Review

Current Advances in TiO₂-Based Nanostructure Electrodes for High Performance Lithium Ion Batteries

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Abstract: The lithium ion battery (LIB) has proven to be a very reliably used system to store electrical energy, for either mobile or stationary applications. Among others, TiO₂-based anodes are the most attractive candidates for building safe and durable lithium ion batteries with high energy density. A variety of TiO₂ nanostructures has been thoroughly investigated as anodes in LIBs, e.g., nanoparticles, nanorods, nanoneedles, nanowires, and nanotubes discussed either in their pure form or in composites. In this review, we present the recent developments and breakthroughs demonstrated to synthesize safe, high power, and low cost nanostructured titania-based anodes. The reader is provided with an in-depth review of well-oriented TiO₂-based nanotubes fabricated by anodic oxidation. Other strategies for modification of TiO₂-based anodes with other elements or materials are also highlighted in this report.

Keywords: battery; anode; titania; anodic oxidation; composite materials; carbon; performance effect; mixed oxides

1. Introduction

Lithium ion batteries indisputably have become the first choice as primary power sources for portable devices and electric vehicles. They offer valuable properties, i.e., long cycle life, high energy density, reasonable production cost, and the ease of manufacturing flexible designs. These properties are the main reasons behind populating lithium ion batteries as the main part in portable devices, and, in addition, to play a central role in the on-going miniaturization of electronics and medical devices. Indeed, developing anode materials for lithium ion batteries with higher performance and competitive price is still the main hurdle to reduce weight and improve performance of LIBs. Early in 1991, Sony introduced the first lithium ion battery to the market in which graphite was used as active anode material, owing to its abundance, low production cost, and reasonable theoretical capacity (372 mAh g⁻¹) [1–3]. This important event aroused the attention of many researchers and motivated them to do extensive work to improve the performance of lithium ion batteries. However, using graphite as anode material is accompanied by several drawbacks. It suffers from severe structure collapse and exfoliation over cycling that originally starts with the formation of solid electrolyte interface (SEI) followed by rapid capacity fading. The low operating voltage of ~0.1 V vs. Li/Li⁺ represents another problem. Such a low potential allows for lithium electroplating at the electrode surface which requires implementing extra materials in the sense of carbon or other materials for safety issues [4]. At a high charging/discharging current rate, lithium dendrites can
easily be formed on the graphite surface due to its high polarization [5]. Such dendrites can move through the separator resulting in an internal short circuit, cell damaging, and warming up until fire (thermal runaway) [6]. Moreover, the use of a graphite-based anode is particularly restricted to low temperatures [7,8]. However, the hybrid electric vehicles (HEVs) and electric vehicles (EVs) are usually charged/discharged at high current rates over a wide temperature range (−30 to +60 °C), where the application of graphite is not suitable and does not meet the EVs requirements. Especially at low temperatures the Li dendrite formation is even enhanced [9]. Therefore, replacing graphite with another material becomes an urgent need. A variety of materials have been proposed as promising candidates for the negative electrode in lithium ion batteries including lithium-metal alloys (Li12M where, M = Sn [10], Al [11], Ga [12], Ge [13], Pb [14], Sb [15], etc.), silicon-based materials (Si nanostructures, Si/C [16], Cu-Si-Al2O3 [17], Ni3Si2/Si [18], etc.), layered metal dichalcogenides (MS2, M = Mo, W, Ga, Nb, and Ta) and transition metal oxides (MO, M = Ti, Sn, etc.) [19]. Figure 1 shows the maximum reversible capacities obtained by some anode materials [20–22]. Although the TiO2 anode shows a relatively low reversible capacity compared to other transition oxides, it exhibits superior cycling stability and Coulombic efficiency. Additionally, they are abundant, environmentally friendly, and obtained by cost-effective production routes. It is known that transition metal oxide-based anodes demonstrate a high irreversible capacity at the first cycle and low Coulombic efficiency [21–23].

![Comparison of the reversible capacity of some anode materials for lithium ion batteries.](image)

TiO2-based materials are being pioneered as negative electrodes capable to overcome the disadvantages of graphite due to their enormous structural stability. This property is related to their negligible or little volume change during cycling (≈4%), stable capacity retention, and fast kinetics for lithium ion insertion/removal [24,25]. Furthermore, the formation of lithium dendrites is effectively suppressed due to the higher delithiation potential (1.7 V vs. Li/Li+) making TiO2 a safe anode material appropriate for various applications. These characteristics are strongly desired to manufacture LIBs in large quantities suitable for mobile and stationary storage applications. Nevertheless, the poor electrical conductivity, low ionic diffusivity, and low theoretical capacity of TiO2 (335 mAh g−1) are the main obstacles hindering the production of high-performance LIBs with titania anodes [24,26]. The reported reversible capacity of bulk TiO2 is only 180 mAh g−1, i.e., half of its theoretical capacity [27,28]. Further Li ion storage into the TiO2 framework is restrained because of the strong repulsive forces among the Li ions. Lithium ion insertion/removal in TiO2 materials is a diffusion controlled process, which depends on the diffusion coefficient and the diffusion length of TiO2 [27,29–31]. The diffusion coefficient is determined by the nature of the materials and the diffusion length depends on the particle size of TiO2. Therefore, many excellent reviews have been reported on the synthesis of various TiO2 nanostructure
anodes such as nanoparticles, nanotubes, and nanowires of pure titania or as composites with other materials for the application of lithium ion batteries [20,27,32,33]. In the following sections, basics concepts of lithium ion battery systems, various TiO$_2$ nanostructures, and detailed information about anodically fabricated TiO$_2$-based negative electrodes are discussed, as they represent the main focus of this review.

2. Lithium Ion Battery System

Generally, a lithium ion battery is a device able to convert chemical energy to electric energy, and vice versa, through electrochemical reactions (oxidation/reduction) between the active materials (anode/cathode) that have a potential difference in the presence of an electrolyte. As described in Figure 2, a LIB is composed of three main components: two electrodes with different electrical potential, and a separator, which electrically isolates the electrodes from each other and allows the Li ions to migrate between the electrodes. The electrolyte is mainly the liquid negotiating medium between the electrodes allowing the migration of Li ions while the separator is completely soaked with the liquid to also avoid being a Li ion barrier.

![Figure 2. Schematic of the operation principles for rechargeable lithium ion batteries.](image)

In commercial cells, the negative electrode (anode) is composed of intercalation compounds that can host lithium ions i.e., carbonaceous materials. The positive electrode (cathode) consists of other intercalation materials that have more positive redox potential such as lithium transition metal oxides, e.g., LiMO$_2$, M = Co, Ni, Mn, or lithium transition metal phosphates e.g., LiFePO$_4$ or LiFePO$_4$/C composites [34–38]. The electrolyte is commonly composed of a solution, containing a lithium salt (i.e., LiPF$_6$) and mixed with liquid alkyl carbonates [34]. The electrochemical reactions of the electrodes undergo a process, in which Li ions are transported between the cathode and the anode (see Figure 2), and accordingly these processes are called “rocking-chair” reactions [39]. During discharging, Li ions de-intercalate from the anode material and the ions are transported through the electrolyte to intercalate into the cathode, which also acts as electron acceptor [40]. Accordingly, the electrons are shuttled through the external circuit providing the current flow. This process is thermodynamically favorable due to the reduction of the cathode materials in which they spontaneously convert from unfavorable high to an energetically more favorable lower valance. On charging, Li ions de-intercalate in reverse from the cathode to re-intercalate into the negative electrode (anode), which acts as electron donor [41].
This oxidation requires an external trigger, which allows a reaction of the anode material to its previous state.

Table 1 shows the superiority of LIBs over other commercial battery systems explained by specific capacity (Wh kg\(^{-1}\)) and energy density (Wh L\(^{-1}\)) [42]. Although Li-based batteries have received extensive attention at both fundamental and applied research levels, further improvement in their electrochemical performance is still required. The latter is hindered by some restrictions in the electrode materials and the electrolyte composition. The electrode materials represent the most important part for development as they mainly determine the efficiency of batteries. To construct high performance LIBs, the electrode materials should meet the following requirements: (1) High surface area and large pore size, as they are important to provide a large exposed surface and more channels for lithium ion migration. This results in short paths and faster diffusion rates for lithium ions that play a crucial role to improve the rate capability. (2) Low volume expansion/shrinkage during lithium insertion/extraction to avoid the cracking and miscontacting between the current collector and the electrode materials to increase the cycling stability. (3) High ionic and electrical conductivity which is required to achieve fast charging and discharging as well as facilitating Li ion insertion. (4) High abundance of the composing materials. (5) Low production costs. (6) Environmentally friendly or easily recyclable.

Table 1. Specific energy and energy densities of commercial rechargeable batteries. Reprint with permission [43]; 2017, American Chemical Society.

<table>
<thead>
<tr>
<th>Rechargeable Battery</th>
<th>Specific Energy, Wh kg(^{-1})</th>
<th>Energy Density, Wh L(^{-1})</th>
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<tbody>
<tr>
<td>Pb–acid</td>
<td>30</td>
<td>80</td>
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<tr>
<td>Ni–Cd</td>
<td>40</td>
<td>90</td>
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<td>145</td>
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<tr>
<td>Ag–Zn</td>
<td>75</td>
<td>200</td>
</tr>
<tr>
<td>Li ion</td>
<td>265</td>
<td>690</td>
</tr>
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3. TiO\(_2\) Anodes

TiO\(_2\) has eight known polymorphs: rutile, anatase, brookite, TiO\(_2\)-B, TiO\(_2\)-R, TiO\(_2\)-H, TiO\(_2\)-II, TiO\(_2\)-III [44]. Among them rutile, anatase and TiO\(_2\)-B have been intensively reported as anode materials for lithium ion batteries over the last decades. Rutile is the most thermodynamically stable phase while anatase and TiO\(_2\)-B are characterized by a metastable nature [45]. However, previous studies showed that nanosized anatase (below 20 nm) is the thermodynamically most stable [46]. At temperatures higher than 600 °C, anatase undergoes a phase transformation to rutile [47]. The electrochemical lithiation/delithiation of TiO\(_2\) polymorphs are described by Equation (1) [29].

\[
x \text{Li}^+ + \text{TiO}_2 + x \text{e}^- \leftrightarrow \text{Li}_x\text{TiO}_2 \quad (0 \leq x \text{ (mole fraction)} \leq 1)
\] (1)

The delithiation reactions strongly depend on the crystallinity, particle size, morphology, surface area, and the involved polymorph. For instance, negligible amounts of Li ions (0.1 Li per Ti atom) are inserted into the rutile structure at room temperature owing to Li ion diffusion into rutile, which is thermodynamically favorable only along the c-axis channels instead of the ab-planes [30,48]. The crystal structures of rutile, anatase and TiO\(_2\)-B are shown in Figure 3. Rutile crystallizes in a tetragonal symmetry with the space group P4\(_2\)/mmm with TiO\(_6\) octahedra sharing edges along the c-direction while the corners are located along the ab-planes [49]. A slight orthorhombic distortion is found for the TiO\(_6\) octahedra [50]. During intercalation, Li ions migrate into the tetrahedral sites neighbored to the ab-planes. This property explains the difficulty of the Li ions to reach the TiO\(_6\) octahedral sites [30]. Therefore, the diffusion coefficient through the c-direction is \(10^{-6} \text{ cm}^2 \text{ s}^{-1}\) which is much larger than that of the ab-planes with \(10^{-14} \text{ cm}^2 \text{ s}^{-1}\) [30,48,51]. With time, Li ion insertion into the rutile bulk is inhibited and is finally disabled due to repulsion forces between the lithium ions and only low capacities are obtained [30].
Figure 3. Structure of (a) rutile, (b) anatase and (c) TiO$_2$-B. The arrows point to the interstitial sites that can host lithium ions.

