First-Principles Forecast of Gapless Half-Metallic and Spin-Gapless Semiconducting Materials: Case Study of Inverse Ti$_2$CoSi-Based Compounds

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Featured Application: Half of the Si atoms in Ti$_{2.25}$Co$_{0.75}$Si are replaced by B, Al, Ga, P, As, and Sb, and the results show that doped Ti$_{2.25}$Co$_{0.75}$Si with an appropriate concentration of impurities could exhibit half-metallic ferromagnetic, gapless half-metallic, and spin-gapless semiconducting states.

Abstract: First-principles calculations were used to investigate several inverse Ti$_2$CoSi-based compounds. Our results indicate that Ti$_2$Co$_{0.75}$Si would keep stable half-metallic properties in a large range of lattice parameter under the effect of hydrostatic strain, and would become a gapless half metal under the effect of tetragonal distortion. Furthermore, we substituted B, Al, Ga, P, As, and Sb for Si in the Ti$_{2.25}$Co$_{0.75}$Si compound. Our results demonstrate that Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$B$_{0.5}$, Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$Al$_{0.5}$, and Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$Ga$_{0.5}$ are half-metallic ferromagnetic materials, and Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$P$_{0.5}$, Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$As$_{0.5}$, and Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$Sb$_{0.5}$ are spin-gapless semiconducting materials. The introduced impurity atoms may adjust the valence electron configuration, change the charge concentration, and shift the location of the Fermi level.

Keywords: first-principles calculation; Heusler compounds; gapless half metals; spin gapless semiconductor

1. Introduction

With the development of nanotechnology and computational materials science, spintronics has developed rapidly in the past 30 years. In order to improve the performance of spin diodes, spin valves, and spin filters, the design of high spin-polarized materials has attracted much attention [1–4]. For half-metallic ferromagnetic compounds with unique electronic structures, one of the two spin channels is semiconducting and the other is metallic. As promising spintronic candidates, they exhibit a complete spin polarization of carriers near the Fermi level [5–12]. A spin-gapless semiconductor is another new kind of spintronic material, which has an almost complete spin polarization and good compatibility with the existing semiconductor industry. By shifting the Fermi
energy at the finite gate voltage, the spin-polarized transport properties of spin-gapless semiconductors can be tuned, which has great prospects for future spintronic applications [13,14].

Half metals and spin-gapless semiconductors are special kinds of materials. Because of their unique electronic structures, they have novel spin-dependent electronic properties. The band structure of these materials has only one energy gap for a specific spin direction, which means that the band gap disappears in the opposite spin direction. This phenomenon leads to the application prospects of high carrier spin polarization and spin-controlled electrical and magnetic features. In recent years, in order to develop new technologies involving spintronics, it has been important to search for new materials with these characteristics. Many of these materials are Heusler alloys with a specific crystalline ordering, which is very important for the unique electronic and magnetic properties of these materials. Therefore, it is crucial to study these alloys and compounds with these novel physical properties.

Heusler alloys are named for the German mining engineer and chemist Friedrich Heusler, who investigated Cu–Mn–Al alloys around the year 1900. Heusler compounds are ternary intermetallic compounds, which have been known since 1903 [15]. These alloys were interesting because some of them were ferromagnetic, even though their constituent atoms were non-ferromagnetic as elements. At that time, Cu2MnAl compounds were proven to be ferromagnetic, although none of the three elements were ferromagnetic. The structure of the alloys was later found to be face-centered cubic (fcc) with a four-atom basis consisting of a single formula unit. Thus, members of this Heusler family with a formula unit A2BC (known as “full” Heuslers) can be viewed as layers consisting of a square lattice of “A” atoms alternating with layers of “B” and “C” atoms, as shown in Figure 1a. A related Heusler family has members with the formula unit ABC, in which half of the “A” atoms of the full Heusler are replaced by vacancies, as shown in Figure 1b. These are known as “half” Heuslers or semi-Heuslers. A third Heusler family with the formula unit A2BC (similar to the “full” Heuslers) consists of alloys that can be viewed as “AB” layers alternating with “AC” layers, as shown in Figure 1c. These are known as “inverse” Heuslers.

