Modulating and Orienting an Anisotropic Zn-Based Metal Organic Framework for Selective CH$_4$/CO$_2$ Gas Separation

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Abstract: This work investigates the morphological control of the anisotropic [Zn$_2$(NDC)$_2$(DABCO)]$_n$ MOF (Metal organic framework) and the subsequent adsorption characteristics for CO$_2$/CH$_4$ gas separation. Morphology of the MOF crystals is controlled by the use of modulators. The addition of acetic acid or pyridine successfully produce rod or plate morphologies, respectively, with each morphology possessing a different major surface pore aperture. Single-component equilibrium and kinetic adsorption data for CO$_2$ and CH$_4$ were collected. Equilibrium analysis indicates a slight selectivity towards CO$_2$ whereas kinetic data unexpectedly shows lower diffusion time constants for CO$_2$ compared to CH$_4$. Mass transfer resistances on each species is discussed. Finally, a coating technique termed solution shearing is used to orient different morphologies on substrates as a film. An increase in film orientation is observed for the rod morphology, indicating that this MOF morphology is a promising candidate to create large area, thin-film applications.

Keywords: MOFs; gas separation; anisotropic MOFs; modulation; oriented crystals; solution shearing

1. Introduction

The efficient separation of CO$_2$ from CH$_4$ is critical for the technoeconomic success of the natural and biogas industries, however current industrial separation techniques are energy intensive or require high capital and operational expenses [1,2]. Common separation processes such as cryogenic distillation require a significant amount of energy and do not align with “green” chemistry practices, highlighting the need to find alternative approaches [1,2]. Recent attempts at making these separations more efficient involve the use of polymer membranes. While these membrane systems require a lower energy input, a lower concentration of feed CO$_2$ is required to prevent the membrane from plasticizing [3]. Other approaches use zeolites, but these materials are often synthesized with non-ideal particle morphologies, offer a limited range of pore sizes and chemistry, and can require energy and capital-intensive synthesis conditions [4]. An ideal separation platform would use easily synthesized and easily tunable materials, and would be effective regardless of intake quantities and concentrations.

Metal organic frameworks (MOFs) are novel materials and could potentially fulfill these requirements. MOFs consist of metal ion clusters bound together by coordinating organic linkers to form a porous, periodic structure [5,6]. Their key features include high surface areas (>1000 m$^2$/g), chemical customizability, and relatively easy and low temperature synthesis, which enable their application in a wide range of areas including catalysis, fuel cell development, drug delivery, data storage, and gas separations [5,7–11].
MOFs have shown promise as selective gas separators due to their ability to sterically and chemically restrict the species that pass through their pores. MOFs have previously been used in combination with a polymer matrix to demonstrate a high selectivity in a CO₂/CH₄ gas mixture [2]. It was hypothesized that the selective permeation was due to the well-defined sorption properties of the microporous, crystalline MOF [2]. Additionally, it has been shown that the unmodulated [Cu₂(NDC)₂(DABCO)]ₙ MOF can separate gases in a CO₂/CH₄ system where CO₂ and CH₄ have differing kinetic diameters of 3.3 Å and 3.8 Å, respectively [12,13]. This system is interesting for gas sorption kinetics due to its different lattice dimensions leading to anisotropic pore sizes (a = b = 10.819 Å, c = 9.635 Å).

Recent studies have shown that these gas adsorption capabilities can be further enhanced through the introduction of modulators during MOF synthesis, by altering the overall crystal growth process [14]. In anisotropic MOFs, such as those in the M₂(dicarboxylate)₂(N-ligand) series, the modulator-based growth control is dramatic and can significantly alter crystal aspect ratios [15–17]. The introduction of modulators during synthesis can target either the carboxylate (h00, o0k) or the amino (00l) planes, inhibiting crystal growth along these planes and directing MOF crystal growth along unmodulated axes (Figure 1) [15–17]. Previous work has demonstrated the [Cu₂(NDC)₂(DABCO)]ₙ (NDC = 1,4-naphthalene dicarboxylate; DABCO = 1,4-diazabicyclo[2.2.2]-octane) member of the [M₂(dicarboxylate)₂(N-ligand)]ₙ MOF series can be modulated to obtain rod or plate morphologies with the use of acetic acid (carboxylate) or pyridine (amino) modulators [18].

