production of ~100 fs (fwhm) hard X-ray pulses at third-generation synchrotron facilities such as the Advanced Light Source (ALS) and the Swiss Light Source (SLS). Figure 1 illustrates the laser slicing principle originally proposed by Zholents and Zolotorev [16] and demonstrated by Schoenlein et al. [15] at ALS. Here, an intense fs-laser pulse with a field strength of $-10^9 \text{ V m}^{-1}$ co-propagates with the stored electron bunch through a wiggler. Under optimal resonant conditions, the high laser peak intensity introduces an energy modulation in the underlying electrons of several MeV. This energy modulation is much larger than the energy spread of the unperturbed electrons in the bunch and, therefore, energy-modulated electrons can be transversely separated from the main beam through the implementation of a bending magnet, and subsequently used to produce fs-X-ray pulses in another bend. Finally, an aperture is applied to select one of the spatially separated fs-X-ray pulses, which then can be used for probing the ultrafast
structural changes. Note that timing jitter here is negligible since the electron beam modulation (or fs-X-ray pulse) and the photoexcitation pulse originate from the same initial laser pulse via beam splitters. All pulse durations below are given in fwhm if not stated otherwise.

![Figure 1. Schematic of the fs-laser slicing method for generating fs-hard X-ray pulses at ALS.](image)

Figure 2 shows recent results obtained by Huber et al. [20] at the FEMTO slicing facility of SLS for the prototypical Peierls 1D charge-density wave (CDW) system, $K_{0.3}MoO_3$. The amplitudon in this material has a frequency (period) of 1.7 THz (590 fs) [23] at $T \approx 0$ K. Fs-X-ray diffraction experiments were performed in a grazing incidence geometry while the $K_{0.3}MoO_3$ single crystalline sample was maintained well below $T_c$. The crystal was excited by 100-fs laser pulses centered at $\lambda = 800$ nm and probed by 80-fs X-ray pulses with $\lambda = 1.8$ Å. The relative intensity changes of the (1 3.252 0.5) reflection of the superlattice lattice (SL) were measured as a function of $t$ (delay) at various photoexcitation fluences (Figure 2a). Results were modeled (Figure 2d) by implementing an equation of motion derived from a double-well potential (Figure 2b). Huber et al. [20] were able to observe the coherent lattice dynamics associated with the CDW formation. The authors interpreted the results as a rearrangement (atomic motion) of the SL distortion evolving along a generalized excitation-dependent potential energy surface. Their observed recovery of the SL distortion remains unclear. The results presented in Figure 2 reflect typical measurements that should be performed in order to extract valuable physical information from time-dependent diffraction data; i.e., many time points as well as different photoexcitation levels are usually required. Thus, depending on the probed volume, diffraction efficiency, and X-ray beam brightness, several weeks of continuous data collection may be necessary. In addition, sample degradation may introduce additional challenges during extensive data acquisition. Laser slicing enabled the generation of fs-X-ray pulses in synchrotrons at the expense of lowering the X-ray beam flux to about $10^2$–$10^3$ photons/pulse, which is comparable to the effective brightness of a fs-hard X-ray plasma source (see below).
Figure 2. Results from FEMTO line (laser slicing) at the Swiss Light Source (SLS). (a) Time evolution of the normalized SL diffraction peak intensity at different excitation fluences (F). The horizontal dashed line in the higher fluence scan represents saturation background. Solid lines in red are fits obtained by implementing an equation of motion derived from a double-well potential that includes a phenomenological damping term. They grey vertical line denotes the time at which the SL diffraction intensity recovers and peaks, $t = 0.35 \text{ ps}$. (b) Double-well potential; the grey potential corresponds to the unperturbed charge-density wave (CDW) state ($\eta = 0$). Note that $\eta$ is a scaled excitation parameter proportional to $F$ so that $\eta = 1$ corresponds to the threshold value for overshooting, i.e., where the double-well shape of the potential vanishes (red curve). The green circle represents the collective atomic displacement of the SL distortion or dimmers along the structural coordinate of the Peierls distortion. The transient quasi-equilibrium position after excitation is labeled $X_{\text{eq}}$. (c) Schematic of the inhomogeneously excited crystal in the case of a high fluence excitation that leads to $\eta_0 > 1$, the $z$ axis corresponds to the axis perpendicular to the surface plane; $\delta_L$ corresponds to the laser penetration depth. (d) Simulated diffraction signals of a thin layer for certain values of $\eta$. Reproduced from Reference [20] with permission from the American Physical Society (APS).

In addition to laser slicing, the operation of synchrotrons in the low alpha mode has also allowed the production of low-intensity X-ray pulses as short as 0.6 ps (rms, root mean square) [24]. There is a legitimate need for attaining ultrashort as well as ultrabright hard X-ray and electron pulses. Generally speaking, excitation fluences must be sufficiently high to transform at least 1% of the molecules (or unit cells) in order to discern structural changes from background signals and a very limited number of materials are able to survive multiple excitation cycles; metals such (Al, Au,
etc.), semiconductors (Si, GaAs, InSb), ceramics and ceramic-like materials (Al$_2$O$_3$, ZnO, YBCO, etc.) are some typical examples. However, radiation labile specimens such as organic compounds and biomolecular systems only allow for a very limited number of pump shots before showing clear signs of degradation. At such excitation intensities, thermal effects, long-lived photochemical intermediates and photoproducts alter the specimen structure.

2.2. Table-Top fs Hard X-ray Plasma Diffractometers

Table-top fs-X-ray plasma diffractometers have been successfully implemented to unveil ultrafast structural dynamics in different materials [25–39]. These time-resolved instruments are based on the use of chirped-pulse amplification [40] with pulse energies in the range of 1–100 mJ depending on the repetition rate of the laser and the average power. Fs-hard X-ray pulses are produced when a solid target is irradiated by fs-laser pulses carrying a peak intensity $I_{\text{peak}} > 10^{16} \text{ W cm}^{-2}$. The generation of fs-X-ray pulses from a plasma source involves the extraction of electrons from the metal target by strong field ionization with a small laser spot. This step is followed by electron acceleration in vacuum and electron re-entrance into the target material owing to the strong electric field. Then, X-ray photons are generated via collisional inner-shell ionization followed by radiative transitions of outer-shell electrons into inner-core holes. Such processes occur every cycle of the electric field of the fs-laser driving pulse.

The source is the main challenge in the design of table-top fs-X-ray plasma diffractometers. The surface of the target material is ablated after each laser shot and, therefore, it must be translated to preserve surface uniformity. Cu tape of about 20 µm in thickness is often utilized as target material producing the characteristic Cu K$_\alpha$ and K$_\beta$ X-ray emission lines. The emission of X-ray photons is highly isotropic (all directions). Hence, the implementation of X-ray optics becomes crucial to obtain a decent photon flux at the sample position. The schematic of a table-top fs-X-ray plasma diffractometer is shown in Figure 3. The X-ray source is driven by 50-fs laser pulses with a central wavelength, $\lambda = 800$ nm. After losses associated with X-ray collection, this instrument delivers at the sample position an effective X-ray photon flux of 5000 Cu K$_\alpha$ photons/pulse with a repetition rate of 1 kHz [38].

![Figure 3. Layout of the table-top fs-X-ray plasma diffractometer at the Max Born Institute.](image)

In this example, a (1 1 1)-oriented single crystalline (SC) Bi sample is photoexcited by 400-nm laser pulses generated by frequency doubling in a β-barium borate (BBO) crystal. The pump arm is mechanically chopped. A photodiode (PD) is used to determine the state of the sample (i.e., excited or unexcited) on shot to shot basis. Diffracted X-ray photons are measured by an energy-resolving CdTe diode (Amptek). The inset shows a spectrum with a very low X-ray flux on the detector. Figure adapted from Reference [38] with permission from the authors.
Figure 4 illustrates some representative measurements obtained by Freyer et al. [39] with the table-top fs-X-ray plasma diffractometer shown in Figure 3 but in a different configuration to perform experiments in transmission geometry (i.e., these measurements required the implementation of a large area high-resolution detector). Freyer et al. [39] studied a polycrystalline sample of \([\text{Fe(bpy)}_3]^2+ (\text{PF}_6^-)_2\). The authors were able to determine the electron density changes that follow a charge transfer reaction (Figure 4g–h). Recall that X-ray photons scatter off the electron density, i.e., they interact with the electron cloud and, therefore, variations in diffracted intensities (Figure 4b–f) correspond to changes in electron density arising from charge redistribution and/or nuclear rearrangements. Freyer et al. [39] carried out a careful analysis of the electron density maps that applies to centrosymmetric crystals under relatively low excitation fluence. The authors found that each photoexcited complex largely affects its surroundings, highlighting the many-body character of this charge transfer. They concluded that the PF6− counterions play a key role in charge relocation with a behaviour in the solid state that is markedly different from that in diluted liquid solutions where the spatial separation among solvated anions and cations is much larger. Similar anionic effects were found in \((\text{EDO-TTF})_2\text{PF}_6\) by Gao et al. [41] through the implementation of FED.

![Figure 4. Results from the above table-top fs-X-ray plasma source.](image)

More recent efforts in the development of fs-hard X-ray plasma sources driven by mid-infrared (mid-IR) lasers demonstrated an increase in brightness of about 25 times [42]. The emission efficiency of X-ray photons increases with the kinetic energy of the re-entering electron, which is proportional to \(I_{\text{peak}} \lambda^2\). Thus, the application of intense fs-mid-IR lasers may bring the effective brightness of table-top fs-hard X-ray diffractometers to the level of \(\sim 10^5\)–\(10^6\) photons/pulse (at sample position). This is about one order of magnitude below the flux achieved at the Sub-Picosecond Photon Source (SPPS) [43]. SPPS was a test facility that operated at the Stanford Linear Accelerator Center (SLAC) before the
Linac Coherent Light Source (LCLS) became available in 2009 (see section below). In addition to the above, fs-mid-IR drivers have been recently applied for the generation of coherent ultrahigh harmonics in gases reaching keV-photon energies [44,45]. Although high harmonic generation (HHG) is not yet an alternative for the production of fs-hard X-ray pulses for coherent diffraction, HHG sources with photon frequencies between the vacuum UV and soft X-ray regime have found applications in fs-spectroscopies and attosecond (att, 1 att = 10^{-18} s) metrologies [44–65].