TiO$_2$-B has a monoclinic structure with $C_{2}$ symmetry, which contains corrugated sheets of edge- and corner sharing TiO$_6$ polygons [52]. A distorted squared-based pyramid replaces the octahedra due to some long Ti-O bonds (2.20–2.25 Å), which are larger in both anatase (1.937–1.966 Å) and rutile (1.946–1.983 Å) [53]. The open structure of TiO$_2$-B provides one-dimensional infinite channels, which can accommodate the volume changes during lithium ion insertion without lattice deformation [54]. Pseudocapacitive behavior was also reported for TiO$_2$-B, which results in a faster diffusion rate during charging/discharging [55].

Anatase has a tetragonal structure with the space group $I4_1/amd$, in which distorted edge-sharing TiO$_6$ octahedra are stacked in one-dimensional zigzag chains [24,56]. The empty TiO$_6$ zigzag channels represent diffusion paths for Li ion intercalation. Usually, a phase transition in the tetragonal anatase phase takes place due to the strong Li-Li repulsive forces resulting in an orthorhombic distortion [50,56]. Owing to the Li$^+$ insertion into the structure, anatase exceeds Li$_{0.05}$TiO$_2$. The changes of unit cell induced by Li ion intercalation usually result in decreasing the $c$-axis and increasing the $b$-axis but the total volume changes for the Li ion insertion is less than 4% due to the low total Li content [24].

4. TiO$_2$ Nanostructures for LIBs

4.1. TiO$_2$ Nanoparticles

TiO$_2$ nanoparticles have been approved as effective anode materials in LIBs. The particle size of TiO$_2$ represents the key factor, which defines reversible capacity and rate performance. When the particle size decreases to nanometer ranges, the surface area increases in consequence and the lithium ion diffusion path is shortened resulting in an improved Li ion insertion capacity. Wagemaker et al. [57] reported on a comparative study among TiO$_2$ nanoparticles with different crystal particle sizes.
(7–40 nm) to explore the impact of particle sizes on the insertion reactions. They found a dramatic increase of Li capacity and Li ion solubility with decreasing sizes of the TiO₂ nanoparticles. Moreover, the small particle sizes improve the rate capability of the electrodes. Figure 4a schematically explains how anatase microparticles can accommodate only up to half a mole of Li ions while the nanosized particles can deliver up to one mole of Li ions per mole TiO₂ [57].

Very fine anatase particles with an average size of 6 nm and a specific surface area of 258 m² g⁻¹ showed an even higher specific capacity in comparison with particles of 15 and 30 nm in diameter and specific areas of 83 and 57 m² g⁻¹, respectively, as shown in Figure 4b. Besides that, the rate capability was also increased by decreasing the particle size [58]. Several studies reported that the kinetics of Li ion insertion significantly depend on the crystallite size [57,59–62]. The phase diagram of various compositions of lithiated TiO₂ versus particle size explains that the particles with 7 nm size or smaller are fully transformed into Li₁TiO₂ reaching the maximum theoretical capacity [57]. Generally, in nanomaterials, the insertion reaction strongly depends on the energetics of the phase boundaries. During the lithiation process of small anatase nanoparticles, only one phase is present in a single particle i.e., anatase or Li-titanate without phase boundaries in this particle [57]. The absence of phase boundaries in small particles is the main reason for the enhancement of Li ion solubility and the solid solution behavior in the single-phase particles. Additionally, the surface strain that occurs between the different intercalated phases is thermodynamically suppressed in small particles. Similar behavior was also experimentally noticed for rutile supported with simulation studies [63]. Jamnik and Maier [64] reported that in small particles (<100 nm), the outer particle surface tension affects the thermodynamics of the Li ion insertion. Size-dependent performance of rutile nanoparticles was investigated by Jiang et al. [65]. The highest initial capacity of about 378 mAh g⁻¹ is demonstrated for rutile with a particle size of 15 nm (Figure 4c) at 0.05 A/g. A capacity of 207 mAh g⁻¹ was retained after 20 discharging cycles.

Figure 4. (a) Schematic of the impact of particle sizes on the insertion capacity of anatase reprinted with permission from ref. [57]; (b) Voltage profile of anatase nanoparticles with 6 (A6), 15 (A15), and 30 (A30) nm in diameter, adapted with permission from ref. [58]; (c) The initial capacity profiles of rutile nanoparticles with 15 (R15), 30 (R30), and 300 (R300) nm in diameter, adapted with permission from ref. [65].
Theoretical modeling studies were performed by Sushko et al. [66] to investigate the relation between particle size and ionic conductivity of TiO$_2$. These studies demonstrated that the ionic conductivity is remarkably improved if the particle size of TiO$_2$ is below 20 nm due to the higher charge transport of Li ions and electron accumulation on the nanoparticle boundaries. In contrast, when the nanoparticles are larger than 20 nm, charge separation is dominant, hence lower ionic conductivity is obtained [66]. Similar behavior was also found for anatase microparticles [57].

To prepare nanoparticles, the TiO$_2$ morphology in terms of particle size and surface area was controlled by different synthesis techniques such as sol-gel and solvothermal methods. For instance, Kubiak et al. [67] used sol-gel and mini-emulsion processes to produce mesoporous TiO$_2$ with different particle sizes (9–12 nm) and pore diameters (7–15 nm). The electrochemical tests showed the lithium insertion capacity is dramatically improved by high surface area and small particle sizes [67]. The authors also found that there is a relation between particle size and the pseudocapacitive effect, where double layer capacity and pseudocapacitity are also increased by reducing the particle size. Nanocrystalline anatase with an average particle size of 5 nm displayed an enhanced Li ion storage capacity compared to 10 nm sized. In addition, faster charging and discharging rates were observed for these nanoparticles owing to the Faradaic reactions, which occur at the electrode surface and control the whole insertion reactions. Similar improvement in electrochemical performance of anatase nanoparticles with average sizes of 8 nm, prepared by the hydrolysis of an organotitanium precursor solution through a sol-gel process with subsequent spray-drying or a hydrothermal treatment was reported by Wilhelm et al. [68]. The prepared nanoparticles can deliver up to 140 mAh g$^{-1}$ at 0.1 C. Anatase nanoparticles prepared by a tenside-assisted hydrolysis with a solvothermal after treatment procedure were tested as anodes and showed a reversible capacity of 196 mAh g$^{-1}$ sustained over 100 cycles at a current rate of 0.2 C [69].

However, formation of TiO$_2$ particles in the nanoscale is not always useful to improve its Li ion storage, as there is an optimal size range which can positively affect their performance and other sizes do not. For instance, well-dispersed anatase nanoparticles fabricated by a sol-gel method exhibited a considerable enhancement in their Li ion insertion ability when the particle size ranged between 8 and 25 nm [70].

Great interest was paid to further improve the lithium storage performance of zero dimensional TiO$_2$ by coating the TiO$_2$ surface with carbon to overcome the poor lithium ion diffusivity and low electrical conductivity. In typical traditional synthesis methods, incorporation of carbon into TiO$_2$ is conducted by hydrothermal heating of metal salts in the presence of carbon sources such as glucose. However, controlling the carbon content as well as obtaining a homogeneous carbon distribution over the TiO$_2$ surface is hardly achieved. Lui et al. [71] reported on the hydrothermal carbon-coating treatment to fabricate a sandwich-like structure of a TiO$_2$@C hollow sphere composite. As a result of combining carbon and TiO$_2$, the TiO$_2$@C hollow spheres showed enhanced reversible capacity (240 mAh g$^{-1}$) with good capacity retention and high rate capability compared to the lower capacity (120 mAh g$^{-1}$) of uncoated TiO$_2$ commercial nanoparticles (Degussa P25). Incorporation of carbon into porous TiO$_2$ nanoshells was studied by Wang et al. [72] who succeeded in controlling the carbon content in TiO$_2$@C composites to realize a highly reversible lithium ion storage (Figure 5a). The preparation procedure includes two steps where in the first one TiO$_2$ hollow spheres were coated with a resorcinol-formaldehyde layer via a sol-gel method. The second step involves a thermal treatment to carbonize the polymer and to form a crystalline TiO$_2$ shell. The TiO$_2$@C electrode showed a capacity of ~425 mAh g$^{-1}$ at a current rate of 0.1 C. The specific capacity of this electrode decreased to ~150 mAh g$^{-1}$ when the current rate was increased to 10 C (Figure 5b). In addition, such a composite demonstrated a reversible capacity of ~190 mAh g$^{-1}$, which is slightly decreased to 170 mAh g$^{-1}$ after more than 300 charging/discharging cycles at 2 C (Figure 5c). The ability to precisely control the carbon content of the TiO$_2$@C composites makes this preparation route highly attractive compared to traditional hydrothermal preparations.
Graphene is a promising candidate of the carbon family for incorporation into TiO$_2$ as it is considered to show excellent electron transport. Coating of TiO$_2$ nanoparticles with a graphene layer provides pathways for electron transport resulting in a higher electrical conductivity, which overcomes the internal resistance of TiO$_2$. Furthermore, these conductive boundaries serve as protective layers to prevent the direct contact between the TiO$_2$ and the electrolyte followed by an enhanced stability of the active materials and low parasitic electrolyte consumption. Various studies report on the fabrication of TiO$_2$-graphene hybrid nanostructure for improved Li-ion insertion. Wang et al. [73] used an in-situ technique to fabricate self-assembled nanocrystalline TiO$_2$ with graphene utilizing anionic sulfate surfactants to stabilize graphene in aqueous solutions (Figure 5d). The obtained hybrid nanostructure showed a doubling of the Li ion insertion capacity of the pure TiO$_2$ as a result of an increased electrical conductivity induced by graphene (Figure 5e,f). In another study [75], a TiO$_2$ nanoparticles@graphene composite was prepared in-situ by the hydrolysis of TiCl$_4$ in the presence of graphene oxide nanosheets subsequently reduced by hydrazine hydrate. The obtained TiO$_2$-graphene composites were tested for Li ion intercalation as anodes demonstrating a reversible capacity of 60 mAh g$^{-1}$ at a high current rate of 5 A g$^{-1}$ with negligible fade over 400 cycles. The unique conductivity of graphene sheets combined with well-dispersed TiO$_2$ nanoparticles led to a superior electrochemical performance in Li ion storage.

