Parameter Optimization for Composite Structures of Microperforated Panel and Porous Metal for Optimal Sound Absorption Performance

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Received: 9 October 2019; Accepted: 6 November 2019; Published: 9 November 2019

Featured Application: The obtained optimal sound absorption performance can promote practical application of a composite structure of a microperforated panel and porous metal in noise reduction.

Abstract: The composite structure of a microperforated panel and porous metal is a promising sound absorber for industrial noise reduction, sound absorption performance of which can be improved through parameter optimization. A theoretical model is constructed for the composite structure of a microperforated panel and porous metal based on Maa’s theory and the Johnson–Champoux–Allard model. When the limited total thickness is 30 mm, 50 mm, and 100 mm respectively, dimensional optimization of structural parameters of the proposed composite structure is conducted for the optimal average sound absorption coefficient in the frequency range (2000 Hz, 6000 Hz) through a cuckoo search algorithm. Simulation models of the composite structures with optimal structural parameters are constructed based on the finite element method. Validations of the optimal composite structures are conducted based on the standing wave tube method. Comparative analysis of the theoretical data, simulation data, and experimental data validates feasibility and effectiveness of the parameter optimization. The optimal sandwich structure with an actual total thickness of 36.8 mm can obtain the average sound absorption coefficient of 97.65% in the frequency range (2000 Hz, 6000 Hz), which is favorable to promote practical application of the composite structures in the fields of sound absorption and noise reduction.

Keywords: parameter optimization; sound absorption performance; composite structure; porous metal; microperforated panel; limited total thickness

1. Introduction

The noises generated by large mechanical and electrical apparatuses are major component of industrial noise, which not only impair health of the operators, but also are detrimental to the residents living around the workshops [1]. In addition to traditional control strategies [2,3], such as the application of equipment with less noise, reasonable layout of the workshops, appropriate planting of vegetation, and wearing of personal protective appliance, installation of a proper acoustic absorber
around the noise source or on the wall of the workshop is an effective method to reduce reflecting superposition of the noise [4]. This is favorable to effectively decrease the noise inside and outside the workshop, therefore the development of a novel acoustic absorber is one of the research focuses in the field of industrial noise reduction.

Many sound absorbing materials and structures have been developed to reduce industrial noise. Maa [5,6] proposed the classical microperforated panel and proved it an effective and simple method to reduce the industrial noise within the low-and-medium frequency range. Ning et al. [7] further developed the novel microperforated panel with arbitrary cross-sectional perforations, and the research products indicated that changing cross-sectional roughness of the perforations was an efficient method to improve its sound absorption performance. Yang et al. [8] pointed out that porous metal could achieve a high sound absorption coefficient in the medium-and-high frequency range, and Bai et al. [9] further improved sound absorption efficiency of the porous metal through the compression process and quantificationally investigated the effect of the compression ratio. In addition to these traditional sound absorbing materials and structures, some novel acoustic meta-structures and metamaterials are also proposed [10–14]. Cheng et al. [10] has developed a 0.15λ-thick, 15%-filling ratio ultra-sparse meta-surface based on artificial Mie resonance. With careful design of the coupled resonators by Li et al. [11,12], over 99% energy absorption at the central frequency of 511 Hz with a 50% absorption bandwidth of 140 Hz was achieved. An acoustic super-lens using single-phase metamaterials with star-shaped structure were proposed by Chen et al. [13,14], which could obtain band gap and double-negative properties. However, fabrication costs of the acoustic metamaterials are high in general and the structures of them are usually complicated at present, which limit their practical applications. Meanwhile, each single traditional sound absorber has its weakness, such as finite absorption band, excessive occupied space, and so on. Thus, the composite structure consisting of a single sound absorber is considered as the development direction of novel acoustic absorbers.

Sound absorption performances of flax fiber and its reinforced composite, as well as balsa wood, were evaluated by Zhang et al. [15] and Zheng et al. [16] respectively, and it showed that the natural-materials-based sandwich structure has a high sound absorption coefficient within the high frequency range. Kim et al. [17,18] proposed a composite sound absorption structure, and the composite helical-shaped sound absorber coated with the carbon fiber exhibits excellent sound absorption property, especially within the low frequency range. Barium titanate/nitrile butadiene rubber (BT/NBR) and polyurethane (PU) foam were combined to prepare sound absorbing material with an alternating multilayered structure by Jiang et al. [19–21], and it has excellent sound absorption performance within the low frequency range due to the organic combinations of airflow resistivity, resonance absorption, and interface dissipation. Lv et al. [22,23] took discarded polyester as reinforced material and thermoplastic polyurethane as matrix material to fabricate a three-layer structural composite for sound absorption, research results of which indicate that the proposed composite has better sound absorption property and application prospects than the monolayer samples. Among these composite structures, the combination of a microperforated panel and porous metal is considered as a promising acoustic absorber for reducing industrial noise in the workshop, because it has the advantages of wide absorption band, fine fire resistance, high strength, excellent machinability, and a low manufacturing cost [24,25]. Therefore, the composite structures of a microperforated panel and porous metal were investigated and optimized in this study.