Figure 1. Schematic of the modulation process for the [Zn₂(NDC)₂(DABCO)]ₙ MOF. Acetic acid (red pyramids) competitively coordinates with 1,4-naphthalene dicarboxylate (red rods) to direct growth in the [001] direction, while pyridine (blue pyramids) competitively coordinates with DABCO (blue spheres) to direct growth in the [100] and [010] direction.

The intrinsic anisotropy of the unit cell, combined with modifying the crystal aspect ratio, exposes pore apertures of different dimensions on the crystal surface. The choice of modulator determines which pore aperture is exposed as the major pore aperture on the crystal surface, allowing for selection of the surface pore dimension, as well as the total internal channel length of each pore type. For example, the use of an amino modulator creates a plate morphology where a carboxylate-carboxylate aperture predominates on the crystal surface, while the use of a carboxylate

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modulator creates a rod morphology where more of the carboxylate-amino aperture is present on the surface of the crystal. These morphologies can be used to create and tune molecular sieves for specific separation applications within the same topology.

While many examples of the effect of modulators on individual MOF crystal growth have been studied, controlling the overall orientation of these crystals for membrane applications is also important. Previous work has shown that MOF crystals can be oriented on mixed matrix membrane post-synthesis, which then show an increased performance in separation applications [19]. Ghorbanpour et al. [20] have also shown that MOF crystals can be oriented post-synthesis through a solution shearing technique to form highly ordered thin films. These are highly desirable qualities for gas separation membranes, as oriented thin films, along with controlled crystal aspect ratios, allow for a higher flux than packed beds while retaining performance [21].

In this work, we synthesized and characterized the \([\text{Zn}_2(\text{NDC})_2(\text{DABCO})_n] \) MOF and controlled its morphology using pyridine and acetic acid as modulators to form plates and rods, respectively. We then demonstrated the change in steric separation selectivity using these two crystal morphologies in a single component adsorption system for both CO\(_2\) and CH\(_4\). We tested this performance in a competitive adsorption environment. Finally, using solution shearing and drop casting, we show differing thin film orientation of the modulated crystals for future applications as thin film separation membranes.

2. Materials and Methods

2.1. Materials

The following chemicals were purchased from Sigma Aldrich (St. Louis, MO, USA): dimethyl formamide (DMF, \(\geq 99.8\%)\), acetone (\(\geq 99.9\%)\), Zn(CH\(_3\)COO)\(_2\)·2H\(_2\)O (\(\geq 99.0\%)\), and DABCO (\(\geq 99\%)\). 1,4-napthalenedicarboxylic acid (98+%) was purchased from Alfa Chemistry (Ronkonkoma, NY, USA), while pyridine (ACS grade), acetic acid (ACS grade), toluene (99.9%), and isopropyl alcohol (laboratory grade) were purchased from Fisher Chemical (Hampton, NH, USA). Quartz tubes were purchased from Quartz Scientific, Inc (Fairport Harbor, OH, USA). CO\(_2\) (99.99%), CH\(_4\) (99.97%), and N\(_2\) (99.999%) gases were purchased from Praxair Inc (Danbury, CT, USA).

2.2. Synthesis of \([\text{Zn}_2(\text{NDC})_2(\text{DABCO})_n] \) MOFs

In a typical unmodulated MOF synthesis, a solution with 0.050 g of DABCO, 0.196 g of 1,4-NDC and 13.20 g of DMF was added to a solution of 0.277 g of Zn(CH\(_3\)COO)\(_2\)·2H\(_2\)O and 19.82 g of DMF for a final molar ratio of Zn/DABCO/1,4-NDC/DMF of 2.8:2:1:400. The total mixture was stirred for 25 min, after which it was poured into a 50 mL Teflon lined acid digestion vessel (Parr Instruments, Moline, IL, USA) and heated at 100 \(^\circ\)C for 24 h.

The same process was applied to synthesizing \([\text{Zn}_2(\text{NDC})_2(\text{DABCO})_n] \) rod and plate morphologies with the addition of a modulator. To synthesize rods, a solution with 0.045 g of DABCO, 0.171 g of 1,4-NDC and 11.80 g of DMF was added to a solution of 0.247 g of Zn(CH\(_3\)COO)\(_2\)·2H\(_2\)O, 3.37 g of acetic acid, and 17.70 g of DMF for a final molar ratio of Zn/DABCO/1,4-NDC/acetic acid/DMF of 2.8:1:2:125:400. The total mixture was stirred for 25 min, after which it was poured into a 50 mL Teflon lined acid digestion vessel (Parr Instruments, Moline, IL, USA) and heated at 100 \(^\circ\)C for 24 h.

