Abstract: Fly-rock induced by blasting is an undesirable phenomenon in quarries. It can be dangerous for humans, equipment, and buildings. To minimize its undesirable hazards, we proposed a state-of-the-art technology of fly-rock prediction based on artificial neural network (ANN) models and their robust combination, called EANNs model (ensemble of ANN models); 210 fly-rock events were recorded to develop and test the ANN and EANNs models. Of the sample, 80% of the whole dataset was assigned to develop the models, the remaining 20% was assigned to confirm the models developed. Accordingly, five ANN models were designed and developed using the training dataset (i.e., 80% of the whole original data) first; then, their predictions on the training dataset were ensembled to generate a new training dataset. Subsequently, another ANN model was developed based on the new set of training data (i.e., EANNs model). Its performance was evaluated through a variety of performance indices, such as MAE (mean absolute error), MAPE (mean absolute percentage error), RMSE (root-mean-square error), $R^2$ (correlation coefficient), and VAF (variance accounted for). A promising result was found for the proposed EANNs model in predicting blast-induced fly-rock with a MAE = 2.777, MAPE = 0.017, RMSE = 4.346, $R^2$ = 0.986, and VAF = 98.446%. To confirm the performance of the proposed EANNs model, another ANN model with the same structure was developed and tested on the training and testing datasets. The findings also indicated that the proposed EANNs model yielded better performance than those of the ANN model with the same structure.

Keywords: mining; fly-rock; ANN; EANNs; ensemble technique; bench blasting; artificial intelligence

1. Introduction

Fly-rock induced by blasting is a particular concern of engineers and mining enterprises. Although the blasting techniques have been improved, there are still many hazards produced by blasting operations, especially fly-rock [1–3]. It is considered as one of the prime causes of explosion-related accidents on open-cast mines [4–6]. In fact, estimating the distance of fly-rock was proposed very
early based on experimental techniques (e.g., [7–9]). However, due to improper energy use factors of explosives, such as improper stemming, excessive powder factor, inadequate burden, unfavorable geological conditions, to name a few, the uncontrolled rocks are still propelled beyond the security area [10–12]. Therefore, empirical techniques were unable to explain the relationship between fly-rock and influencing factors adequately, and were uncontrollable in predicting whether blast-induced fly-rock was unavoidable.

To overcome the limitations of empirical methods, data-mining techniques were studied and applied by many scientists for predicting fly-rock in blasting operations. Its effectiveness has been proven not only in fly-rock forecasts but also in general technical issues [11–31]. For estimating the distance of fly-rock, Monjezi et al. [32] used a branch of artificial intelligence (AI), namely ANN (artificial neural network), based on the blasting parameters (i.e., powder factor, the diameter of borehole, blast ability index, stemming length, and a charge per delay). Finally, the charge per delay was defined as the most critical factor for reducing fly-rock. Similar works using the ANN technique for predicting fly-rock were also conducted by Ghasemi et al. [33], and Trivedi et al. [34]. Another machine-learning algorithm of AI, namely SVM (support vector machine), was also applied to predict the fly-rock distance by [35], Manoj, Monjezi [36]. ANFIS (adaptive neuro-fuzzy inference system) was also an AI technique that has been successfully applied by Trivedi et al. [37], for predicting the fly-rock distance with an excellent result.

However, conventional AI techniques do not seem to satisfy scientists. Therefore, Hasanipanah et al. [38] utilized an optimization algorithm, namely PSO (particle swarm optimization), for developing a robust equation for fly-rock prediction. Another meta-heuristic algorithm (i.e., differential evaluation algorithm-DE) was also used by Dehghani and Shafaghi [39] to combine with the dimensional analysis algorithm (DA) for estimating fly-rock distance. Its performance was confirmed by a variety of empirical techniques in their study. Based on the actions of fireflies, Faradonbeh et al. [40] also optimized blasting parameters to minimize the distance of fly-rock, using the firefly algorithm (FA). The genetic algorithm (GA) was also included to optimize the recurrent fuzzy neural network (RFNN), for predicting the fly-rock distance [41]. Under the optimal power of GA, an optimal RFNN model was established with a promising result in their study.

An overview of the related works indicated that many AI techniques had been developed to predict the fly-rock distance. However, they have not been confirmed in different areas with different geological conditions. Furthermore, new methods/models are always the targets of research by scientists aiming to improve the accuracy of the previous forecast models, minimizing the risks posed by fly-rock. Therefore, we proposed a state-of-the-art technology of fly-rock prediction based on ANN models and their robust combination, namely EANNs (ensemble of ANN models).

