Auto-Generation System Based on Fractal Geometry for Batik Pattern Design

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Featured Application: This study proposes an auto-generation system for batik patterns design, which is conducive to the spread and promotion of intangible culture such as batik. Ordinary users can use this system to generate their favorite batik patterns for personalization. The system can assist in the creation of batik patterns to promote artistic creation.

Abstract: In order to obtain the automatic simulation generation of traditional handmade batik patterns in a computer, this paper proposes the automatic generation method of batik flower patterns based on fractal geometry. Firstly, we analyze the fractal characteristics of batik flowers and design an automatic flower generation algorithm based on a two-dimensional iterated function system (IFS) and a curve function. The algorithm forms a complete flower pattern. Secondly, a nonlinear function is defined and the flower pattern is introduced into the nonlinear function to iterate and change. On this basis, we present an automatic generation method of different distribution patterns for flower patterns which obtains the most effective range of each parameter value for each function. Finally, in order to verify the feasibility of the automatic generation method of batik flower patterns, we develop an automatic generation experiment system for batik patterns via an interactive way of working. The results show that the user or designer can quickly and automatically simulate a series of flower patterns by changing the relevant parameter values, realizing the digitization and innovative design of the pattern and enriching the batik pattern base.

Keywords: fractal geometry; iterated function system; flower pattern; batik; auto-generation

1. Introduction

Batik is one of three printing techniques which were used in ancient China. It is a handicraft of traditional textile printing and dyeing performed by ethnic minorities in China and is part of the outstanding intangible cultural heritage of China. Batik patterns overwhelmingly have high artistic value and have recorded and expressed the development, changes, and spread of Chinese minority culture. Various elements are first combined to form a series of basic patterns which are then repeated and combined in order to produce a complete batik pattern, as shown in Figure 1. The layout map usually consists of a four-square layout and is obtained by the repeated transformation of a single pattern. Typically, the main pattern is selected, transformed, and then a dotted decorative pattern is added to create a final layout pattern. These basic patterns are obtained by depicting objects in the natural environment, and mainly include natural patterns and geometric patterns, with the natural patterns including animal patterns and plant patterns [1].
Plant patterns mainly include leaves, chrysanthemums, lotuses, peaches, sunflowers, cockscombs, and so on. Guizhou ethnic minorities live in a natural environment of beautiful mountains and rivers and the beautiful scenery inspires their creation. The patterns are painted with bold changes and exaggerated treatment without being limited by the real objects. The flowers and plants in the mountain stream become the objects of creation because they can draw out varieties of the subject matter by the sort of plants and flowers’ appearance with disparate style. Guizhou batik uses a large number of plants and flowers which can not only be seen everywhere in daily life but also contain good wishes and hopes [2]. Flowers are a common and popular plant pattern, because they represent the prosperous and propitious wishes of the family.

The traditional batik production method is purely manual. It is of extremely low production efficiency, which is not conducive to the spread, development, and promotion of intangible cultural heritage. It is a mode of work which is not conducive to the individualization of batik patterns in batik products nor the intelligent upgrade of China’s printing and dyeing industry. As a result, computer graphics have begun to be used in pattern design to convert traditional batik patterns into digital patterns. Intelligent design technology used to generate digital patterns is not only conducive to the digital protection of traditional batik and enriching the diversity of batik patterns but also can adapt to the intelligent upgrading of China’s printing and dyeing industry. The automatic generation system proposed in this paper can not only adapt to the intelligent upgrade of the printing and dyeing industry but also promote the development of the printing and dyeing industry, and is conducive to the dissemination and promotion of non-material culture such as batik. Ordinary users can use the system to generate favorite batik patterns for personalization. Designers can use the system to assist in the artistic creation of batik patterns to facilitate artistic creation.

Applying digital technology to the design of traditional batik patterns can significantly enrich the batik patterns. Zhang Xiaohong [3] has proposed combining fractal matrix iteration with the automatic evolution of cloud model cells and has generated a large number of fractal patterns by setting times of iteration and evolution. However, the details of the artistic pattern generated are uncertain. Cui Jia [4], based on the shape grammars method, has used a free B-spline curve in the Zhuang embroidery design to derive an initial design concept and a new difference algorithm. Its feature matrix, however, is specified by the expert or system designer and cannot be adjusted automatically. Li Shiguang [5] has proposed a specific method for simulating batik printing patterns according to the characteristics of cracks in batik printing patterns, which can only produce cracks related to batik patterns. In order
to solve the shortcomings, as mentioned above, of the generated patterns, this paper proposes an automatic generation method of batik flower patterns based on a fractal geometry iterated function system (IFS). It can not only effectively simulate traditional hand-dyed batik flower patterns but also quickly and automatically simulate a series of flower patterns by changing the relevant parameter values to realize the digital design of the batik flower pattern.

The paper is organized as follows. In Section 2 we briefly introduce the current state of fractal geometry and fractal pattern generation. The fractal features of batik flower patterns and the fractal method of IFS are introduced in Section 3. The flow of the algorithm and the automatic generation process is presented in Section 4. After the experiment and analysis, the valid value of each parameter in the algorithm function is obtained in Section 5. The automatic generation system for batik patterns is introduced in Section 6. In Section 7 we analyze and compare the features of original batik patterns and generated patterns. Finally, conclusions and future work are given in Section 8.