After cooling for 1 h, the precipitate was centrifuged and washed once with fresh DMF and twice with EtOH. The resulting product was then heated to 80 \(^\circ\)C under ~3 kPa vacuum overnight and stored as a powder under vacuum.

2.3. Characterization

All X-ray diffraction (XRD) patterns were recorded on a PANalytical Empyrean X-ray diffractometer (Malvern Pananalytical, Egham, UK) with a Cu K-\(\alpha\) beam (\(\lambda = 1.54 \text{ Å}\)). Scans were
completed from 20 of 7° to 70° with a step size of 0.0035°. For Brunauer, Emmet, Teller isotherm (BET) analysis, MOF samples of 15–25 mg were degassed at 70 °C until a pressure of $1.3 \times 10^{-3}$ kPa was obtained, after which the samples were heated at 80 °C for 8 h. BET surface areas were measured using nitrogen adsorption isotherms collected on a Micromeritics ASAP 2020 instrument (Micromeritics, Norcross, GA, USA) at a relative pressure range of 0.01–0.05 relative to the nitrogen saturation pressure at 77 K. SEM micrographs were collected with a FEI Quanta 650 at 3 kV with a spot size of 4 at various magnifications.

2.4. CO$_2$ and CH$_4$ Kinetic and Equilibrium Experiments

Single-component adsorption equilibrium and kinetics of CO$_2$ and CH$_4$ were measured volumetrically using a Micromeritics ASAP 2020 Surface Area and Porosity Analyzer using the Rate of Adsorption Software (ROA v1.02, Micromeritics, Norcross, GA, USA) at 273.15 K with pressures up to 105 kPa. Initially, 100–400 mg of MOF sample was degassed using the same process outlined for BET isotherms. Samples were degassed between subsequent runs by holding a pressure of $1.3 \times 10^{-3}$ kPa for minimum of 5 h at room temperature and stored under nitrogen atmosphere. Kinetic data was taken at pressures of ~53 kPa and ~93 kPa. At these pressures, adsorbate was dosed into the sample chamber nominally at 5 cm$^3$/g and the resulting change in pressure was recorded and converted to an uptake volume as a function of time. The first 1 s of data was discarded to account for valve switching time and gas expansion into the sample chamber. The final adsorption amount at 1.05 atm was used as the equilibrium quantity.

For multi-component adsorption experiments, MOF samples were sieved to particle sizes between 250 and 600 µm, after which 30–70 mg of sieved material was gently mixed with 105 mg of crushed cordierite sieved to the same size. The mixture was loaded between quartz wool in a quartz tube reactor (inner diameter: 6.35 mm, length: 457 mm). The tube was set into a Lindbergh Mini-Mite furnace for temperature control. Gas concentrations and flows were controlled using MKS mass flow controllers. The adsorption experiments were initiated by generating a step change of the adsorbate concentrations in the reactor [22]. Prior to the multi-component adsorption experiment, the quartz tube reactor was heated to 60 °C and nitrogen gas was passed over the sample for a minimum of 20 min to remove any residual water. After cooling to room temperature, separation tests were run by introducing a gas mixture of ~1000 ppm CO$_2$, ~1000 ppm CH$_4$, balanced by N$_2$, flowrates were adjusted based on the mass of MOF samples to keep a constant space velocity. Controls were taken of an empty reactor and a reactor containing only cordierite to determine dead volume effects on measurements. The composition of the downstream was analyzed every second by an MKS MultiGas 2030 (MKS Instruments, Inc., Andover, MA, USA).

2.5. Solution Shearing of [Zn$_2$(NDC)$_2$(DABCO)]$_n$ Particles

A solution shearing procedure previously outlined by Ghorbanpour et al. was used to make thin films from particle suspension [20]. Solution shearing was conducted on 1 cm × 1 cm silicon wafers washed thoroughly with toluene, acetone, and isopropyl alcohol prior to the deposition of 20 µL of 5 wt./wt. % MOF/EtOH solution on the silicon wafer substrate. The substrate was heated to 60 °C, and the shearing blade was translated at speeds of 0.1, 0.25, and 0.5 mm/s for each morphology. Drop-cast samples were created by depositing 20 µL of 5 wt. % MOF/EtOH solution on silicon wafers substrates heated to temperatures of 60 °C. The orientation of the solution sheared MOF thin film was quantified by dividing the intensity of the (110) peak by the (001) peak intensity in the XRD.