The properties of Heusler compounds can be altered by element substitution, but no single set of properties can characterize the entire Heusler family. Heusler alloys are expected to play an important role in spintronics, magneto-optical reading-recording devices, magnetic tunnel junctions, or tunneling magnetoresistance devices, due to their various multifunctional magnetic properties [16,17]. In the past years, several inverse binary- and ternary-Heusler alloys with a high Curie temperature, as well as quaternary-Heusler alloys, were theoretically predicated to exhibit spin-gapless semiconducting electronic structures [18,19]. Moreover, the bulk and thin films of MnCoAl and TiMnAl films were experimentally fabricated [20–23]. More recently, with first principle calculations, Ti2MnAl0.5Sn0.5 and Ti2MnAl0.5In0.5 were proven to be half metal and spin-gapless semiconductor, respectively [24].

Magnetic Heusler compounds are widely used in spintronic applications. The Heusler semiconductor can be used as either a spin-conserved tunneling barrier or a spin-transporting spacer in a Heusler ferromagnet–Heusler semiconductor–Heusler ferromagnet heterojunction, which has been extensively investigated in recent years. The magnetic Heusler compound is useful and meaningful for its potential integration into magnetic multilayer devices toward some spin valves, as well as for other opportunities and new phenomena.

In addition to these spintronic applications mentioned above, Heusler compounds, with other excellent properties, were studied extensively in the past several years. For instance, several Heusler compounds can be used as solar cell materials, thermoelectric materials, topological materials, magneto-optical materials, magneto-caloric materials, shape-memory materials, heavy-Fermion materials, superconductors, semiconductors, and so on [25–28].

In this work, the electronic structures and magnetic properties of the Ti2CoSi inverse Heusler alloy were calculated when a quarter of Co atoms were replaced by Ti. Then, the effects of hydrostatic strain and tetragonal deformation on the electronic structures and magnetic properties of the Ti2.25Co0.75Si compound were studied. Meanwhile, half of the Si atoms in Ti2.25Co0.75Si were replaced by B, Al, Ga, P, As, and Sb, and the results show that doped Ti2CoSi with an appropriate
concentration of impurities could be a half-metallic ferromagnet, a gapless half metal, or a spin-gapless semiconductor.

2. Materials and Methods

2.1. Structure of Materials

Structurally, the large Heusler family is described by only two variants, namely: the so-called full-Heusler \( \text{X}_2\text{YZ} \) phase, which is usually crystallized in the \( \text{Cu}_2\text{MnAl} \)-type (\( \text{L}_2^1 \)) structure, and the half-Heusler \( \text{XYZ} \) phase with a \( \text{C}_1 \text{b} \) structure, where \( \text{X} \) is a transition metal, \( \text{Y} \) may be a transition metal or a rare metal, and \( \text{Z} \) is a main group element. For full-Heusler alloys, if the atomic number of \( \text{Y} \) is higher than that of \( \text{X} \), making the \( \text{Y} \) element more electronegative than the \( \text{X} \) element, the inverse Heusler structure of \( \text{Hg}_2\text{CuTi} \)-type can be observed [29]. This structure adopts an \( \text{F}-\text{4}\text{3}m \) space group, and the atoms obey the following filling rules: \( \text{X} \) in \((0, 0, 0)\) and \((0.25, 0.25, 0.25)\), and \( \text{Y} \) and \( \text{Z} \) in \((0.5, 0.5, 0.5)\) and \((0.75, 0.75, 0.75)\), respectively [30].

2.2. Computational Methods

For investigating the electronic structures and magnetic properties of these pure and doped inverse Heusler alloys, ab initio calculations were carried out by using the density functional theory (DFT) with the standard generalized gradient approximations (GGA) of Perdew, Burke, and Erzerhof (PBE) to deal with the exchange correlation functional [31–36]. The cutoff energy for the plane wave was set to be 500 eV, and the \( \mathbf{k} \) point meshes for the Brillouin zone were set to be \( 12 \times 12 \times 12 \). In addition, the convergence for the difference on the total energy was set to be \( 1 \times 10^{-6} \) eV/atom [37,38].