The research target of this study was to develop a novel acoustic absorber for the industrial noise reduction in a workshop, and the corresponding frequency range was (2000 Hz, 6000 Hz). Taking this practical demand into account, three kinds of composite structures were proposed and investigated, which included the porous metal + cavity + microperforated panel + cavity (here-after labeled as PCMC), microperforated panel + cavity + porous metal + cavity (here-after labeled as MCPC), and porous metal + cavity + microperforated panel + cavity + porous metal + cavity (here-after labeled as PCMCPC). Meanwhile, porous metal + cavity (here-after labeled as PC) and microperforated panel + cavity (here-after labeled as MC) were studied for contrast. In practical
applications, the total thickness of the sound absorber is a critical factor, because the available space
to install the sound absorber is limited. Therefore, sound absorption performances of these five kinds
of acoustic absorbers with the limited total thickness of 30 mm, 50 mm, and 100 mm were investigated
respectively in this study. A theoretical model was constructed for the composite structure of a
microperforated panel and porous metal by the transfer matrix method based on the Maa’s theory [26]
and the Johnson–Champoux–Allard model [27]. According to this model, the dimensional optimization
of structural parameters of the proposed composite structure was conducted by the cuckoo search
algorithm [28,29]. The achieved optimal structural parameters were introduced in the simulation
model based on the finite element method for the preliminary verification [30,31]. In accordance with
the achieved optimal structural parameters, the required microperforated panels were fabricated by
precision laser beam machining [32], and the porous metals were prepared by electrodeposition [33].
According to the standing wave tube method [34–37], sound absorption coefficients of the prepared
composite structure were measured by the AWA6128A detector for the experimental validation of the
theoretical model and optimization algorithm. Through comparison of theoretical data, simulation
data, and experimental data, a novel method to investigate and optimize sound absorption performance
of the composite structure of microperforated panel and porous metal was proposed and validated.

2. Materials and Methods

2.1. Modeling of the Composite Structure

Schematic diagrams of the proposed composite structures are shown in Figure 1a,c,e, which
corresponded to the composite structures of PCMC, MCPC, and PCMCPC, respectively. The PC and
MC were investigated as the contrast, as shown in the Figure 1b,d respectively. The parameters for the
microperforated panel and its corresponding cavity included diameter of the hole \( d \), distance between
the neighboring holes \( b \), thickness of the panel \( t \), and length of the cavity \( D_a \), and those for the porous
metal and its corresponding cavity consisted of thickness of the material \( d_p \) and length of the cavity
\( D_p \). For clarity in the Figure 1e, parameters for the preposition porous metal and its corresponding
cavity were labeled as \( d_b \) and \( D_b \) respectively, and those for the postposition porous metal and its
corresponding cavity were labeled as \( d_f \) and \( D_f \) respectively. The sound absorption mechanism of the
microperforated panel could be obtained based on Maa’s theory [5,6,26] and that of the porous metal
could be achieved according to the Johnson–Champoux–Allard model [8,9,27], and theoretical models
for the proposed composite structures could be calculated through the transfer matrix method [38,39].
The transfer matrixes for relevant structures were as follows.

![Figure 1](image-url)
Figure 1. Schematic diagrams of the investigated composite structures and corresponding labels of their structural parameters. (a) porous metal + cavity + microperforated panel + cavity (PCMC); (b) porous metal + cavity (PC); (c) microperforated panel + cavity + porous metal + cavity (MCPC); (d) microperforated panel + cavity (MC); (e) porous metal + cavity + microperforated panel + cavity + porous metal + cavity (PCMCPC).

2.1.1. Transfer Matrix for the Porous Metal

Transfer matrix $P$ for the porous metal can be calculated using Equation (1). Here $k_p$ is the wave number in the porous material, which is obtained using Equation (2); $Z_p$ is characteristic impedance of the porous metal, which can be achieved using Equation (3); $d_p$ is the thickness of the porous metal [8,9,27,36,37]. Transfer matrix of the preposition porous metal and that of the postposition porous metal in Figure 1e are symbolized as $P_f$ and $P_b$ respectively.

$$
[P] = \begin{bmatrix}
\cos(k_p d_p) & jZ_p \sin(k_p d_p) \\
\frac{1}{jZ_p} \sin(k_p d_p) & \cos(k_p d_p)
\end{bmatrix},
$$  

\[
k_p = \omega \sqrt{\frac{\rho(\omega)}{K(\omega}}.
\]

\[
Z_p = \sqrt{\frac{\rho(\omega)K(\omega)}}.
\]
In the Equations (2) and (3), the symbol $\omega$ is the angular frequency, which can be calculated using Equation (4); $K(\omega)$ is the complex effective bulk modulus, which can be calculated using Equation (5); $\rho(\omega)$ is complex effective density, which is derived by Equation (6) \cite{8,9,27,36,37}.

\[
\omega = 2\pi f,  \tag{4}
\]

\[
K(\omega) = \gamma P_0 \left[ \gamma - (\gamma - 1) \left( 1 - N_u \left( \frac{8\omega \rho P_r}{\sigma \rho} + N_u \right)^{-1} \right) \right]^{-1}, \tag{5}
\]

\[
\rho(\omega) = \rho \left[ 1 + \left( \frac{3^2}{4} + \frac{4\omega \rho}{\sigma \rho} \right)^{-0.5} - j \frac{\sigma \rho}{\omega \rho} \left( 1 + \frac{\omega \rho}{4\sigma \rho} \right)^{0.5} \right]. \tag{6}
\]