2. Dataset Used

This study was undertaken at a quarry mine in Vietnam, where the distance from residential was about 450–500 m (Figure 1). Herein, blasting was used as the primary technique for rock fragmentation using 75 mm of the borehole. Although many solutions have been proposed to minimize the distance of fly-rock; however, there are still many potential risks of unsafe activity due to fly-rock.

In order to investigate the causes, as well as the distance of fly-rock, we collected the basic parameters of 210 blasting events, including explosive charge per delay, powder factor, stemming, spacing, burden, and fly-rock distance, abbreviated as W, PF, ST, S, B, and FR, respectively. These parameters were also used for estimating FR by many previous scientists (e.g., [10,42–44]). Subsequently, the experimental datasets were analyzed and visualized.

To measure the distance of FR in this study, the iGeoTrans app was installed on an iPhone Xs Max, as shown in Figure 2. This app can work on iOS devices, which is a product of Hanoi University of Mining and Geology (HUMG), Hanoi, Vietnam [45]. iGeoTrans used a GPS (Global Positioning System) to mark the positions of blast points and the maximum distance of FR in this study. The remaining parameters (input parameters) were extracted from the blast patterns in blasting design, such as W,
PF, ST, S, and B. Table 1 lists the properties of the dataset used in this research. Besides, a matrix of the characteristics of the FR database was established, as shown in Figure 3. In which “Corr” was abbreviated as “Correlation.”

Figure 1. Location and overview of the study site.

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Table 1. Details of the parameters of blasting work in this study.

<table>
<thead>
<tr>
<th></th>
<th>B (m)</th>
<th>S (m)</th>
<th>ST (m)</th>
<th>W (Kg)</th>
<th>PF (kg/m^3)</th>
<th>FR (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Minimum</td>
<td>1.272</td>
<td>2.010</td>
<td>0.5194</td>
<td>166.3</td>
<td>0.2578</td>
<td>101.1</td>
</tr>
<tr>
<td>Mean</td>
<td>2.090</td>
<td>3.021</td>
<td>1.3038</td>
<td>1236.4</td>
<td>0.4013</td>
<td>167.7</td>
</tr>
<tr>
<td>Maximum</td>
<td>2.982</td>
<td>4.137</td>
<td>2.5236</td>
<td>2820.5</td>
<td>0.5963</td>
<td>290.1</td>
</tr>
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3. Artificial Neural Network (ANN)

Over the past few decades, the term “ANN” has become notable and has been adopted by a wide variety of applications, including atmospheric science, renewable energy systems, civil engineering [46,47], microwave computer-aided design, medicine and treatment, and natural resources research [48–54]. It is a branch of the AI family inspired by human brain biological neurons. The underlying architecture of ANN consists of input layers, hidden layer(s), and an output layer [55–57]. Here, layers are developed by fundamental elements of ANN well known as many highly interconnected neurons (nodes or processing elements) along with activation function [58,59]. The primary purpose of the input layer is to communicate the output layer via the hidden layer(s) using weight values and activation function. Usually, the network’s weights are adjusted (changes) and, accordingly, processed to obtain the desired response. Moreover, the ANN system with single hidden layer is adequate to compute the specified problem [60,61]. Whereas, ANN with two or more hidden layers pattern may create complex glitches [12]. The input elements (nodes) has been received the feature variables from raw environmental information and forwarded to the hidden layer. In this layer, it obtains knowledge of previous nodes and performs computations using encoded by weights and yield net input. Subsequently, the net input has been processed to the output layer through an activation function [62]. In the output layer, it has received the previous process information from the hidden layer(s) and computes the desired output with less error and more accurate. In the current study, the parameters include W, R, B, P, S, and FR and are considered as inputs and output, respectively.

Figure 3. Matrix of the attributes used in the fly-rock database.
In order to predict blast-induced fly-rock efficiently, the following ANN architecture model was adopted and as depicted in Figure 4.

![Diagram of ANN Architecture](image)

Figure 4. Artificial neural network (ANN) architecture for predicting blast-induced fly-rock efficiently.

4. Combination of Multiple ANN Models

The ensemble is well-known as a robust technique to improve the accuracy of the individual models [63]. Herein, a combination of multiple ANN models was conducted to solve the problem of fly-rock. In other words, five ANN models were jointed to create a new ANN model (called the EANNs model), for estimating FR herein. Note that the five ANN models were considered as the five independent models, and they must be developed first; then, a combination of the five developed ANN models was carried out. The framework of an ensemble of the ANN models is shown in Figure 5.