Owing to their high conductivity, stability, and the ease of manufacturing, carbon nanotubes (CNTs) were used as a further excellent candidate to synthesize highly valuable TiO$_2$ composite anodes. Core-shell CNTs/TiO$_2$ (Figure 5g,h) were prepared by hydrolysis of tetrabutyl titanate and showed a...
specific capacity of ~240 mAh g\(^{-1}\) at a current density of 5 A g\(^{-1}\) exhibiting a threefold increase in capacity compared to pure TiO\(_2\) (62 mAh g\(^{-1}\)) at the same current density (Figure 5i). The enhancement in capacity was attributed to the better electron supply due to the CNTs enabling the TiO\(_2\) shells to store higher lithium ion concentrations [74].

**Excursus: Nanoparticulate TiO\(_2\) Contributions in Redox-Flow Lithium Ion Batteries**

The redox-flow battery (RFB) is one of the most promising energy storage systems that provides high capacity and energy density suitable for numerous applications e.g., in the automotive sector but is also heavily discussed for large-scale stationary power storage units for renewable power production and grid stability. A typical flow battery is composed of three components, (i) an electrochemical cell-power output unit in which, two adjacent electrochemical half cells, containing porous electrodes are separated by a semipermeable membrane, (ii) two energy storage tanks (anolyte and catholyte) each filled with redox-active species are dissolved in a solvent serving as electrolyte, (iii) a pumping unit which circulates the anolyte and catholyte between the power output cells and the energy storage tanks [76–79]. The operation principle is based on oxidation and reduction reactions between the electroactive transition metal ion species at the surface of a porous electrode in the electrochemical cells. The two electrolyte solutions, which represent the active electrode materials, are pumped into a membrane-divided stack allowing for ion migration of the conducting salt and not the redox-active species and the electron transfer [76–78]. The vanadium redox-flow battery is one of the famous flow battery examples established in the market for large-scale storage [80]. One of the main obstacles hindering the breakthrough of redox-flow batteries in the market is the poor solubility of electroactive species and the dead weight of non-redox-active materials in the electrolyte which limits the energy density of the battery [76,81,82]. A promising approach to increase the energy density of flow batteries was explored by integrating solid lithium intercalation compounds mixed with conductive materials into the flow solutions containing lithium ions [77,79–82]. This approach, known as redox-flow lithium-ion battery (RFLB), bundles together the advantages of the high energy density of lithium ion battery and the flexibility of the redox-flow battery. In such a battery system, the energy is stored in the Li-intercalation materials, as in conventional batteries, which are statically present in the energy storage tanks. TiO\(_2\) has been investigated as anode materials in RFLB. Pan et al. [83] reported the reversible Li-storage of anatase by chemically using two redox mediators, bis(pentamethylcyclopentadienyl)cobalt [Co(Cp*)\(_2\)] and cobaltocene [Co(Cp)\(_2\)]. The Li ions are intercalated into TiO\(_2\) suspended in the electrolyte without attaching TiO\(_2\) onto the electrodes of the flow channel. Anatase delivered a reversible capacity of 0.33 Li ions per TiO\(_2\). Further confirmation of the achieved capacity was obtained by theoretical calculations using density functional theory (DFT). Jia et al. [84] used a full cell configuration of RFLB, in which LiFePO\(_4\) and TiO\(_2\) were utilized as the cathodic and anodic materials, respectively. The RFLB exhibited good cycling performance demonstrating an energy density of ~500 Wh L\(^{-1}\). The energy storage ability of RFLB are negatively affected by the formation of a solid electrolyte interface on the electrode surface due to the reduction of the alkyl carbonate of the electrolyte at a potential less than 0.8 V vs. Li/Li\(^+\) resulting in a slow charge transfer, especially when graphite is used as solid anodic material. Using active anode materials with operating voltage higher than the decomposition potential of the electrolyte, such as TiO\(_2\) and Li\(_4\)Ti\(_5\)O\(_{12}\), the formation of the solid electrolyte interface is effectively suppressed and hence, allows for better ionic transport and improved intercalation characteristics [80].

4.2. TiO\(_2\) Nanorods, Nanoneedles, Nanowires, and Nanofibers

The main drawback of TiO\(_2\) nanoparticles as anodes in LIBs is the missing contact between the particle boundaries, which results in poor electronic and ionic conductivity [65,68]. Additionally, the random motion of the electrons through the particles, as there are no defined pathways for the electron transport, hinders the electron separation at the current collectors [70,85]. Furthermore, the nanoparticles with high surface area possess higher surface energies compared to bulk materials.
These particles can aggregate during the synthesis process or even during an electrochemical intercalation and thus the surface area decreases accordingly [85]. Indeed, the formed aggregates restrain the electrolyte in reaching a particle surface causing a severe capacity drop.

Fabrication of TiO$_2$ with particular one-dimensional morphologies such as nanorods, nanoneedles, and nanowires could significantly overcome the nanoparticles’ drawbacks and improve their lithium ion insertion ability. Experimental work showed that the porous nature of the nanowires allows a good contact between electrolyte and electrode material and accommodates the strain resulting from changing the crystal dimensions after the electrochemical insertion reaction. As an example flower-like rutile nanorods (Figure 6a) were synthesized by hydrolysis of a TiCl$_4$/ethanol solution at 50 °C [86]. The obtained nanorods showed a considerably higher reversible capacity and cycling stability than spherical rutile nanoparticles (Figure 6b). The significant improvement in battery performance was attributed to the rod geometry of rutile oriented along the $c$-direction of the unit cell, which is thermodynamically favorable for lithium ion insertion [86]. Fabrication of anatase nanotubes can be performed easily via rutile powders which have been hydrothermally treated at 500 °C and 700 °C in alkaline media (10 M NaOH) (Figure 6c). Reproducible discharging capacity (~175 mAh g$^{-1}$) was also noticed for anatase nanotubes after 10 cycles at a 0.1 C rate (Figure 6d) [87]. A similar synthesis route was reported by Kim et al. [88]. They further treated the obtained nanotubes/nanorods at a temperature between 300 °C and 400 °C to transform the present nanotubes into nanorods. Bao et al. [89] succeeded in hydrothermally producing porous anatase nanorods at a lower temperature (200 °C) in an alkaline medium using a NaOH/KOH mixture. The resulting nanorods showed a high initial discharging capacity of 212 mAh g$^{-1}$ at a current density of 60 mA g$^{-1}$, which was retained for 30 discharging/charging cycles. Gao et al. [90] developed a method to prepare anatase nanorods. For this, TiCl$_4$ undergoes a hydrolysis with caustic soda and the obtained hydrolysate is hydrothermally treated at 110 °C. The material exhibited a lithium insertion capacity of 206 mAh g$^{-1}$ with good reversibility at a current density of 50 mA g$^{-1}$. Rutile nanoneedles with about 25 nm in diameter and 100 nm in length were prepared from titanium isopropoxide by a reverse microemulsion mediated sol-gel method (Figure 6e). The nanoneedle electrode was capable of achieving an initial specific capacity of 305 mAh g$^{-1}$ (Figure 6f) [91]. Wang et al. [92] reported on the fabrication of anatase nanowires with a minor TiO$_2$-B phase content via the hydrothermal treatment of commercial P25 powders (Degussa) followed by an annealing step at 400 °C (Figure 6g). These nanowires demonstrated a high specific capacity of 280 mAh g$^{-1}$ at a current density of 140 mA g$^{-1}$ upon 40 cycles with a Coulombic efficiency of 89% (Figure 6h). Wu et al. [93] developed a room temperature hydrothermal method without using a Teflon-lined autoclave to prepare anatase nanowires from Ti(OC$_4$H$_9$)$_4$. This material was characterized with a reversible capacity of 216 mAh g$^{-1}$ at a current density of 20 mA g$^{-1}$. Anatase particles were converted into TiO$_2$-B nanowires with diameters ranging from 20 to 40 nm by a hydrothermal method in the presence of an aqueous solution of NaOH [94].

A binder-free electrode composed of TiO$_2$ nanofibers was prepared by an electrospinning technique followed by a calcination step at 400 °C in air [95]. The TiO$_2$ nanofibers showed a specific capacity of 175 mAh g$^{-1}$ at a current rate of 0.3 C with a Coulombic efficiency between 96% and 100% over 50 cycles.
Figure 6. (a) SEM image of the flower-like rutile nanorods and (b) their galvanostatic cycling at 0.1 C adapted with permission from ref. [86]. (c) TEM image of TiO$_2$ nanotubes synthesized by treating of rutile with NaOH at 125 °C and (d) their performance denoted in image with symbol (a) adapted with permission from ref. [87]. (e) TEM image of as-prepared rutile nanoneedles, (f) their discharge cycling and voltage profiles appear in the inset adapted with permission from ref. [91]. (g) SEM image of the as-prepared TiO$_2$ nanowires, their discharging capacity and (h) Coulombic efficiency at different current densities adapted with permission from ref. [92].
The electrochemical performance of 1D TiO$_2$ nanoarchitectures can be further improved by coating or doping with carbonaceous materials that improve both the electrical and ionic conductivities. Goriparti et al. [96] synthesized carbon-doped TiO$_2$ nanowires by a hydrothermal method and employed them as anodes in LIBs. The as-prepared C-doped TiO$_2$ nanowires offered enhanced reversible capacity of 306 mAh g$^{-1}$ at a current rate of 0.1 C with long term cycling (1000 charging/discharging cycles) compared to the undoped TiO$_2$ nanowires. Controlled hydrolysis was developed by Shen et al. [97] to fabricate a 3D hybrid nanocomposite of TiO$_2$-graphene-CNTs. This study showed that combining conductive graphene sheets and CNTs results in an excellent electron transport and supports Li ion intercalation into TiO$_2$ nanoparticles. A specific capacity of $\approx 120$ mAh g$^{-1}$ was obtained at a high current rate (10 C) maintained for 100 cycles. The hybrid electrode also exhibited a significantly high rate capability when tested at various current rates from 0.5 to 30 C.