3. Results and Discussion

3.1. Crystal Structures and Lattice Parameters

As shown in Figure 2a, the crystal structure of the regular Heusler alloy \( \text{Ti:CoSi} \) has a face-centered cubic structure with the following atomic positions: \( \text{Ti} \) \((0, 0, 0)\), \( \text{Ti} \) \((0.5, 0.5, 0.5)\), \( \text{Co} \) \((0.25, 0.25, 0.25)\), and \( \text{Si} \) \((0.75, 0.75, 0.75)\). Figure 2b shows that the inverse structure possesses 16 atoms in the unit cell with the following atomic positions: \( \text{Ti} \) \((0, 0, 0)\), \( \text{Co} \) \((0.5, 0.5, 0.5)\), \( \text{Ti} \) \((0.25, 0.25, 0.25)\), and \( \text{Si} \) \((0.75, 0.75, 0.75)\). From the previous study, it is known that the inverse Heusler alloy \( \text{Ti:CoSi} \) is a spin-gapless semiconductor with an integer magnetic moment of 3 \( \mu_\text{B} \) at the equilibrium lattice constant of 6.03 Å. With the GGA calculations, we found that the inverse \( \text{Ti:CoSi} \) alloy evinces gapless semiconducting characteristics at the equilibrium lattice parameter of 6.02 Å, which derives 0.16% less than from the previous investigation, demonstrating that our research is reasonable.
For determining the magnetic ground state of these materials, we calculated the energies of the ferromagnetic (FM) and anti-ferromagnetic (AFM) states. The energy differences between the AFM and FM states are listed in Table 1. The positive values illustrate that the energy of the FM state is smaller than that of the AFM state, indicating that the FM state is the magnetic ground state of these materials. At the same time, the minimized energies were obtained by computing the total energy among a large range of lattice parameters. The equilibrium lattice parameters are 6.01 Å and 6.04 Å for Ti2.25Co0.75Si0.5B0.5 and Ti2.25Co0.75Si0.5P0.5, which is smaller than that of Ti2.25Co0.75Si, as the radius of Si is larger than that of the B and P atoms. The calculated values are 6.13 Å, 6.13 Å, 6.12 Å, and 6.25 Å for Ti2.25Co0.75Si0.5Al0.5, Ti2.25Co0.75Si0.5Ga0.5, Ti2.25Co0.75Si0.5As0.5, and Ti2.25Co0.75Si0.5Sb0.5, respectively.

3.2. Electronic Structures and Magnetic Properties

The electronic band structures of the Ti2.25Co0.75Si alloy at its equilibrium lattice constant were calculated and are shown in Figure 3a. The spin-up and spin-down electronic bands are indicated by blue and red lines, respectively. When we replaced 25% cobalt with titanium in a cubic cell, a Ti2.25Co0.75Si alloy was achieved. It can be seen that the spin-up direction shows a metallic behavior and the spin-down direction evinces a semiconducting behavior with an indirect band gap of 0.22 eV around the Fermi level. The valence band maximum (VBM) and conduction band minimum (CBM)
are located at R and M points, respectively. Thus, Ti<sub>2.25</sub>Co<sub>0.75</sub>Si is a half-metallic ferromagnetic material with an integer magnetic moment of 7 μB (see Table 1). The calculated values of P were 98% for Ti<sub>2.25</sub>Co<sub>0.75</sub>Si<sub>0.5</sub>B<sub>0.5</sub> and Ti<sub>2.25</sub>Co<sub>0.75</sub>Si<sub>0.5</sub>Ga<sub>0.5</sub>, and 96% for Ti<sub>2.25</sub>Co<sub>0.75</sub>Si<sub>0.5</sub>P<sub>0.5</sub>, and 100% for the other studied compounds in this work, where P = |N↑(E<sub>F</sub>) − N↓(E<sub>F</sub>)| / [N↑(E<sub>F</sub>) + N↓(E<sub>F</sub>)], and N↑(E<sub>F</sub>) and N↓(E<sub>F</sub>) are the spin-dependent density of states at the Fermi level [39–41].