![Diagram of ANN Ensemble](image)

Figure 5. Context of the ANNs ensemble for estimating fly-rock distance (FR) in this work.
5. Performance Indexes for Evaluation of the Models

For model evaluation, this study used five statistical indexes, including MAE (mean absolute error), MAPE (mean absolute percentage error), RMSE (root-mean-squared error), VAF (variance accounted for), and $R^2$ (correlation coefficient). They are computed as follow:

\[
\text{MAE} = \frac{1}{n} \sum_{i=1}^{n} |y_{flyrock,i} - \hat{y}_{flyrock,i}|
\]

\[
\text{MAPE} = \frac{100\%}{n} \sum_{i=1}^{n} \frac{|y_{flyrock,i} - \hat{y}_{flyrock,i}|}{y_{flyrock,i}}
\]

\[
\text{RMSE} = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (y_{flyrock,i} - \hat{y}_{flyrock,i})^2}
\]

\[
\text{VAF} = \left(1 - \frac{\text{var}(y_{flyrock,i} - \hat{y}_{flyrock,i})}{\text{var}(y_{flyrock,i})}\right) \times 100
\]

\[
R^2 = 1 - \frac{\sum_{i} (y_{flyrock,i} - \hat{y}_{flyrock,i})^2}{\sum_{i} (y_{flyrock,i} - \overline{y}_{flyrock})^2}
\]

where $y_{flyrock,i}$ is the $i^{th}$ of measured fly-rock; $\hat{y}_{flyrock,i}$ is the $i^{th}$ of predicted fly-rock; $\overline{y}_{flyrock}$ is mean of measured values of fly-rock distance; $n$ indicates number of observations in the training or testing datasets.

6. Results

Before developing the ANN and EANNs models for predicting FR, the original dataset was divided randomly into two parts: (1) training part (80% of the whole original database); (2) testing part (20% remained).

As illustrated in Figure 5, five ANN models were developed first; then, they were combined as a new generation of ANN model (i.e., EANNs model). To avoid the over-fitting of the ANN models, the original dataset was normalized by a min–max scale in the range of [-1, 1]. Finally, five ANN models were selected for predicting FR in the first step, including ANN 5-7-5-1, ANN 5-10-8-1, ANN 5-14-9-1, ANN 5-18-13-1, and ANN 5-21-16-1. An ANN model for predicting FR in this study is illustrated in Figure 6. Subsequently, an ensemble of the five developed ANN models was conducted (i.e., EANNs model). The structure of the proposed EANNs model is shown in Figure 7. Accordingly, the structure of the EANNs model includes three hidden layers (i.e., 5-25-21-15-1); therefore, to have a complete conclusion, the EANNs model was used to train and test the original data (called ANN 5-25-21-15-1 model). The results of the FR predictive models are computed in Tables 2 and 3.

Based on the statistical indexes in Tables 2 and 3, the ANN models (six sub-models) performed very well in estimating FR. Their performance is relatively uniform. Notably, the third sub-model (i.e., ANN 5-14-9-1) seems to provide the lowest performance among the six ANN models. For the proposed EANNs model, the high red intensity has revealed that its performance is superior in this study. It should be noted that the EANNs model was developed based on an ensemble of the first five ANN models in Tables 2 and 3, and the sixth ANN model was only developed based on the original database to compare with the EANNs model (with the new database based on the predictions of the first five ANN models). The promising results of the proposed EANNs model were validated through the statistical indexes in Tables 2 and 3. Remarkably, the sixth ANN model (i.e., ANN 5-25-21-15-1) has three hidden layers that have the same structure as those of the proposed EANNs model; however, its performance was lower than those of the proposed EANNs model. Thus, the use of the available
ANN models as the sub-models to build a new model (i.e., EANNs model) has led to significant improvement in predicting FR. Figure 8 shows the accuracy of different ANN and EANNs models. Furthermore, a comparison of the proposed EANNs model (on the new database) and an ANN model with the same structure (on the original database) is shown in Figure 9.

**Figure 6.** The ANN 5-7-5-1 model for estimating FR.

**Figure 7.** The proposed EANNs model (ensemble of the ANN models) for estimating FR.
Table 2. Statistical indexes of the models for a set of data in the training.