As already explained, high conductivity and good electron transport, especially at high temperature, positions graphene as a good additive to form composites with TiO$_2$ in order to reduce the internal resistance and decrease the irreversible heat which is produced from charging and discharging processes. TiO$_2$ nanotube@graphene composites were explored by Wang et al. [98] prepared by a single-step hydrothermal synthesis. The composites presented a high storage capacity of 357 mAh g$^{-1}$ at 10 mA g$^{-1}$ when used as anodes in LIBs. The tubular structure of TiO$_2$ and the good electronic properties of graphene are the main reasons behind the excellent performance of such a composite. In addition, TiO$_2$ nanorod arrays were grown onto graphene sheets by a modified seed-assisted hydrothermal preparation. A sandwich-like nanocomposite of rutile nanorods/graphene was observed exhibiting largely improved reversible charging/discharging capacities and an enhanced robust rate capability compared to pure TiO$_2$ nanorods. The observed better performances were mainly attributed to superior conductivity and the unique structure of such a composite that supports excellent insertion reactions [99]. Zuniga et al. [100] produced multichannel hollow nanofibers of a TiO$_2$/C composite by a force spinning process, in which polyvinylpyrrolidone (PVP) and titanium (IV) butoxide were used as precursors. The as-formed precursor-based nanofibers were thermally treated at 280 °C in air and subsequently with another carbonizing step at 550 °C in the presence of argon atmosphere to finally obtain TiO$_2$/C. The binder-free electrode from this nanocomposite demonstrated a specific capacity of $\approx 229$ mAh g$^{-1}$ when cycled at a current density of 100 mA g$^{-1}$ with a Coulombic efficiency of 98% after 100 charging/discharging cycles. The authors ascribed the superior cycling performance of the TiO$_2$/C hollow nanocomposite to the increased reactive sites due to the high surface area (123 m$^2$/g) of the one-dimensional hollow nanofiber compared to non-hollow TiO$_2$/C (61 m$^2$/g), as well as the reduced diffusion length of the Li$^+$ ions to achieve a higher Li ion intercalation. Thirugunanamam et al. [101] fabricated graphene-wrapped TiO$_2$ nanofibers by electrospinning. The graphene/TiO$_2$ nanofibers showed a doubled surface area according to the Brunauer-Emmett-Teller model compared to pure TiO$_2$ nanofibers before wrapping with graphene (54 m$^2$/g). High reversible capacities of up to 200 mAh g$^{-1}$ were demonstrated at a current rate of 0.1 C. Meanwhile, pure TiO$_2$ nanofibers delivered only 160 mAh g$^{-1}$ at the same current density. The porous nature of the material coupled with a high surface area provided more favorable Li ion storage sites. The effect of graphene on the electrical and ionic conductivity helped to achieve high rate performance and reversibility. Ding et al. [102] succeeded in growing ultrathin anatase nanosheets on graphene as support by a solvothermal method. A reversible capacity of up to 161 mAh g$^{-1}$ was demonstrated by this composite anode after 120 charging/discharging cycles at a current rate of 1 C. The unique structure of the composite is closely attributed to the high electrochemical performance. Flower-like nanostructures of a TiO$_2$/graphene composite were prepared by Xin et al. [103] using a hydrolysis method. The TiO$_2$/graphene composite demonstrated a capacity of about 230 mAh g$^{-1}$ at 0.1 C exhibiting high rate capability and cycling stability up to a current rate of 50 C in a half cell experiment. TiO$_2$ nanoparticles with porous texture along with highly conductive graphene enabled fast electron transfer and better Li ion diffusion resulting in outstanding reversibility with average capacity fading of 0.03% per cycle. However, in another study, Choi et al. [104] prepared TiO$_2$/graphene nanocomposites by self-assembling and
tested them in a full cell configuration versus LiFePO₄. The full cell showed ≈125 mAh g⁻¹ specific capacity with negligible fade even after 700 charging/discharging cycles when tested at a current rate of 1 C.

4.3. Porous TiO₂ Nanostructures

Application of porous TiO₂ nanostructures is another promising approach to decrease the diffusion paths of Li ions in the electrode material and, thus, develop their insertion performance. The specific nature of porous nanostructures and the high surface area allow for good wettability and better permeability of the electrolyte, facilitating excellent charge transfer across the electrode material at the electrode/electrolyte interface. Particular attention has been paid to synthesize nanoporous TiO₂ with different morphologies including 0D, 1D, 2D, and 3D structures. To generally show the positive effect of porosity in 0D nanostructures, porous TiO₂ nanospheres were fabricated by a simple sol-gel method followed by thermal annealing. The electrochemical measurements indicate that the obtained material with such a porous structure was able to deliver higher reversible capacities than dense TiO₂ nanospheres without porosity [105]. The fabrication of such porous structures is commonly performed by template-free and template-assisted methods [54]. In the template-free approach, a hydrothermal process is used to obtain core-shell structured mesoporous TiO₂ spheres while in the template-assisted procedure, surfactants are utilized. The main advantages of this preparation route are the ability to fabricate well-ordered and uniform mesopores with high surface area. Zero-dimensional (0D) nanoporous hollow spheres were synthesized using carboxyl functionalized polystyrene TiO₂ spheres as a template (Figure 7a). As anode materials, such hollow spheres showed a reversible capacity of 230 mAh g⁻¹ when cycled at a current density of 33.5 mA g⁻¹ (Figure 7b). With this measure, additional surface capacities may be generated for such porous structures resulting in good Li ion storage properties [106]. The relation between porosity and lithium storage characteristics was investigated by Saravanna and co-workers [107]. They fabricated various mesoporous TiO₂ nanoparticles (10–20 nm particle size) with different pore sizes (5.7–7 nm) by a soft template method in which titanium isopropoxide was selected as a titanium source with different cationic surfactants of various chain lengths. The specific surface area of the prepared samples increases from 90 to 135 m² g⁻¹ with increasing pore diameters. The electrochemical results showed a high specific capacity of 268 mAh g⁻¹ of the sample with the highest surface area. The improved performance was ascribed to the high surface area which provides much larger voids for increased Li ion accommodation. Wang et al. [108] developed a facile microwave-assisted hydrothermal method to produce porous TiO₂ spheres with a subsequent annealing step at 500 °C. When tested as electrodes in LIBs, they showed a stable Li ion storage capacity of 184 mAh g⁻¹ at 1 C.

Indeed, coating 0D mesoporous TiO₂ with carbon, as often utilized, not always results in a high specific capacity. For instance, Zhang et al. [109] reported the synthesis of a C-coated mesoporous TiO₂-graphene sheets composite via a one-step solvothermal synthesis. The sandwich-like structure of this hybrid composite was applied as electrode for LIBs exhibiting an initial capacity of 145 mAh g⁻¹ at a current density of 0.2 A g⁻¹. Only a specific capacity of 111 mAh g⁻¹ was achieved after 100 cycles.

One-dimensional (1D) structures of TiO₂ with a mesoporous rod-like morphology were reported by Jiang et al. [110] by ultraviolet irradiation of titanium glycolate previous to a heat treatment. A reversible capacity of 161 mAh g⁻¹ at a current density of 1 A g⁻¹ was demonstrated and retained for 40 cycles. Anatase nanorods were also synthesized by a low temperature colloidal synthesis from a thermal decomposition of titanium precursors containing a coordinating agent such as oleic acid. In this preparation route oleic acid is utilized as a capping agent to prevent the nanoparticle agglomeration during the synthesis process as well as providing a carbonaceous percolating network to cover the porous nanorods. The electrode composite showed a specific capacity of 250 mAh g⁻¹ at a rate of 1 C confirming the superiority of such a porous, coated structure [111]. Core-shell nanocomposites from mesoporous Fe₂O₃ nanorods-TiO₂ were synthesized by thermal treatment of FeOOH@TiO₂ [112]. The composite electrode delivered a reversible capacity of 860 mAh g⁻¹ at a current density of 1 A g⁻¹.
demonstrating a prolonged cycling stability over 1000 charging/discharging cycles. The high capacity obtained by such an electrode was attributed to the unique structure with the mesoporous texture of the composite as well as the synergetic effect originating from the high capacity of the Fe$_2$O$_3$ core with a durable TiO$_2$ shell. In another study, Wang et al. [113] succeeded in fabricating hierarchical TiO$_2$/Fe$_2$O$_3$ fiber-in-tube architectures with a TiO$_2$ fiber as the core and Fe$_2$O$_3$ as the shell by electrospinning. High initial capacities of up to 987 mAh g$^{-1}$ were demonstrated at a current density of 100 mA g$^{-1}$ with 65% capacity retention after 240 cycles.

Hierarchically ordered porous TiO$_2$ with 2D structures have received great interest especially as negative electrodes in LIBs. These unique porous nanostructures provide a rapid reactant transport through the larger pore diameters as well as a high surface area which is obtained from the smaller pores acting as active sites for the adsorption/desorption of the reactants. Recently, 2D hierarchically ordered porous anatase with a specific surface area of 486 m$^2$ g$^{-1}$ was synthesized by chemical etching of amorphous TiO$_2$ powder using acetic acid [115]. The obtained texture is defined by micropores with a range of 2 to 6 nm and mesopores of 15 to 80 nm. A reversible specific capacity of 191 mAh g$^{-1}$ was demonstrated for this hierarchical structure at a current rate of 1 A g$^{-1}$ and this capacity is retained for 60 cycles [115]. Higher capacity obtained by hierarchical, porous anatase structures with high surface area and uniform pore size distribution compared to nonporous TiO$_2$ is attributed to Li$^+$ ion intercalation in the conventional octahedral sites of the bulk material and an additional storage possibility in extra sites at interfaces. Jamnik and Maier [64,116] proposed a storage mechanism which is called ‘Job-sharing’ to explain how the reversible Li ion storage capacity is achieved at the interfaces of the hierarchical TiO$_2$ nanostructures with high surface areas. This mechanism explains why lithium ions are stored in the accessible interstitial sites of the electrode, whereas the electrons are stored in another phase, such as the conductive carbon additives or the SEI layer [117]. The synergetic effect of a
lithium ion-accepting and an electron-accepting phase triggers additional storage capacity through the ease of charge separation \cite{117, 118}. This interfacial capacity phenomenon is kinetically favored for the nanostructure with high volume fractions of interfacial areas, especially when the electrode is directly cycled at high current rates without starting with a low rate at first \cite{117}. Jin et al. \cite{118} prepared hierarchical nanosheets with a yolk-shell structure arranged as a highly porous microsphere shell and a dense mesoporous core by a solvothermal alcoholysis. The pore diameter of the outer 2D nanosheet shell is about 15 nm and of the inner mesoporous core of about 3 nm. These particular structures offer a stable porous framework that allows for electrolyte diffusion by capillary attraction and also buffer the volume increase along with the lithium ion intercalation/extraction reactions. Prolonged galvanostatic cycling over 700 cycles was performed by such an electrode exhibiting a reversible specific capacity of 225 mAh g\(^{-1}\) \cite{118}.