2.3. Introduction to Fourth-Generation Fs-Hard X-ray Sources: X-ray Free Electron Lasers

Since the first ultrabright shot of fs-hard X-rays at LCLS in 2009, four additional XFEL user facilities [66–71] became operational: SACLA (Japan, 2011), PAL-XFEL (Korea, 2016), SwissFEL (Switzerland, 2016), and EuXFEL (Germany, 2017). Figure 5 shows the schematic of SACLA. In an XFEL, ultrabright electron bunches are created in an RF-photoinjector or a DC electron gun and accelerated by a linac to kinetic energies that normally range from 5 GeV to 15 GeV (up to 17.5 GeV at EuXFEL). As the case of synchrotrons, the duration of the X-ray pulses corresponds to the length of the electron bunches in the undulator. Magnetic chicanes are commonly used to compress the electron bursts before they arrive to the undulator. Depending on the electron bunch charge, X-ray pulses with typical lengths ranging from 5 fs to 400 fs can be readily obtained via self-amplified spontaneous emission (SASE), and even Fourier limited X-ray pulses through the implementation of self-seeding [72]. In addition, sub-fs X-ray pulses are also attainable by selectively spoiling the transverse emittance of the electron beam [72,73]. With up to ~10^{13} X-ray photons/pulse XFELs produce peak fluxes which are about 10^{4–10^{5}} times brighter than synchrotrons. Perhaps the only disadvantage of XFELs over synchrotrons is the fact that each electron bunch in an XFEL experiences a single pass before hitting a block at the end of the beam line. Such high X-ray flux, relatively small bandwidth ~10^{–3}–10^{–2} (SASE), and short pulse duration ~100 fs provide XFELs outstanding single-shot diffraction quality for ultrafast structural dynamics. In the following sections, the main structural techniques currently implemented at XFEL facilities will be introduced.

Figure 5. Schematic of SACLA: a compact XFEL. EG, 500 keV electron gun; DF, deflector with collimator; SHB, 238 MHz subharmonic buncher; BS, 476 MHz booster; L-CC, L-band correction cavity; L-APS, L-band alternating periodic structure (APS) typed standing-wave cavity; C-CAT, C-band correction acceleration tube; S(C)-TWA, S(C)-band travelling-wave acceleration tube; BCn (n ≈ 1–3), nth bunch compressor; EDS, electron beam diagnostic section; SM, switching magnet; UND, undulator line; BLn (n = 1, 3), nth beam line; XDS, X-ray diagnostic system; EHA, experimental hall; OH, optical hutch; EH, experimental hutch. Only two beam lines beamlines (BL1 and BL3) were available in 2012. SACLA has the capability to install five independent FEL beamlines, and there are three currently in operation. Please refer to Reference [66] for details about each insertion device. Image adapted with permission from Springer Nature.
2.4. Main Applications at X-ray Free Electron Lasers (XFELs) for the Study of Structure and Dynamics of Matter

2.4.1. Serial Fs-X-ray Crystallography

Serial fs-nanocrystallography (SFX) [74–92] has been one of the first methods implemented at XFELs. The approach is illustrated in Figure 6a. Here, a μm-sized crystal is intercepted by the intense X-ray pulse to generate a diffraction pattern which encodes the relative orientation between the crystal and the X-ray beam. The process is repeated a number of times until sufficient amount of data is accumulated for structural refinement. The success of this technique relies on an approach called self-terminating diffraction gates, i.e., obtaining sufficient diffraction information when a sample crystal falls apart while an ultra-intense X-ray pulse propagates through it. Experiments at LCLS and simulations involving intense X-ray pulses with energies of up to 3 mJ \( [1 \times 10^{13} \text{ photons/pulse @ 2 keV (λ = 6 Å)}] \) and durations between 30 fs and 400 fs showed that a unique mechanism to ultrashort pulses allows structural information to be collected from crystalline samples using high radiation doses without the requirement for the pulse to terminate before the onset of sample damage. During exposure to a single X-ray pulse focused into a 10 μm² spot with \( I_{\text{peak}} \approx 10^{17} \text{ W cm}^{-2} \) a large fraction of the atoms in a protein crystal absorb a photon. This leads to an ultrafast cascade of secondary energy relaxation processes, lattice temperatures of \( \approx 500,000 \text{ K} \), high pressure, and the ultimate explosion of the sample. The onset of disorder is illustrated in Figure 6b for a small model molecule. As can be observed, the long-range order is completely gone in about 100 fs, and therefore the sample may lose its crystallinity during the transit time of the X-ray pulse. Figure 7 shows the effect of disorder on the accumulation of Bragg peak intensities for an intense X-ray pulse of duration \( \Delta t = 150 \text{ fs} \). Since disorder affects higher-resolution peaks in a stronger manner, the counting turns off sooner for higher-resolution Bragg reflections. The aforementioned experiments and modelling demonstrate that SFX does not require X-ray pulses to be shorter than the onset of long-range structural disorder. Instead, the impulsive heating leading to large-amplitude uncorrelated displacement of atoms destroys the crystalline order and shuts down Bragg diffraction. Therefore, SFX measurements in combination with simulations offer a way to characterize the order-to-disorder dynamics, correct for Bragg termination, find optimal X-ray pulse parameters, and perform structural refinement. The success of SFX is highlighted by the determination of a multitude of protein structures from (typically) sub-10 μm crystals [74–92]. It should be mentioned that the necessity of fs-X-ray pulses for attaining high-resolution structures of radiation-sensitive specimens is questionable. Serial millisecond crystallography at a synchrotron beamline, for instance, equipped with the same high-viscosity injector and a high frame-rate detector allowed for typical protein crystallographic experiments to be performed at room temperature [94]. In addition, fs-electron diffraction has also enabled the structural determination of radiation labile organic crystals at room temperature [41]. Low-dose micro-electron diffraction \( [95,96] \) (microED) is, in fact, likely to become the most convenient and economical approach for determining the structure of sub-μm crystals. Samples must, however, withstand the high vacuum conditions in the electron column or otherwise be kept at cryogenic temperatures. The main advantage of fs-X-ray probes relies on their ability to elucidate the dynamics of large protein systems. These large molecules are difficult to resolve with FED owing to the relatively low transverse coherence length (high transverse emittance) of fs-electron sources [4,5] (vide infra Sections 3.2 and 3.3).
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It has been argued that the combined use of a large crystal and XFEL pulses should provide inherently better structures than those obtained by SFX. In this technique the crystal must be very large and the distance between successive X-ray shots greater than the diameter of the damaged irradiated spot. This approach has been successfully applied at SACLA to obtain the structure of bovine heart cytochrome c oxidase (CcO) at 1.9 Å [97] and photosystem II (PS II) at 1.95 Å [98]. However, it has been shown that SFX can indeed deliver sub-1.5 Å from crystals of photoactive yellow protein (PYP) at room temperature [81].

Figure 6. Serial fs-nanocrystallography (SFX) approach. (a) A suspension of \( \mu \text{m} \)-crystals flows in a liquid jet across the X-ray beam, and diffraction is recorded using a pair of 512 \( \times \) 1024-pixel pnCCD detectors. The lower half detector is placed further from the beam center than the upper half detector to increase the accessible range of scattering angles. Thousands of individual diffraction patterns are recorded from single \( \mu \text{m} \)-crystals with pulse lengths up to 300 fs to a resolution of 0.76 nm. (b) Onset of disorder in a crystalline lattice during an ultra-intense 100-fs X-ray pulse. Sample: lysergic acid diethylamide. Atomic displacements were calculated using Cretin [93]. For this small molecule, crystalline order is largely destroyed by 100 fs. Adapted from Reference [92] with permission from Springer Nature.
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Figure 7. Plot of relative accumulation of Bragg signal for $I_{\text{peak}} = 1 \times 10^{17}$ W cm$^{-2}$ and a pulse duration $\Delta t = 150$ fs. Bragg intensities initially accumulate at the same rate proportional to $I_{\text{peak}}$. As expected, disorder affects higher-resolution peaks sooner (alike to the Debye–Waller effect) and termination of Bragg intensity accumulation may occur during the transit of the X-ray pulse through the crystal, leading to apparent pulse lengths ($\Delta t_{\text{app}}$) shorter than the duration of the incident pulse. In this case, $\Delta t_{\text{app}} = 40$ fs (black vertical dashed line), which is close to the turn-off time for the highest-resolution peaks at 0.76 nm. Figure adapted from Reference [92] with permission from Springer Nature.

Another possible method to bring µm-crystals to the X-ray beam path is the implementation of fixed-target crystallography chips [99–102]. Very recently, Schulz et al. [99] demonstrated a hit-and-return (HARE) approach based on the use of fixed-target crystallography chips mounted on a translation stage system. The HARE method enables time-resolved serial synchrotron crystallography with time resolution from milliseconds to seconds or longer. Figure 8 shows one of employed crystallography chips and some characteristic time-resolved structural results obtained from µm-crystals of *Rhodopseudomonas palustris* fluoroacetate dehalogenase (FAcD) soaked with a photocaged substrate as a model system. For more information vide infra reference [99].
were used to trigger the structural changes, while time-delayed 80-fs XFEL pulses (\( \lambda = 1.8 \text{ Å} \)) probed the structural rearrangements. A time stamping tool was implemented in order to bring the timing error from \(~300 \text{ fs} \) (intrinsic uncorrected shot-to-shot timing noise) to \(~50 \text{ fs} \) (see Section 2.5 below). Differential electron density maps were calculated from the differential structure factors (light minus dark). Barends et al. [107] found that their results are consistent with the conceptual view of MbCO-Mb complexes.

