

Article

# Finite Element Analysis of Reinforced Concrete Bridge Piers including a Flexure-Shear Interaction Model

Alessandro Rasulo <sup>1,\*</sup>, Angelo Pelle <sup>2</sup>, Davide Lavorato <sup>2</sup>, Gabriele Fiorentino <sup>2</sup>, Camillo Nuti <sup>2</sup> and Bruno Briseghella <sup>3</sup>

<sup>1</sup> Department of Civil and Mechanical Engineering, University of Cassino and Southern Lazio, 03043 Cassino, Italy

<sup>2</sup> Department of Architecture, Roma Tre University, Largo G. B. Marzi 10, 00153 Roma, Italy; angelo.pelle@uniroma3.it (A.P.); davide.lavorato@uniroma3.it (D.L.); gabriele.fiorentino@uniroma3.it (G.F.); c.nuti@uniroma3.it (C.N.)

<sup>3</sup> College of Civil Engineering, Fuzhou University, Fuzhou 350108, China; bruno@fzu.edu.cn

\* Correspondence: a.rasulo@unicas.it

Received: 31 January 2020; Accepted: 11 March 2020; Published: 25 March 2020

**Abstract:** This paper discusses the seismic behavior of reinforced concrete (RC) bridge structures, focusing on the shear–flexure interaction phenomena. The assessment of reinforced concrete bridges under seismic action needs the ability to model the effective non-linear response in order to identify the relevant failure modes of the structure. Existing RC bridges have been conceived according to old engineering practices and codes, lacking the implementation of capacity design principles, and therefore can exhibit premature shear failures with a reduction of available strength and ductility. In particular, recent studies have shown that the shear strength can decrease with the increase of flexural damage after the development of plastic hinges and, in some cases, this can cause unexpected shear failures in the plastic branch with a consequent reduction of ductility. The aim of the research is to implement those phenomena in a finite-element analysis. The proposed model consists of a flexure fiber element coupled with a shear and a rotational slip spring. The model has been implemented in the OpenSEES framework and calibrated against experimental data, showing a good ability to capture the overall response.

**Keywords:** seismic assessment; reinforced concrete; bridge structures; flexure-shear failure; finite element analysis; collapse modes

---

## 1. Introduction

Damage due to earthquakes can have a significant impact on transportation networks, in particular on bridges that represent the weakest component of those networks. Structural and non-structural damage in bridges can, indeed, produce significant losses both in terms of a prolonged traffic disruption and in terms of the repairs required to assure again the viability of the damaged bridges [1,2]. In order to prevent those nefarious outcomes, in recent decades, great effort has been made for the assessment of the seismic vulnerability of bridges, specifically on reinforced concrete (RC) bridges constructed before the adoption modern seismic codes.

Modern bridge structures are able to resist the seismic action with a response that assures high levels of dissipation of energy thanks to an inelastic behavior characterized by large ductile deformation cycles. To achieve this performance objective, modern design codes have implemented

in their provisions plastic design principles aimed at preventing the activation of brittle damage mechanisms.

On the other hand, existing bridge structures have been designed when many sites were not classified as seismically prone and adopting older construction standards, relying on the admissible stress method, with levels of seismic demand (if any) much lower than the ones currently adopted. Therefore, the resulting structures were conceived to respond in the elastic range, leaving a false sense of security that the actual resistances (well beyond the nominal ones considered in the design process) would be assured by the adopted safety coefficients and by the inelastic behavior of materials and structures. On the contrary, the lack of a hierarchy of strengths that would be lately assured by the implementation, in modern codes, of capacity design principles, would not prevent the occurrence of non-ductile failure modes reducing the extent of the inelastic response [3–6].

A typical characteristic of existing bridge piers is the presence of a low percentage of transversal reinforcement, usually represented by poorly detailed and highly spaced stirrups, that would be considered substandard according to the construction practice adopted today [7].

According to the experimental evidence, structures with such a characteristic can show a premature shear failure, limiting the capacity to undergo inelastic deformation and therefore dissipate energy. In fact, several researches and studies on shear strength have evidenced that, even in the case those piers have been initially designed with nominal shear capacity exceeding the shear in equilibrium with flexural yielding, those piers could still fail early in shear due to the detrimental action of inelastic flexural deformations on the shear strength [8,9].

Indeed, the widening of flexural–shear cracks due to cyclic inelastic deformations, especially in the plastic-hinge region, reduce the ability of concrete to transfer the shear action through mechanisms relying on aggregate interlock. As a consequence, there is a sectional shear capacity reduction, showing that under cyclic loading the shear strength of columns can be heavily dependent on the inelastic deformations and that shear strength degrades with ductility more quickly than flexural strength. Thus, it is important, when assessing the seismic response of existing structures to take into consideration in the numerical model the insurgence of those complex interaction phenomena affecting the overall response of the bridge structures.