Three-dimensional (3D) porous structures were also studied for the application in lithium ion storage. The synthesis of 3D interconnected hierarchical structures composed of porous urchins was reported by Cai et al. \cite{114} (Figure 7c) and was performed hydrothermally from TiO\(_2\) and oleylamine as precursors followed by an ion-exchange and a calcination process. When evaluated as anode material, the 3D structure showed a lithium ion storage capacity of 206 mAh g\(^{-1}\) at 0.5 C after 100 cycles (Figure 7d). The formation of 3D hierarchical nanoporous anatase via the hydrolysis of titanium glycolate was reported by Shin et al. \cite{117}. A lithium ion storage capacity of 302 mAh g\(^{-1}\) was observed for such microporous anodes with superior cycling stability. The experimental results of this study have proven that 64% of the achieved capacity is attributed to two major storage processes which are bulk insertion and pseudo-capacitive interfacial storage modes. The electrochemical performance of such a material reflects the importance of the high surface area of microporous TiO\(_2\) in generating additional pseudo-capacitance. Recent work demonstrated a simple in-situ preparation of ordered 3D macroporous TiO\(_2\) anodes using a polystyrene templated carbon cloth. The 3D electrodes provided a specific capacity of 174 mAh g\(^{-1}\) when cycled at a current density of 2 A g\(^{-1}\) \cite{119}. The pore size and the thickness effects on the electrochemical performance of the 3D porous electrodes were prepared by atomic layer deposition and optimized during a systematic study of Ye et al. \cite{120}. The results revealed that decreasing the pore sizes and thickness of the 3D electrode, improved its power performance and the diffusivity of Li ions across the electrode/electrolyte interface.

4.4. TiO\(_2\) Nanotubes Prepared by Electrochemical Anodization

The one dimensional (1D) tubular structure of TiO\(_2\) is of great scientific interest as well as practical significance particularly when the nanotubes are highly ordered and perfectly aligned in close packed arrays. These outstanding characteristics are realized by the potentiostatic anodization of Ti substrates as it is a simple, straightforward, and cost-effective preparation technique (see Figure 8). The majority of the reported preparation methods only result in random networks of TiO\(_2\) nanotubes with uncontrolled dimensions. However, template-assisted atomic layer deposition (ALD) can produce nanotubes with controlled geometries. This extensive preparation is reflected in the high cost of the resulting product and the operating expense, like the apparatus, and thus, limits the use and the benefit \cite{121}.

The first anodic oxidation study of pure Ti metal and Ti-6Al-4V alloy substrates resulted in uniform porous films of TiO\(_2\) as reported by Zwilling et al. \cite{122} in 1999. However, a previous report before Zwilling’s work explored the anodization of Ti substrates in the presence of fluoride ions which only resulted in a porous structure \cite{123}. In 2001, Grimes and co-workers \cite{124} succeeded in synthesizing well-defined nanotube arrays by the anodic oxidation of Ti substrates in an HF-containing electrolyte. These results aroused a lot of attention and pushed the research towards the optimization of synthesis parameters (i.e., electrolyte configurations, applied voltage, reaction time, pH, agitation, and temperature, etc.), to understand the formation mechanism and to employ these nanotubes in various research-near applications.
Extensive studies proved that the TiO$_2$ nanotubes obtained by anodic oxidation are self-organized, well-aligned perpendicularly to the substrate, and exhibit uniform tube diameters, and wall thicknesses as well as high surface areas. Furthermore, the nanotube dimensions (i.e., diameter, wall thickness, and tube length) can be precisely controlled by tuning the applied voltage, the employed temperature, and the electrolyte composition especially by the F$^-$ concentration [122–127]. The anodization is normally performed in a two-electrode electrochemical cell with the metal or alloy sheets as the working electrode and platinum foil or graphite as counter electrode in aqueous or organic electrolytes containing F$^-$ ions as shown in the schematic of Figure 9. Aqueous HF solutions were first used as electrolytes to manufacture TiO$_2$ nanotube arrays with tube lengths below 500 nm [123,128]. Replacing the aqueous solutions with organic electrolytes composed of ethylene glycol as main solvent in addition to a fluorine source such as NH$_4$F at high pH values enables TiO$_2$ nanotube formation with lengths reaching up to 1 millimeter [128–130].

The nanotubes fabricated with these electrolytes always exhibited average diameters and wall thicknesses larger than 50 nm and 15 nm, respectively. Using neutral electrolytes such as those containing (NH$_4$)$_2$SO$_4$ with NH$_4$F leads to a reduced dissolution rate of TiO$_2$ resulting in nanotube arrays with lengths in the micrometer range [131]. These electrolytes are known as establishing mild oxidation conditions for the Ti substrates. Please note that the chemical composition of the electrolyte also plays a central role in the physical properties of the fabricated nanotubes [132,133]. For instance, addition of acetic acid results in the formation of robust tubes. Furthermore, increasing the F$^-$ concentration allows control of the tube wall thickness [131,132].

**Figure 8.** (a) Schematic illustration of the formation of TiO$_2$ nanotubes by the anodization of a Ti substrate. SEM micrograph of anodized Ti substrates in formamide-based electrolyte containing 0.2 M NH$_4$F at different anodization voltage (b) 20 V, (c) 40 V, and (d) 60 V. (e) The cross-sectional view while the inset shows the bottom view of the nanotubes prepared at 60 V reprinted with permission from ref. [125].
Excursus: The Mechanism of Nanotube Formation by Anodic oxidation

The formation mechanism of TiO2 nanotubes is basically similar to the mechanism of formation of porous alumina as roughly described by Equations (2)-(5) [133–135]. At the beginning of an anodization process, the Ti substrate is exposed to the electrolyte and a compact oxide layer of TiO2 is formed on the substrate surface due to the interaction between Ti metal and H2O as described in Equation (3a) [107]. In addition, the initially obtained oxide layer is subjected to an electric field-aided dissolution to produce Ti4+ cations where, the Ti-O bonds can easily be broken due to the high polarization effect originating from the electric field [136,137].

\[
\text{Ti} \rightarrow \text{Ti}^{4+} + 4e^- \quad (2)
\]
\[
\text{Ti} + 6\text{H}_2\text{O} \rightarrow \text{TiO}_2 + 4\text{H}_3\text{O}^+ + 4e^- \quad (3a)
\]
\[
\text{Ti}^{4+} + 8\text{H}_2\text{O} \rightarrow \text{Ti(OH)}_4 + 4\text{H}_3\text{O}^+ \quad (3b)
\]
\[
\text{Ti(OH)}_4 \rightarrow \text{TiO}_2 + 2\text{H}_2\text{O} \quad (4)
\]

At the same time, hydrogen evolution occurs at the cathodic side as the complementary reaction according to Equation (5) [138].

\[
8\text{H}_3\text{O}^+ + 8e^- \rightarrow 4\text{H}_2 + 4\text{H}_2\text{O} \quad (5)
\]

Note that, as soon as the voltage is applied, the electric field induces the anodic dissolution of the Ti surface to form Ti4+ ions (Equation (2)) as well as the generation of oxygen anions (O2−) by deprotonation of H2O molecules or OH− ions that are present in the electrolyte [131,133]. The created oxygen anions migrate from the electrolyte/oxide interface across the previously formed oxide layer to reach the metal surface while the Ti4+ ions diffuse from the metal surface at the metal/oxide interface towards the oxide/electrolyte interface [139]. Therefore, the growth of the oxide layer described in Equation (4) mainly depends on the ion formation (Ti4+ and O2−) process. The interaction between Ti4+ and O2− and the diffusion rate of both Ti4+ and O2− into the oxide layer is supported by the electrical field. Indeed, the presence of fluoride ions in the electrolyte represents the main key in producing self-organized tubular morphology in the previously formed compact oxide layer. In the main, two reactions are forced by the fluoride ions, the first is a complexation reaction in which they react with the Ti4+ cations ejected to the oxide/electrolyte interface to form [TiF6]2− species as displayed in Equations (6) and (7) [140].

\[
\text{Ti}^{4+} + 6\text{F}^- \rightarrow [\text{TiF}_6]^{2-} \quad (6)
\]
\[
\text{TiO}_2 + 6\text{HF}^- \rightarrow [\text{TiF}_6]^{2-} + 2\text{H}_2\text{O} + 2\text{H}^+ \quad (7)
\]

The second reaction is a chemical attack of the compact oxide layer explained in Figure 10.
Fluoride ions chemically dissolve TiO$_2$ by forming [TiF$_6$]$^{2-}$, which is a water soluble species, causing small pits (Equation (6)) [123,138]. These pits represent preferential sites for the electric field assisted dissolution. With time, these pits become deeper and wider and the materials are converted into tubes with the high dissolution rate at these active sites [141]. Therefore, the nanotube heights during the anodization process are controlled by the balance between the rate of electrochemical oxidation and chemical etching. Application of a high anodization voltage leads to an increased electrochemical oxidation compared to the rate of chemical etching. Consequently, a thick layer of TiO$_2$ nanotubes can be formed before reaching the equilibrium between both rates.

4.5. Anodically Fabricated TiO$_2$ Nanotubes (NTs) as Potential Anodes in LIBs

As discussed above, the anodic oxidation offers the ability to tune the nanotube dimensions producing well-ordered and high surface area TiO$_2$ nanotube arrays perpendicularly attached to the Ti substrate. These easily tunable properties open up the possibility for various applications, especially as anodes in lithium ion batteries. The porous nature of such nanotubes can effectively decrease the lithium ion pathway, thus allowing for high lithium ion accessibility of the electrode material [142]. This property, in turn, decreases the polarization of the anode material and triggers a high charging/discharging rate. The high surface area enables intimate contact between the electrode material and the electrolyte causing low charge resistance. Since the formed nanotubes are sized below 20 nm in wall thickness, the one-dimensional structure of the nanotubes is flexible and can buffer volume changes originating from lithium ion insertion and removal.