**Figure 8. Hit-and-return (HARE) method.** (a) An empty chip is shown as a control. The yellow arrows point out underdeveloped features, which appear semi-transparent under infrared (IR) light illumination. (b) Loaded chip with yellow arrows representing crystals sitting in the features of the chip. Crystals sitting inside of the features can be clearly distinguished from crystals on its surface and from empty features. (c) Changes in fluoroacetate dehalogenase (FAcD) electron density as a function of time for the active site subunits A and B. Electron density maps are at a cutoff of 2\( \sigma \) (green, protein; blue, ligand (highlighted with red circle)). Figure adapted from Reference [99] with permission from Springer Nature.

### 2.4.2. Time-Resolved Fs-X-ray Crystallography and Scattering

Since the very first ultrafast structural experiments at SPPS [43,103,104], the brightness of XFELs has increased by about one million fold, allowing for the study of more complex systems and photoinduced phenomena such as protein dynamics in crystalline [105–112] and liquid phases, [113] bond formation in the [Au(CN)\(_2\)]\(^-\) trimer in solution, [114,115] lattice dynamics in individual gold nanoparticles, [116] ultrafast melting of charge and orbital order in PCMO, [117] non-linear lattice dynamics [118] and CWD order in YBCO, [119] visualization of breathing modes in nanocrystals at extreme photoexcitation conditions, [120] photoinduced insulator-to-metal (IM) transitions, [121] warm dense matter physics, [122] and ultrafast crystallization [123] and melting [124] in shock-compressed crystals.

Figure 9a–d shows time-resolved X-ray diffraction results obtained by Barends et al. [107] at LCLS in the investigation of the ultrafast structural dynamics that follows CO photodissociation in Myoglobin-CO (MbCO). Early time-dependent structural changes are clearly visible. In this work, horse heart MbCO \( \mu \)-crystals were injected in random orientations within a thin liquid microjet to be intercepted by the XFEL beam, i.e., the same sample delivery method commonly implemented in the aforementioned SFX experiments. Photolyzing 150-fs optical laser pulses (centered at \( \lambda = 532 \text{ nm} \)) were used to trigger the structural changes, while time-delayed 80-fs XFEL pulses (\( \lambda = 1.8 \text{ Å} \)) probed the structural rearrangements. A time stamping tool was implemented in order to bring the timing error from \(~300 \text{ fs} \) (intrinsic uncorrected shot-to-shot timing noise) to \(~50 \text{ fs} \) (see Section 2.5 below). Differential electron density maps were calculated from the differential structure factors (light minus...
dynamics, in which ultrafast modes of the heme couple with collective lower-frequency protein motions [125,126] and subsequent large-scale protein motions. Here, Arnlund et al. [113] used multiphoton excitation of the photosynthetic reaction center of \( B. \) viridis \( \text{RC}_{\text{vir}} \) to perform time-resolved (TR) wide-angle X-ray scattering (WAXS) measurements. Here, Arnlund et al. [113] concluded that XFELs facilitate the direct visualization of ultrafast structure of \( \text{Mb} \), as well as the electron density difference following photoexcitation for \( t = +0.5 \text{ ps} \) and \( t = +10 \text{ ps} \). The orientation in (b) is rotated by 90° with respect to the orientation in (c) and (d). Figure adapted from Reference [107] with permission from Science AAAS. Right panel: Time-dependent changes in wide-angle X-ray scattering (WAXS) data recorded from detergent-solubilized samples of \( \text{RC}_{\text{vir}} \). (e) Experimental setup illustrating the microjet of solubilized \( \text{RC}_{\text{vir}} \) (green), X-ray detector, XFEL beam (orange) and 800-nm pump laser (red). (f) Time-resolved WAXS structure factor difference, \( \Delta S(q, t) = S_{\text{light}}(q, t) - S_{\text{dark}}(q) \), recorded as a function of \( t \). Linear sums of the four basis spectra (red) shown in (h) are superimposed upon the experimental difference data (black). (g) Time-dependent amplitudes of the components C1–C4 used to extract the basis spectra. (h) Basis spectra extracted from the experimental data by spectral decomposition. Figure adapted from Reference [113] with permission from Springer Nature.

Figure 9e–h illustrates a very similar experimental layout implemented by Arnlund et al. [113] to perform time-resolved (TR) wide-angle X-ray scattering (WAXS) measurements. Here, Arnlund et al. [113] used multiphoton excitation of the photosynthetic reaction center of \( B. \) \textit{viridis} \( \text{RC}_{\text{vir}} \) to demonstrate that TR-WAXS data recorded using XFEL radiation can capture ultrafast protein conformational changes in solution. The probe beam consisted of 40-fs X-ray pulses containing 2.6 \( \times \) 10\(^{12} \) photons/pulse (\( \lambda = 2.1 \text{ Å} \)) focused into a 10-\( \mu \text{m}^2 \) spot. Detergent-solubilized \( \text{RC}_{\text{vir}} \) samples were photoactivated using 500-fs optical pulses (\( \lambda = 800-\text{nm} \)) with a fluence of 530 mJ cm\(^{-2} \); this level of excitation leads to considerable multiphoton absorption since it is very close to
the universal threshold for plasma formation (~1 J cm\(^{-2}\)) \[127\]. Figure 9g depicts the separation of TR-WAXS data (Figure 9f) into their major components by spectral decomposition. The extracted spectral components are presented in Figure 9h. C1 is an ultrafast component, C2 is a protein component that displays the expected oscillatory features, and C3 and C4 are components that relate to heating effects. Arnland et al. [113] concluded that XFELs facilitate the direct visualization of ultrafast protein motions. However, it should be noted that the interpretation of TR-WAXS data from solution phase requires the assistance of calculated structure factors from molecular dynamics (MD) simulations [128,129]. Moreover, depending on the solute under investigation the input of quantum mechanically optimized geometries [129,130] may be necessary. Time-resolved X-ray absorption spectroscopy (TR-XAS) is another approach for the study of molecular dynamics in solution with great sensitivity to structural changes.

2.4.3. Fs-X-ray Absorption Spectroscopy

Fs-X-ray absorption spectroscopy (fs-XAS), often in combination with fs-X-ray emission and other relevant spectroscopies, [131] has emerged as a powerful technique to monitor structural dynamics in solution, [132–140] crystalline phases, [141–143] and even at surfaces. [144] XAS is element-specific and depending on the element and core-shell involved in the process, X-ray photon energies usually range from 100 eV to 100 keV. There are two main regions in XAS: X-ray photoexcitation below the ionization threshold (IE) gives rise to pre-edge bands that arise from transitions to unoccupied or partially filled orbitals. For photon energies slightly above IE, there is a jump in the absorption cross-section and the quasi-bound photoelectron with low kinetic energy, and therefore high cross-section, undergoes multiple-scattering events with the surrounding atoms. This leads to a strong oscillatory behavior in the X-ray absorption spectrum. This region is denoted as XANES (X-ray absorption near-edge structure) or NEXAFS (near-edge X-ray absorption fine structure). As the kinetic energy of the photoelectron increases, the cross-section decreases and weaker modulations, in the so-called EXAFS (extended X-ray absorption fine structure) region appear as a consequence of single scattering contributions. The surrounding molecular arrangement is encoded in the observed absorption features, and therefore the structural information can be recovered through the application of well-established data analysis protocols. [145,146]

Initial pioneering fs-XAS experiments were performed at the femtosecond lines of SLS [133,134,143] and ALS [135,136] via laser slicing (see Section 2.1 above). With the advent of XFELs, the enhancement in signal to noise ratio (SNR) in fs-XAS data is remarkable. The main challenge, however, in the use of XFEL radiation for fs-XAS experiments is the intrinsic spectral instability arising from the stochastic nature of SASE. The rather broad SASE bandwidth (for spectroscopy) requires the use of a monochromator while large variations in the central wavelength results in large shot-to-shot intensity fluctuations of the order of 100%. There are normalization protocols that implement non-invasive shot intensity monitors to account for such large fluctuations. The application of dispersive spectrometers seems to be another suitable detection approach. [147,148] Figure 10a (red symbols) illustrate results obtained by Gawelda et al. [140] at the micro-XAS synchrotron beam line of SLS. Here, intense 100-fs pump pulses (\(\lambda = 400\) nm) excite an aqueous solution of \([\text{Fe(bpy)}_3]^{2+}\) while 100-ps tunable monochromatic hard X-ray pulses probe the photoinduced changes by XANES at \(t = +50\) ps. The differential XANES spectrum is shown in Figure 10b together with fs-XANES measurements (blue stars) performed by Bressler et al. [133] at the FEMTO line of SLS (laser slicing, see Section 2.1) for the same system at \(t = +300\) fs utilizing 100-fs hard X-ray pulses. The lack of brightness caused by laser slicing is evident. Recent results obtained by Mara et al. [138] at LCLS (see Figure 10, bottom panel) illustrate the near \(10^{10}\) increase in ray flux. They implemented Fe K-edge fs-XANES and fs-XES to directly probe the ligand environment of the iron and its spin state, respectively. Mara et al. [138] were able to unambiguously revealed the geometric and electronic structural dynamics of photoexcited ferrous cytochrome c (cyt c), providing a direct correlation between axial ligand rebinding to the Fe and the temperature decay. The latter enabled experimental
quantification of a protein entatic contribution towards the stabilization and control of an active site metal-ligand bond.