In past decades different attempts have been made to propose computational models able to couple flexural and shear effects. Those models offer a huge variety of solutions depending on the complexity and the sophistication of the numerical procedure adopted to represent the physical problem, from a relatively simple approach in which a translational spring, representing the shear behavior, is added [10–12] to frame models where sophisticated, multi-dimensional, constitutive laws are employed [13–17].

## 2. Objectives and Methods

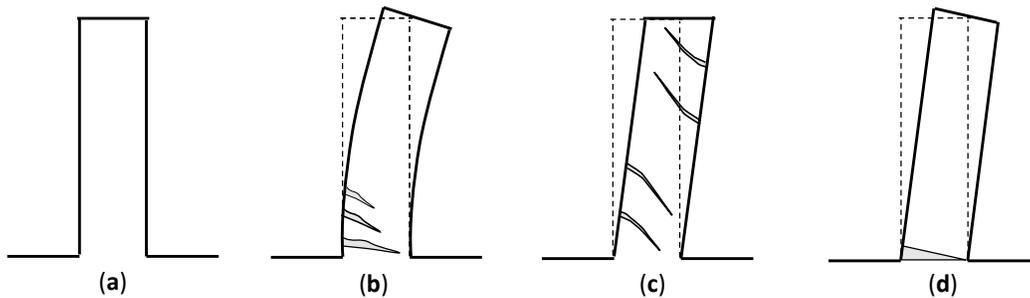
The present study aims at contributing to the modelling capability of RC bridge elements under seismic loading. To pursue this objective, a simple phenomenological model has been presented, considering the most relevant damage modes of existing RC bridge elements. Particular emphasis in the development of the model has been given to the study of the shear–flexure interaction, that is deemed a pivotal issue for the assessment of existing RC piers. The available formulations, contained either in recent codes of practice or in research documents, have been discussed. Those models are generally calibrated on empirical tests. A database of experimental tests on specimens characterized by mechanical and reinforcing properties typical of substandard bridge element has been retrieved in order to test the validity of the proposed model.

## 3. Numerical Model

### 3.1. Model Outline

In this research the seismic response of a RC bridge pier is studied through a numerical model based on a three-component approach, in which the following coexisting behavioral mechanisms are accounted for: flexure, shear and bonding. As schematically depicted in Figure 1, the lateral

displacement of a cantilever bridge pier can, indeed, be idealized as the sum of those three components.



**Figure 1.** Idealized components of horizontal displacement: (a) Original undeformed configuration as a cantilever column; (b) bending deformation; (c) shear deformation and (d) bonding deformation.

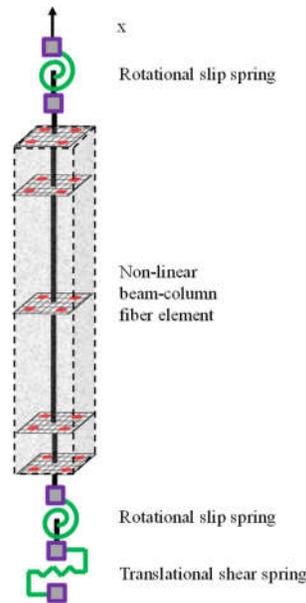
Flexure is by far the most relevant aspect in determining the seismic response of a bridge pier and it is also the most investigated.

The bonding is essentially responsible for the additional displacement due to the slippage of the longitudinal reinforcing bars in the anchoring concrete. In most cases this phenomenon can be represented as a fixed-end rotation of the pier due to the strain penetration carried by the steel bars anchoring into the foundation concrete. This additional displacement can also account for the possible extra effects due to reinforcement interruption (due to limitations in steel bar lengths or to concrete casting performed in stages) and consequent need to splicing the reinforcement by overlapping the bars.

Finally, regarding shear deformation, in general it is admitted that in slender columns the contribution of the shear flexibility on the total displacement can be neglected: it starts to have a significant effect only on squat elements with a low height-to-depth ratio. However, it becomes relevant in any case, if the element is expected to be damaged in shear.

The proposed computational model has been developed using the finite element method within the OpenSEES framework for seismic analysis [18]. Specifically, a two dimensional (2D) nonlinear finite element model has been employed, by means of a three-component model, in which the three aforementioned deformability contributions (flexure, shear, and slip) are separately considered and modelled.

As illustrated in Figure 2, a fiber-based, nonlinear beam-column element has been connected at each end of the column together with a zero-length rotational spring to account for the bond-slip behavior and a zero-length translational spring to account for the shear behavior. Since the element is loaded only at the ends (no distributed loads are applied along the element length and no competent mass is assigned to the element during a dynamic analysis) the shear internal force is constant, so that just one translational spring is sufficient for the shear behavior. In the case of a typical bridge pier cantilever schematization, the rotational and translational springs should be added just to the fixed end.