3. Results and Discussion

3.1. Characterization of Modulated [Zn$_2$(NDC)$_2$(DABCO)]$_n$

By extending the rationale developed by Pham et al., rod and plate morphologies of the [Zn$_2$(NDC)$_2$(DABCO)]$_n$ MOF can be created with the use of acetic acid (carboxylate) or pyridine
(amine) modulators, respectively [18]. Figure 2 shows scanning electron microscope (SEM) images of particles synthesized with no modulator, 1.6 M acetic acid as modulator, and 1.6 M pyridine as modulator. Compared to the unmodulated synthesis, the modulated syntheses show larger crystals. The acetic acid modulator shows the formation of rod-like crystals, and the pyridine modulator shows the formation of plate-like crystals. This confirms that modulating for different coordination modes in a MOF composed of two distinct linkers can yield drastically different morphologies. It should be noted that at similar modulator concentrations, the [Zn$_2$(NDC)$_2$(DABCO)]$_n$ MOF was found to produce single crystals which are a magnitude greater in size than the previously reported [Cu$_2$(NDC)$_2$(DABCO)]$_n$ MOF [18]. Aspect ratios of these crystals are described in Table 1 showing both modulators increase the aspect ratio of their respective morphologies. The unmodulated MOF shows slight preferential growth to a rod-like morphology. While the major axis for the rod morphology is in the [001] direction, the major axes for the plate morphology are in the [100] and [010] directions (Figure 1). It should be noted the major planes on each particle (i.e., the surfaces parallel to the major axis or axes) are associated with the carboxylate-carboxylate or carboxylate-amine pore aperture as a result of the anisotropic crystal structure.

![Figure 2. SEM image of [Zn$_2$(NDC)$_2$(DABCO)]$_n$ (a) unmodulated resulting in bulk morphology (b) 1.6 M acetic acid as a modulator resulting in rod morphology and (c) 1.6 M pyridine as a modulator resulting in plate morphology. Scale bars are 5 µm.](image)

<table>
<thead>
<tr>
<th>Morphology</th>
<th>Minor Axis (µm)</th>
<th>Major Axis (µm)</th>
<th>Aspect Ratio</th>
<th>Major Surface Plane(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bulk</td>
<td>0.3 ± 0.1</td>
<td>0.6 ± 0.3</td>
<td>2.1 ± 1.1</td>
<td>N/A</td>
</tr>
<tr>
<td>Rod</td>
<td>1.2 ± 0.5</td>
<td>10.5 ± 5.4</td>
<td>10.1 ± 5.3</td>
<td>(100), (010)</td>
</tr>
<tr>
<td>Plate</td>
<td>0.4 ± 0.1</td>
<td>2.7 ± 0.4</td>
<td>6.9 ± 2.5</td>
<td>(001)</td>
</tr>
</tbody>
</table>

Table 1. Minor axis, major axis, and aspect ratio measurements for different morphologies of [Zn$_2$(NDC)$_2$(DABCO)]$_n$.

Figure 3 shows powder x-ray diffraction (PXRD) data collected for [Zn$_2$(NDC)$_2$(DABCO)]$_n$ MOF synthesis with and without the presence of the amine and carboxylate modulators compared to a simulated diffraction pattern. These patterns show that the modulators do not alter the crystal structure. It should be noted that texture in the bulk powder sample is observed. Differing relative intensities in the peaks, specifically in those matching the (001) and (110) planes, are recorded for different morphologies. Since particle orientation affects the relative intensity of diffraction peaks, these patterns indicate a preferential crystal orientation for a bulk powder. This is likely due to particle morphology influencing packing, orienting particles along their major axes and with respect to the substrate [23]. This effect is highlighted in Figure 2c, where plates are observed to orient in stacks.
3.2. Adsorption Isotherms

Nitrogen isotherms of the synthesized [Zn$_2$(NDC)$_2$(DABCO)]$_n$ MOF were used to verify the microporosity of the synthesized material for the bulk and modulated samples (Figure S1). The BET surface area (Table 2) and isotherms are comparable to that of reported values for the Zn and Cu analog of [M$_2$(NDC)$_2$(DABCO)]$_n$ (M = Zn, Cu) [15,18]. Experiments show that the [Zn$_2$(NDC)$_2$(DABCO)]$_n$ surface area measurements are highly sensitive to the drying procedure (Table S1). The sensitivity is likely due to solvent stabilization effects observed in the [Zn$_2$(dicarboxylate)$_2$(N-ligand)]$_n$ MOF family [15]. Previous results have shown that a MOF with a similar zinc-based topology had reduced crystallinity after activation, indicating a partial collapse of the framework [15]. Given this information, it is difficult to ascertain surface area contributions from defects due to modulation (i.e., defect engineering) or degradation from activation for the different modulated syntheses. However, a similarity in measured surface area between morphologies shows that any effect is similar in all three cases.