In the Equation (4), $f$ is sound frequency, and its range is (2000 Hz, 6000 Hz) in this study. In the Equations (5) and (6), $\gamma$ is specific heat ratio of the air, 1.40; $P_0$ is static pressure of the air, 1.013 $\cdot$ 10\(^5\) Pa; $N_u$ is the Nusselt number, 4.36; $j$ is symbol of the imaginary number, $j^2 = -1$; $\rho$ is density of the air, 1.21 kg $\cdot$ m\(^{-3}\); $\mu$ is the perforating rate, which can be calculated using Equation (11); $k_r$ is the acoustic resistance constant, which can be obtained using Equation (12); $\omega$ is still the angular frequency; $k_m$ is the acoustic mass constant, which can be derived using Equation (13) \cite{26,38}. In the Equations (12) and (13), $k$ is the perforated panel constant, which can be calculated using Equation (14). $d$, $b$, and $t$ represent the diameter of the hole, distance between the neighboring holes, and thickness of the panel, respectively, which are consistent with definitions of structural parameters of the microperforated panel in the Figure 1.

\[
\varepsilon = \frac{\pi}{4} \left( \frac{d}{b} \right)^2, \tag{11}
\]

\[
k_r = \sqrt{1 + \frac{k^2}{32} + \frac{\sqrt{2}}{8} k_d^2}. \tag{12}
\]
\[ k_m = 1 + \left( \frac{9 + k^2}{2} \right)^{-0.5} + 0.85 \frac{d}{l}, \] (13)

\[ k = \sqrt{\frac{\omega}{\mu + \nu}} \frac{d}{\frac{\omega}{\mu + \nu}}, \] (14)

2.1.3. Transfer Matrix for the Cavity

Transfer matrix \( S \) for the cavity can be calculated using Equation (15). Here \( \omega \) is still the angular frequency; \( c \) is the acoustic velocity in air, \( 340 \text{m} \cdot \text{s}^{-1} \); \( D \) is length of the cavity.

\[
[S] = \begin{bmatrix}
\cos\left(\frac{\omega}{c} D\right) & j \rho c \sin\left(\frac{\omega}{c} D\right) \\
\frac{1}{\rho c} \sin\left(\frac{\omega}{c} D\right) & \cos\left(\frac{\omega}{c} D\right)
\end{bmatrix}. \tag{15}
\]

In order to make a distinction among the different cavities, transfer matrixes for the cavities behind the microperforated panels in the Figure 1a,c–e are symbolized as \( S_a \); those behind the porous metal samples in the Figure 1a–c are symbolized as \( S_p \); those behind the preposition porous metal and those behind the postposition porous metal in the Figure 1e are symbolized as \( S_b \) and \( S_f \) respectively.

2.1.4. Sound Absorption Coefficient of the Composite Structure

Based on the obtained transfer matrixes for the porous metal, microperforated panel, and the cavity, total transfer matrixes \( TT \) for the investigated five composite structures can be derived by the Equations (16)–(20), respectively, which correspond to the sound absorbers in the Figure 1a–e. By this method, sound absorption coefficient \( \alpha \) of the investigated composite structures can be calculated, as shown in Equation (21).

\[
TT_a = \begin{bmatrix} TT_{a11} & TT_{a12} \\ TT_{a21} & TT_{a22} \end{bmatrix} = [P][S_p][M][S_a], \tag{16}
\]

\[
TT_b = \begin{bmatrix} TT_{b11} & TT_{b12} \\ TT_{b21} & TT_{b22} \end{bmatrix} = [P][S_p], \tag{17}
\]

\[
TT_c = \begin{bmatrix} TT_{c11} & TT_{c12} \\ TT_{c21} & TT_{c22} \end{bmatrix} = [M][S_a][P][S_p], \tag{18}
\]

\[
TT_d = \begin{bmatrix} TT_{d11} & TT_{d12} \\ TT_{d21} & TT_{d22} \end{bmatrix} = [M][S_a], \tag{19}
\]

\[
TT_e = \begin{bmatrix} TT_{e11} & TT_{e12} \\ TT_{e21} & TT_{e22} \end{bmatrix} = [P_b][S_b][M][S_a][P_f][S_f], \tag{20}
\]

\[
\alpha = \frac{4 \text{Re} \left( \frac{TT_{11}}{TT_{21}} \cdot \frac{1}{\rho c} \right)}{\left[ 1 + \text{Re} \left( \frac{TT_{11}}{TT_{21}} \cdot \frac{1}{\rho c} \right) \right]^2 + \left| \text{Im} \left( \frac{TT_{11}}{TT_{21}} \cdot \frac{1}{\rho c} \right) \right|^2}. \tag{21}
\]

2.2. Parameter Optimization by the Cuckoo Search Algorithm

Sound absorption performance of the composite structure is mainly determined by its structural parameters, which can be judged from the constructed theoretical model in the Section 2.1. For the given porous metal sample, the influencing factors were its thickness and length of the rear cavity. With regard to the microperforated panel absorber, the influencing factors were diameter of the hole, distance between the neighboring holes, thickness of the panel, and length of the rear cavity. A simple investigation on influence of the structural parameters to the sound absorption performance was
conducted by selecting a series of varied parameters for the composite structure of PCMC in the Figure 1a with the same total thickness of 40 mm, as shown in the Figure 2, and the corresponding selected parameters are summarized in the Table 1. It can be observed that the changes of structural parameter led to notable variety of sound absorption coefficient, which indicated that optimization of structural parameters of the composite structure was not only an essential, but also an effective method to develop the desired sound absorber.