**Figure 2.** Numerical finite element model adopted in this study ( $x$  is the element local axis).

### 3.2. Flexural Behavior

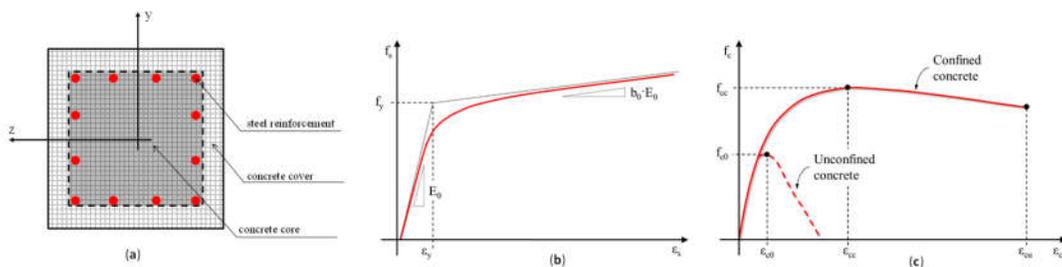
The flexural behavior has been modelled with a distributed plasticity approach using a nonlinear force-based beam-column element, with a fiber discretization of the section.

The peculiarity of a finite element with a force formulation is that it employs force shape functions (derived by equilibrium considerations) to obtain the internal forces (at section level) once the external forces acting at the nodes of the element are known.

The vantage of that approach is that, provided no loads are applied along the element length, just one element can be sufficient to capture the bending behavior of the whole cantilevered pier, despite the fact that the formation of plastic hinges at the fixed end of the element will produce a concentration of non-linear curvatures.

The overall response of the element is obtained through the integration of the non-linear responses obtained over the different sections of the element. In practice, the integral is substituted by a weighted summation adopting some numerical integration scheme over a certain number of monitored sections. In our case, a Gauss–Lobatto 5 node scheme was adopted.

In order to analyze the non-linear response of the element cross-sections, those have been discretized in fibers, as depicted in Figure 3a. Since a reinforced concrete element is essentially composed by two different materials, namely casted in place concrete and steel reinforcing bar, two different kinds of constitutive relationship are used to describe the mechanical behavior of those materials, and assigned to relevant fibers within the element sections.



**Figure 3.** Properties of a RC section: (a) Fiber discretization of the section ( $y$  and  $z$  are the element local axis); (b) steel reinforcement and (c) cover (unconfined) and core (confined) concrete constitutive law (the meaning of the symbols is given in the text).

The longitudinal steel reinforcement has been modelled by the Menegotto and Pinto [19] constitutive law (Steel02 uniaxial material in OpenSEES). With reference to Figure 3b  $f_y$  and  $\varepsilon_y$  are, respectively, the yield strength and strain of the reinforcement whilst  $E_0$  is the elastic modulus and  $b_0$  an adimensional parameter accounting for post-yield stiffening.

The concrete has been modelled in OpenSEES using the Concrete04 uniaxial material which is based on the Popovics law [20]. The concrete on the section cover has been considered unconfined, whilst the concrete in the section core has been considered as confined, using the Mander et al. model [21]. With reference to Figure 3c,  $f_{co}$  and  $f_{cc}$  are, respectively, the strength of unconfined and confined concrete, whilst  $\varepsilon_{co}$  and  $\varepsilon_{cc}$  are the corresponding strains.

### 3.3. Slipage Behavior

The slippage of the reinforcing bars will cause rigid-body rotation of the column, that produces an additional source of the deformation, that can be significant.

Several bond slip models are available in literature for deformed bars [22–25].

In order to account for the slippage in the numerical model, a rotational slip springs at the bottom of the element with linear constitutive relationship was used and its stiffness is given by [26]:

$$K_{slip} = \frac{8uEI_{eff}}{f_y\phi_{long}} \quad (1)$$

where  $\phi_{long}$  is the diameter of longitudinal rebar,  $f_y$  is the yield strength of longitudinal rebar,  $u$  is the average tension on the surface between the longitudinal reinforcement and the concrete that can be calculated as  $0.5\sqrt{f'_c}$  where  $f'_c$  is the concrete compressive strength and  $EI_{eff}$  is the effective stiffness that can be evaluated by [27]:

$$\begin{cases} EI_{eff} = 0.2EI & \text{if } 0.2 \geq \frac{P}{A_g f'_c} \\ EI_{eff} = EI \left( \frac{5}{3} \frac{P}{A_g f'_c} - \frac{40}{30} \right) & \text{if } 0.2 \leq \frac{P}{A_g f'_c} \leq 0.5 \\ EI_{eff} = 0.7EI & \text{if } 0.5 \leq \frac{P}{A_g f'_c} \end{cases} \quad (2)$$

where  $P$  is axial load,  $A_g$  is gross area of section,  $E$  is the Young's module of the concrete and  $I$  is the section inertia moment ( $bh^3/12$ ).