2. Related Work

2.1. Fractal Geometry

Fractal geometry, also known as “nature’s geometry”, is a kind of geometry that studies irregular geometry. Irregular geometry refers to those seemingly chaotic rules with specific internal laws, such as meandering coastlines and rolling mountains. The research object of traditional geometry is the integer dimension, e.g., zero-dimensional points, one-dimensional lines, two-dimensional surfaces, and three-dimensional solids. The research object of fractal geometry is a non-negative real number dimension such as 0.63.

On that basis, fractals have the following characteristics [6].

1. Self-similarity, which may include precise self-similarity—the same at all scales; quasi-self-similarity—similar patterns on different scales, where small copies of the entire fractal may contain distorted and degenerate forms; statistical self-similarity—random repetition of a pattern so that a number or statistical measurement remains across scales [7]; qualitative self-similarity—such as time series [8]; or multifractal scaling [9–12]—represented by multiple fractal dimensions or scaling rules.

2. Fine or detailed structure on any small scale. The result of this structure is that fractals may have emergent properties [13].

3. Local and global irregularities are not easily described in traditional Euclidean geometric languages. For images of fractal patterns, this has been expressed by phrases such as “smoothly stacked surfaces” and “whirlpools on vortices” [14].

Fractals can be created by the following fractal generating technologies.

1. IFS—uses fixed geometric replacement rules; may be stochastic or deterministic [15,16].
2. Strange attractors—use iterations of a map or solutions of a system of initial-value differential or difference equations that exhibit chaos.
3. L-systems—use string rewriting; may resemble branching patterns or turtle graphics patterns [17,18].
4. Escape-time fractals—use a formula or recurrence relation at each point in a space (such as a complex plane); usually quasi-self-similar; also known as “orbit” fractals.
5. Random fractals—use stochastic rules.
6. Finite subdivision rules—use a recursive topological algorithm for refining tiling [19] and are similar to the process of cell division [20].

Hence, in this paper, fractal geometry can be used to generate flower patterns with self-similarity, self-affine, and scale-free characteristics.
2.2. Fractal Pattern Generation

At present in the reprinting and dyeing industry, pattern generation based on fractal geometry is a research hotspot. Hariadi [21] has used the Fourier transform to directly generate a batik master pattern with fractal features. Aswin [22] has proposed a fractal pattern generated by an L-system as a decorative pattern. In the literature [23–25], starting from the fractal characteristics of the batik pattern, the above fractal technique has been used to generate various fractal patterns similar to traditional batik patterns. The fractal pattern is similar to the traditional batik pattern in spirit but not in shape. Muhamad [26] and his team, the “Pixel People Project”, developed the software jBatik for the simulation of Indonesian-style digital wax patterns based on fractal algorithms; the software is not universal for printing and dyeing patterns in other areas such as China and Africa, however.

Zhang Dongya [27] has used Visual Basic language to study single-rule and multi-rule algorithms in a deterministic L-system and has obtained a rich and varied L-system graph by transforming the parameters in the algorithm. However, only a few pattern generation methods can be implemented, so it is necessary to study the generation characteristics and rules of other types of maps. Yuan Qingni [28] has proposed using an iterated function system to generate a bionic butterfly pattern as a batik pattern. However, this method can only generate butterfly patterns and is not universal. Zhang Xinwei [29] has improved the shape grammar and applied it to the formal expression of pattern configuration and at the same time has proposed the manual and automatic extraction of configuration based on this method. However, this method cannot extract fractal patterns, and the efficiency of the algorithm has room for improvement.

Yuan Huifen [30] has proposed a fractal pattern generation method based on the matrix Kronecker product and has applied it to the design of Wangjiang cross stitch. It is necessary, however, to establish a pattern Boolean matrix model and carry out multilevel fractal processing. Wang Shuhuan [31] has used the programming software Visual Basic6.0 to study the generation method of the Mandelbrot set and Julia set on a complex plane to realize its visualization. A series of varying fractal maps were obtained by changing the form of the iterative function and the fractal pattern was applied to the textile using printing techniques. However, the fractal image needed to be selected and processed with the help of Photoshop which is an image processing software. Lu Lisa [32] has used the C++ language to write a fractal pattern based on generator and escape time algorithms and has conducted a secondary design of the generated pattern in pattern design software. Finally, the designed pattern program was woven.

In this paper, fractal geometrics using a combination of an iterated function system and curve function can not only automatically generate batik flower patterns but also can automatically generate a series of different flower patterns merely by modifying the parameter values.

3. Fractal Characteristics of Batik Patterns and Fractal Algorithms

3.1. Fractal Characteristic of Batik Flower Patterns

The batik pattern is of symbolic significance. The flower pattern of traditional batik indicates the prosperous and propitious wealth of the family. In Figure 2, we can see that the batik flower pattern has a self-similar characteristic. In the first pattern, the inner and outer petals are quasi-self-similar. In the second pattern, the outer layer of the dotted pattern in the petals is self-similar to the central pattern. In the third and fourth patterns, with regard to the boundary contour of the petals, these are obtained by affine changes of an individual petal. That is to say, these patterns of the flower have same or similarly shaped features in different hierarchies. There is a relationship between the different hierarchies that governs enlargement, reduction, or affine change. It can be seen that this is a self-similar pattern because fractal patterns can be almost the same at different levels and fractal geometry can be applied to the design of batik flower patterns. It can be seen from Figure 1 that the
overall layout of the batik pattern is mainly symmetrical, double-square, four-square, or circular. These layouts have the self-similarity, self-affine, and scale-free characteristics of fractals.