It is also important to study the effect of the possible lattice distortion during the process of film deposition on the electronic structures. The influences of compression and tetragonalization on the magnetic properties of the Ti<sub>2.25</sub>Co<sub>0.75</sub>Si compound were investigated. Figure 4a presents the position of the CBM and VBM of the spin-down channel as a function of the lattice constant. Upon compressing the lattice strain, the half-metallic properties can be kept between a range from 5.78 Å to 6.35 Å, indicating that the half-metallic characteristics of Ti<sub>2.25</sub>Co<sub>0.75</sub>Si can be preserved when the lattice constants are changed by ~4.9%~4.4% in relation to the equilibrium lattice constant. Figure 4b presents the position of the CBM and VBM of the spin-down channel as a function of the c/a ratio. Under the influence of tetragonalization, we found that the alloy experiences the transformation from a magnetic metal to a traditional half metal to a gapless half metal, and finally to a magnetic metal. For a Ti<sub>2.25</sub>Co<sub>0.75</sub>Si compound, a gapless half metal can be obtained when the lattice parameter, c, is expanded by 12%. The corresponding electronic band structures (c/a = 1.12) are plotted in Figure 3b. It can be seen that majority-spin electrons pass through the Fermi level, while the CBM and VBM of the minority spin just touch the Fermi level at R and A points, respectively.

<table>
<thead>
<tr>
<th>Compound</th>
<th>a&lt;sub&gt;0&lt;/sub&gt; (Å)</th>
<th>ΔE (eV)</th>
<th>μ&lt;sub&gt;tot&lt;/sub&gt; (μB)</th>
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<tr>
<td>Ti&lt;sub&gt;2.25&lt;/sub&gt;Co&lt;sub&gt;0.75&lt;/sub&gt;Si</td>
<td>6.08</td>
<td>1.171</td>
<td>7.00</td>
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<tr>
<td>Ti&lt;sub&gt;2.25&lt;/sub&gt;Co&lt;sub&gt;0.75&lt;/sub&gt;Si&lt;sub&gt;0.5&lt;/sub&gt;B&lt;sub&gt;0.5&lt;/sub&gt;</td>
<td>6.01</td>
<td>0.607</td>
<td>5.00</td>
</tr>
<tr>
<td>Ti&lt;sub&gt;2.25&lt;/sub&gt;Co&lt;sub&gt;0.75&lt;/sub&gt;Si&lt;sub&gt;0.5&lt;/sub&gt;Al&lt;sub&gt;0.5&lt;/sub&gt;</td>
<td>6.13</td>
<td>0.592</td>
<td>5.00</td>
</tr>
<tr>
<td>Ti&lt;sub&gt;2.25&lt;/sub&gt;Co&lt;sub&gt;0.75&lt;/sub&gt;Si&lt;sub&gt;0.5&lt;/sub&gt;Ga&lt;sub&gt;0.5&lt;/sub&gt;</td>
<td>6.13</td>
<td>0.673</td>
<td>5.00</td>
</tr>
<tr>
<td>Ti&lt;sub&gt;2.25&lt;/sub&gt;Co&lt;sub&gt;0.75&lt;/sub&gt;Si&lt;sub&gt;0.5&lt;/sub&gt;P&lt;sub&gt;0.5&lt;/sub&gt;</td>
<td>6.04</td>
<td>0.705</td>
<td>8.91</td>
</tr>
<tr>
<td>Ti&lt;sub&gt;2.25&lt;/sub&gt;Co&lt;sub&gt;0.75&lt;/sub&gt;Si&lt;sub&gt;0.5&lt;/sub&gt;As&lt;sub&gt;0.5&lt;/sub&gt;</td>
<td>6.12</td>
<td>0.830</td>
<td>9.00</td>
</tr>
<tr>
<td>Ti&lt;sub&gt;2.25&lt;/sub&gt;Co&lt;sub&gt;0.75&lt;/sub&gt;Si&lt;sub&gt;0.5&lt;/sub&gt;Sb&lt;sub&gt;0.5&lt;/sub&gt;</td>
<td>6.25</td>
<td>0.963</td>
<td>9.00</td>
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Figure 4. The energy of conduction band minimum (CBM) and valence band maximum (VBM) of the spin-down channel as a function of (a) the lattice constant and (b) the c/a ratio for Ti<sub>2.25</sub>Co<sub>0.75</sub>Si.
Figure 5. Spin-resolved electronic band structures of (a) Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$B$_{0.5}$, (b) Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$Al$_{0.5}$, and (c) Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$Ga$_{0.5}$ at the equilibrium lattice parameters. The zero of the energy scale is set at the Fermi energy. The blue and red solid lines represent the spin-up and spin-down states, respectively.
In the following, we substituted half of the silicon with B, Al, Ga, P, As, and Sb atoms in the cubic cell of Ti$_{2.25}$Co$_{0.75}$Si compound. The spin-resolved electronic band structures of the investigated compounds in the equilibrium lattice parameters were computed and are presented in Figures 5 and 6. For Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$B$_{0.5}$, Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$Al$_{0.5}$, and Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$Ga$_{0.5}$, although the Fermi level shifts into a low region of energy with the decrease of the valence electrons, the majority-spin electrons still pass through the Fermi level and the minority-spin bands evince semiconducting characteristics with a band gap, indicating that they are also half metallic. In particular, we found that for Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$B$_{0.5}$ and Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$Ga$_{0.5}$, the VBM of the spin-down channel touched the Fermi level at T point, demonstrating two quasi-gapless half metals. We also found that the minority spin band gap of Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$B$_{0.5}$ was smaller than that of Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$Al$_{0.5}$ and Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$Ga$_{0.5}$. The reason for this may be that the atomic radius of the boron atom is relatively small, which leads to a certain chemical pressure, and then reduces the band gap. For the cases of Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$P$_{0.5}$, Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$As$_{0.5}$, and Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$Sb$_{0.5}$, the spin-up bands open a seamless gap, and the Fermi level is located at this zero-gap as a result of the increase of valence electrons. Generally speaking, spin-gapless semiconductors can be divided into four categories, as follows: (i) one spin channel is semiconducting and the other spin channel is gapless; (ii) one spin channel is semiconducting and the VBM touches the Fermi level, while the other spin channel is gapless; (iii) there is a gap for both spin-up and spin-down channels, nonetheless, both the VBM of the spin-up channel and the CBM of