![Figure 2. Qualitative comparisons of sound absorption coefficient of the composite sound absorbing structures with the varied structural parameters.](image)

### Table 1. The selected parameters for studying their influence on the sound absorption performance.

<table>
<thead>
<tr>
<th>Serial Number</th>
<th>Porous Metal</th>
<th>Microporated Panel</th>
<th>Average Sound Absorption Coefficient in Frequency Range (2000 Hz, 6000 Hz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0001</td>
<td>12</td>
<td>15</td>
<td>0.1</td>
</tr>
<tr>
<td>0002</td>
<td>14</td>
<td>12</td>
<td>0.2</td>
</tr>
<tr>
<td>0003</td>
<td>16</td>
<td>9</td>
<td>0.3</td>
</tr>
<tr>
<td>0004</td>
<td>18</td>
<td>6</td>
<td>0.4</td>
</tr>
<tr>
<td>0005</td>
<td>20</td>
<td>3</td>
<td>0.5</td>
</tr>
</tbody>
</table>

Total thickness of the composite sound absorbing structure is an important factor that affects its practical application, which consists of thickness of the porous metal, thickness of the panel, and length of each rear cavity. Total thickness $T$ of the five composite structures in the Figure 1 can be calculated using Equation (22).

$$
T = \begin{cases} 
  d_p + D_p + t + D_a & \text{for structure in Figure 1a} \\
  d_p + D_p & \text{for structure in Figure 1b} \\
  t + D_a + d_p + D_p & \text{for structure in Figure 1c} \\
  t + D_a & \text{for structure in Figure 1d} \\
  d_f + D_f + t + D_a + d_b + D_b & \text{for structure in Figure 1e}
\end{cases} \quad (22)
$$

Supposing the limit for total thickness of the sound absorber is $T_0$, it is determined by the available space for installing the sound absorber. The normal range $T_0$ in a common workshop is 10–100 mm, so the selected constraint conditions of $T_0 = 30$ mm, $T_0 = 50$ mm, and $T_0 = 100$ mm were investigated in this research. In addition to the total thickness, each structure parameter also has the constraint condition for the practical application. Thickness of the porous metal $d_p$ and that of the microporated panel $t$ shall be not too small, otherwise strength and stiffness of the formed composite structure will be too low. Meanwhile, according to the definition of the microporated panel and process capability of the used precise machine tool, the diameter of the hole $d$ and distance of the neighboring holes $b$ should be in a reasonable range. Therefore, constraint conditions for the parameter optimization of the composite structure are summarized in Equation (23).
\[
\begin{aligned}
T &\leq T_0 \\
d_p, d_b, d_f &\geq 1 \cdot 10^{-4} m \\
t &\geq 1 \cdot 10^{-4} m \\
d &\geq 1 \cdot 10^{-4} m \\
b &\geq 1 \cdot 10^{-3} m \\
D_a, D_p, D_f, D_b &\geq 0
\end{aligned}
\]  
(23)

Judging from the results in the Figure 2, it could also be observed that the sound absorption performance was not only decided by the structural parameters, but also be affected by the selected frequency range \((f_{\text{min}}, f_{\text{max}})\). For the varied frequency ranges, the optimal choice for structural parameters is different. Therefore, taking into account the normal frequency range of the major noise generated by the common large mechanical and electrical equipment in the workshop in this study, the investigated frequency range was set to be \((2000 \text{ Hz}, 6000 \text{ Hz})\). In fact, the optimization method proposed in this research was also applicable for the circumstances with other frequency ranges or other constraint conditions.

The cuckoo search algorithm is considered as an effective method in solving the continuous optimization problem [35–37,41,42], which was proposed by Yang and Deb in 2009 [28,29] based on the obligate brood parasitic behavior of some cuckoo species in combination with the Levy flight behavior of some birds and fruit flies. The cuckoo search algorithm can be expressed around the following ideal rules: (1) each cuckoo lays one egg at a time and selects a nest randomly; (2) the best nest with the highest quality egg can pass onto the new generations; (3) the number of host nests is fixed, and the egg laid by a cuckoo can be discovered by the host bird with the probability \(p_a \in [0, 1]\) [28,29,35–37,41,42]. With respect to a certain cuckoo \(i\) and a given generation \(t\), the new solution \(x_i^{(t+1)}\) can be generated from the former solution \(x_i^{(t)}\) according to the Levy flight mechanism, as shown in Equation (24) [28,29,35–37,41,42].

\[
x_i^{(t+1)} = x_i^{(t)} + \alpha \circ\text{Levy}(s, \lambda).
\]  
(24)

Here \(\alpha (\alpha > 0)\) is the step size, which decides how far a random walker can go for a fixed number of iterations. In most common cases, \(\alpha = O(1)\) can be used. The product \(\circ\) means the entry-wise multiplications. \(\text{Levy}(s, \lambda)\) represents the step length, as shown in the Equation (25), which follows the Levy distribution. \(s\) in Equation (25) is the step size drawn from the Levy distribution [28,29,35–37,41,42].

\[
\text{Levy}(s, \lambda) \sim s^{-\lambda}, (\lambda \in (1, 3]).
\]  
(25)

Basic calculation process of the standard cuckoo search algorithm is summarized and shown in Table 2 [28,29]. Maximization of the average sound absorption coefficient of the investigated composite structures in the frequency range \((2000 \text{ Hz}, 6000 \text{ Hz})\) was treated as the optimization target. Moreover, the constructed theoretical sound absorbing models for the composite structures in the Section 2.1 was considered as the objective function. Furthermore, the constraint conditions listed in Equation (23) were taken into account during the optimization process.
Table 2. Basic calculation process of the standard cuckoo search algorithm.