![Figure 2. Batik flower patterns.](image)

3.2. Iterated Function System

IFS is one of the most commonly used fractal methods. The graphics generated by this method are self-similar. Fractal geometry is dissimilar from traditional geometry. The fractal graph produced by the IFS is usually not an integer dimension and can be of an arbitrary dimension. The fractal graph is usually calculated and drawn in a two-dimensional plane space.

A two-dimensional IFS is a finite collection of n functions $F_i$ from $\mathbb{R}^2$ to $\mathbb{R}^2$. The solution of the system is the set $S$ in $\mathbb{R}^2$ (and hence an image) that is the fixed point of Hutchinson’s recursive set equation [33]:

$$S = \bigcup_{i=0}^{n-1} F_i(S),$$

In Equation (1), as implemented and popularized by Barnsley [34], the functions $F_i$ (see Equation (2)) are linear (technically they are affine as each is a two by three matrix capable of expressing scale, rotation, translation, and shear):

$$F_i(x, y) = (a_ix + b_iy + e_i, c_ix + d_iy + f_i),$$

In order to facilitate the proofs and guarantee convergence of the algorithms, the functions are normally constrained to be contractive, that is, to bring points closer together.

4. Auto-Generation Algorithm Based on Fractal Geometry

In this work, an auto-generation algorithm based on fractal geometry was used to design batik flower patterns. Two-dimensional IFS implemented the algorithm in the fractal method. The algorithm mainly includes two parts: generation of essential flower patterns and generation of different flower layout patterns. In the first step, the essential elements of flower leaves are generated through a superellipse curve function and iterated repeatedly to create the flower leaves pattern. In the second step, the essential elements of petals are generated by the function of the rose curve and are repeatedly iterated to generate the pattern of the petals. In the third step, the pistil pattern is generated by the Hypocycloid function. In the fourth step, the function of the rose curve and circular curve is used to generate the pattern of the flower core and an entire flower pattern is generated by combining the above patterns. In the fifth step, the transformation function is used to iterate the entire flower pattern to generate various pattern layouts. According to the number of iterations, a flower pattern layout such as a symmetrical layout, double-square layout, or four-square layout can be generated. The algorithm flow is shown in Figure 3.
4.1. Generating the Flower-Leaves Pattern

The basic shape of the flower-leaves was based on a generalization of the Gabriel Lame curve or the superellipse curve, which is a closed curve similar to an ellipse which retains the geometric features of the semi-major axis and the semi-minor axis but has different overall shapes. In the Cartesian coordinate system, the curve equation may be given as

\[
\frac{x^n}{a^n} + \frac{y^n}{b^n} = 1 \quad \text{or} \quad \begin{cases} 
    x(t) = a \times \left| \cos(t) \right|^\frac{n}{2} \times \text{sgn}(\cos(t)) \\
    y(t) = b \times \left| \sin(t) \right|^\frac{n}{2} \times \text{sgn}(\sin(t)) 
\end{cases},
\]

where \( a, n, a_n, b \) are positive numbers. When \( n \) is a positive number \( p/q \), each quadrant of the hyperelliptic curve is a \( p/q \)-order planar algebraic curve [35]. In particular, when \( a = b = 1 \) and \( n \) is an even number, it is an \( n \)-order Fermat curve. In this case it is non-singular but in general it is singular. If the numerator is not even, the curves are stitched together from portions of the same algebraic curve in different directions.

Thus, after the proper transformation of form, the superellipse curve equation applicable to the Cartesian coordinate system is obtained, and may be written as

\[
\begin{align*}
    x(t) &= r_1 \times |\cos(t)|^\frac{n}{2} \times \text{sgn}(\cos(t)) \\
    y(t) &= r_2 \times |\sin(t)|^\frac{n}{2} \times \text{sgn}(\sin(t))
\end{align*}
\]

with \( a, b > 0, t \in [0, \pi] \),

\[
x(t) = r_1 \times |\cos(t)|^\frac{n}{2} \times \text{sgn}(\cos(t)) \\
y(t) = r_2 \times |\sin(t)|^\frac{n}{2} \times \text{sgn}(\sin(t))
\]

\[ a, b > 0, t \in [0, \pi] \]

\[
\frac{x^n}{a^n} + \frac{y^n}{b^n} = 1 \quad \text{or} \quad \begin{cases} 
    x(t) = a \times \left| \cos(t) \right|^\frac{n}{2} \times \text{sgn}(\cos(t)) \\
    y(t) = b \times \left| \sin(t) \right|^\frac{n}{2} \times \text{sgn}(\sin(t)) 
\end{cases},
\]
where \( r_1 \) represents the length of the semi-major axis and \( r_2 \) represents the length of the semi-minor axis. Note that \( t \) is not a fixed angle of the figure but is just a parameter.