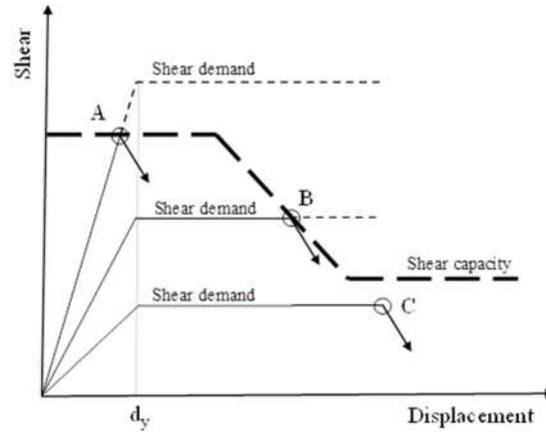
### 3.4. Shear Behavior

In the past, different shear-capacity models have been proposed to account for the flexure-shear coupling, leading to the strength degradation of columns with deformation.

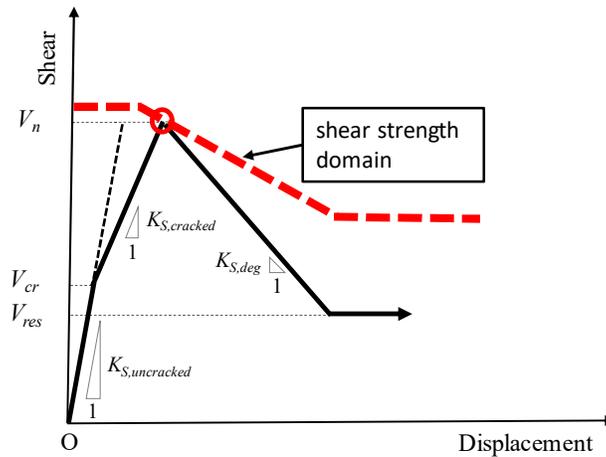
The first one was the formulation codified in the ATC seismic design guidelines, where a shear-capacity curve degrading with displacement ductility was proposed (Figure 4).

In this study the phenomenological model illustrated in Figure 5 has been adopted for modelling the shear spring, accounting for both strength and deformation components due to shear action.

As shown in Figure 5, the first two branches represent the backbone behavior of the shear component of the element before the intersection with the shear strength domain (marked with a red circle) and the start of the degrading branch.



**Figure 4.** ATC model for shear-strength degradation ( $d_y$ : yielding displacement). Three cases are considered: (A) shear failure before flexural yielding (pure shear failure); (B) shear failure after flexural yielding (shear-flexural failure); (C) flexural failure.



**Figure 5.** Phenomenological model for the shear spring.

The pre-cracking shear stiffness  $K_{S,uncracked}$  can be calculated through the elasticity theory:

$$K_{S,uncracked} = \frac{GA_v}{H} \tag{3}$$

$$G = \frac{E_c}{2(1+\nu)} \approx 0.4E_c \tag{4}$$

where  $H$  is the column height,  $G$ ,  $E_c$ , and  $\nu$  are respectively the shear, Young’s, and Poisson’s moduli of concrete, and  $A_v$  is the shear effective area of the column.

In general, this stiffness is contributing to a minor displacement increase, since even in squat elements the flexural stiffness is significantly smaller, but it can be useful to modify the fiber element formulated within OpenSEES as an Euler-Bernoulli beam-column to a full Timoshenko element.

The post-cracking shear stiffness  $K_{S,cracked}$  can be calculated considering the deformation of transversal steel through the diagonal cracks. Park and Paulay [27] proposed an equivalent strut-model:

$$K_{S,cracked} = \frac{\rho_w \sin^4(\theta) \cot^2(\theta)}{\sin^4(\theta) + 10\rho_w} E_s A_v \tag{5}$$

where  $\rho_w$  is the transversal steel reinforcement ratio,  $\theta$  is the angle between the diagonal cracks and the member axis and  $E_s$  is the Young's modulus of steel.

In Figure 5 the shear-strength domain represents the maximum shear that the column can sustain. As it is evident, that limit state curve is not constant, as in the usual formulation contained in most design codes (like Eurocode 2 or ACI-318), but is dependent with the displacement and the element once reached the maximum strength, will follow the degrading branch.

In the literature, there are several shear-capacity models that have been proposed to account for the shear-strength degradation of columns under seismic loading [9,28–30]. It is worth noting that all the aforementioned formulations are defined in terms of total displacement (i.e., the sum of single displacement components) so that the shear-strength domain has been placed in Figure 5 (where the displacement is defined just in terms of shear deformations) only for illustration purposes.