Figure 10. Time-resolved X-ray absorption spectroscopy (XAS). Top panels (a–c): time-resolved X-ray absorption near-edge structure (XANES) for aqueous \([\text{Fe(bpy)}_3]^2+\). (a) Fe K-edge XANES spectrum of the low spin (LS) ground state (black trace) and of the high spin (HS) quintet state (red dots). The latter is determined from the LS spectrum and the transient spectrum measured at \(t = +50\) ps after fs-laser excitation (Gawelda et al. [140] synchrotron microXAS line at SLS). (b) Transient XANES spectrum (difference between red symbols and black trace shown in panel (a)). The blue stars represent the transient spectrum recorded at \(t = +300\) fs via laser slicing at SLS. (c) Time scan of the signal (blue points) at the B-feature (arrow in panel (b)) as a function of \(t\). The inset shows a long time scan up to a 10-ps time delay. The red trace is the simulated signal assuming a simple kinetic model to describe the spin conversion process. The vertical arrow displays the expected effect of an elongation of 0.2 Å for the Fe-N bond distance difference between the LS and HS states. Error bars are ±1 standard deviation. Figure adapted from Reference [133] with permission from Science AAAS. Bottom panels (d–g): Ultrafast x-ray absorption spectra of ferrous cyt c. (d) Superimposed spectra of ground-state (GS, black) and excited-state (ES, green) cyt c, showing the edge, white line, and shape resonance regions. (e) Cyt c heme structural model used in simulations. Fits (blue) to the GS (f) and ES (g) spectra (red) and associated structural parameters, derived from simulations. The fit residuals are in yellow at the bottom with the obtained structures above. Figure adapted from Reference [138] with permission from Science AAAS.

2.5. Timing Techniques at XFEL Facilities

The intrinsic time resolution of XFELs is limited by synchronization noise (or timing jitter in rms) to about 100–200 fs [72,149,150] with 100 fs reflecting short-term pulse-to-pulse variations.
In order to fully exploit the potential of ultrashort hard X-ray pulses for monitoring faster dynamic phenomena different schemes have been proposed and implemented for the characterization of X-ray pulses. [149–158] Note that any useful characterization tool should provide single-shot sensitivity since a large component of the XFEL timing noise comes from shot-to-shot fluctuations. Ideally, one would like to access the temporal and spectral profiles of each X-ray pulse as well as its relative timing with respect to the fs-optical driving pulse; being the latter the bare-minimum. Among all current options, single-shot, single-cycle terahertz (THz) pulse streaking presents the advantage of characterizing both the temporal pulse shape of the free electron laser (FEL) pulse and its relative arrival time. The experimental arrangement implemented by Grguraš et al. [149] at FLASH (DESY, Hamburg) is shown in Figure 11a. A~3 mJ, 50-fs laser pulse (λ = 800 nm) is split into two parts; most of the pulse energy is used for THz generation via pulse front tilting for phase matched optical rectification in a LiNbO₃ non-linear crystal [159,160]. The remainder (tens of µJ) is used for in situ THz-field characterization by electro-optic sampling (EOS) in a ZnTe crystal. Optical rectification produced about 4 µJ, 2-ps, single-cycle THz pulses centered at 0.6 THz. Figure 11b–d illustrates the THz streaking principle. In order to determine both the temporal shape and the relative arrival time, the FEL pulse should be within the streaking window of the THz vector potential denoted in Figure 11d by Δt, which in this case Δt~600 fs. Note that the streaking window should be larger than the intrinsic timing jitter to guarantee that most (if not all) FEL pulses become potentially useful (i.e., they are timed). Grguraš et al. [149] demonstrated the use of single-cycle THz pulses for the characterization of extreme ultraviolet (XUV) FEL pulses. Appropriate target atoms can be chosen to extend THz streaking into the hard X-ray regime where the main disadvantage is the large reduction in the photoionization cross-section when compared to soft X-rays [72,161].

Figure 11. Single-shot, single-cycle THz streaking. (a) Experimental setup: A fs-laser pulse from a Ti:Sapphire, appropriately delayed with respect to the free electron laser (FEL) pulse, is split into two parts. Most of the pulse energy is used for tilted-wavefront THz generation in LiNbO₃. The remaining part can be used for characterizing the THz pulse via electro-optic sampling (EOS). This could be done in situ (prior streaking measurements) in a zinc telluride (ZnTe) nonlinear crystal positioned at the gas target location.
In the streaking measurement, the collinear FEL photon pulse ejects a burst of photoelectrons from the gas, with a temporal profile identical to the incident soft XUV/X-ray FEL pulse. The THz pulse is used to streak the photoelectron burst and consequently characterize the FEL pulse. (b-d) Schematic of the operational principle: Blue and red curves represent the electric field and corresponding vector potential of the single-cycle THz pulse. The vertical axis corresponds to the kinetic energy of the photoelectron emission, which is determined by a time of flight (TOF) spectrometer. (a) The FEL pulse does not overlap with the THz pulse, and therefore the kinetic energy distribution of photoelectrons ejected by the FEL pulse is unaffected. (c) The FEL pulse overlaps with an extreme of the THz vector potential, leading to a maximally downshifted photoelectron spectrum with minimized spectral broadening. (e) Temporal overlap occurs near the zero crossing within the effective streaking window (Δt) of the vector potential where the time of arrival as well as the temporal profile can be determined. Figure adapted from Reference [149] with permission from Springer Nature.

The aforementioned THz streaking method is probably one of the most elegant characterization tools, which is sensitive to fluctuations in SASE amplification and in combination with a dispersive X-ray spectrometer [147,148] could provide a quasi-complete description of XFEL pulses. However, the most popular timing methods at XFELs, owing to simplicity, are spatial [150,154–157,162,163] and spectral [150,152] encoding. These are cross-correlation techniques based on X-ray induced material changes and confer a means to determine the relative timing between the fs-optical pump pulse and the X-ray probe pulse. Figure 12 illustrates a spectrogram approach recently introduced by Hartmann et al. [158] that combines the best features (or avoids the disadvantages) of spatial and spectral encoding to provide an outstanding timestamping error of sub-1 fs (rms). With such a timing method in hand, and routine 5-fs optical and 5-fs SASE X-ray pulses, the effective time-resolution of XFELs is now down to the 5-fs level providing the possibility to monitor high frequency vibrational modes and electronic coherences.

![Figure 12. Schematic of the single-shot geometry for measurement of the spectrogram.](image)

(a) The X-ray and optical beams are crossed in a silicon nitride membrane and their relative delay is encoded in the spatial beam profile of the optical probe. The crossing angle α and beam diameters define the time window in which the X-ray-induced absorption is probed. (b) Measured spectrogram using an unpumped normalization spectrogram to calculate the change in transmission. The result of the two-step edge-finding algorithm to determine the X-ray arrival time is overlaid as a black dashed line. Figure adapted from Reference [158] with permission from Springer Nature.
3. Structural Techniques Involving Ultrashort Electron Pulses

3.1. Introduction to Femtosecond Electron Diffraction (FED)

Since the very first stroboscopic experiments utilizing electron pulses as structural probes in time-resolved diffraction experiments in the 1980s, [164,165], there has been a continuous progress in the development of brighter and faster electron diffractometers. This advancement has occurred alongside several breakthrough ultrafast electron diffraction (UED) discoveries in the gas phase, [166–173] and in solid crystalline materials measured in reflection [174–178] and transmission [41,179–196] geometries. Great progress has been achieved in terms of FED (or UED) technology, with three main types of approaches being widely implemented in our research community (ordered in increasing design complexity and cost): (i) Compact (direct current, DC) FED designs, (ii) Hybrid (DC-RF) FED setups (i.e., with electron pulse rebunching) and (iii) Relativistic (RF) FED instruments. Figure 13 presents the layout of a compact FED setup with a conventional DC fs-electron source. The main difference among FED instruments is configuration/design of the electron gun, which is highlighted in Figure 13 by a dashed box. In a DC fs-electron source, electrons are generated via photoemission and accelerated by a DC electric field. A magnetic lens (ML) is used to focus the electron pulse propagation distance to the sample and, therefore, improves the temporal resolution (vide infra).

![FED layout](image)

**Figure 13. Femtosecond electron diffraction (FED) layout for a compact electron gun design.** In the present compact FED setup, a fs-optical pulse (green) generates, via the photoelectric effect, a fs-electron bunch by back-illuminating an ultrathin ~20-nm thick gold film. Electrons are accelerated by a 100 kV DC potential drop. A magnetic lens can be implemented before or after the sample to focus the diffraction pattern on the detector screen. Note that the ML could be placed after the sample (akin to an objective lens in a transmission electron microscope (TEM)). This configuration greatly reduces the electron pulse propagation distance to the sample and, therefore, improves the temporal resolution (vide infra).

A 300 kV DC-FED setup currently under development at the Ultrafast electron Imaging Lab (UeIL) of the University of Waterloo is shown in Figure 14. As can be observed, FED systems are laboratory scale tools, which depending on their design may even fit on top of optical tables. Care should be taken when operating FED instruments at acceleration voltages >30 kV; energetic electrons produce via corona discharge may lead to the generation of X-rays when impacting the walls...
of the vacuum chamber. Therefore, proper radiation shielding in addition to dosage monitors are a must in FED laboratories.

![300-kV DC FED apparatus at the Ultrafast electron Imaging Lab (UeIL)](image)

Figure 14. 300-kV DC FED apparatus at the Ultrafast electron Imaging Lab (UeIL). Left panel displays the 300-kV power supply, and the optical table with beam transport optics. Right panel shows the 300-kV FED instrument surrounded by a radiation enclosure.