Hence, we can apply the nonlinear function \( V_0 \) to generate the essential elements of the flower leaves.

\[
V_0 : \begin{cases} 
    x(t) = l \times 2 \times |\cos(t)|^a \times \text{sgn}(|\cos(t)|), l \in [0, 1], t \in [0, \pi] \\
    y(t) = l \times 0.5 \times |\sin(t)|^b \times \text{sgn}(|\sin(t)|), a > 0, b > 0 
\end{cases}
\]

(6)

In Equation (6), the parameters \( a \) and \( b \) jointly control the shape of the flower-leaves pattern and the parameter \( l \) controls the size of the flower-leaves pattern.

Subsequently, repeated iterations are carried out based on function \( V_0 \) and each iteration function is represented by \( V_{0j} \), but each iteration is only a repeated mapping of the graph. Then, a mixed vector coefficient \( V_{ij} \) is introduced to change the pattern of repeated mapping. So

\[
F_{0i}(x, y) = \sum_{j} v_{ij} V_{0j}(x, y),
\]

(7)

where the iteration parameter \( i \) is an integer that changes sequentially from 0 to \( n-1 \). Using this extension, we obtain the flower-leaves pattern function \( F_{0}(x, y) \) based on Equation (7), as shown in Figure 4a.

4.2. Generating the Petals Pattern

The basic shape of the petals was generated based on a rhodonea curve or a rose curve, which was plotted in the polar coordinate system as \([36,37]\)

\[
\rho = \cos(n\theta) \text{ or } \rho = \sin(n\theta),
\]

(8)

where \( n \) is a positive integer. Where \( n \) is an even number, when the value of \( \theta \) changes from 0 to 2\( \pi \), the entire graph of the rose will be accurately drawn once. When \( n \) is an odd number, this will occur in the interval between 0 and \( \pi \).

Thus, after the appropriate transformation of form, the rose curve equation applicable to the Cartesian coordinate system is obtained, and can be written as

\[
\begin{cases} 
    x = a \cos(nt) \cos(t) \\
    y = a \cos(nt) \sin(t) 
\end{cases}, \quad t \in [0, 2\pi],
\]

(9)

where \( a \) represents the length of the petals, the number of petals is \( n \) when \( n \) is odd, and the number of petals is \( 2n \) when \( n \) is even. The value of \( t \) ranges from 0 to 2\( \pi \).

We can therefore apply the nonlinear function \( V_1 \) to generate the basic elements of the petals, i.e.,

\[
V_1 : \begin{cases} 
    x = a_1 \cos(2t) \cos(t) \\
    y = a_1 \cos(2t) \sin(t) 
\end{cases}, \quad t \in [0, 2\pi],
\]

(10)

where \( a_1 \) represents the length of the petal, at which point \( n \) takes a value of 2, and the value of \( t \) ranges from 0 to 2\( \pi \), meaning four petals can be generated for each iteration.

Subsequently, repeated iteration was carried out based on function \( V_1 \). \( V_{1j} \) represents each iteration function, but each iteration is only the repeated mapping of graphs. Then, a mixed vector coefficient \( V_{ij} \) is introduced to change the pattern of repeated mapping. So

\[
F_{1i}(x, y) = \sum_{j} v_{ij} V_{1j}(x, y),
\]

(11)

where the iteration parameter \( i \) is an integer that changes sequentially from 0 to \( n-1 \). Using this extension, we obtain the petal pattern function \( F_{1}(x, y) \) based on Equation (11), as shown in Figure 4b.
4.3. Generating the Pistils Pattern

A star shape which was generated based on the circular hypocycloid was used as the basic shape of the pistils. In geometry, the hypocycloid is a special planar curve produced by a trajectory fixed on a small circle that rolls within a larger circle. It is equivalent to a cycloid, but it is not a circle that scrolls along a line, rather, it scrolls within a circle. If the smaller circle has a radius $r$ and the larger circle has a radius $R = kr$, the parametric equation of the curve can be given in any of the following ways:

$$
\begin{align}
    x &= (R-r) \cos(\theta) + r \cos\left(\frac{R-r}{r} \theta\right) \\
    y &= (R-r) \sin(\theta) - r \sin\left(\frac{R-r}{r} \theta\right) \\
\end{align}
$$

In Equation (11), if $k$ is a rational number, such as in the simplest terms $k = p / q$, then the curve has $p$ cusps. If $k$ is an irrational number, the curve never closes and fills the space between the larger circle and the circle of radius $R - 2r$.

Thus, after the proper transformation of form, the circular hypocycloid equation applicable to the Cartesian coordinate system is obtained, and can be written as

$$
\begin{align}
    x &= \frac{r}{q} ((q-1) \cos(t) + \cos(qt-t)) \\
    y &= \frac{r}{q} ((q-1) \sin(t) - \sin(qt-t)) \\
\end{align}
$$

where $r$ is the length of the pistil, $m$ is the number of pistils, and $n$ is used to control the shape of the cusps. We can therefore apply the nonlinear function $V_2$ to generate the basic elements of the stamens, i.e.,

$$
V_2:\begin{cases}
    x = \frac{r_i}{q} ((q-1) \cos(t) + \cos(qt-t)) \\
    y = \frac{r_i}{q} ((q-1) \sin(t) - \sin(qt-t)) \\
\end{cases},
$$

where $r_1$ represents the length of the pistil and $m$ represents the number of pistils and further determines the value of $n$ as 5.