![Figure 6. Spin-resolved electronic band structures of (a) Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$P$_{0.5}$, (b) Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$As$_{0.5}$, (c) Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$Sb$_{0.5}$ at the equilibrium lattice parameters. The zero of the energy scale is set at the Fermi energy. The blue and red solid lines represent the spin-up and spin-down states, respectively.](image-url)
the spin-down channel are in contact with the Fermi level; and (iv) one spin channel is gapless, and for the other spin channel, the Fermi level touches the edge of the conduction bands. For Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$P$_{0.5}$, the spin-up channel is gapless and the CBM touches the Fermi level in the spin-down channel. Thus, it belongs to the fourth type. For Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$As$_{0.5}$ and Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$Sb$_{0.5}$, the spin-up channel is gapless, while the spin-down channel is semiconducting. As a consequence, they should belong to the first type. Nevertheless, for Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$As$_{0.5}$, the CBM of the down spins stand too close to the Fermi level. Thus, the singular electromagnetic transport effect can only be observed at very low temperatures. For Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$Sb$_{0.5}$, there is also a very small gap in the spin-up channel. Thereby, strictly speaking, it would be a spin-polarized narrow band-gap semiconductor. However, at a finite temperature, the compound would present the typical electromagnetic transport phenomenon of the spin-gapless semiconductor.