As shown in Figure 3, the failure is activated when the shear capacity curve (bold black dash line) intercept the shear demand curve (black line) which represent the global behavior of the column gives by the summation of the flexure, slippage and shear behaviors.

In the Sezen and Moehle [9] model, the nominal shear strength is given as the summation of the contribution from concrete  $V_c$  and the transverse reinforcement  $V_s$ :

$$V_n = V_c + V_s \tag{6}$$

where the concrete contribution can be calculated by:

$$V_c = k \left( \frac{0.5\sqrt{f'_c}}{a/d} \sqrt{1 + \frac{P}{0.5\sqrt{f'_c}A_g}} \right) 0.8A_g \text{ (MPa)} \tag{7}$$

while the steel contribution can be calculated by:

$$V_s = k \frac{A_w f_y d}{s} \tag{8}$$

where  $f'_c$  is the compressive strength of concrete,  $A_g$  is gross area of section,  $P$  is the axial load,  $a$  is the shear span (distance between the maximum moment section to point of inflection),  $d$  is effective depth of the section,  $A_w$  is the transversal reinforcement area,  $f_y$  is the yield strength of the transversal reinforcement. The factor  $k$  is the parameter which considers the variation of shear strength with the increase of displacement ductility and is defined to be equal to 1.0 for displacement ductility less than 2, to be equal to 0.7 for displacement ductility  $\mu_\Delta$  exceeding 6, and to vary linearly for intermediate displacement ductility, as shown in Figure 6.

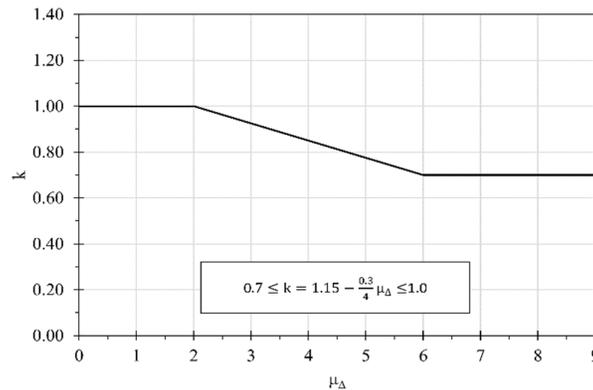


Figure 6. The factor  $k$  after Sezen and Moehle [9] (in Equations (7) and (8)).

In the Biskinis et al. model [28] the nominal shear strength is calculated as the summation of three contribution from concrete  $V_c$ , transversal reinforcement  $V_s$  and axial load  $V_P$ :

$$V_n = V_c + V_s + V_P \tag{9}$$

where the concrete contribution is given by:

$$V_c = k \left[ 0.16 \max(0.5; 100\rho_{tot}) \left( 1 - 0.16 \min\left(5; \frac{a}{h}\right) \right) \sqrt{f'_c} A_g \right] \quad (10)$$

the transversal reinforcement contribution is given by Equation (8), as in the previous model, and the contribution of axial load is given by:

$$V_p = \frac{h-c}{2a} \min(P; 0.55A_g f'_c) \quad (11)$$

where  $\rho_{tot}$  is the total longitudinal reinforcement ratio,  $h$  is the depth of the section, and  $c$  is the neutral axis depth.

The factor  $k$  is only function of the plastic part of the displacement ductility and is given by:

$$k = 1 - 0.05 \cdot \min(5; \mu_{\Delta}^{pl}) \quad (12)$$

where:

$$\mu_{\Delta}^{pl} = \frac{\Delta - \Delta_y}{\Delta_y} = \frac{\theta - \theta_y}{\theta_y} \quad (13)$$

where  $\Delta$  and  $\theta$  are respectively the displacement and rotation at the point considered while  $\Delta_y$  and  $\theta_y$  are respectively the yielding displacement and yielding rotation.

Similar to this model is the Kowalsky and Priestley model [30]. In fact, the nominal shear strength can be evaluated by the Equation (9) where the concrete contribution can be calculated by:

$$V_c = \alpha\beta\gamma\sqrt{f'_c}(0.8A_g) \quad (14)$$

where the  $\alpha$  factor is function of the ratio  $a/d$ , the  $\beta$  factor is function of the longitudinal steel ratio  $\rho_l$ , and the  $\gamma$  factor is function of the ductility curvature  $\mu_v$ , as shown in Figures 7–9.