Subsequently, repeated iteration was carried out based on function $V_2$. $V_{2j}$ represents each iteration function but each iteration is only the repeated mapping of graphs. Then, a mixed vector coefficient $V_{ij}$ was introduced to change the pattern of repeated mapping. So

$$
F_{2i}(x, y) = \sum_{j} v_{ij} V_{2j}(x, y),
$$

where the iteration parameter $i$ is an integer that changes sequentially from 0 to n-1. Using this extension, the pistil pattern function $F_2(x, y)$, based on Equation (15), was able to be obtained, and is shown in Figure 4c.

4.4. Generating the Flower-Core Pattern

The basic shape of the flower-core was generated based on the rhodonea curve or the rose curve and was expressed by the curve equation in the Cartesian coordinate system as follows:

$$
\begin{align}
    x &= \cos(nt) \cos(t) \\
    y &= \cos(nt) \sin(t) \\
\end{align}
$$

Thus, after the appropriate transformation of form, the rose curve equation applicable to the Cartesian coordinate system is obtained, and can be written as

$$
\begin{align}
    x &= a \cos(nt) \cos(t) \\
    y &= a \cos(nt) \sin(t) \\
\end{align}
$$
where $a$ represents the length of the petal and $n$ controls the number of petals. When $n$ is odd, the number of petals is $n$, and when $n$ is even, the number of petals is $2n$.

Then, the circular curve draws at the center of the flower, and Equation (18) in the Cartesian coordinate system is given as follows:

$$x^2 + y^2 = 1 \text{ or } \begin{cases} x = \cos(t) \\ y = \sin(t) \end{cases}$$

Thus, after the proper transformation of form, the circular curve equation applicable to the Cartesian coordinate system is obtained, and may be written as

$$\begin{cases} x = a \cos(t) \\ y = a \sin(t) \end{cases}$$

where $a$ is the radius of the circle and $t$ is in the range 0 to $2\pi$.

We can therefore apply the nonlinear function $V_3$ to generate the basic elements of the flower-core:

$$V_3 : \begin{cases} x_{31} = a_2 \cos(4t) \cos(t) \\ y_{31} = a_2 \cos(4t) \sin(t) \\ x_{32} = a_3 \cos(t) \\ y_{32} = a_3 \sin(t) \end{cases}, t \in [0, 2\pi],$$

Subsequently, repeated iteration was carried out based on function $V_3$. $V_{3j}$ represents each iteration function, but each iteration is only the repeated mapping of graphs. Then, a mixed vector coefficient $V_{ij}$ is introduced to change the pattern of repeated mapping. So

$$F_{3i}(x, y) = \sum_{j} v_{ij} V_{3j}(x, y),$$

where the iteration parameter $i$ is an integer that changes sequentially from 0 to $n-1$. Using this extension, the flower-core pattern function $F_3(x, y)$ based on Equation (21) was able to be obtained, as shown in Figure 4d.

4.5. Generating the Flower Pattern Layout

Through the above process we were able to obtain the complete flower pattern. At this time, we defined a non-linear function $V_4$, which we named $JuliaN$, and which contained the parameters $P_1 = JuliaN.Power$ and $P_2 = JuliaN.dis$, where $power$ affects the number of flower patterns and $dis$ affects the distance from each point of the flower pattern to the origin.

$$V_4 : \begin{cases} x = r \frac{t_1}{P_1} \cos(t_1) \\ y = r \frac{t_2}{P_2} \sin(t_2) \end{cases},$$

where $t_1 = \cos^{-1} \frac{x}{r} + \frac{2\pi}{P_1}$, $t_2 = \sin^{-1} \frac{y}{r} + \frac{2\pi}{P_2}$, $r = \sqrt{x^2 + y^2}$.

We therefore brought the complete flower pattern into function $V_4$ and at the same time carried out iteration and change. At this time, function $F_4(x, y)$ is defined as follows:

$$F_{4i}(x, y) = \sum_{j} v_{ij} V_{4j}(x, y),$$

In Equation (23), the parameter $V_{ij}$ is a mixed vector that causes the pattern of the repeated map to change, and the iterative parameter $i$ is an integer that changes sequentially from 0 to $n-1$.

The final transformation is like a non-linear camera. The entire flower pattern can generate different layouts by change the function $F_4(x, y)$. According to the different number of i iterations,
through the change of the iterative function $F_i(x, y)$, are able to obtain the symmetric layout, the double-square layout, and the four-square layout.

![Figure 4. Flower pattern generation process.](image)

5. Experiment and Analysis

Our automatic generation algorithm for batik flower patterns was implemented and completed in Python 3.6. In this experiment, several flower patterns and continuous layouts were generated by setting parameters in each function. By analyzing the experimental results, the most effective range of each parameter value in each function could be obtained.