Systematical studies supported with theoretical analysis were carried out to evaluate the Li ion storage of bare anodically fabricated TiO$_2$ and the conventional randomly oriented TiO$_2$ nanotubes mixed mechanically with 10% conductive carbon [143]. The results presented excellent electrochemical performance for the nanotubes prepared by anodization with a six-fold increase in capacity at a current density of 10 C compared to randomly organized TiO$_2$ nanotubes even after mixing with conductive carbon. These superior performances are ascribed to the good electrical contact between the nanotube oxide layer and the Ti substrate, which serves as current collector. This mixing with conductive carbon. These superior performances are ascribed to the good electrical contact between the nanotube oxide layer and the Ti substrate, which serves as current collector. This mixing with conductive carbon.
oxide layer and the Ti substrate, which serves as current collector. This arrangement leads to an increased electrical conductivity of the whole electrode [143]. Wei et al. [144] reported the effect of nanotube diameters and wall thicknesses on the storage performance and cycling stability of TiO$_2$. The nanotubes demonstrated a volumetric capacity of 180 mAh cm$^{-3}$. The results showed that 96.4% of the initial capacity was retained after 140 cycles for TiO$_2$ with 50 nm pore diameter and 25 nm wall thickness. When the tube diameter and wall thickness increased to 100 nm and 40 nm, respectively, a rapid capacity fading to only 53% of the original capacity was observed.

In the next sections, various approaches are discussed which affect the electrochemical properties of TiO$_2$ nanotubes prepared by anodization such as the employed electrolyte, the degree of crystallinity, the annealing atmosphere, structure modifications with carbonaceous materials, post-anodization, and the influence of other transition metal oxides.

4.5.1. Amorphous and Crystalline TiO$_2$ Anodes

Generally, TiO$_2$ nanotubes prepared by electrochemical anodization are amorphous. Previous studies showed that the crystalline anatase phase is formed by annealing of the NTs at a temperature above 280 °C in air. At temperatures higher than 450 °C a mixture of well crystalline anatase and small amounts of rutile are obtained [127]. A temperature between 600 to 900 °C is required for the complete phase transition from anatase to rutile [47,145]. Other studies showed that single-phase anatase is obtained after annealing of mixed or coated TiO$_2$ nanotubes at 450 °C. Nevertheless, the crystallization process of the NT depends on the specific chemical composition of the used metal and on the local diffusion of the alloying element. For example, Nb increases the conversion temperature of anatase to rutile [146]. Hence, rutile is not formed in the grown nanotubes on Ti6Al7Nb even when they are annealed at 550 °C. Alternatively, Fe concentration in a Ti-Fe alloy can promote the formation of rutile and decrease the anatase phase [147].

Particular interest was paid to investigate the relation between the degree of crystallinity and the electrochemical performance of TiO$_2$ nanotubes as anodes for lithium ion batteries. Experiments were conducted by Ivanov et al. [148] which revealed that the amorphous TiO$_2$ structure promotes a higher lithium ion diffusion rate than the crystalline anatase structure. The reason was attributed to larger amount of disorders and defects in the amorphous state than in the crystalline one. These defects offer bigger channels or more diffusion paths for Li ion migration. In addition, the low mechanical stress and less rigid nature owned by amorphous TiO$_2$ facilitate intercalation in large amounts [145,149]. Furthermore, Ryu et al. [150] reported a comparative study of amorphous vs. crystalline TiO$_2$ NTs and their storage capacity, rate capability, and cycling stability. The as-prepared and post-annealing NTs showed similar pore diameters (30–50 nm) and tube heights (8.2 μm). The voltage profiles of the amorphous tubes reach much higher specific capacities than the crystalline TiO$_2$ (Figure 11) due to the higher Li ion diffusivity in the amorphous structure. The rate capability of amorphous and crystalline anatase NTs was investigated by Fang et al. [151]. Amorphous TiO$_2$ exhibited a high rate capability compared to crystalline anatase fabricated with the same morphological features. This phenomenon is proven by the higher Li ions diffusion coefficient of amorphous TiO$_2$ compared to anatase.

Tighineanu et al. [152] studied the influence of annealing temperature and time on the ionic conductivity of TiO$_2$ nanotube arrays. The ionic conductivity of TiO$_2$ mainly depends on the conversion process from amorphous TiO$_2$ to the crystalline phases, where anatase showed a higher electrical conductivity than rutile-containing tube arrays. The optimal annealing temperature to obtain low resistance materials was found to be between 250 and 450 °C. This work also showed that crystalline anatase is obtained by annealing amorphous TiO$_2$ at 250 °C for a longer time up to 20 h [152]. Mixed compositions of anatase and rutile in the TiO$_2$ nanotube arrays, after thermal treatment above 580 °C, demonstrated higher areal capacity than that achieved by single anatase NTs [153]. The authors associated the enhanced insertion capacity with the higher Li ion diffusion coefficient of rutile in playing a stronger role than the improved electrical conductivity of anatase.
4.5.3. Influence of the Annealing Atmosphere on the Properties of TiO$_2$ Nanotube Anodes

Considerable attention has been drawn to the annealing atmosphere of the TiO$_2$ nanotubes as an important factor for their electrochemical storage properties. Experiments explored how the annealing atmosphere can affect the morphology and the present crystalline phases of the nanotube arrays. Free-standing TiO$_2$ nanotubes annealed in Ar atmosphere showed morphological features which differ from those obtained during annealing in air as presented in Figure 12a,b [154]. Furthermore, the electrochemical tests showed better performances for the sample annealed in Ar compared to that annealed in air (Figure 12c).

This behavior was explained by the presence of significant amounts of carbon mixed with the thermally treated nanotubes leading to improved electrical conductivity. Enhanced initial lithium ion insertion capacity up to 240 mAh g$^{-1}$ at a current density of 320 mA g$^{-1}$ was reported by Liu et al. [155] for anatase nanotube arrays when they were annealed in a N$_2$ atmosphere at 300 °C.

The achieved capacity decreased as the annealing temperature increased. The authors correlated their observation to the lower storage ability of rutile obtained by phase transformation from anatase at high temperatures leading to a reduced overall electrode capacity. Lu et al. [156] investigated the use of H$_2$/95% Ar as a reducing atmosphere to thermally treat the anodized TiO$_2$ NTs. Structural and morphological changes were observed for the annealed nanotubes in this reducing atmosphere associated with an improvement in their electrochemical rate performance during lithium insertion measurements. Results of the detailed experiments indicate the hydrogen treatment produced a large number of oxygen vacancies inside the crystal lattice of TiO$_2$, which represents active sites for Li ion diffusion and intercalation [156].
4.5.4. Free-Standing TiO$_2$ Nanotube Membranes

In addition to the nanotubes grown on Ti foils, there is great interest in using the TiO$_2$ nanotube membranes after the detachment from the substrates, especially when they can be used in applications like microbatteries. Wei et al. [157] reported a two-step anodization process followed by a thermal treatment to fabricate TiO$_2$ nanotube films. The TiO$_2$ membranes were separated from the Ti substrates by sonication. The resulting 3D free-standing TiO$_2$ nanotube layers were evaluated as anodes for microbatteries and exhibited an areal capacity of 0.46 mA cm$^{-2}$ (i.e., 184 mAh g$^{-1}$) at a current density of 0.05 mA cm$^{-2}$. Furthermore, these membrane electrodes demonstrated excellent cycling stability over 500 cycles with an overall capacity loss of about 6%. The found areal capacity depends on the nanotube length. Interestingly, by using two anodization steps, TiO$_2$ nanotubes with small pore diameter are formed. This aspect was utilized by Liu et al. [158] to produce nanotubes of 20 nm in length which showed excellently enhanced electron transport.

The above-mentioned approaches were aimed at increasing lithium ion storage performance by optimizing the nanotube dimensions, annealing temperature, and the environment to reduce the internal resistivity of the TiO$_2$ materials, but the poor electrical conductivity needs to be improved. Doping or coating TiO$_2$ nanotubes with other materials which are more conductive, such as graphene or CNTs, is usually the general protocol to overcome the conductivity obstacles.

Figure 12. SEM micrographs of the TiO$_2$ nanotubes thermally treated in (a) Ar in (b) air atmosphere and (c) the rate capability of each electrode, (d) voltage profile curves of the first discharge cycle of TiO$_2$ membranes, a, b, c representing annealed at 450 °C, 600 °C, and 800 °C in air, with d, e, f being 450 °C, 600 °C, 800 °C in Ar, respectively. Adapted with permission from ref. [154].
4.5.5. TiO$_2$ Nanotubes/Carbon Composites

Similar to TiO$_2$ nanoparticles and nanowires, doping of TiO$_2$ nanotubes with highly conductive materials were explored. Here, the aim was to improve the electronic conductivity of TiO$_2$ using carbon composites which provide more electrons to the TiO$_2$ surface to achieve a higher Li ion storage at very fast charging/discharging rates. Kilinic et al. [159] succeeded in fabricating C-doped TiO$_2$ nanotubes grown on Ti foils by anodic oxidation. Doping was performed through two different methods. The first is an in-situ synthesis during the anodic oxidation process. The key point here is the anodic oxidation electrolyte which must contain a carbon source such as polyvinyl alcohol. The second is a heat treatment method in which the anodized TiO$_2$ nanotubes are subjected to a thermal treatment at $500 \, ^\circ C$ under a $N_2/C_2H_2$ flux (1:1). Furthermore, carbon-modified anodically prepared TiO$_2$ nanotubes were also investigated by Mole et al. [160] by thermal treatment in a CH$_4$/H$_2$ atmosphere in the presence of Fe. A threefold increase in the double layer capacitance was demonstrated by C-TiO$_2$ nanotubes compared to the pure TiO$_2$ nanotube electrodes due to the improved charge transfer obtained by the presence of carbon and iron dopants. In addition, Chen et al. [161] developed a simple method to fabricate Au/RGO-TiO$_2$ NT composites via electrolysis of chloro-auric acid and graphene oxide on the surface of anodically fabricated TiO$_2$ nanotubes. These composite materials were only tested as photocatalysts. Fabrication of binary CNTs@TiO$_2$ composite anodes was recently studied by Madian et al. [162]. They synthesized a network of multiwalled CNTs laterally deposited onto the surface of anodically grown TiO$_2$ using a simple spray pyrolysis technique (Figure 13a,b). The CNTs@TiO$_2$ composite electrodes showed enhanced electrochemical performances over a current density range between 50 and 500 $\mu A \, cm^{-2}$ exhibiting a 1.5-fold increase in the areal capacity compared to pure thermally treated and untreated TiO$_2$ anodes (Figure 13c). The noticed electrochemical performance was ascribed to the improved charge transport and electronic conductivity of the composite anode due to the presence of a highly conductive network of CNTs that interfaced the TiO$_2$ NT. In addition, this tightly interwoven network can function as a second charge collector. In such studies, similar improvement in the electrochemical performance was observed for the CNT-coated TiO$_2$-CoO NTs compared to the mixed TiO$_2$-CoO NT.