The transversal contribution is given by:

$$V_s = \frac{A_w f_y (d - c - \delta)}{s} \cdot \cot \theta \quad (15)$$

where  $\delta$  is the concrete cover and  $s$  is the transverse reinforcement spacing. The axial load contribution is given by:

$$V_p = \begin{cases} P \frac{h-c}{2a} & \text{if } P > 0 \\ 0 & \text{if } P \leq 0 \end{cases} \quad (16)$$

Finally, the model by Elwood and Moehle [29] introduce a drift capacity model based on observations from the experimental database, it is different than previous model because it allows to evaluate the drift ratio at shear failure rather than the shear strength. The empirical equation is:

$$\frac{\Delta_s}{L} = \frac{3}{100} + 4\rho_w - \frac{1}{40} \frac{v}{\sqrt{f'_c}} - \frac{1}{40} \frac{P}{A_g f'_c} \geq \frac{1}{100} \quad (MPa) \quad (17)$$

where  $\Delta_s/L$  is the drift ratio at shear failure,  $\Delta_s$  is the displacement where the shear degradation begin,  $L$  is the height of the column,  $\rho_w$  is the transverse reinforcement ratio and  $v$  is the nominal shear stress ( $V_{max}/A_g$ ).

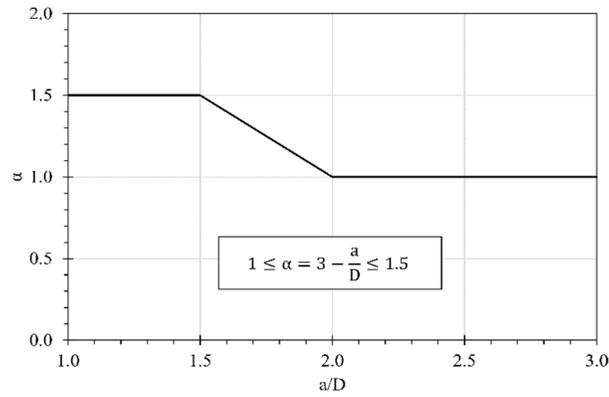


Figure 7. The factor  $\alpha$  after Kowalsky and Priestley [30] (in Equation (14)).

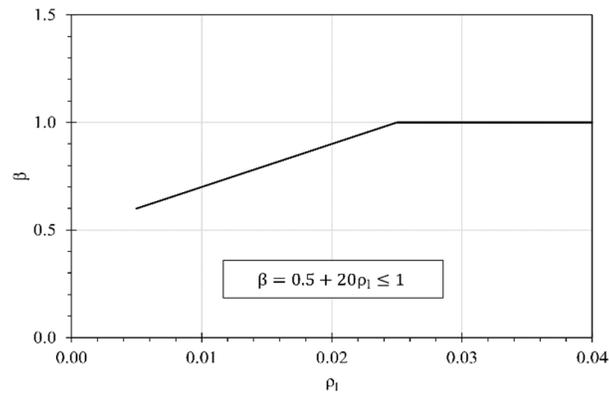


Figure 8. The factor  $\beta$  after Kowalsky and Priestley [30] (in Equation (14)).

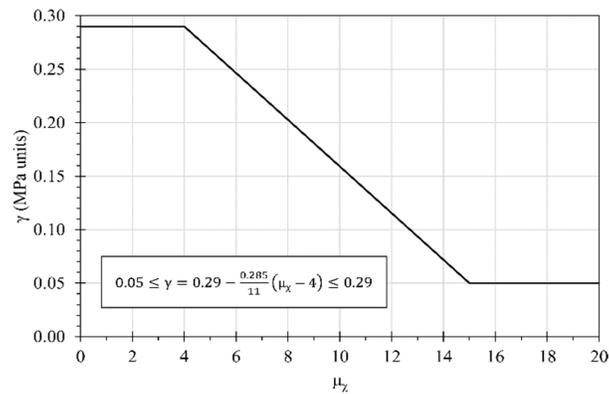


Figure 9. The factor  $\gamma$  after Kowalsky and Priestley [30] (in Equation (14)).

### 3.5. Interaction Model

In order to ensure that correct coupling is established between flexural, slip and shear behavior, a control is performed at element level through equilibrium and compatibility conditions.

In particular, thanks to the series arrangement of the three model components (the two zero length springs and the force-based beam column element) representing the pier under lateral load, the shear force acting in each element will be the same, but the deformation development of each element will be different for different cases.

In particular is discussed here the interaction between the flexural and shear behavior, as schematized in Figure 10a. In the proposed model all the shear deformation is concentrated in the translational shear spring whilst the flexural deformation is modelled by the beam-column element.