Table 2. BET surface areas and standard error calculated from nitrogen isotherms at 77 K for three (3) samples of the bulk morphology and four (4) samples of the plate-like and rod-like morphologies of [Zn$_2$(NDC)$_2$(DABCO)]$_n$ and a reference value.

<table>
<thead>
<tr>
<th>Morphology</th>
<th>BET Surface Area (m$^2$/g)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Zn$_2$(NDC)$_2$(DABCO) Bulk [25]</td>
<td>1000</td>
</tr>
<tr>
<td>Bulk</td>
<td>1226 ± 16</td>
</tr>
<tr>
<td>Rod</td>
<td>1100 ± 68</td>
</tr>
<tr>
<td>Plate</td>
<td>946 ± 127</td>
</tr>
</tbody>
</table>

Figure 4 shows the single-component isotherms for CO$_2$ and CH$_4$ of [Zn$_2$(NDC)$_2$(DABCO)] at 273 K for different morphologies. The total uptake of each species follows the same trend as BET surface area measurements, where lower quantities of CO$_2$ and CH$_4$ are adsorbed by lower surface area morphologies. This behavior is expected for physisorption as the quantity adsorbed is a function of the accessible surface area. The Langmuir isotherm model (Equation (1)) provides an accurate approximation of the adsorption with fitting parameters listed in Table 3.
where \( q \) is the quantity adsorbed per mass of adsorbate, \( a_m \) is the maximum adsorbed quantity per adsorbate mass to form a complete monolayer, \( b \) is the affinity or Langmuir constant and \( P \) is the dosing pressure.

\[
q = a_m \frac{bP}{1 + bP}
\]

Figure 4. Adsorption isotherms for bulk, plate and rod morphologies of \([\text{Zn}_2(\text{NDC})_2(\text{DABCO})]_n\) at 273 K for (a) \( \text{CO}_2 \) and (b) \( \text{CH}_4 \).

Table 3. Langmuir isotherm fitting parameters \((a_m \text{ and } b)\), Henry’s constant \((K)\) and \( \text{CO}_2/\text{CH}_4 \) selectivity for different morphologies of \([\text{Zn}_2(\text{NDC})_2(\text{DABCO})]_n\).

<table>
<thead>
<tr>
<th>Morphology</th>
<th>Adsorbate</th>
<th>( a_m ) (mmol/g)</th>
<th>( b ) (kPa(^{-1}))</th>
<th>( K ) (mmol/g kPa)</th>
<th>( \text{CO}_2/\text{CH}_4 ) Selectivity, ( \alpha )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bulk</td>
<td>( \text{CO}_2 )</td>
<td>12.78</td>
<td>0.0066</td>
<td>0.0842</td>
<td>3.85</td>
</tr>
<tr>
<td></td>
<td>( \text{CH}_4 )</td>
<td>9.38</td>
<td>0.0023</td>
<td>0.0219</td>
<td></td>
</tr>
<tr>
<td>Rod</td>
<td>( \text{CO}_2 )</td>
<td>10.35</td>
<td>0.0069</td>
<td>0.0716</td>
<td>4.46</td>
</tr>
<tr>
<td></td>
<td>( \text{CH}_4 )</td>
<td>5.26</td>
<td>0.0031</td>
<td>0.0161</td>
<td></td>
</tr>
<tr>
<td>Plate</td>
<td>( \text{CO}_2 )</td>
<td>10.21</td>
<td>0.0070</td>
<td>0.0719</td>
<td>4.26</td>
</tr>
<tr>
<td></td>
<td>( \text{CH}_4 )</td>
<td>6.16</td>
<td>0.0027</td>
<td>0.0169</td>
<td></td>
</tr>
</tbody>
</table>
The product of $a_m$ and $b$ yield another constant termed Henry’s constant ($K$), which provides a linear approximation of the adsorption isotherm. The ratio of Henry’s constants for CO\textsubscript{2} and CH\textsubscript{4} provides an equilibrium selectivity, $\alpha$.