3.2. Electrons as Structural Probes: Fermionic Nature and Source Brightness

The electron is an interesting elementary particle to play with. Its spin of one-half makes the electron a fermion and as such “no two electrons can share the same state” (Pauli exclusion principle). Therefore, an equivalent process to that of light amplification by stimulated emission of radiation (laser), which arises from the bosonic behaviour of photons, is not possible for electrons. One of the challenges is thus to develop an electron source with sufficient coherence and brightness to resolve the ensuing atomic motions. There is in fact a fundamental “quantum limit” to electron beam brightness (\(B_Q\)) enforced by the Heisenberg uncertainty principle. Note that the minimum angular divergence a laser beam can achieve is also given by the uncertainty principle. However, there is no fundamental boundary to laser brightness besides practical and physical constraints usually dictated by the damaging threshold of amplifying laser medium. [40] The definition of electron beam brightness (in German, “Richstrahlwert”) was initially introduced by von Borries and Ruska [197] in 1939, (Equation (1)):

\[
B = \frac{I}{A_s \Omega}
\]

where \(I\) is the current; \(A_s\) the areal spot size at focal point; and \(\Omega\) the beam divergence in sr.

Equation (1) has now evolved into different quasi-equivalent forms depending on the background of the scientific community. Beam accelerator scientists prefer working in position-momentum phase space owing to the invariance of the six-dimensional (6D) phase-space density (\(\rho_{6D}\)) or volume (\(V_{6D}\)) imposed by the Liouville’s theorem (as long as beam dynamics can be described by Hamilton’s equations).

\(V_{6D}\) is the volume occupied by the electron bunch in this 6D phase space \((x, p_x, y, p_y, z, p_z)\), which is proportional to the product of the normalized rms beam emittances \(\varepsilon_{nx}\varepsilon_{ny}\varepsilon_{nz}\), (Equation (2)):

\[
V_{6D} \propto \varepsilon_{nx}\varepsilon_{ny}\varepsilon_{nz}
\]

where \(\varepsilon_{nq} = \frac{1}{m_0c} \sqrt{\langle q^2 \rangle \langle p_q^2 \rangle - \langle q \rangle^2 \langle p_q \rangle^2} \approx \frac{1}{m_0c} \sigma_{q \sigma_{p_q}}\) and \(q = x, y, z\). Hence, (Equation (3)):

\[
B_{6D} = \frac{N_e}{V_{6D}} \propto \frac{N_e}{\sigma_{x \sigma_{p_x}} \sigma_{y \sigma_{p_y}} \sigma_{z \sigma_{p_z}}}
\]

where \(\sigma\) are variances or rms spreads in positions \(x, y, z\); and momenta \(p_x, p_y, p_z\).
The result from Equation (3) is a true figure of merit that can be compared against the quantum degenerate limit, (Equation (4)):

$$B_Q = \left(\frac{m_0 c}{\hbar}\right)^3 \frac{2e}{\lambda c^3} \approx 10^{25} \text{ A m}^{-2}$$

where $\lambda_c$ is known as Compton wavelength.

Note that for a paraxial electron beam propagating in the $z$ direction, the brightness can also be written as, (Equation (5)):

$$B_{6D} \propto \frac{N e}{\sigma_x \sigma_{p_x} \sigma_y \sigma_{p_y} \sigma_E \sigma_t} \propto \frac{I}{\lambda \sigma_p x \sigma_p y \sigma_E \Omega}$$

where $\sigma_E$ and $\sigma_t$ are the energy and time variances, respectively.

The latter expression (Obtained after considering a given longitudinal momentum $p_z$ (or electron kinetic energy) such thus $\lambda_s \propto \sigma_x \sigma_y$ and $\Omega \propto \sigma_{p_x} \sigma_{p_y}$) in Equation (5) is referred to as “brilliance” and is a common figure of merit to characterize photon beams. Note that by assuming a value for $\sigma_E$ and removing such dependence from Equation (5) we recover Equation (1). For very instructive derivations related to electron beam/source brightness please vide infra references [198–207].

3.3. Transverse Electron Beam Properties: Transverse Emittance and Coherence Length

Regardless of the chosen definition of brightness, a reality check shows that even the most advanced electron sources present a $B_{6D}$ that is several orders of magnitude below the quantum limit, $B_Q$. There is still a lot of room for improvement and in most practical applications the transverse and longitudinal phase spaces are weakly coupled; therefore it is more convenient to treat them separately. The transverse electron beam coherence length ($L_x \propto \varepsilon_{nx}^{-1}$) is defined as follows, (Equation (6)):

$$L_x = \frac{\lambda_{dB}}{2\pi \sigma_\theta} = \frac{\lambda_{dB} p_x}{2\pi \sigma_{p_x}} = \frac{\hbar}{2\pi \sigma_{p_x}}$$

where $\lambda_{dB}$ is the de Broglie wavelength and $\sigma_\theta$ the rms angular spread or variance.

$L_x$ (or $\varepsilon_{nx}$) is an essential electron beam parameter. For instance, it is known that in XFELs the value of $\varepsilon_{nx}$ at the entrance of the undulator corresponds to the wavelength of the X-rays produced ($\lambda$) according to, (Equation (7)):

$$\frac{\varepsilon_{nx}}{\beta \gamma} \ll \frac{\lambda}{4\pi} \approx 208 \beta = \frac{v}{c}$$

where $v$ is the electron speed, and $\gamma$ is the Lorentz factor.

Equation (7) links electron beam and X-ray beam properties and highlights the importance of attaining more intense and coherent electron sources. Thus, by reducing $\varepsilon_{nx}$ (or increasing $L_x$) one could in principle achieve shorter photon wavelengths or reduce the length of the linac [208].

The design and implementation of better and more efficient photocathodes is currently an area of active research. Generally speaking, the spatial resolution provided by a given photon or electron source is determined by its transverse ($L_x$) and longitudinal or temporal ($L_l$) coherences. The expression for longitudinal coherence of photons is easily deduced by replacing $\lambda_{dB}$ by $\lambda$ in Equation (6).

Thus, for photons, (Equation (8)):

$$L_x = \frac{\lambda}{2\pi \sigma_\theta}$$

and (Equation (9)):

$$L_l = \frac{\lambda^2}{2 |\Delta \lambda|}$$
Then, given $E = \frac{h c}{\lambda}$, and therefore $|\Delta E| = |\Delta \lambda|/\lambda$; we obtain (Equation (10)):

$$L_1 = \frac{\lambda E}{2 |\Delta E|}$$  
(10)

On the other hand, $L_1$ for electrons becomes, (Equation (11)):

$$L_1 = \frac{\lambda dB^2}{2 |\Delta \lambda dB|}$$  
(11)

and considering $\lambda dB_p \approx \lambda dB_p z \approx h$, we obtain $|\Delta p_z| \approx h/|\Delta \lambda dB|$ and, (Equation (12)):

$$L_1 \approx \frac{h}{2 |\Delta p_z|}$$  
(12)

Note that assuming $|\Delta p_z| \approx |\Delta p_x|$ and combining Equations (6) and (12), we obtained $L_x \approx L_1$, which seems to indicate that transverse and longitudinal coherences should have a similar effect on the spatial resolution of X-ray and electron diffractometers. However, the small de Broglie wavelength or small scattering angles ($\theta \ll 1$) of keV-electrons makes the effect of $L_1$ negligible. Equivalently, one could introduce an effective longitudinal coherence length $L_{1,\text{eff}} \approx L_1 \theta \gg L_x$ by noting that their effects on the diffraction peak widths are weighted by their relative projections on the screen. Hence, the spatial resolution in FED experiments is limited by $L_x$, which is about 3 nm for conventional electron sources. In the case of synchrotron and XFEL sources, the transverse coherence, given by Equation (8), is in the order of several $\mu$m and thus, $L_1$ governs the spatial resolution. Considering typical XFEL beam parameters $\lambda \approx 0.1$ nm and bandwidth $\approx 10^{-3}$, we obtain $L_1 \approx 50$ nm. This suffices to spatially resolve systems with relatively large unit cells or large molecules such as proteins. Moreover, if necessary, the bandwidth can be reduced through the use of a monochromator in order to increase $L_1$. This is perhaps the main advantage of XFELs over FED instruments, which have not yet succeeded in monitoring protein dynamics. On the other hand, the scattering cross section for electrons is approximately $10^{5}$–$10^{6}$ higher than X-rays for the same energy and are about 1000-fold less damaging [209–211]. These facts make electrons a better probe of matter at the nanoscale.

3.4. Temporal Resolution in the Absence of Repulsive Interactions

For decades the main challenge has been to break the ps-temporal resolution barrier in FED experiments. Electrons are not only fermions but also charged particles, and therefore it is extremely challenging to keep them together and preserve the temporal resolution. Coulomb repulsion or space-charge effects lengthen the pulse during its propagation towards the sample. In fact, the instrument response function of FED setups is given by the electron pulse duration at the sample position (the pump pulse is usually much shorter). The use of single-electron or low-density electron sources resulted in the first and simplest alternative to reduce space-charge effects and preserve the temporal resolution [176,177,212,213]. However, there are only few samples capable of withstanding the repetitive photoexcitation conditions necessary to build a statistically meaningful (high SNR) diffraction pattern. Time-resolved electron diffraction experiments employing single-electron bursts rely on the accumulation of multiple events averaged over $\sim 10^3$ pump-probe cycles to obtain a diffraction pattern with sufficient quality. To collect the data in a reasonable amount of time, single-electron sources often require the use of high repetition rate lasers $\geq 100$ kHz. This procedure leads to accumulated heating effects that can significantly deteriorate the sample and even introduce artifacts, see supplementary information in Reference [41]. Therefore, it is essential to reach both ultrashort and ultrabright electron pulses to enable the study of structural dynamics in susceptible
solid-state molecular materials. High-repetition electron sources are then best suited for gas phase experiments (molecular beams) in which the sample is refreshed between successive excitation pulses. Nevertheless, it is interesting to consider the limiting case in which the interactions among electrons within the bunch are switched off. This limit offers an idea of the “optimal” temporal resolution achievable by a DC FED instrument, such as the one shown above in Figure 13.