4.5.6. Mixed Oxide Nanotubes

The fabrication of ordered mixed transition metal oxide nanotubes is usually obtained by two approaches, the first includes more than one preparation step in which the nanotubes are first fabricated via the usual synthesis procedures discussed above (such as anodization or atomic layer deposition) and are subsequently subjected to doping or coating processes. The second approach is realized by a single preparation step in which Ti-based alloys are used as substrates for the anodization to directly form mixed oxide tubes onto the surface. For instance, Co$_3$O$_4$ nanoparticles@TiO$_2$ nanotubes were synthesized by the electrodeposition of Co$_3$O$_4$ onto the grown TiO$_2$ nanotubes (Figure 14a). The Co$_3$O$_4$@TiO$_2$ composite was explored for lithium ion storage [163]. The coated Co$_3$O$_4$ layer leads to an increase of the Li ion insertion capacity which is related to the improved ionic conductivity as well as contributing to the overall electrode capacity itself. An interesting in-situ preparation process during the anodization of Ti foils was reported by Cao et al. [164] to produce Co$_3$O$_4$-doped TiO$_2$ nanotubes in which Co(NO$_3$)$_2$$\cdot6H_2O$ was utilized as cobalt source in the anodic oxidation electrolyte. This composite material showed enhanced photovoltaic properties under visible light but no results concerning energy storage applications were reported. Self-doping and electrodeposition techniques were employed to achieve uniform copper filling from the bottom to the top of the TiO$_2$ nanotubes [165]. That strategy was proposed to enhance the conductivity of the tube bottoms using a conductive copper coating. Similar to copper-filled TiO$_2$ nanotubes, a-Fe$_2$O$_3$ was selected and prepared by a pulse electrodeposition to finally form Fe$_2$O$_3$ nanorod/TiO$_2$ nanotube composites [166]. This approach allows for the growing of Fe$_2$O$_3$ rods with various lengths ranging between 50 and 550 nm according to the deposition time. In another study, Fe$_2$O$_3$ hollow nanorods were formed
on the outer and inner surface of anodically fabricated TiO$_2$ to prepare 3D hierarchical structures of Fe$_2$O$_3$@TiO$_2$ [167].

![Figure 13. SEM micrographs of uncovered (a) TiO$_2$ nanotubes, (b) CNTs@TiO$_2$ composite, (c) TiO$_2$-CoO NT, (d) CNTs@TiO$_2$-CoO NT. (e) The electrochemical performance of CNTs@TiO$_2$ and CNTs@TiO$_2$-CoO composite electrodes, (f) typical voltage profiles for the 10th, 20th, 30th, 40th, and 50th cycles against areal capacity of TiO$_2$-CoO NT anodes, adapted with permission from ref. [162].]
TiO\textsubscript{2} partially cracked composites. The assembled electrodes demonstrated good capacitive behavior as via anodic oxidation followed by the electrodeposition of MoO\textsubscript{3} and, thus, improved the overall electrode performance [171]. SnO\textsubscript{2} up to 85% after 50 cycles. The TiO\textsubscript{2} µ for Li ion storage by limiting the voltage ranges to 1.2–0.01 V vs. Li\textsuperscript{+}. Sn and SnO\textsubscript{2} supercapacitor and were not tested as a Li ion battery.

Gobal et al. [170] investigated the electrodeposition of Zn-Ni onto TiO\textsubscript{2} nanotubes in alkaline solution to the insertion capacity of the whole electrode was ascribed as a possible reason for the increased capacity. Guan et al. [169] reported an easily controllable synthesis of MoO\textsubscript{3}-doped TiO\textsubscript{2} nanotube arrays via anodic oxidation followed by the electrodeposition of MoO\textsubscript{3}. The MoO\textsubscript{3}-modified nanotube electrodes were able to deliver twice the areal capacity of bare TiO\textsubscript{2}. However, the electrochemical impedance spectra (EIS) analysis demonstrated that the Li ion transfer into TiO\textsubscript{2} is blocked by a thick layer of deposited MoO\textsubscript{3} nanoparticles. Therefore, the contribution of MoO\textsubscript{3} nanoparticles to the insertion capacity of the whole electrode was ascribed as a possible reason for the increased capacity. Gobal et al. [170] investigated the electrodeposition of Zn-Ni onto TiO\textsubscript{2} nanotubes in alkaline solution subsequently after thermal annealing at 300 °C to form NiO-ZnO/TiO\textsubscript{2} nanoporous but partially cracked composites. The assembled electrodes demonstrated good capacitive behavior as supercapacitor and were not tested as a Li ion battery.

To strengthen the anodic behavior of TiO\textsubscript{2} NTs, SnO\textsubscript{2} nanowires were grown on the surface of TiO\textsubscript{2} NTs by a two-step method in which the previously anodized TiO\textsubscript{2} nanotubes were subjected to an electrodeposition process. Sn and SnO\textsubscript{2} present in the mixed oxide electrodes were tested for Li ion storage by limiting the voltage ranges to 1.2–0.01 V vs. Li\textsuperscript{+}/Li [171]. An areal capacity of 140 µAh cm\textsuperscript{-2} was demonstrated by a 2 µm thick Sn/SnO\textsubscript{2} layer with a capacity retention of up to 85% after 50 cycles. The TiO\textsubscript{2} NTs helped to buffer the volume changes of the Li-Sn alloys and, thus, improved the overall electrode performance [171]. SnO\textsubscript{2} deposited coaxially onto TiO\textsubscript{2} nanotubes were synthesized by post electrodeposition and the corresponding SEM image is presented.

**Figure 14.** (a) SEM images of Co\textsubscript{3}O\textsubscript{4}-coated TiO\textsubscript{2} nanotubes obtained at photodeposition time of 4 h and (b) their areal capacities measured at different current densities, (c) voltage profile curves of bare TiO\textsubscript{2} (A), as-synthesized Co\textsubscript{3}O\textsubscript{4}/TiO\textsubscript{2}-1 with Co\textsubscript{3}O\textsubscript{4} loading of 0.12 mg cm\textsuperscript{-2} (B) and Co\textsubscript{3}O\textsubscript{4}/TiO\textsubscript{2}-2 with Co\textsubscript{3}O\textsubscript{4} loading of 0.25 mg cm\textsuperscript{-2} (C) electrodes as anodes in the 10th cycle adapted from ref. [163]. (d) SEM image of Fe\textsubscript{3}O\textsubscript{4} nanorods on TiO\textsubscript{2}. (e) Cycling performances of Fe\textsubscript{3}O\textsubscript{4}@TiO\textsubscript{2} in comparison with bare TiO\textsubscript{2} and (f) their voltage profile in the 1st and 2nd cycles. Adapted with permission from ref. [167].

The preparation technique includes the hydrolysis of Fe\textsuperscript{3+} ions to grow FeOOH nanospindles followed by the thermal transformation to Fe\textsubscript{2}O\textsubscript{3} nanorods as presented in Figure 14d,e. This heterojunctional composite was integrated as electrode in an LIB and demonstrated an outstanding electrochemical performance with an areal capacity of about 600 µA cm\textsuperscript{-2} that was retained for 50 cycles at a current density of 100 µA cm\textsuperscript{-2} (Figure 14f). Homogenous VO\textsubscript{2} nanoparticles were also deposited onto TiO\textsubscript{2} nanotube arrays by chemical vapor deposition. The well-dispersed VO\textsubscript{2} particles on the nanotube surface make TiO\textsubscript{2} a highly attractive catalytic material for different reactions [168]. Guan et al. [169] reported an easily controllable synthesis of MoO\textsubscript{3}-doped TiO\textsubscript{2} nanotube arrays via anodic oxidation followed by the electrodeposition of MoO\textsubscript{3}. The MoO\textsubscript{3}-modified nanotube electrodes were able to deliver twice the areal capacity of bare TiO\textsubscript{2}. However, the electrochemical impedance spectra (EIS) analysis demonstrated that the Li ion transfer into TiO\textsubscript{2} is blocked by a thick layer of deposited MoO\textsubscript{3} nanoparticles. Therefore, the contribution of MoO\textsubscript{3} nanoparticles to the insertion capacity of the whole electrode was ascribed as a possible reason for the increased capacity. Gobal et al. [170] investigated the electrodeposition of Zn-Ni onto TiO\textsubscript{2} nanotubes in alkaline solution subsequently after thermal annealing at 300 °C to form NiO-ZnO/TiO\textsubscript{2} nanoporous but partially cracked composites. The assembled electrodes demonstrated good capacitive behavior as supercapacitor and were not tested as a Li ion battery.
in Figure 15a [172]. The prepared monohybrids displayed a good electrical conductivity and, thus, an enhanced electrochemical performance for Li ion storage (Figure 15b). As previously mentioned, template-assisted atomic layer deposition (ALD) is considered as an alternative technique to fabricate TiO$_2$ with controlled tubular geometry but expensive infrastructure and growth time may limit this approach. Kim et al. [173] reported on the fabrication of SnO$_2$/TiO$_2$ NT heterostructures by ALD. The resulting mixed oxide electrodes offer a specific capacity of 100 mAh g$^{-1}$ in the second cycle. However, a capacity of 300 mAh g$^{-1}$ was maintained by this electrode even after 50 cycles. The surface modification by SnO$_2$ was designated to enhance the lithium insertion rate and, thus, increased the specific capacity of such electrode composite compared to pure TiO$_2$ (250 mAh g$^{-1}$).

Figure 15. (a) SEM image of coaxial SnO$_2$@TiO$_2$ nanotubes synthesized by post electrodeposition. (b) Their galvanostatic charging-discharging curves obtained at a current rate of 100 µA cm$^{-2}$, adapted from ref. [172]. TEM images of an atomic layer deposition (ALD)-grown SnO$_2$. (c) The magnified images obtained from three different regions are presented as insets with (d) galvanostatic charging-discharging curves measured at a current rate of 0.1 C, adapted with permission from ref. [173].

Surface modification to TiO$_2$ nanotubes can also be carried out by deposition of Li$_3$PO$_4$ on the surface as presented by Lopez et al. [174]. The obtained 3D structure of Li$_3$PO$_4$-coated TiO$_2$ was assembled as electrode and was tested for lithium ion storage. The electrochemical results revealed a reversible capacity of 110 mAh g$^{-1}$ achieved for over 190 cycles at a rate of 5 C. The lithium phosphate was proposed in that composite as ionic conductor which improved the electrical and ionic conductivity of TiO$_2$ [174]. Alternatively, a straightforward approach used to fabricate self-organized mixed oxide nanotube arrays is found in the anodic oxidation of Ti-based alloys.