<table>
<thead>
<tr>
<th>Standard Cuckoo Search Algorithm</th>
</tr>
</thead>
<tbody>
<tr>
<td>1: Objective function ( f(x), x = (x_1, x_2, \ldots, x_d)^T );</td>
</tr>
<tr>
<td>2: Generate initial population of ( n ) host nests ( x_i (i = 1, 2, \ldots, n) );</td>
</tr>
<tr>
<td>3: while ((t \leq \text{MaxGeneration}) ) or (stop criterion) do</td>
</tr>
<tr>
<td>4: Get a cuckoo (say, ( i )) randomly and generate a new solution by Levy flights;</td>
</tr>
<tr>
<td>5: Evaluate its quality/fitness ( F_i );</td>
</tr>
<tr>
<td>6: Choose a nest among ( n ) (say, ( j )) randomly;</td>
</tr>
<tr>
<td>7: if ( F_i \geq F_j ) then</td>
</tr>
<tr>
<td>8: replace ( j ) by the new solution;</td>
</tr>
<tr>
<td>9: end if</td>
</tr>
<tr>
<td>10: A fraction (( P_a )) of worse nests are abandoned and new ones are built at new locations;</td>
</tr>
<tr>
<td>11: Keep the best solutions (or nests with quality solutions);</td>
</tr>
<tr>
<td>12: Rand the solutions and find the current best;</td>
</tr>
<tr>
<td>13: end while</td>
</tr>
<tr>
<td>14: Postprocess results and visualization;</td>
</tr>
</tbody>
</table>

Through the cuckoo search algorithm, optimization of structural parameters of the proposed composite structures in Figure 1 could be obtained, which have been summarized in Tables 3–5 corresponding to the given limited total thickness of 30 mm, 50 mm, and 100 mm, respectively. Comparisons of the theoretical optimal average sound absorption coefficients with different limited total thickness of 30 mm, 50 mm, and 100 mm are shown in the Figure 3. It could be judged from the optimization results that the composite structure of PCMCPC exhibited the best sound absorption performance, and optimal average sound absorption coefficient in the frequency range (2000 Hz, 6000 Hz) exceeded 98% with the total thickness of 30 mm. Moreover, sound absorption performance of the composite structure of PCMC was close to that of the PCMCPC. It could be found that the optimal parameters for the composite structure of MC with the various limited total thicknesses were all same, as shown in Tables 3–5. This result indicates that sound absorption performance of the MC was insufficient, and it could not be improved by increasing the total thickness, which could also be judged from the result in Figure 3. Furthermore, sound absorption performance of the composite structure of MCPC was significantly improved by increasing the limited total thickness, as shown in Figure 3. It is interesting to note that the optimal length of the cavity for the composite structure of PC was 0, no matter what the limited total thickness was, as shown in Tables 3–5. It could also be observed that optimal average sound absorption coefficient of the porous metal rose along with increase of the thickness, which is consistent with the normal sound absorption principle of porous materials [8,9].

Table 3. Summarized optimal parameter of composite structure with limited total thickness 30 mm.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>PCMC</th>
<th>PC</th>
<th>MCPC</th>
<th>MC</th>
<th>PCMCPC</th>
</tr>
</thead>
<tbody>
<tr>
<td>( d ) (mm)</td>
<td>0.15</td>
<td>–</td>
<td>0.17</td>
<td>0.16</td>
<td>0.16</td>
</tr>
<tr>
<td>( t ) (mm)</td>
<td>0.10</td>
<td>–</td>
<td>0.10</td>
<td>0.10</td>
<td>0.10</td>
</tr>
<tr>
<td>( b ) (mm)</td>
<td>1.00</td>
<td>–</td>
<td>1.00</td>
<td>1.00</td>
<td>1.00</td>
</tr>
<tr>
<td>( d_f ) (mm)</td>
<td>21.02</td>
<td>30.00</td>
<td>–</td>
<td>–</td>
<td>21.13</td>
</tr>
<tr>
<td>( D_a ) (mm)</td>
<td>–</td>
<td>–</td>
<td>12.10</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>( D_b ) (mm)</td>
<td>8.88</td>
<td>–</td>
<td>0.00</td>
<td>12.38</td>
<td>0.00</td>
</tr>
<tr>
<td>( D_f ) (mm)</td>
<td>0.00</td>
<td>0.00</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>( D_f ) (mm)</td>
<td>–</td>
<td>–</td>
<td>0.00</td>
<td>–</td>
<td>–</td>
</tr>
</tbody>
</table>