Neglecting relativistic effects, the longitudinal broadening (\(\Delta l\)) of the electron pulse can be approximated by

\[
\Delta l \approx \frac{t_t \Delta v_0}{v_z} \approx \frac{(2d_a + d_s) \Delta v_0}{v_z^2} \approx \left( \frac{d_a}{eV} + \frac{d_s}{2eV} \right) \Delta p_0
\]

where \(V\) is the applied DC voltage that satisfies \( \frac{m_0 v_z^2}{2} = eV\), and \(\Delta p_0\) is the initial momentum spread.

Although Equation (13) suitably approximates the temporal spread gained in the cathode-anode region through a very simple and straightforward derivation, it was found to over exaggerate the pulse broadening occurring in the drift region. A more detailed derivation that includes relativistic effects shows that, [214] Equation (14):

\[
\Delta t_p \approx \left[ \frac{d_a eV}{v_z} \left( 1 - \frac{v_0}{v_z} \right) + \frac{d_s v_0}{m_0 \gamma^3 v_z^3} \right] \Delta p_0
\]

and Equation (15):

\[
\Delta t_p \approx \frac{d_a}{eV} \Delta p_0 \text{ if } v_z \gg v_0
\]

Equation (15) has been derived for an applied constant DC electric field (E), and therefore \(E d_a = V\) provides the following compact expression for the temporal broadening in the absence of space-charge effects, Equation (16):

\[
[\Delta t_p \approx \frac{\Delta p_0}{e|E|}] 
\]

Optimal photoemission conditions in the limit of low electron density bursts with \(|E| = 10 \text{ MV m}^{-1}\) have shown to deliver electron pulses as short as 80 fs. [215] Ideally one would like to preserve such temporal resolution with pulses containing >10^3 electrons in a beam with a transverse size of about 100 µm.

3.5. Bright Compact Direct Current (DC) FED Setups

It was not until the work of Siwick et al. [179] demonstrating the first fully resolved structural transition using 600 fs electron pulses that it was realized that space-charge effects could be diminished by reducing the electron propagation distance and maximizing the extraction field, \(|E|\). Detailed N-body simulations and mean-field analytic models provided a greater understanding of pulse propagation dynamics of sub-relativistic electron bunches [216–219]. Nowadays, the use of charge-tracking programs, [220,221] that are required for the proper design of FED instrumentation, is routine. Historically, charge-tracking algorithms and powerful software packages were implemented by accelerator physicists, yet for a while UED scientists were largely unaware of this development due to the lack of interaction between communities.

Despite having a much simpler design than that of MeV relativistic machines, compact FEDs have provided unprecedented results in the study of novel crystalline materials. Several representative
experiments performed in transmission and reflection geometries with compact FED instruments are shown in Figures 15 and 16, respectively. FED has been found to be particularly advantageous for the investigation of 2D materials [183,185,186,222]. Figure 15a,b presents results obtained by Eichberger et al. [183] for the study of 1T-TaS$_2$, a prototypical CDW system. FED has enabled the observation of atomic motions on timescales short enough to follow even the effect of non-equilibrium electronic distribution in this strongly correlated crystal. Since FED provides diffraction information over the entire 2D Brillouin zone at once, it is capable of unveiling different processes that give rise to changes in diffracted intensities. Figure 15c,d illustrates FED measurements gathered by Waldecker et al. [190] in the investigation of Ge$_2$Sb$_2$Te$_5$ (GST), a phase-change compound commonly used for optical data storage. In this study, the combination of transient absorption/reflectivity and FED data allowed the authors obtain a microscopic picture of the initial steps in the photoinduced amorphization process in GST. Figure 15e–m presents FED results in Me$_4$P[Pt(dmit)$_2$]$_2$ (Me$_4$P = tetramethylphosphonium, dmit = 1,3-dithiol-2-thione-4,5-dithiolate), a crystalline system with a relatively large unit cell (a = 2.89 Å, b = 12.6 Å, c = 37.4 Å). Ishikawa et al. [223] applied transient reflectivity and FED to elucidate the key molecular motions that couple to an orbital-driven charge transfer reaction, i.e., a dimer expansion and a librational mode. These results illustrate the potential of advanced FED instruments to address fundamental structural phenomena occurring in increasingly complex molecular systems. On the other hand, FED experiments in reflection geometry (reflection high-energy electron diffraction, RHEED) with 30 keV electrons enabled the investigation of an indium (In) monolayer adsorbed on a (1 1 1)-Si surface (see Figure 16). At room temperature, the In atoms form regular arrays of quasi-one-dimensional (4 × 1) zigzag wires, separated by rows of silicon atoms as shown in Figure 16c. Around 125 K, a first-order Peierls-like transition to the (8 × 2) CDW phase occurs that is accompanied by a metal-to-insulator transition, see Figure 16a. With a temporal resolution of about 330 fs achieved via the implementation of pump pulse front tilting, [176,177] Frigge et al. [178] enabled the observation of In–In bond breaking and formation that drive the structural transition through the non-thermal excitation of critically damped soft phonon modes.
At room temperature, the In atoms form regular arrays of quasi-one-dimensional (4 × 1) electrons enabled the investigation of an indium (In) monolayer adsorbed on a (1 1 1)-Si surface (see excitation of critically damped soft phonon modes. In–In bond breaking and formation that drive the structural transition through the non-thermal implementation of pump pulse front tilting, [176,177]. Frigge et al. [178] enabled the observation of transition, see Figure 16a. With a temporal resolution of about 330 fs achieved via the Peierls-like transition to the (8 × 2) CDW phase occurs that is accompanied by a metal-to-insulator zigzag wires, separated by rows of silicon atoms as shown in Figure 16c. Around 125 K, a first-order structural phenomena occurring in increasingly complex molecular systems. On the other hand, FED experiments in reflection geometry (reflection high-energy electron diffraction, RHEED) with 30 keV structural phenomena occurring in increasingly complex molecular systems. On the other hand, FED experiments in reflection geometry (reflection high-energy electron diffraction, RHEED) with 30 keV...
where electrons are born. bursts as short as 30 fs (12 fs rms). The idea here is to shape the cathode in order to increase the supply \[224\]. Note that the cathode’s surface since most of the temporal broadening occurs during the initial stage of electron propagation \[225\]. Hence, a more general expression for Equation (16) follows, Equation (17):

\[
\Delta t_p \approx \frac{\Delta p_0}{e|E_g|}
\]

where \(|E_g|\) is the magnitude of the geometrical electric field at the cathode’s surface, i.e., in the area where electrons are born.

Equation (17) stresses the need to achieve both high electric field strengths and low initial momentum (or energy) spread at the cathode’s surface in order to minimize the temporal broadening caused by \(\Delta p_0\) as well as additional broadening arising from instabilities in the high-voltage power supply \[224\]. Note that \(\Delta p_0\) affects both the temporal and spatial resolutions (see definition of \(L_x\) in Equation (6)).

Figure 17 illustrates a new DC fs-electron source concept capable of generating multi-electron bursts as short as 30 fs (12 fs rms). The idea here is to shape the cathode in order to increase the...
geometrical electric field at the surface, i.e., in the area from which electrons are photoemitted. The main challenge is then to avoid vacuum breakdown (i.e., electrical discharges).

\[
\Delta p \approx \Delta p_0 e^{E_g} \quad (17)
\]

where \( E_g \) is the magnitude of the geometrical electric field at the cathode's surface, i.e., in the area from which electrons are photoemitted. The main challenge is then to avoid vacuum breakdown (i.e., electrical discharges).

\[
E_{s,c} = \beta_m \beta_g |V_c| \quad (18)
\]

Figure 17. Ultrafast electron source concept for the generation of <15-fs (rms) multi-electron bursts. (a) Schematic of the electron source concept. Equipotential and magnetic field lines calculated using Poisson Superfish, [226] are shown in red and green, respectively with a value of \( |E_g| = 50 \text{ MV m}^{-1} \).

(b,c) Results from ASTRA simulations. (b) Electron pulse duration (\( \sigma_t \), in fs) as a function of the number of electrons per bunch (#e\(^{-}\)). Black trace corresponds to our 300-kV DC FED design with \( d_a = 5 \text{ cm} \) and a total cathode-sample distance \( d_T = 10 \text{ cm} \). Blue and red traces correspond to compact 100 kV DC FED setups (with flat electrodes) with \( d_T = 2 \text{ cm} \) and constant electrostatic fields of \( |E_z| = 20 \text{ MV m}^{-1} \) and 10 MV m\(^{-1} \), respectively. (c) Dependence of electron pulse duration (without space-charge effects) as a function of \( |E_g| \). Electrons in simulations were generated at the cathode surface considering a temporal (longitudinal) Gaussian profile of 6 fs (rms) [14 fs (fwhm)], an initial energy spread of 0.2 eV, and a lateral (transverse) Gaussian spot size of 50 \( \mu \text{m} \) (rms). The solid trace in panel (c) was obtained from a fit implementing Equation (20). Figure adapted from Reference [224].

The critical surface vacuum breakdown is given by, Equation (18): \[
|E_{s,c}| = \beta_m \beta_g |V_c|/d_a \quad (18)
\]

where \( |E_{s,c}| \) is the magnitude of the critical surface vacuum breakdown field, \( \beta_m \) and \( \beta_g \) are microscopic and geometrical field enhancement factors, respectively, and \( V_c \) is the critical applied potential drop over the cathode-anode separation distance, \( d_a \).