[Zn\textsubscript{2}(NDC)\textsubscript{2}(DABCO)] demonstrates moderate selectivity towards CO\textsubscript{2} compared to CH\textsubscript{4}. This value is comparable to selectivity for other MOFs under similar conditions such as the ZIF family (3.9–10.1) [26], MIL-101 (3–5) [27] and MOF-177 (4.43) [28]. The higher affinity of CO\textsubscript{2} to adsorb on the surface is likely due to a higher quadrupole moment [27,29]. Both modulated morphologies (amine and carboxylate) show a moderate increase in selectivity compared to the bulk. This may be because more defect sites are preferentially interacting with CO\textsubscript{2} [30], however more work is required to confirm this interaction.

3.3. Surface Pore Aperture and CO\textsubscript{2}/CH\textsubscript{4} Kinetic Selectivity

As previously mentioned, the major surface for each crystal morphology, defined as the surfaces parallel to the crystal major axes, is associated with a crystallographic plane. More specifically, the plate morphology will have a major surface with a pore entrance aperture defined by the carboxylate-carboxylate frame, whereas the rod morphology will have a major surface with a pore entrance aperture defined by the carboxylate-amine frame (Figure 1). Each pore aperture is expected to present different mass transfer resistances [31]. Therefore, diffusional differences between carboxylate-carboxylate and carboxylate-amine pore apertures will exist and variation in kinetic selectivity between morphologies can be expected for the differently sized adsorbates CO\textsubscript{2} and CH\textsubscript{4}.

Given the high aspect ratio of each morphology, a significant portion of diffusion is expected to occur through the major surface pore.

Figure 5 shows representative data taken for the uptake of CO\textsubscript{2} and CH\textsubscript{4} for the bulk morphology. CH\textsubscript{4} is adsorbed more quickly, reaching 90% of the total uptake at around 50 s compared to about 125 s for the CO\textsubscript{2}. This contradicts other work in microporous MOFs, which determined the diffusion of CO\textsubscript{2} is much quicker than CH\textsubscript{4} due to the difference in kinetic diameter [32]. However, such a trend agrees with the Knudsen diffusion model, which states molecules with larger mass will diffuse more slowly in pores with a diameter below that of the mean free path, as is the case for gas in microporous materials. To better understand the diffusion of each species with respect to morphologies, we apply a single-component adsorption micropore diffusion control model developed by Ruthven et al. [33] to adsorption rate data collected for CO\textsubscript{2} and CH\textsubscript{4} that has successfully been applied to several MOF particle systems [27,34].

\[ \frac{m}{m_{\infty}} \approx \frac{6}{\sqrt{\pi}} \frac{D_c t}{r_c^2} - \frac{3 D_c t}{r_c^2} \]  

(2)

where $m/m_{\infty}$ is the mass uptake relative to the equilibrium uptake mass, $D_c$ is the intracrystalline diffusivity, $r_c$ is the crystal radius, and $t$ is time. It should be noted Equation (2) is valid for $m/m_{\infty} < 0.85$ [33]. This model assumes the intracrystalline diffusion resistances are much greater than macroporous resistances in particle aggregates, diffusion is constant within the crystalline material, and the concentration of adsorbate is constant outside of the particle. All of these assumptions are valid given that the free diffusivity of gases in macropores are much greater than those in the micropores [33], the gases do not condense in the micropores under the sampling conditions, and the sample tube volume can be approximated as an infinite reservoir compared to the volume adsorbed.
with the framework [35,36]. A two-fold increase in diffusion time constant is observed for CH\(_4\) (Table S2). We hypothesize that the MOF is unstable which results in the disparity in equilibrium values compared to those for the single-component isotherms. Follow up XRD data taken of samples

Table morphology adsorbs 2–4 times as much CO\(_2\) and CH\(_4\) than other tested morphologies at equilibrium (Table S2). We hypothesize that the MOF is unstable which results in the disparity in equilibrium values compared to those for the single-component isotherms. Follow up XRD data taken of samples