Although several binary and ternary mixed oxide nanotubes were fabricated by the anodization of Ti-Fe [148], Ti-Ta, Ti-Nb [175], Ti-Pd [176], Ti-Al [177], Ti-Mo [178], Ti-V [179], Ti-W [180], Ti-Mn [181], Ti-Ni [182], Ti-Mo-Ni [183], and Ti-6Al-4V [184] alloys, only some of them were applied as electrodes in lithium ion batteries. As an example, well-ordered mixed Ti-Mn-O nanotubes were grown on the surface of a Ti-8Mn alloy by anodization [181]. The mixed oxide anodes were integrated with a LiCoO$_2$ cathode to assemble a full cell battery. These mixed oxide nanotubes showed a capacity of 474 mAh g$^{-1}$ which was held for 30 cycles. A decent electrode of ordered TiO$_2$/Nb$_2$O$_5$ nanotubes
demonstrated long-term cycling stability and higher reversible lithium storage capacity than pure TiO$_2$ nanotube arrays prepared under similar conditions [185]. Madian et al. [125] showed the ability to fabricate self-ordered CoO/TiO$_2$ NTs by the anodic oxidation of two-phase Ti-Co alloy, as presented in Figure 16. This hybrid oxide anode was synthesized at 60 V, and demonstrated an areal capacity of 600 $\mu$Ah cm$^{-2}$ corresponding to 315 mAh g$^{-1}$ at a current density of 10 $\mu$A cm$^{-2}$ with a Coulombic efficiency of 96%. Such electrodes showed a 1.6 increase in the capacity compared to pure TiO$_2$ NT synthesized under the same conditions preserving 88% of their initial capacity over 100 cycles.

Madian et al. [186] worked on the improvement of TiO$_2$ NT arrays for potential anode application with single phase Ti-Sn alloys. Different Sn concentrations (1–10 at %) were utilized to grow well-organized Ti-Sn-O NT. The as-prepared nanotubes on a TiSn$_1$ alloy at 40 V (Figure 17a,b) exhibited an areal capacity of 405 $\mu$Ah cm$^{-2}$ (i.e., 212 mAh g$^{-1}$) at a current density of 504 $\mu$A cm$^{-2}$ with a superior cycling stability over 400 cycles as shown in Figure 17c. A 1.4 times higher capacity was demonstrated by these mixed oxide electrodes compared to the pure TiO$_2$ NT fabricated under similar conditions. This effect was attributed to the high surface area and the improved ionic conductivity due to the presence of SnO$_2$ NTs on the (TiSn)$_2$O$_2$ NTs, resulting in a higher lithium ion diffusion rate. The tubular structure of the mixed oxide electrodes remained unaffected over the electrochemical cycling.
An enormous number of studies have investigated the synthesis and modifications of TiO$_2$-based nanostructured electrodes to look for improved electrochemical performance when applied to lithium ion batteries. Table 2 summarizes the most promising electrochemical results on TiO$_2$ nanotubes and TiO$_2$/SnO$_2$ anodes. TiS (green circles), T5S (blue circles), and T10S (black circles) correspond to the nanotubes prepared on the TiSn$_1$, TiSn$_5$, and TiSn$_{10}$ alloy substrates, respectively, adapted with permission from ref. [186].

5. Summary

An enormous number of studies have investigated the synthesis and modifications of TiO$_2$-based nanotubes by anodic oxidation has been extensively addressed here because this technique may possibly reach all the previously defined property and market criteria. Additionally, critical aspects affecting the electrochemical performance of the anodically prepared TiO$_2$ nanotubes are highlighted. These aspects include the formation mechanism, the impact of morphology, crystallinity, annealing atmosphere and temperature, surface modification with carbonaceous materials, and mixing with other transition metal oxides. Moreover, we pointed out the recent methods used to synthesize mixed oxide nanotubes, either with two-step or single-step preparation methods. In short, this report is designated to guide and help the science in this field to overcome the challenges presented above and to give nanostructured TiO$_2$ oxide systems a real chance for a broad application.

Figure 17. (a) SEM micrographs of the TiSn$_1$ alloy anodized at 40 V for 5 h; (b) Cross-sectional view of the nanotubes grown at 40 V. The inset in (b) shows the uniform growth of the nanotubes. (c) Galvanostatic cycling obtained at a current density of 504 mA cm$^{-2}$ for pure TiO$_2$ (dark red circles) and TiO$_2$/SnO$_2$ anodes. T1S (green circles), T5S (blue circles), and T10S (black circles) correspond to the nanotubes prepared on the TiSn$_1$, TiSn$_5$, and TiSn$_{10}$ alloy substrates, respectively, adapted with permission from ref. [186].
Table 2. Electrochemical performance of various TiO₂ nanostructure based anodes.

<table>
<thead>
<tr>
<th>Composition</th>
<th>Synthesis</th>
<th>Capacity after 20th Cycle</th>
<th>Current Rate</th>
<th>Number of Reversible Cycles</th>
<th>Reference</th>
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<tr>
<td>Rutile nanoparticles</td>
<td>Commercially obtained</td>
<td>207 mAh g⁻¹</td>
<td>0.05 A g⁻¹</td>
<td>20</td>
<td>[107]</td>
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<tr>
<td>Anatase nanoparticles</td>
<td>solothermal</td>
<td>196 mAh g⁻¹</td>
<td>0.2 C</td>
<td>100</td>
<td>[65]</td>
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<tr>
<td>TiO₂-BC hollow spheres</td>
<td>sol-gel hydrothermal</td>
<td>170 mAh g⁻¹</td>
<td>2 C</td>
<td>300</td>
<td>[72]</td>
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<tr>
<td>TiO₂ nanoparticles</td>
<td>in-situ hydrolysis</td>
<td>70 mAh g⁻¹</td>
<td>5 A g⁻¹</td>
<td>400</td>
<td>[75]</td>
</tr>
<tr>
<td>Core-shell CNFs/TiO₂</td>
<td>hydrolysis</td>
<td>240 mAh g⁻¹</td>
<td>5 A g⁻¹</td>
<td>100</td>
<td>[74]</td>
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<tr>
<td>Anatase nanorods</td>
<td>hydrolysis</td>
<td>206 mAh g⁻¹</td>
<td>50 mA g⁻¹</td>
<td>30</td>
<td>[96]</td>
</tr>
<tr>
<td>Anatase nanowires</td>
<td>hydrolysis</td>
<td>280 mAh g⁻¹</td>
<td>140 mA g⁻¹</td>
<td>40</td>
<td>[97]</td>
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<tr>
<td>TiO₂ nanofibers</td>
<td>electropinning</td>
<td>170 mAh g⁻¹</td>
<td>0.3 C</td>
<td>50</td>
<td>[95]</td>
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<tr>
<td>C-doped TiO₂ nanowires</td>
<td>hydrothermal</td>
<td>306 mAh g⁻¹</td>
<td>0.1 C</td>
<td>1000</td>
<td>[96]</td>
</tr>
<tr>
<td>TiO₂ NTs/graphene</td>
<td>hydrothermal</td>
<td>357 mAh g⁻¹</td>
<td>10 mA g⁻¹</td>
<td>50</td>
<td>[98]</td>
</tr>
<tr>
<td>TiO₂/C hollow nanofibers</td>
<td>force spinning</td>
<td>229 mAh g⁻¹</td>
<td>100 mA g⁻¹</td>
<td>100</td>
<td>[100]</td>
</tr>
<tr>
<td>Graphene-wrapped TiO₂ nanofibers</td>
<td>electropinning</td>
<td>200 mAh g⁻¹</td>
<td>0.1 C</td>
<td>35</td>
<td>[101]</td>
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<td>Anatase/graphene nanosheets</td>
<td>solothermal</td>
<td>161 mAh g⁻¹</td>
<td>1 C</td>
<td>120</td>
<td>[102]</td>
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<td>TiO₂/graphene</td>
<td>hydrolysis</td>
<td>230 mAh g⁻¹</td>
<td>0.1 C</td>
<td>100</td>
<td>[103]</td>
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<td>TiO₂ nanoporous hollow spheres</td>
<td>template-assisted</td>
<td>230 mAh g⁻¹</td>
<td>33.5 mA g⁻¹</td>
<td>50</td>
<td>[106]</td>
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<td>Mesoporous TiO₂ nanoparticles</td>
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<td>268 mAh g⁻¹</td>
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<td>[107]</td>
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<td>C-coated mesoporous</td>
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<td>111 mAh g⁻¹</td>
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<td>TiO₂@graphene sheets</td>
<td>thermal treatments</td>
<td>860 mAh g⁻¹</td>
<td>1 A g⁻¹</td>
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<td>[112]</td>
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<td>Fe₃O₄ nanoparticles-TiO₂</td>
<td>chemical etching</td>
<td>857 mAh g⁻¹</td>
<td>10 mA g⁻¹</td>
<td>240</td>
<td>[113]</td>
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<td>Hierarchical TiO₂/Fe₃O₄ fiber-in-tube</td>
<td>electropinning</td>
<td>191 mAh g⁻¹</td>
<td>1 A g⁻¹</td>
<td>60</td>
<td>[115]</td>
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<tr>
<td>Hierarchically ordered porous anatase</td>
<td>solothermal alcoholysis</td>
<td>225 mAh g⁻¹</td>
<td>1 C</td>
<td>70</td>
<td>[118]</td>
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<tr>
<td>TiO₂ NTs</td>
<td>anodization</td>
<td>140 mAh g⁻¹</td>
<td>0.1 C</td>
<td>1000</td>
<td>[145]</td>
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<tr>
<td>3D free-standing TiO₂ NTs</td>
<td>anodization</td>
<td>184 mAh g⁻¹</td>
<td>0.05 mA cm⁻²</td>
<td>500</td>
<td>[157]</td>
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<td>SnO₂/TiO₂ NTs</td>
<td>atomic layer deposition</td>
<td>250 mAh g⁻¹</td>
<td>0.1 C</td>
<td>50</td>
<td>[173]</td>
</tr>
<tr>
<td>Ti-Mn-O NTs</td>
<td>anodization</td>
<td>474 mAh g⁻¹</td>
<td>175 mA g⁻¹</td>
<td>30</td>
<td>[181]</td>
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<tr>
<td>CoO/TiO₂ NTs</td>
<td>anodization</td>
<td>600 μAh cm⁻²</td>
<td>10 μA cm⁻²</td>
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<td>[125]</td>
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<tr>
<td>TiO₂/CoO NTs</td>
<td>anodization</td>
<td>405 μAh cm⁻²</td>
<td>504 μA cm⁻³</td>
<td>400</td>
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<td>450 μAh cm⁻²</td>
<td>50 μA cm⁻²</td>
<td>90</td>
<td>[156]</td>
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</table>

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