Taking Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$B$_{0.5}$ and Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$P$_{0.5}$, for example, we discussed the orbital-resolved spin polarization. The total density of the states (DOS) and partial DOS for Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$B$_{0.5}$ and Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$P$_{0.5}$ obtained using GGA, are presented in Figure 7. The DOS around the Fermi level is heavily dominated by the 3d states of the Ti and Co atoms. It was found that the 3d states of Co are mainly distributed from $-1$ to $-3$ eV, while the 3d states of Ti are mainly distributed around and beyond the Fermi level. The electronic configurations of the Ti and Co atoms are 3d$^4$4s$^2$ and 3d$^7$4s$^2$, respectively. Thus, the Ti atom with less than half of the filling valence electron shell is mainly distributed at high energy levels, and the Co atom with more than half the filling valence electron shell is mainly distributed at low energy levels. It was also found that the impurity atoms play a key role in adjusting the valence electron concentration of the compound, and shift the Fermi level upwards or downwards. For Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$B$_{0.5}$, the acceptor doping moves the Fermi level downwards, and thus the Fermi level is submerged in the deeper energy region. For Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$P$_{0.5}$, the donor doping moves the Fermi level upwards, and thus the Fermi level is able to be pulled out of the filled bands and is located at the nearly zero band gap.

The results show that the spin-up and spin-down states around the Fermi level are predominantly derived from the Ti-d and Co-d states, and the d–d hybridization is the main origin for spin polarization. In order to understand this matter intuitively, we drew the spin density plots of Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$B$_{0.5}$ and Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$P$_{0.5}$ (see Figure 8), which are defined as the difference of spin-up and spin-down states. We can see that the spin density predominantly concentrates on the Ti and Co atoms, evincing that the spin polarization is mainly from the Ti and Co atoms. For these compounds, the magnetic moments are predominantly due to the Ti-d and Co-d electrons. The large exchange splitting of the Ti-d and Co-d states leads to a large magnetic moment.

![Figure 7](image-url)

**Figure 7.** The total density of the states (DOS) of (a) Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$B$_{0.5}$ and (b) Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$P$_{0.5}$ at the equilibrium lattice parameters. The partial DOS of (c) Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$B$_{0.5}$ and (d) Ti$_{2.25}$Co$_{0.75}$Si$_{0.5}$P$_{0.5}$ at the
equilibrium lattice parameters. The black, red, blue, and orange solid lines indicate the Ti-d, Co-d, Si-p, and B (P)-p states, respectively.

Figure 8. The spin densities of (a) \( \text{Ti}_2\text{Co}_{0.75}\text{Si}_{0.5}\text{B}_{0.5} \) and (b) \( \text{Ti}_2\text{Co}_{0.75}\text{Si}_{0.5}\text{P}_{0.5} \) at the equilibrium lattice parameters.

4. Conclusions

In summary, we have determined the structural, electronic, and magnetic properties of inverse Ti$_2$CoSi-based compounds. By adjusting the concentration of titanium and cobalt, the fabricated Ti$_2$Co$_{1-x}$Si compound is half metallic, that is, single-channel spin polarized. The majority-spin bands are strongly metallic, while the minority-spin bands are semiconductor-like around the Fermi level. This gap has previously been reported by other authors, and is formed as a result of the strong 3d–3d hybridization between the two transition-metal atoms [42–45]. It is thought that this 3d–3d interaction is essential for the formation of the gap at the Fermi level. Under the influence of isotropic hydrostatic pressure, the Ti$_2$Co$_{1-x}$Si alloy can preserve the half-metallic feature between a range of 5.78 Å to 6.35 Å. Nevertheless, it would transform to a gapless half metal upon the tetragonalization of the lattice. Tetragonal deformation could modify the crystal symmetry and vary the position of the edge of the bands, especially at some high-symmetry points in the reciprocal space. Our further calculations on Ti$_2$Co$_{0.75}$Si$_{0.5}$B$_{0.5}$, Ti$_2$Co$_{0.75}$Si$_{0.5}$P$_{0.5}$, and other doped compounds demonstrate that the doped foreign impurity is able to adjust the valence electron concentration of the compound and shift the Fermi level upwards or downwards, creating several different electronic structures around the sensitive Fermi level.

Author Contributions: S.D. and L.F. designed the project. L.Z. and J.D. performed the calculations and prepared the manuscript. All of the authors analyzed the data and discussed the results. All authors have read and agreed to the published version of the manuscript.

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