Note that \( |V_c|/d_a^{-1} = |\langle E_z \rangle| \), where \( |\langle E_z \rangle| \) is the magnitude of the average critical applied field and \( \beta_g |\langle E_z \rangle| \) equals what we refer to as the geometrical critical surface electric field, \( |E_{g,c}| \). Thus, Equation (19):

\[
|E_{s,c}| = \beta_m |E_{g,c}| \quad (19)
\]

Values of \( |E_{s,c}| \) have been found to be 6.5–10 GV m\(^{-1} \) for refractory metals [227–229] while \( \beta_m \) is governed by the surface roughness with \( \beta_m \approx 100 \) for mirror-like finished and \( \beta_m \approx 1 \) for a roughness free surface. Note that field emitters approach the limit \( \beta_m \approx 1 \), and thus \( |E_{s,c}| \approx |E_{g,c}| \). For a bulky
surface with $\beta_m = 100$, we obtain $|E_{g,c}| \approx 60–100 \text{ MV m}^{-1}$, and therefore $|E_g| < 60 \text{ MV m}^{-1}$ should in principle be achievable.

A more detailed analysis of these and additional simulations show that the temporal broadening in the absence of space-charge effects follows, Equation (20)

$$\sigma_{t, \Delta \epsilon_0} = k \sqrt{\Delta \epsilon_0 / |E_g|}$$

where $\Delta \epsilon_0$ is the initial energy spread and $k$ is a constant that depends on the type of initial electron distribution ($k = 991 \text{ fs MV m}^{-1} eV^{-1/2}$ for isotropic).}

It should be noted that Equation (20) and Equation (16) are equivalent since $\Delta \epsilon_0 \approx \epsilon_0$, and therefore $\Delta P_{\parallel,0} \propto \sqrt{\Delta \epsilon_0}$. Initial preliminary tests at UeIL indicate, however, that achieving $|E_g| > 30 \text{ MV m}^{-1}$ seems to require ultrahigh vacuum conditions, which are currently out of reach in our FED vacuum chamber designed to obtain a background pressure of $10^{-7}$ torr. A next-generation FED setup will be developed at UeIL to attain 30-fs multielectron bursts.

### 3.6. Ultrabright Hybrid DC-Radio Frequency (RF) FED Setups: Compression of Electron Pulses

Electron pulse compression methods are based on either the static [230–234] or active [235–239] application of electric or magnetic fields that can reverse the longitudinal momentum-position distribution of the electrons in the bunch. These electron beam components effectively act as a temporal lens and the sample is to be positioned at the temporal focal point. Among all proposed and/or demonstrated approaches for electron pulse rebunching, the implementation of a cylindrical TM$_{010}$-RF cavity [235–239] became the most widely accepted and successful method. Figure 18 illustrates the electron pulse compression principle in a hybrid 100-kV DC-RF FED instrument. The RF pill lens provides an axial electric field which is uniform along the cavity axis and varies in time according to $E_z(z, t) = E_0(z) \cos(2\pi f + \varphi)$; $f \approx 3 \text{ GHz}$ is the resonant frequency of the cavity and $\varphi$ a phase that assures that the electron pulse does not experiences any net gain or loss of energy. The choice of a frequency of 3 GHz was made to benefit from the existing S-band technology used by the RF accelerator community, in which this frequency is a standard.

![Figure 18. Layout of a hybrid DF-RF FED setup.](image)

The electron bunch is represented by a colored gradient where faster electrons are in violet and slower electrons in red. The electron pulse is generated via the photoelectric effect. This part is essentially the same as in a compact DC electron gun. The longitudinal momentum-space distributions within the electron bunch are illustrated below. The effect of the axial RF electric field is to invert the longitudinal momentum–space distribution causing the electron bunch to recompress during its propagation towards the sample, which is located at the temporal focal point. Magnetic lenses (MLs) are used to control the transverse dimension of the electron beam. Figure adapted from Reference [4] with permission from IOP Publishing.

N-particle simulations [236] and an experimental demonstration [237] showed that such an approach can indeed provide ultrashort electron bursts containing $#e^- > 10^6$. However, laser-RF synchronization noise has limited (until very recently, see below) the instrument response of hybrid DF-RF FED setups to about 300–400 fs [238,239]. Ultrabright fs-electron bunches provided unique
insights into photoinduced phenomena in strongly correlated materials including labile and poorly conductive organic crystals. Figure 19 shows some characteristic results obtained by Gao et al. [41] and Morrison et al. [189] in the FED study of (EDO-TTF)$_2$PF$_6$ and VO$_2$, respectively.

**Figure 19.** Movies recorded with 100-kV hybrid DC-RF FED setups. Key molecular motions leading to charge delocalization in (EDO-TTF)$_2$PF$_6$. (a–c) Photoinduced time-dependent structural changes in (EDO-TTF)$_2$PF$_6$. (a) Differences between the diffraction patterns of the photoinduced phase and the initial low temperature (LT) phase as a function of $t$. (b) Difference between the diffraction patterns of the high-temperature (HT) and LT phases. Formation of a photo-induced transient intermediate structure (TIS). (c) Unit cells illustrating the arrangement of EDO-TTF molecules and PF$_6$ counter-ions in the LT-unit cell. Major structural changes are illustrated using different background colours in the central unit cell: flat EDO-TTF moieties have a green background, bent EDO-TTF moieties have a pink background, and PF$_6$ anions have a cyan background. Green sticks denote the atomic displacements from the initial LT structure to the TIS (left) and the HT-type structure (right); displacements were magnified 10 and 5 times, respectively, for clarity. (d) Evolution of phase-transition parameter $\xi$ in a $(\xi_F, \xi_B, \xi_P)$-Cartesian configuration space (left) and each of its components as a function of $t$ in the formation of TIS (right), $F, B$ and $P$ denote flat, bent EDO-TTF, and PF$_6$ moieties, respectively. Figure adapted from Reference [41] with permission from Springer Nature. Photoinduced metal-like phase of monoclinic VO$_2$. (e–h) Photoinduced time-dependent structural changes: (e) background-subtracted FED data from $t = 0$ to 20 ps. Vertical lines indicate different groups of reflections that are relevant to monitor the monoclinic (M1) to rutile (R) photoinduced structural transition. (f) Overall differences in the diffraction intensities from $-0.5$ to 20 ps. (g) Time-resolved diffraction intensity changes showing fast ($\approx 300$ fs) and slow ($\approx 1.6$ ps) dynamics. (h) Fluence dependence of the fast and slow signal amplitudes as measured for two selected Bragg reflections; inset, transient transmittance measurements. (i) Diffraction difference spectrum for the fast dynamics from $-0.5$ to 1.5 ps. The change in diffracted intensity is plotted with respect to $-1$ ps. (j) Diffraction intensity difference for the slow dynamics. The change in diffracted intensity from 2 to 10 ps (referenced to 2 ps) is shown. Figure adapted from Reference [189] with permission from Science AAAS.

Gao et al. [41] studied the formation of a light-induced TIS in (EDO-TTF)$_2$PF$_6$ that is distinct from its LT and HT phases but resembles optical properties of the HT metallic phase [240,241]. Morrison et al., [189] on the other hand, discovered a metal-like M1 phase of VO$_2$; see hatched...
region in Figure 19c, in which electronic and nuclear degrees of freedom are decoupled, suggesting that the insulating properties of VO$_2$ may arise from Mott physics.

Different synchronization methods have been put forward to reduce the timing jitter noise in hybrid ultrabright DC-RF FED setups [242–244] in order to bring this technology to its maximum potential. An elegant and convenient approach that solved this long-lasting problem has been recently demonstrated by Otto et al. [244] who brought the noise level (long term >10 h) below 50 fs (rms)—limited by the resolution of their streak camera. Their lockbox is based on the use of an ultrabroadband photodiode (12.5 GHz), a low phase-noise CW amplifier, and a bandpass filter that produces the high harmonic signal that drives the RF cavity and acts as a reference in a phase feedback loop, i.e., a phase comparator that feeds from an antenna integrated into the cavity. With the time arrival jitter under long-term control, more exciting results are expected to come from these ultrabright electron sources as Siwick’s team plans to commercialize their lockbox.

In addition to RF pill lens for electron pulse compression, the use of intense few-cycle THz pulses has recently emerged as a means to control ultrabright electron bunches [245]. Figure 20 illustrates the experimental layout implemented by Kealhofer et al. [245] for THz compression and electron pulse characterization. The authors used butterfly-shaped metal resonators to mediate the interaction between the electrons and the THz fields. The first resonator in the beam path acts as a compressor whereas a second unit serves as a streaking device. It should be noted that the implementation of THz pulses instead of RF cavities nearly eliminates the timing jitter drifts that were found to be as small as 4 fs (rms). Thus, Kealhofer et al. [245] demonstrated a technique that will certainly find applications in the field of ultrafast structural dynamics.

![Figure 20. All-optical control and metrology of electron pulses.](image)

**Figure 20. All-optical control and metrology of electron pulses.** Experimental setup: a 1-ps laser pulse from a Yb:YAG regenerative amplifier is frequency doubled and generates an electron pulse from a thin-film gold photocathode. The laser also drives two optical-rectification stages, each generating single-cycle THz pulses with energy of up to 40 nJ. (Inset) THz resonator structures are laser-machined in a 30-mm-thick aluminum foil. The first element, used for compression, is oriented at 45° to the electron beam, providing time-dependent longitudinal forces on the electrons. The second THz resonator, used for streaking, is oriented normal to the beam, resulting in time-dependent transverse deflection. Figure adapted from Reference [245] with permission from Science AAAS.