Optimal average sound absorption coefficient | 98.15% | 86.45% | 89.99% | 88.64% | 98.37%
Table 4. Summarized optimal parameter of composite structure with limited total thickness 50 mm.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>PCMC</th>
<th>PC</th>
<th>MCPC</th>
<th>MC</th>
<th>PCMC</th>
<th>PCMCPC</th>
</tr>
</thead>
<tbody>
<tr>
<td>$d$ (mm)</td>
<td>0.15</td>
<td>–</td>
<td>1.80</td>
<td>0.16</td>
<td>0.16</td>
<td></td>
</tr>
<tr>
<td>$t$ (mm)</td>
<td>0.10</td>
<td>–</td>
<td>0.10</td>
<td>0.10</td>
<td>0.10</td>
<td></td>
</tr>
<tr>
<td>$b$ (mm)</td>
<td>1.00</td>
<td>–</td>
<td>1.90</td>
<td>1.00</td>
<td>1.00</td>
<td></td>
</tr>
<tr>
<td>$d_b$ (mm)</td>
<td>26.17</td>
<td>50.00</td>
<td>–</td>
<td>–</td>
<td>26.21</td>
<td></td>
</tr>
<tr>
<td>$d_f$ (mm)</td>
<td>–</td>
<td>–</td>
<td>49.90</td>
<td>–</td>
<td>10.49</td>
<td></td>
</tr>
<tr>
<td>$D_a$ (mm)</td>
<td>10.77</td>
<td>–</td>
<td>0.00</td>
<td>12.38</td>
<td>0.00</td>
<td></td>
</tr>
<tr>
<td>$D_b$ (mm)</td>
<td>0.00</td>
<td>0.00</td>
<td>–</td>
<td>–</td>
<td>0.00</td>
<td></td>
</tr>
<tr>
<td>$D_f$ (mm)</td>
<td>–</td>
<td>–</td>
<td>0.00</td>
<td>–</td>
<td>0.00</td>
<td></td>
</tr>
</tbody>
</table>

Optimal average sound absorption coefficient 99.09% 95.45% 95.14% 88.64% 99.21%

Table 5. Summarized optimal parameter of composite structure with limited total thickness 100 mm.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>PCMC</th>
<th>PC</th>
<th>MCPC</th>
<th>MC</th>
<th>PCMC</th>
<th>PCMCPC</th>
</tr>
</thead>
<tbody>
<tr>
<td>$d$ (mm)</td>
<td>0.17</td>
<td>–</td>
<td>1.62</td>
<td>0.16</td>
<td>0.93</td>
<td></td>
</tr>
<tr>
<td>$t$ (mm)</td>
<td>0.10</td>
<td>–</td>
<td>0.10</td>
<td>0.10</td>
<td>0.21</td>
<td></td>
</tr>
<tr>
<td>$b$ (mm)</td>
<td>1.00</td>
<td>–</td>
<td>1.78</td>
<td>1.00</td>
<td>1.03</td>
<td></td>
</tr>
<tr>
<td>$d_b$ (mm)</td>
<td>83.09</td>
<td>100.00</td>
<td>–</td>
<td>–</td>
<td>0.92</td>
<td></td>
</tr>
<tr>
<td>$d_f$ (mm)</td>
<td>–</td>
<td>–</td>
<td>96.16</td>
<td>–</td>
<td>92.67</td>
<td></td>
</tr>
<tr>
<td>$D_a$ (mm)</td>
<td>12.64</td>
<td>–</td>
<td>3.74</td>
<td>12.38</td>
<td>4.84</td>
<td></td>
</tr>
<tr>
<td>$D_b$ (mm)</td>
<td>0.00</td>
<td>0.00</td>
<td>–</td>
<td>–</td>
<td>0.30</td>
<td></td>
</tr>
<tr>
<td>$D_f$ (mm)</td>
<td>–</td>
<td>–</td>
<td>0.00</td>
<td>–</td>
<td>0.17</td>
<td></td>
</tr>
</tbody>
</table>

Optimal average sound absorption coefficient 99.32% 99.24% 99.64% 88.64% 99.64%

**Figure 3.** Comparisons of theoretical optimal average sound absorption coefficients of the composite structures with the different limited total thickness of 30 mm, 50 mm, and 100 mm.

Detailed distributions of sound absorption coefficients of the five composite structures with the limited total thicknesses of 30 mm, 50 mm, and 100 mm are shown in the Figure 4a–c, respectively. It could be found that except the data for MC, the sound absorption performances of the other four composite structures were accordingly improved along with increase of the limited total thickness, which were consistent with the result shown in Figure 3. Meanwhile, it could be observed that undulation of the sound absorption coefficients was reduced along with increase of the limited total thickness. Especially when the limited total thickness reached 100 mm, minimum of the sound absorption coefficient in the (2000 Hz, 6000 Hz) for the investigated composite structures
(except the MC) exceeded 98%, which almost realized unity absorption in the investigated frequency range. Moreover, it could be observed that along with increase of the limited total thickness, the composite structure of PC and that of MCPC achieve obvious improvement in sound absorption performance, the average sound absorption coefficients of which were improved from 86.45% to 99.24% and 89.99% to 99.64%, respectively.