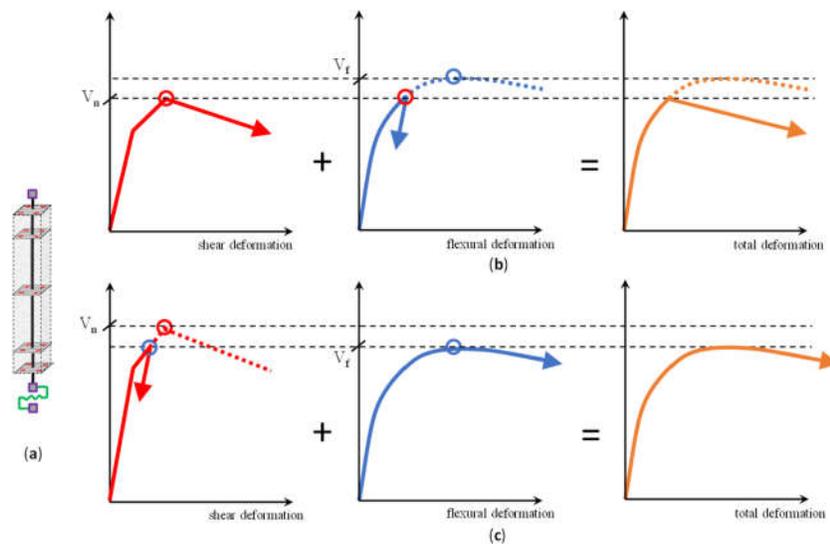
OpenSEES introduced, as an interaction model, the LimitStateMaterial command, based on Elwood works (2004), used to construct a uniaxial hysteretic material object with, among others, damage and post-damage unloading stiffness based on ductility.

This command overcomes the pitfall of a simplistic shear-flexure interaction model represented by having a shear spring in series with a beam column element. In a very simple serial model, indeed, if the shear strength (the maximum of the shear spring response) is less than the bending yield strength (the shear corresponding to the development of the plastic hinges), the total response is correctly dominated by a brittle failure occurring in the elastic branch. If, on the other hand, the shear strength is higher than the bending yield strength, then the model is not able to capture any shear degradation, in contrast with theoretical and experimental evidence. Actually, in the latter case, when the initial shear strength is higher than yielding strength, but close enough to it, when degrading with the increase of inelastic deformation could be lower. In this case the activation of shear damage in the plastic branch is expected, as shown in Figure 4 (case B), this leads the structural response of the column to follow the degrading branch of the shear-strength-domain of Figure 5. In order to improve the series model, the LimitStateMaterial associated with LimitCurve command can be used to define a limit shear surface defined by the drift capacity model proposed by Elwood, with the use of the shear-failure domain given by Equation (17).

The behavior of the shear spring and bending beam-column element are illustrated schematically in Figure 10.

If the shear capacity  $V_n$  of the pier is lower than its flexural strength  $V_f$ , the pier will have a response controlled by the shear behavior as shown schematically in Figure 10b. Before reaching the shear capacity  $V_n$ , shear response and flexural response will develop simultaneously in accordance with the solid line in the figure and once the shear demand reaches the shear strength,  $V_n$ , a shear failure occurs and the shear response enters into descending range where significant deterioration behavior occurs, conditioning the overall response, that cannot develop forces higher than the shear strength.

If the shear capacity  $V_n$  of the column is higher than flexural strength  $V_f$ , the pier will have a response controlled by the flexural behavior as shown schematically in Figure 10c. Before reaching the flexural capacity  $V_f$ , shear response and flexural response will develop simultaneously in accordance with the solid line in the figure and once the shear demand reaches the flexural strength  $V_f$ , a flexural failure occurs and the flexural response enters into descending range, conditioning the overall response, that cannot develop forces higher than the shear strength.



**Figure 10.** Combination of the single response components in shear-flexure interaction model: (a) Two-component model; (b) Response controlled by shear failure and (c) Response controlled by flexural failure.

Adopting the proposed model, prior to the activation of the degrading branch, the response will follow the behavior given by the summation of flexure and shear (as in the simple serial spring model). After each step, the limit curve model checks if the force and deformation have exceeded the limit surface. If the limit curve has not been exceeded, the analysis continues at the next step without any change to the response. If the limit curve has been exceeded, then the behavior is redefined according to the degrading slope  $K_{deg}$ , and the residual strength  $F_{res}$  both indicated in Figure 11.

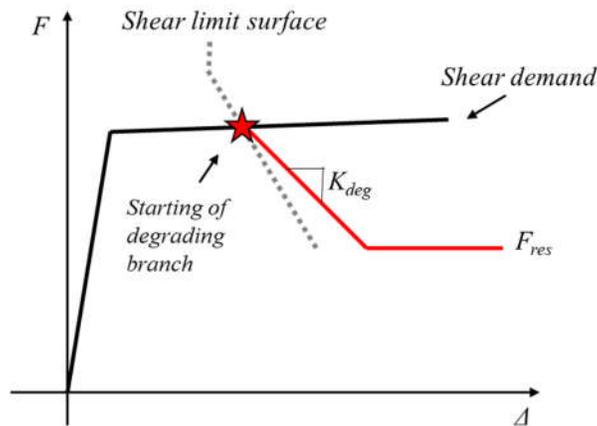


Figure 11. Redefinition of backbone after failure.