3.7. Ultrabright Relativistic FED Setups: RF-Photoinjectors

RF-photoinjectors are capable of producing ultrabright and ultrashort electron bursts, which are currently exploited as probes in relativistic FEDs. The use of radiofrequency allows for routine extraction fields $\approx 100$ MVm$^{-1}$ to be attained. Additionally, RF-photoinjectors are capable of producing ultrabright and ultrashort pulses of electrons with kinetic energies that are usually within the range of 1–5 MeV for FED measurements.

At these energies, the space-charge effects that lead to pulse broadening are largely suppressed due to relativistic effects that diminish Coulombic repulsion in by a factor of $\gamma^2$ in both the longitudinal and transverse directions [246]. The progress in the development of relativistic FED setups over the last 10 years has been tremendous. Photoinjectors were originally optimized for higher bunch
charges $\#e^- > 10^9$ (instead of $\#e^- \approx 10^6$–$7$) as well as for higher kinetic energies to be used as sources in XFELs. Relativistic FED was found to be of great importance to XFELs since the generation of high-quality low emittance electron beams are beneficial to both technologies. University-based pioneering MeV FED setups have been developed at UCLA [184,207] and Osaka, [187,247] and later launched at BNL, [192] SLAC [171–173,193–196] and DESY [248,249]. The amount of existing knowhow in accelerator centers has been critical to obtain stable RF-photoinjectors with minimal laser-RF timing noise to reach $\approx 100$ fs (rms) temporal resolution [250].

Recent results obtained at the MeV-UED line of SLAC are shown in Figure 21 for the study of CH$_3$I in the gas phase. Relativistic FED is the ideal tool for monitoring structural dynamics in molecular beams. Electron pulses moving at near the speed of light are necessary to avoid temporal broadening caused by velocity mismatch between the optical pump pulse and the electron probe pulse [4,251]. Yang et al. [173] conducted the first direct observation of a nuclear wave-packet with atomic spatiotemporal resolution during nonadiabatic processes involving conical intersections. More experiments with similar level of details are expected for the investigation of ultrafast structural dynamics in the gas phase.

![Figure 21. Relativistic ultrafast gas-phase electron diffraction.](image-url)

(a) Schematic of relativistic FED experiment. (b) A model for a CF$_3$I molecule oriented along the laser polarization axis. (c) Simulated pair distribution function (PDF) for a molecular ensemble with a $\cos^2 \theta$ angular distribution. (d) A model for a CF$_3$I molecule oriented perpendicular to the laser polarization. (e) Simulated PDF for a molecular ensemble with a $\sin^4 \theta$ angular distribution. The laser polarization is indicated by the double-headed arrow. Gray, light green, and purple represent carbon, fluorine, and iodine, respectively. (f) Potential energy surfaces depicting the two-channel excitation in CF$_3$I along the C–I bond length coordinate, with major states labeled and reaction pathways marked by arrows. Color coding indicates different electronic states and highlight the complexity of reaction. (g) Experimental $\Delta$PDF$_\parallel$. The dashed line at 200 fs shows a rough separation between contributions from the one-photon and the two-photon channels. (h) Experimental time evolution of $\Delta$PDF$_\parallel$ at 2.14, 2.52, and 2.90 Å. A comb illustrates the first two periods of the C–I stretching vibration. (i) Simulated $\Delta$PDF$_\perp$ of the two-photon channel. (j) Simulated time evolution of $\Delta$PDF$_\perp$ at 2.14, 2.52, and 2.90 Å. Figure adapted from Reference [173] with permission from Science AAAS.
3.8. Compact Ultrafast Low-Energy FED: Metallic Tip as Coherent Electron Sources

The use of sharp field emission tips triggered by fs-laser pulses [252–262] provides a unique alternative to reach the required transverse source coherence for the ultrafast dynamical study of large molecular structures. Low-energy fs-electron sources based on field emitters are attracting increasing interest in the community. Emission from an atom wide tip should in principle reach the quantum limit opening opportunities for lensless imaging (or point projection) [259,263–265] and coherent diffraction [260,266]. Figure 22 outlines results obtained by Müller et al. [259] for the study of ultrafast photocurrents in nanowires. The authors implemented a point projection that conferred sub-100 fs temporal and ≈10 nm spatial resolutions. Müller et al. [259] demonstrated an imaging tool capable of monitoring small electric fields around semiconductor nanowires (NWs) and photocurrents by taking advantage of the high sensitivity of sub-keV fs-electron pulses combined with the large magnification of their point projection source.

![Figure 22. Setup for time-resolved low-energy electron point projection mode (PPM).](image)

(a) PPM operating principle: photoelectrons, generated from a nanotip by an ultrashort laser pulse, are accelerated towards the sample positioned several μm away from the tip. A pump laser pulse, variably delayed from the electron probe, photoexcites the sample. An electrostatic lens is used to switch between divergent and collimated (not shown here) diffraction modes. (b–d) Point projection microscopy of axially doped NWs. InP NWs (radius 15 nm, length 3.5 mm) with p-i-n axial doping profile and 60-nm i-segment in the center are spanned across 2-μm holes in a gold substrate. Instead of being a real shadow image of the objects shape, projection images are strongly influenced by local fields surrounding the NW. In addition, a spatial inhomogeneity (marked by the white arrows in (c)) is observed (d). (e–g) Femtosecond imaging of ultrafast photocurrents. (e) Projection image of the same NW as in panel (b) recorded in pulsed fs-PPM mode at negative t. Photoexcitation by an ultrashort laser pulse leads to a transient, spatially inhomogeneous change of the projected NW diameter (h, normalized difference plot). Data recorded at 70 eV electron energy; scale bars: 500 nm.
Different dynamical behavior and amplitudes of the transient diameter change $\Delta d_{\text{NW}}$ are observed for the p- and n-doped segments along the NW (f), where an empirical three-exponential function was fitted to the data. Both segments show a fast initial photoinduced effect with 10–90 rise times in the p- and n-segments of 140 and 230 fs, respectively, followed by multi-exponential decay on the fs-to-few picosecond time scale. As $\Delta d_{\text{NW}}$ is directly proportional to the transient electric field change, the derivative $\Delta d_{\text{NW}}/dt$ plotted in the inset in (f) is a direct measure of the instantaneous photocurrent inside the NW. Surface states cause effective radial doping leading to band bending at the NW surface as sketched in (g), where $r$ is the radial coordinate, causing a radial photocurrent of electrons, $j_{r}$, and holes, $j_{h}$, after photoexcitation. This leads to a pump-induced transient shift $\Delta$ of the energies of the conduction band edge (ECB) and valence band edge (EVB), and hence a shift of the vacuum level ($E_{\text{vac}}$) (red shaded area), compared to the reference level $E_{\text{ref}}$ (given by the environment), with the magnitude of the shift depending on the specific band bending and doping level. Figure adapted from Reference [259] with permission from Springer Nature.

The advances in tip-based photoemitters and nanofabrication techniques have made it possible to achieve ps-resolution with ultrafast low-energy electron diffraction (ULEED) in backscattering mode. Storeck, Vogelgesang et al. [261,262] developed a novel $\mu$m-sized electron gun, which can be brought close to the investigated surface to diminish temporal broadening. The $\mu$m-sized electron source is presented in Figure 23 alongside ULEED results obtained in the study of 1T-TaS$_2$. The significantly improved spatial resolution of this tip source allowed for spot-profile analysis, resolving the phase-ordering kinetics in the nascent incommensurate charge density wave phase.

![Figure 23. Ultrafast low-energy electron diffraction (ULEED) setup and high-resolution diffraction pattern from 1T-TaS$_2$.](image)

Figure 23. Ultrafast low-energy electron diffraction (ULEED) setup and high-resolution diffraction pattern from 1T-TaS$_2$. (a) Schematic of the experimental setup for ULEED. Inset: electron micrograph of an electrochemically etched tungsten tip used as a photoemitter. (b) $\mu$m-sized laser-driven electron gun. Inset: tungsten tip, visible through the hole for laser illumination. (c) Electron pulse durations of the $\mu$m-sized electron gun (16.4 ps at 100 eV) and the $\mu$m-sized electron gun (1.4 ps at 50 eV). (d) $\mu$m-sized electron gun prepared by nanofabrication. (e) LEED pattern of the near commensurate CDW room-temperature phase, recorded with pulsed 100-eV electrons from the $\mu$m-sized electron gun (logarithmic colour scale). A retarding voltage of $-20\,\text{V}$ is applied at the detector front plate. (f) Line profile of the (1 T) diffraction peak, illustrating high transversal coherence of the source. The fitted spot width of 0.03 Å$^{-1}$ (fwhm) corresponds to a transfer width of 21 nm. (g) Close-up of region marked in e, showing second-order CDW diffraction spots (h). Line profile of CDW diffraction spots shown in g, fitted with Lorentzian peak profiles. Figure adapted from Reference [262] with permission from Springer Nature.

4. Conclusions

The future of fs-X-ray and fs-electron sources is very bright with several XFEL facilities readily available for use and a relatively small but quickly growing community of FED developers. There are other promising techniques for the generation of ultrashort electron pulses, which have not been discussed here. For instance, laser plasma electron accelerators [267–273] are quickly improving
through the reduction of the large energy spread that has limited their application as FED sources. Another interesting candidate is the cold-atom electron source, [202,274–281] which has recently been proposed as an alternative to photoinjectors owing to the large reduction in electron beam emittance that should considerably improve the X-ray beam properties. Moreover, important advances have been made in the development and implementation of dynamic and ultrafast electron microscopes [3,282–289]. We are already transiting the era of atomically resolved movies, with more advanced experiments and exciting discoveries soon to come.

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**References**


23. Travaglini, G.; Wachter, P.; Marcus, J.; Schlenker, C. The Blue Bronze K


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