![Graph](image)

**Figure 4.** Distributions of sound absorption coefficients of the optimal composite structures in theory. (a) Composite structures with limited total thickness 30 mm corresponding to parameters in Table 3; (b) composite structures with limited total thickness 50 mm corresponding to parameters in Table 4; (c) composite structures with limited total thickness 100 mm corresponding to parameters in Table 5.
3. Results and Discussions

3.1. Verification by Finite Element Simulation

Taking the most complex composite structure of PCMCP for example, the simulation model for preliminary verification of the optimal dimensional parameters was constructed in the software of Virtual Lab Acoustics based on the finite element method [30,31], as shown in Figure 5. With respect to the other four composite structures, the simulation was realized by adjusting parameters of the porous metal 1, porous metal 2, cavity 1, cavity 2, cavity 3, and the microperforated panel in the constructed model according to the optimal parameters in the Tables 3–5 respectively. Size of each element in this simulation model was 5 mm, and it was a triangular mesh in the thickness direction, which indicated that it utilized 897 points in the calculation process. The plane wave was loaded in the acoustic source inlet and used as the sound source input. Effect of the microperforated panel was represented by the transfer relation admittance between two surfaces, which was calculated according to the structural parameters in the Tables 3–5. Through testing peak sound level and valley sound level at the microphone 1 and microphone 2 respectively, sound absorption coefficient of the detected sound absorber at a certain frequency could be calculated. By this method, sound absorption coefficients of the investigated composite structures were simulated.

![Figure 5.](image-url) Simulation model for the sound absorption coefficient of the composite sound absorbing structure.

Comparisons of the sound absorption coefficient of the theoretical result and that of the simulation result are shown in Figure 6. It can be observed that the distributions of sound absorption coefficients of the composite structures in the simulation results were in accordance with those in the theoretical results. Especially for the composite structure of MC, the simulation result was almost same with the theoretical result, which indicated that the constructed model for the microperforated panel based on Maa’s theory was accurate. With respect to the other four composite structures, the differences between the simulation result and the theoretical result were generated in constructing model of the porous material according to the Johnson—Champoux—Allard model, which has been used in studying the relationship between sound absorption performance of the porous material and its structural parameters [8,9]. With an increase of the limited total thickness, deviations between the simulation results and the theoretical results were reduced, because sound absorption coefficients in the frequency range (2000 Hz, 6000 Hz) were close to 100% both in the theoretical result and in the simulation result. Meanwhile, the absolute deviation of corresponding average sound absorption coefficient was smaller than 1% between the simulation results and the theoretical results. Therefore, it was preliminarily concluded that the optimal structural parameters obtained by the cuckoo search algorithm were reasonable and accurate.
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Figure 6. Comparison of the sound absorption coefficient in theory and that obtained by simulation.
(a) Composite structures with limited total thickness 30 mm corresponding to parameters in Table 3; (b) composite structures with limited total thickness 50 mm corresponding to parameters in Table 4; (c) composite structures with limited total thickness 100 mm corresponding to parameters in Table 5.
3.2. Validation of the Optimal Composite Structures

Detections of sound absorption coefficients of the composite sound absorbing structures were obtained by the AWA6128A detector (Hangzhou Aihong instruments Co., Ltd., China), as shown in Figure 7 [40–42]. The diameter of cross-section of the AWA6128A detector is 96 mm, and its measurable frequency range is (1500 Hz, 6640 Hz). Length of the slideway is 1000 mm, which supports motion of the pulley to detect peak value and valley value of the reflected wave. Measurable thickness of the detected acoustic absorber (including the cavity) was 0–60 mm, which indicated that the proposed composite structures with the limited total thickness of 100 mm go beyond the measuring range of the equipment. In fact, the sound absorber with total thickness of 100 mm has few application prospects in the industrial noise reduction, because it takes too much space. It can be found that composite structure of PCMC and that of PCMCPC can obtain relative better sound absorption performances among the proposed composite structures. Thus, these two composite sound absorbing structures with limited total thickness of 30 mm and 50 mm were prepared and assembled according to the optimal structural parameters in Tables 3 and 4, and the samples are shown in Figure 8. The utilized porous copper sample in this research was purchased from YiYang Foam Metal New Material Co., Ltd., Yiyang, Hunan, China, and thicknesses of the common samples provided by the supplier were 2 mm and 5 mm. Therefore, in order to reduce fabrication cost, each used porous metal sample included some standard blocks and one special block, as shown in Figure 8. Moreover, length of the rear cavity was adjusted by the sample holder in Figure 8a.

![Figure 7](image_url)

**Figure 7.** Schematic diagram of AWA6128A detector for measuring the sound absorption coefficient. (a) Structure diagram; (b) physical picture.
used porous metal sample included some standard blocks and one special block, as shown in Figure 8. Moreover, length of the rear cavity was adjusted by the sample holder in Figure 8a.

Figure 7. Schematic diagram of AWA6128A detector for measuring the sound absorption coefficient. (a) Structure diagram; (b) physical picture.

Figure 8. The prepared optimal composite structures. (a) Optimal PCMC with limited total thickness of 30 mm; (b) optimal PCMCPC with limited total thickness of 30 mm; (c) optimal PCMC with limited total thickness of 50 mm; (d) optimal PCMCPC with limited total thickness of 50 mm.

Sound absorption coefficients were achieved according to the standing wave tube method [8,9,34–37,40–42], as shown in the Figure 9. It was found that distribution and tendency of the sound absorption coefficients in the experimental result were consistent with those in the theoretical result. The selected porous metal was porous copper, and its structural parameters were consistent with those in the theoretical modeling process. The desired microperforated panels were fabricated by laser beam drilling of the steel spring plates according to the corresponding structural parameters. Taking the machinability and optional parameters of the equipment into consideration, the diameter of the hole $d$ and distance of the neighboring holes $b$ of the optimal structural parameters for the microperforated panels were handled to keep two decimal places. Meanwhile, considering common dimension of the steel spring plate easy to buy, thickness of the panel $t$ was also kept two decimal places for the approximation. Lengths of the cavities $D_a$, $D_f$, and $D_b$ were adjusted by the additive manufacturing of blocks with the desired sizes.