<table>
<thead>
<tr>
<th>Morphology</th>
<th>CO(_2) (D_e/r_c) (s(^{-1})) (\times 10^{-3})</th>
<th>CH(_4) (D_e/r_c) (s(^{-1})) (\times 10^{-3})</th>
<th>CO(_2)/CH(_4) Kinetic Selectivity</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bulk</td>
<td>1.57 ± 0.07</td>
<td>5.24 ± 0.44</td>
<td>0.300 ± 0.028</td>
</tr>
<tr>
<td>Rod</td>
<td>1.73 ± 0.13</td>
<td>8.75 ± 0.74</td>
<td>0.197 ± 0.022</td>
</tr>
<tr>
<td>Plate</td>
<td>1.88 ± 0.15</td>
<td>4.72 ± 0.27</td>
<td>0.399 ± 0.039</td>
</tr>
</tbody>
</table>

Attempting to replicate these results in a competitive adsorption environment showed the rod morphology adsorbs 2–4 times as much CO\(_2\) and CH\(_4\) than other tested morphologies at equilibrium (Table S2). We hypothesize that the MOF is unstable which results in the disparity in equilibrium values compared to those for the single-component isotherms. Follow up XRD data taken of samples

Figure 5. Fractional uptake versus time for the bulk morphology of [Zn\(_2\)(NDC)\(_2\)(DABCO)]\(_n\) at 273 K for CO\(_2\) and CH\(_4\).
run in the multi-component reactor showed significant degradation in crystallinity, confirming [Zn$_2$(NDC)$_2$(DABCO)$_n$]$_n$ is not stable under ambient conditions (Figure S2). Given the differing equilibrium uptakes, we hypothesize each morphology degrades at a different rate, and that the stability of anisotropic MOFs may depend on morphology and major surface bond mode.

3.4. Orientation of [Zn$_2$(NDC)$_2$(DABCO)$_n$]$_n$ Particle Films

Previous studies by our group have shown that well faceted MOF morphologies can be utilized in combination with flow coating techniques to control the crystal orientation of MOF thin films [20]. Orienting MOFs, to obtain selected pore apertures on substrates is desirable for high performance separations membranes [38,39]. Solution shearing is a meniscus guided flow coating technique where a particle suspension or solution can be deposited on a substrate using a blade [40,41]. As the blade is translated across the substrate at a prescribed speed, an evaporation front develops such that the crystalline material is deposited as a film in a controlled manner. The evaporation rate and fluid dynamics during deposition can be controlled by tuning the substrate temperature, blade speed, wetting properties of the substrate, or the solvent used for the suspension. Given our previous results with aligning faceted MOF particles and the well-faceted, high aspect ratio of the MOF used in this study, we identified the [Zn$_2$(NDC)$_2$(DABCO)$_n$]$_n$ morphologies as good candidates for creating oriented thin films.

The different [Zn$_2$(NDC)$_2$(DABCO)$_n$]$_n$ morphologies are drop cast and solution sheared with varied blade speeds, and the orientation of the solution sheared MOF thin films are measured by evaluating the orientation number, defined as the ratio of the intensities of the (110) and (001) peaks for each sample. As previously mentioned, the relative intensity of peaks can be used to determine the degree of orientation of a crystalline sample. It should be noted this method is not a precise measure of the orientation as peak intensity is a function of many factors in a polydisperse crystalline systems [42], however it can show the deviation of crystal texture from an isotropically distributed powder. Table 5 shows the orientation number for each morphology with varying film deposition techniques. The further an orientation number is from the ratio of intensities scattered by the (110) and the (001) planes for an isotropic powder (orientation number = 2.98), the more oriented the film. For lower orientation numbers, the (001) peak intensity increases and therefore the (001) crystal plane is preferentially oriented with respect to the substrate. For higher orientation numbers, the (110) peak increases, indicating that the (100) and (010) planes are preferentially oriented with respect to the substrate.

<table>
<thead>
<tr>
<th>Morphology</th>
<th>Isotropic Powder</th>
<th>Powder</th>
<th>Dropcast</th>
<th>Solution Sheared at 0.25 mm/s</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bulk</td>
<td>2.98</td>
<td>4.11</td>
<td>4.05</td>
<td>4.67</td>
</tr>
<tr>
<td>Rod</td>
<td>2.98</td>
<td>7.75</td>
<td>40.63</td>
<td>43.50</td>
</tr>
<tr>
<td>Plate</td>
<td>2.98</td>
<td>2.19</td>
<td>1.11</td>
<td>1.23</td>
</tr>
</tbody>
</table>