<table>
<thead>
<tr>
<th>Model</th>
<th>MAE</th>
<th>MAPE</th>
<th>RMSE</th>
<th>VAF</th>
<th>$R^2$</th>
<th>Rank for MAE</th>
<th>Rank for MAPE</th>
<th>Rank for RMSE</th>
<th>Rank for VAF</th>
<th>Rank for $R^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>ANN 5-7-5-1</td>
<td>3.301</td>
<td>0.021</td>
<td>6.231</td>
<td>97.563</td>
<td>0.976</td>
<td>6</td>
<td>5</td>
<td>5</td>
<td>5</td>
<td>5</td>
</tr>
<tr>
<td>ANN 5-10-8-1</td>
<td>3.416</td>
<td>0.022</td>
<td>6.413</td>
<td>97.419</td>
<td>0.974</td>
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<tr>
<td>ANN 5-14-9-1</td>
<td>3.326</td>
<td>0.021</td>
<td>6.122</td>
<td>97.648</td>
<td>0.976</td>
<td>5</td>
<td>5</td>
<td>6</td>
<td>6</td>
<td>5</td>
</tr>
<tr>
<td>ANN 5-18-13-1</td>
<td>3.482</td>
<td>0.023</td>
<td>6.309</td>
<td>97.502</td>
<td>0.975</td>
<td>3</td>
<td>3</td>
<td>4</td>
<td>4</td>
<td>3</td>
</tr>
<tr>
<td>ANN 5-21-16-1</td>
<td>3.674</td>
<td>0.023</td>
<td>6.672</td>
<td>97.206</td>
<td>0.972</td>
<td>2</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>ANN 5-25-21-1</td>
<td>3.695</td>
<td>0.024</td>
<td>6.361</td>
<td>97.460</td>
<td>0.975</td>
<td>1</td>
<td>1</td>
<td>3</td>
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</tr>
<tr>
<td>EANNs</td>
<td>2.908</td>
<td>0.019</td>
<td>4.954</td>
<td>98.464</td>
<td>0.985</td>
<td>7</td>
<td>7</td>
<td>7</td>
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<td>7</td>
</tr>
</tbody>
</table>

Note: MAE (mean absolute error), MAPE (mean absolute percentage error), RMSE (root-mean-squared error), VAF (variance accounted for), and $R^2$ (correlation coefficient).

Table 3. Statistical indexes of the models for a set of data in the testing.

<table>
<thead>
<tr>
<th>Model</th>
<th>MAE</th>
<th>MAPE</th>
<th>RMSE</th>
<th>VAF</th>
<th>$R^2$</th>
<th>Rank for MAE</th>
<th>Rank for MAPE</th>
<th>Rank for RMSE</th>
<th>Rank for VAF</th>
<th>Rank for $R^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>ANN 5-7-5-1</td>
<td>3.227</td>
<td>0.019</td>
<td>5.71</td>
<td>97.242</td>
<td>0.974</td>
<td>4</td>
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<tr>
<td>ANN 5-10-8-1</td>
<td>3.162</td>
<td>0.019</td>
<td>5.55</td>
<td>97.349</td>
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</tr>
<tr>
<td>ANN 5-14-9-1</td>
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<td>0.02</td>
<td>5.684</td>
<td>97.225</td>
<td>0.975</td>
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<tr>
<td>ANN 5-18-13-1</td>
<td>3.322</td>
<td>0.021</td>
<td>5.459</td>
<td>97.437</td>
<td>0.975</td>
<td>2</td>
<td>2</td>
<td>6</td>
<td>6</td>
<td>3</td>
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<tr>
<td>ANN 5-21-16-1</td>
<td>3.300</td>
<td>0.021</td>
<td>5.945</td>
<td>96.919</td>
<td>0.973</td>
<td>3</td>
<td>2</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>ANN 5-25-21-1</td>
<td>3.568</td>
<td>0.022</td>
<td>5.541</td>
<td>97.373</td>
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<td>1</td>
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<tr>
<td>EANNs</td>
<td>2.777</td>
<td>0.017</td>
<td>4.346</td>
<td>98.446</td>
<td>0.986</td>
<td>7</td>
<td>7</td>
<td>7</td>
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</tr>
</tbody>
</table>

Figure 8. Accuracy of different ANN and EANNs models in estimating fly-rock.
Although the EANNs’ performance is outstanding; however, the effects of the input parameters need to be taken into account to evaluate the importance of the inputs for predicting FR. Accordingly, the sensitivity of the input parameters was analyzed, as shown in Figure 10. Eventually, ST and W were found to have the most effect on the training of the proposed EANNs model, whereas the remaining parameters (i.e., PF, S, B) also affect the model, but not much.

7. Conclusions

Fly-rock is an undesirable phenomenon that is generated by mine blasting. It is evaluated as the most dangerous phenomenon among the side effects of blasting. This study introduced a state-of-the-art technology of fly-rock prediction with high accuracy based on ANN models and their robust combination (i.e., EANNs). The findings indicated that the proposed EANNs’ performance was improved significantly when compared to the sub-models (i.e., ANN models). In other words, individual ANN models have served as positive input variables to improve the accuracy of the proposed EANNs model. This finding is impressive, and it should be applied in experimental conditions to control the distance of fly-rock, reducing the risks to humans and equipment.


Funding: This research received no external funding.

Acknowledgments: The authors would like to thank Hanoi University of Mining and Geology (HUMG), Hanoi, Vietnam; Duy Tan University, Da Nang, Vietnam; and the Center for Mining, Electro-Mechanical research of HUMG.
Conflicts of Interest: The authors declare no conflict of interest.

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