In addition, quantitative comparisons of average sound absorption coefficient in the theoretical result, simulation result, and experimental result are summarized in Table 6. It can be observed that the actual average sound absorption coefficient of four investigated composite structures exceeded 96%, though they are slightly smaller than those of the corresponding theoretical result. The major reason for this phenomenon is that there exists fabrication error in the preparation of porous metals and microperforated panels. Meanwhile, measuring error in the measuring process also affected the experimental result, although each sound absorber was measured by more than 10 times to reduce the accidental measuring error. By this method, feasibility and effectiveness of these optimal composite structures were validated.
Uncertainties exist in the validation process, one of which is about material design of the composite structure and the other is about characterization of the sound absorption coefficient. Thickness of the utilized porous metal samples has fabrication error, especially those special blocks, which was measured by a vernier caliper. It can be found that uncertainty of thickness of the used porous metal sample was ±0.01 mm and that of the microperforated panel was ±0.004 mm.
From the Table 3, Table 4 and Figure 9, it can be found that the actual total thickness of the optimal composite structure sometimes did not reach the presupposed limited total thickness, which indicated that the actual sound absorption efficiency of the investigated composite structure was even better. Therefore, comparisons of the actual total thickness with different presupposed limited total thickness are shown in the Table 7. When the presupposed limited total thickness was 50 mm, the actual total thickness for the composite structure of PCMCPC was 36.8 mm and lengths of all the 3 cavities were 0 mm, which indicated that this sandwich structure is a promising sound absorber with high absorption efficiency and low total thickness. Meanwhile, actual total thickness of the optimal composite structure of PCMC with the limited total thickness of 50 mm was 37.04 mm (including the cavity with length of 10.77 mm), and its average sound absorption coefficient of 96.76% was close to that 97.65% of corresponding optimal PCMCPC with thickness of 36.8 mm. Thus, taking complexity of the composite structure into account, the PCMC can also be treated as novel sound absorber with fewer utilized materials for reduction of the industrial noise.

**Table 7.** Summarized actual total thickness with the different presupposed limited total thickness.

<table>
<thead>
<tr>
<th>Limited Total Thickness (mm)</th>
<th>PCMC (mm)</th>
<th>PC (mm)</th>
<th>MCPC (mm)</th>
<th>MC (mm)</th>
<th>PCMCPC (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>30.00</td>
<td>30.00</td>
<td>30.00</td>
<td>12.20</td>
<td>12.48</td>
<td>30.00</td>
</tr>
<tr>
<td>50.00</td>
<td>37.04</td>
<td>50.00</td>
<td>50.00</td>
<td>12.48</td>
<td>36.80</td>
</tr>
<tr>
<td>100.00</td>
<td>95.24</td>
<td>100.00</td>
<td>100.00</td>
<td>12.48</td>
<td>98.60</td>
</tr>
</tbody>
</table>

### 4. Conclusions

Sound absorption performance of the composite structure of microperforated panel and porous metal was modeled, optimized, simulated, measured, and analyzed in this study. A feasible method to develop the desired sound absorber for the effective reduction of industrial noise was proposed and the following conclusions were obtained from the research results.

1. Theoretical models of the sound absorption performance of the composite sound absorbing structures were derived by the transfer matrix method, and the sound absorption coefficients were calculated by a series of equations, which provided an objective function for the structural parameter optimization process and the contrast accordance for the further finite element simulation and the following experimental validation.
(2) Structural parameters of the composite structure were optimized through the cuckoo search algorithm when the desired frequency range was (2000 Hz, 6000 Hz) and the limited total thickness was 30 mm, 50 mm, and 100 mm, respectively. The distributions and optimal averages of the sound absorption coefficients indicated that the proposed composite structures with the optimal structural parameters were excellent sound absorbers.

(3) Simulation models of the composite structure with optimal structural parameters were built based on the finite element method. Detailed comparative analysis of the theoretical result and the simulation result was conducted, and the calculated absolute deviation of corresponding optimal average sound absorption coefficient was smaller than 1%, which gave a preliminarily verification to the optimization results.

(4) Experimental validations of the optimal composite structures were conducted through the AWA6128A detector based on the standing wave tube method. The sandwich structure of porous metal 26.21 + cavity 0 + microperforated panel 0.1 + cavity 0 + porous metal 10.49 + cavity 0 with an actual total thickness 36.8 mm obtained the average sound absorption coefficient of 97.65% in the frequency range (2000 Hz, 6000 Hz), which indicated that the optimization of structural parameters was an effective way to develop the desired acoustic absorber and would be favorable to promote the application of the composite structures in the field of industrial noise reduction.


Funding: This research was funded by the National Natural Science Foundation of China, grant number 51505498; Natural Science Foundation of Jiangsu Province, grant number BK20150714; National Key R&D Program of China, grant number 2016YFC0802900; Hong Kong Scholars Program, grant number XJ2017025.

Acknowledgments: The authors wish to express their sincere thanks to Hangzhou Aihong Instruments Co., Ltd., China for the support of the AWA6128A detector.

Conflicts of Interest: The authors declare no conflict of interest.

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