As previously mentioned, powder XRD scans show slight preferential orientation likely due to morphology influencing packing [24]. Drop cast films have a measurable degree of orientation compared to an isotropic film. The rod and bulk morphologies show preferential orientation for the (100) and (010) to be parallel to the substrate, which is enhanced by solution shearing and drop casting the particle suspensions. The observed orientation is expected for the rod morphology, as the major surfaces are defined by the (100) and (010) plane and are expected to lay flat with the substrate due to shear alignment forces during convective deposition processes [43]. Furthermore, this result agrees with other convective deposition techniques used to orient rod-like particles [43]. It should be noted
the (001) peak was not observed on the diffraction patterns for solution sheared rods. To quantify the orientation, we took the standard deviation of the signal noise as the maximum possible peak value for the (001) (Table 5). As previously mentioned, the bulk material gave a lower aspect ratio, rod-like morphology, which is likely why preferential orientation similar to the higher aspect ratio rods is observed.

The plate morphology shows a modest orientation number with preferential orientation of the (001) plane parallel to the substrate. This corresponds to the major surface of the plate morphology laying on the substrate. The lower degree of orientation for the plates may be explained by the stacking observed in SEM images taken of the plate morphology. In this case, shear alignment forces that orient particles during deposition would be reduced for a lower aspect ratio cluster or a mixture of clusters and plates [43].

It should be noted this result differs from our previous study in that solution shearing enhanced particle orientation compared to drop cast samples. This difference is likely due to the large particle size and high aspect ratios of [Zn$_2$(NDC)$_2$(DABCO)]$_n$ (3–10 µm and 7–10, respectively) compared to UiO-66 in our previous study (<1 µm and 1, respectively) [20]. In this case the larger size is not as greatly affected by the flow coating region during shearing or shear alignment forces exerted on large, high aspect ratio particles are comparable for the solution shearing and drop casting processes. However, more work is required to elucidate the importance of particle morphology and fluid forces on orientation.

4. Conclusions

The anisotropic MOF [Zn$_2$(NDC)$_2$(DABCO)]$_n$ in the [M$_2$(NDC)$_2$(DABCO)]$_n$ (M = metal) family can be modulated in a similar fashion to other metal analogs. Modulation yielded high aspect ratio crystals with different pore apertures on the major surface of a given morphology. Additionally, the modulation of the [Zn$_2$(NDC)$_2$(DABCO)]$_n$ MOF produced larger single crystals than other MOFs in this family, thereby indicating modulators may be used to control crystal size while maintaining morphology within a MOF family. XRD and BET characterization showed modulation had little effect on the crystallinity and microporosity of the resulting materials. Furthermore, it was demonstrated [Zn$_2$(NDC)$_2$(DABCO)]$_n$ has a moderate equilibrium selectivity of around 4 for all morphologies, which is comparable to other MOFs. Kinetic selectivity experiments showed the diffusion of CH$_4$ into the framework as measured by a diffusion time constant was much faster than CO$_2$. We hypothesize this may be due to other interactions controlling the CO$_2$ diffusion as the diffusion constant did not change appreciably between different morphologies (i.e., pore apertures). We further hypothesized the pore aperture defined by the carboxylate-amine frame may be larger, as it allows for faster diffusion of CH$_4$. Finally, oriented films were fabricated using a convective deposition technique termed solution shearing, which can be used for creating high performance selective membranes of oriented thin film MOFs.

Supplementary Materials: The following are available online at http://www.mdpi.com/2073-4352/9/1/20/s1, Figure S1: Representative nitrogen isotherms for varied morphologies of [Zn$_2$(NDC)$_2$(DABCO)]$_n$, Figure S2: PXRD patterns for MOF material pre and post-competitive gas adsorption procedure showing peak broadening for all samples, indicating sample degradation, Figure S3: PXRD patterns for powder, drop cast and solution sheared MOFs. XRDs were taken with the same XRD geometry reported in the main text, with no revolution during the scans. Additionally, these XRDs were taken parallel to the shearing direction of the material. (a) are the bulk material XRDs, while (b) and (c) are the rod and plate morphologies’ XRDs, respectively, Table S1: BET Surface Areas and standard error of [Zn$_2$(NDC)$_2$(DABCO)]$_n$ with differing drying procedures, Table S2: Equilibrium adsorption quantities in competitive adsorption environment, Table S3: Diffusion time constant data for CO$_2$ and CH$_4$ at 700 mmHg and 273 K for multiple trials.

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References