5.1. Setting Parameters to Generate Flower Patterns

In this experiment we used parameter settings to generate the basic elements that make up the flower and the entire flower pattern. Nonlinear functions based on Equation (6) and Equation (10) generated the basic elements of flower-leaves and petals. According to Equation (7) and Equation (11), the parameters $a$, $b$, and $a_1$ affect the shapes of the flower-leaves, and petals. Among these, parameters $a$ and $b$ control the basic shape of the flower-leaves and parameter $a_1$ controls the size of the basic shape of the petals. We fixed the size of the petals and set $b_1 = 1$, that is, the length of the petals to 1. Figure 5 illustrates different basic shapes which were generated by setting the parameters as $a = 0.2$, $b = 1.0$, $a = 0.2$, $b = 5.0$, $a = 0.2$, $b = 10.0$, $a = 0.2$, $b = 20.0$, $a = 0.1$, $b = 10.0$, $a = 0.2$, $b = 10.0$, $a = 0.3$, $b = 10.0$, $a = 0.4$, and $b = 10.0$.

The nonlinear function based on Equation (14) generates the essential elements of pistils. According to Equation (15), the parameters $r_1$ and $m$ affect the shape of the pistil. Among these, parameter $r_1$ controls the size of the basic shape of the pistil and parameter $m$ controls the number of pistils, which are denoted by $m$.

The petal size and number of petals were fixed as $a_1 = 1$, i.e., the petal’s length is 1, and $n = 2$, i.e., the number of petals is 8. Figure 6 illustrates the different basic shapes which were generated by setting parameters as $r_1 = 0.6a_1$, $m = 16$, $r_1 = 0.7a_1$, $m = 16$, $r_1 = 0.8a_1$, $m = 16$, $r_1 = 0.9a_1$, $m = 16$, $r_1 = 0.8a_1$, $m = 8$, $r_1 = 0.8a_1$, $m = 8$, $r_1 = 0.8a_1$, $m = 16$, $r_1 = 0.8a_1$, and $m = 32$. 
The basic shape of the pistil is controlled by parameters \( r_1 \) and \( m \). Firstly, the value of parameter \( m \) was fixed to observe the influence of the change in parameter \( r_1 \) on the pattern. It was found that when the parameter \( r_1 = 0.8a_1 \), the obtained pattern was closest to the original pattern. Secondly, the influence of the change in parameter \( m \) on the pattern was observed for \( r_1 = 0.8a_1 \). It was found that when parameter \( m = 16 \), the distribution of pistils was neither sparse nor dense, and the obtained pattern was closest to the original pattern. Next, we used the basic graphs with \( a = 0.2, b = 10, r_1 = 0.8a_1, \) and \( m = 16 \) to conduct subsequent experiments to generate flower patterns.

The basic elements of flower-cores were generated by a nonlinear function based on Equation (20). According to Equation (21), the parameters \( a_2 \) and \( a_3 \) affect the shape of the flower-core. Parameter \( a_2 \) controls the size of the basic shape of the flower-core and parameter \( a_3 \) controls the size of the round shape of the flower-core. Figure 7 indicates different basic shapes which were generated by setting parameters as \( a_2 = 0.3a_1, a_2 = 0.4a_1, \) \( a_2 = 0.5a_1, \) \( a_2 = 0.6a_1, \) \( a_3 = 0.1a_2, \) \( a_3 = 0.2a_2, \) \( a_3 = 0.3a_2, \) and \( a_3 = 0.4a_2. \)
Parameter \( a_2 \) controls the basic shape of the flower-core. By observing Figure 7, we can see that the pattern obtained when \( a_2 = 0.5a_1 \) is closest to the original pattern. The parameter \( a_3 \) controls the size of the central circle. By observing Figure 7, we can see that the ratio between the two patterns is the most harmonious when \( a_3 = 0.2a_2 \).

The parameters of the entire flower pattern have values of \( a = 0.2, b = 10.0, r_1 = 0.8a_1, m = 16, a_2 = 0.5a_1 \), and \( a_3 = 0.2a_2 \).

5.2. Setting Parameters to Generate Layout Patterns of Flowers

We then generated different layout patterns of flowers based on the above experimental results. According to a transformation function based on Equation (23), we were able to find that different pattern layouts are generated by changing the values of parameters \( P_1 \) and \( P_2 \), where \( P_1 \) controls the number/density of flowers in the layout and \( P_2 \) controls the shape of these flowers. Through the experiments it was found that the valid value range of parameter \( P_1 \) was 2–6 and the valid value range of parameter \( P_2 \) was 0.1–1.0.

Figure 8 shows the pattern layouts for \( P_1 = 4, P_2 = 1P_1 \) and 0.618\( P_1 \) and level = 1, 2, 3, and 4. In these pattern layouts a fractal was produced by Equation (21) in which the flower pattern had the basic shape parameters \( a = 0.2, b = 10.0, r_1 = 0.8a_1, m = 16, a_2 = 0.5a_1, \) and \( a_3 = 0.2a_2 \).

![Figure 7](image1.jpg)

**Figure 7.** Different flower patterns generated by setting parameters \( a_2 \) and \( a_3 \).

![Figure 8](image2.jpg)

**Figure 8.** Layout patterns generated by setting parameters \( P_2 = 1P_1 \) and 0.618\( P_1 \) and level = 1, 2, 3, and 4.
Figure 9 shows the pattern layouts for $P_1 = 4$, $P_2 = 1$, $0.618P_1$ and $level = 1, 2, 3, 4$. In these pattern layouts we rotated the flower patterns of the above experiment by 45 degrees, after which a fractal was produced by Equation (23) in which the basic shape parameters of the flower pattern were $a = 0.2$, $b = 10.0$, $r_1 = 0.8a_1$, $m = 16$, $a_2 = 0.5a_1$, and $a_3 = 0.2a_2$.

By observing Figures 8 and 9 we can see that the value of parameter $P_1$ represents the number of flowers and the layout characteristics. Parameter $P_1 = 2$ gives two flowers and a symmetrical layout; parameter $P_1 = 3$ gives three flowers and a three-circle layout; parameter $P_1 = 4$ gives four flowers and a four-square layout; and parameter $P_1 = 5$ gives five flowers and a five-circle layout. Further, the parameter $P_2$ represents the shape change of each flower pattern.

Next we generated complete flower patterns based on basic flower patterns and constructed a basic batik flower frame based on a specific transformation of functions in where iterative calculations based on Equations (6), (10), (14), and (22) generated the flower patterns. Iterative calculations based on Equation (22) generated flower pattern layouts. Traditional batik flower patterns consist of a variety of decorative patterns, including geometric patterns. We were able to add some geometric patterns to our auto-generated flower patterns to produce beautiful batik patterns.

The essence of the L-system is that it is a rewrite system. Through the empirical generalization and abstraction of the plant object growth process, the state and description rules are initialized and a finite number of iterations are performed to generate a sequence of character which represents the topological construction of the plant. Geometric interpretation of the resulting string produces a very intricate fractal pattern.

Figure 10 shows the beautiful flower patterns which were generated with the geometric patterns added. By analyzing the layout characteristics of batik patterns it was able to be found that the layout characteristics are usually symmetrical or four-square. Therefore, in the final layout pattern, the four-square layout was used as an example. At this time $level = 2$ and the generation pattern can have both a four-square layout and a clear view of the internal structure of the flower. The application of an L-system automatically generates the geometric pattern in the figure. Each geometric pattern is a fractal pattern that is generated by iteration rules and is iterated using these rules.
6. System Implementation

In order to verify the feasibility of the above method, an automatic batik pattern generation system was developed in the operating system Windows XP using Python and Qt. The system uses an interactive working method to parameterize the batik patterns and the user or designer automatically generates a series of different batik patterns by changing the parameter values of the batik pattern.

The digital batik pattern generation system is divided into three major modules: a system work module, a parameter setting module, and a pattern library module. In the process of generating a pattern, the batik pattern is parameterized and the initial value of the batik pattern parameter is assigned to generate an initial batik pattern which is stored in the pattern database. The user can use the initial pattern or modify the initialization parameters to generate the desired batik pattern, return the pattern, and display it in the system. The specific work implementation process of the system is shown in Figure 11.

The system work module is shown in Figure 12. Area 1 is a menu command area, which can perform the essential operations of the transformation of the pattern. Area 2 is a selection of the pattern area, and the pattern to be drawn can be selected from the pattern library. Area 3 is the pattern display area, which is used to display the initial pattern and the pattern which is constructed after modifying the parameters. In this system, the user or designer can select the batik pattern to be drawn in Area 2, while the selected initial batik pattern or modified pattern is displayed in Area 3.
Figure 12. System work module.

The parameter setting module is shown in Figure 13. Area 1 contains the pattern variables, with the left side of the area being used to display the parameters of the pattern which can be changed and the right side being used to allow the input of the values of the parameters. Area 2 is the pattern layout area, the left side of which is used to display the parameters that control the pattern layout change and the right side to input the value of the parameters.

![Parameter setting module](image)

Figure 13. Parameter setting module.

The user selects the pattern to be drawn in the system work module. At this time, the first pattern is generated in the drawing module and the parameter setting module is used to modify the parameters to generate different basic patterns. Taking the flower pattern as an example, several flower patterns may be generated by changing the value of the flower variable, different layout patterns may be generated by changing the values of the layout variables. The parameter value of the flower variable may be adjusted to generate the basic flower pattern. At this point in our experiments, the parameters for controlling the shape of the flower-leaves were set to 0.2 and 20, the parameter for controlling the length of the petal was set to 1, the parameter for controlling the length of the pistil was set to 0.8, and the parameter for controlling the number of petals was set to 16. The parameter to control the length of the flower-core was set to 0.5 and the parameter to control the radius of the flower circle was set to 0.1, with the resulting pattern shown in Figure 14a.
"Positional relationship", and "Symmetry" have been extracted from the flower space structure. "Petals patterns. We have analyzed these batik patterns and extracted their basic features. "Elements number", producing the pattern shown in Figure 14d.

The parameter for controlling the number of iterations was set to 2. Moreover, the parameter for controlling the movement of the iteration pattern in the Y-axis direction was set to 4/3, and the parameter for moving in the X-axis direction was set to 4/3. The resulting flower layout is shown in Figure 14b.

Based on the introduction of rotational variables, the parameter for controlling the rotation of the base pattern was set to 45 and all the base patterns in layout map were rotated 45° clockwise, producing the pattern shown in Figure 14d.

7. Analysis

Through an automatic generation system based on fractal geometry, we were able to generate a large number of batik patterns with novel effects which retained the characteristics of original batik patterns. We have analyzed these batik patterns and extracted their basic features. "Elements number", "Positional relationship", and "Symmetry" were extracted from the shape of the flower, as shown in Table 1. The "Elements number" refers to the essential element types that make up the flower and the "Positional relationship" refers to the relationship between the same elements.
Figure 15 shows the flower patterns generated by the system, the original batik pattern, and the original pattern binarization. Through comparing their basic features, it can be judged as to whether the generated patterns can effectively simulate traditional batik patterns. The primary features of the system-generated flower patterns the original flower patterns are shown in Table 2.

Table 1. Basic features of flower patterns.

<table>
<thead>
<tr>
<th>Basic Features</th>
<th>Evaluation Parameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>Elements number</td>
<td>1, 2, 3, multi</td>
</tr>
<tr>
<td>Positional relationship</td>
<td>Rotation, translation</td>
</tr>
<tr>
<td>Symmetry</td>
<td>None, 1/2, 1/3, 1/4, ..., rotation</td>
</tr>
<tr>
<td>Petals layers number</td>
<td>Single, double, multi</td>
</tr>
<tr>
<td>Petal shape</td>
<td>Rhombus, curved, wavy</td>
</tr>
<tr>
<td>Petals number/layer</td>
<td>6, 7, 8, 9, 10, or more</td>
</tr>
<tr>
<td>Pistils number/petal</td>
<td>None, 1, 2, multi</td>
</tr>
</tbody>
</table>

Flower 1: 2, rotation, 1/8, single, curved, 8, 1
Flower 2: 3, rotation, 1/8, single, wavy, 8, 2
Flower 3: 2, rotation, 1/8, single, rhombus, 8, 2
Flower 4: 2, rotation, 1/6, double, curved, 6, 2
Flower 5: 2, rotation, 1/8, single, curved, 8, multi
Flower 6: 2, rotation, none, multi, curved, 10 or more, none

Comparing the original pattern features with general pattern features, it can be found that the generated flowers 1, 2, 3, and 5 are identical to the original pattern. The generated flower 4 is slightly different from the original pattern. Although there are two layers of petals, the number of petals in the second layer is different, and the number of stamens in the petals is also different. Flower 6 is also different from the original pattern. The flower layout of the original pattern is not a three-square layout; however, the characteristics of the single pattern in the layout map are relatively compatible. The user/designer can select the pattern to be drawn through the system interface and change the shape of the pattern by changing the
initialization parameters. We invited design and non-design students to use the system in order to test whether our system can effectively simulate batik patterns during use.

User A was a design student who liked combining animal patterns and plant patterns to create a batik layout. Among these, the features of the flower were “2, rotation, 1/8, multi, curved, 10 or more, none”, and the butterfly layout was also a four-square layout. The user preferred a mirror-symmetric pattern with a four-square layout, as shown in Figure 16a.

User B was a non-design student who preferred to use plant patterns to create a batik layout. The layout of two different flowers generated a circle layout. The features of the two flowers are “2, rotation, 1/5, single, curved, 5, 2” and “multi, rotation, 1/5, double, curved and wavy, 5, none “. The user tended to use a point-symmetric with the circle layout, as shown in Figure 16b.

![User-generated patterns](image)

**Figure 16.** User-generated patterns.

8. Conclusions

Based on the self-similarity, self-affine and scale-free fractal characteristics of traditional handmade batik flower patterns, this paper has proposed an automatic batik flower pattern generation method based on fractal geometry. Firstly, based on a two-dimensional iterated function system, an automatic flower pattern generation algorithm was proposed. A superellipse curve was introduced to achieve the generation of a flower-leaves pattern, a rose curve was introduced to achieve the generation of a petals pattern, a circular hypocycloid was introduced to achieve the generation of a pistil pattern, and a rose curve and a circular curve were introduced to achieve the generation of a flower-core pattern. Next a nonlinear function was defined, a generated flower pattern was introduced into the nonlinear function, and this function was iterated and changed to complete the pattern generation of different layouts. Finally, the variation law between the pattern shape and the parameter value was studied. Comparing the generated flower pattern features with the original flower pattern features, it could be found that most of the generated patterns’ features are consistent with the original pattern features. Although they differed when it came to some details, this did not affect the final result. A small part of the generated patterns differed in their features but the shape of the difference was still very similar to the original pattern, and no significant defects were produced. The batik patterns generated by the automatic generation system were therefore able to effectively simulate traditional batik patterns. Through experiments, the range of parameter values in each function were able to be obtained and the flower patterns of traditional hand-dyed batik were able to be effectively simulated to realize the automatic generation and digital design of the batik patterns. All the proposed methods were applied and tested and the results reached the expected goal.

Our future work will focus on extending the algorithm to other graphic designs, achieving full automatic simulation of batik patterns, enriching the diversity of batik patterns, and introducing color rendering based on patterns so that these patterns can adapt to the intelligent upgrade of China’s printing and dyeing industry.
**Author Contributions:** G.T. and Q.Y. proposed the generation algorithm of batik flower patterns and its layout; G.T., Q.Y., T.H., and Y.S. established the automatic generation system. Validation, T.H. and Y.S. All authors reviewed the manuscript.

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**References**