#### 4. Numerical Validation

Using the model illustrated in the previous chapter, the experimental behavior of a series of reinforced concrete elements was simulated analytically by the proposed model. The details of the specimens failing in shear are summarized in Table 1.

Table 1. Database of examined reinforced concrete elements.

Rectangular Section												
Reference	Specimen	b (mm)	h (mm)	s (mm)	a/d (---)	$\rho_l$ (---)	$\rho_w$ (---)	$f'_c$ (MPa)	$f_{yl}$ (MPa)	$f_{yw}$ (MPa)	v (---)	Test Type
Lynn A.C. [31]	2CLH18	457.2	457.2	457.2	3.74	0.02	0.0007	26.8	330.7	399.6	0.09	DC
	3CLH18	457.2	457.2	457.2	3.74	0.03	0.0007	26.8	330.7	399.6	0.09	DC
	3SLH18	457.2	457.2	457.2	3.74	0.03	0.0007	26.8	330.7	399.6	0.09	DC
	2SLH18	457.2	457.2	457.2	3.71	0.02	0.0007	27.5	330.7	399.6	0.07	DC
	3CMH18	457.2	457.2	457.2	3.74	0.03	0.0007	25.4	330.7	399.6	0.28	DC
	3CMD12	457.2	457.2	457.2	3.74	0.03	0.0017	25.4	330.7	399.6	0.28	DC
Saatcioglu	U1	350.0	350.0	150.0	3.28	0.03	0.0085	43.6	430.0	470.0	0.00	SC
Ozcebe	U2	350.0	350.0	150.0	3.28	0.03	0.0085	30.2	453.0	470.0	0.16	SC
[32]	U3	350.0	350.0	75.0	3.28	0.03	0.0169	34.8	430.0	470.0	0.16	SC
Hollow Rectangular Section												
Reference	Specimen	b (mm)	h (mm)	s (mm)	a/d (---)	$\rho_l$ (---)	$\rho_w$ (---)	$f'_c$ (MPa)	$f_{yl}$ (MPa)	$f_{yw}$ (MPa)	v (---)	Test Type
Calvi et al. [33]	T250	450.0	450.0	75.0	3.00	0.0177	0.0025	30.3	550.0	550.0	0.07	SC
	T500A	450.0	450.0	75.0	3.00	0.0177	0.0025	29.7	550.0	550.0	0.15	SC
	T500B	450.0	450.0	75.0	3.00	0.0177	0.0025	32.7	550.0	550.0	0.15	SC
	T750	450.0	450.0	75.0	3.00	0.0177	0.0025	30.8	550.0	550.0	0.21	SC

b: column section width; h: column section height; s: stirrup spacing; a/d: aspect ratio (shear span/section depth);  $\rho_l$ : longitudinal reinforcement ratio;  $\rho_w$ : transverse reinforcement ratio;  $f'_c$ : compressive strength of concrete;  $f_{yl}$ : yield strength of longitudinal steel;  $f_{yw}$ : yield strength of transverse steel; v: axial load ratio; Test type: SC (single cantilever), DC (double cantilever).

In Figures 12a and 13a the experimental behavior of specimen 2CLH18 and 3CLH18 are shown. Both the columns had a double cantilever configuration, a square cross-section of  $457 \times 457$  mm. The longitudinal steel reinforcement was placed uniformly around the perimeter of the cross-section and

they were 25 mm (#8) and 32 mm (#10) as nominal diameter for the specimen 2CLH18 and 3CLH18, respectively. The transversal reinforcements were hoop with 9.5 mm (#3) and 457 mm respectively as nominal diameter and spacing ( $\rho_w = 0.0007$ ) for both specimens. The axial force was equal to  $P = 503 \text{ kN}$  ( $\nu = P/(A_g \cdot f'_c) = 0.09$ ). The concrete compressive strength was equal to  $f'_c = 26 \text{ MPa}$ , whilst the longitudinal steel yielding strength was equal to  $f_{yl} = 335 \text{ MPa}$  and the transversal steel yielding strength was equal to  $f_{yw} = 400 \text{ MPa}$ .

The two specimens have the same shear strength due to the identical transversal reinforcements while the higher longitudinal reinforcement of the specimen 3CLH18 leads a higher yielding force than the specimens 2CLH18. As a consequence the experimental response of the two specimens experience two different collapse modes: the first one (2CLH18) has a typical response dominated by flexure up to collapse due to the reaching of the available ductility whilst the second one shows clearly a strength degradation in the plastic branch due to shear failure immediately after the onset of the flexural yielding. The two specimens exemplify well the two cases reported in Figure 10.

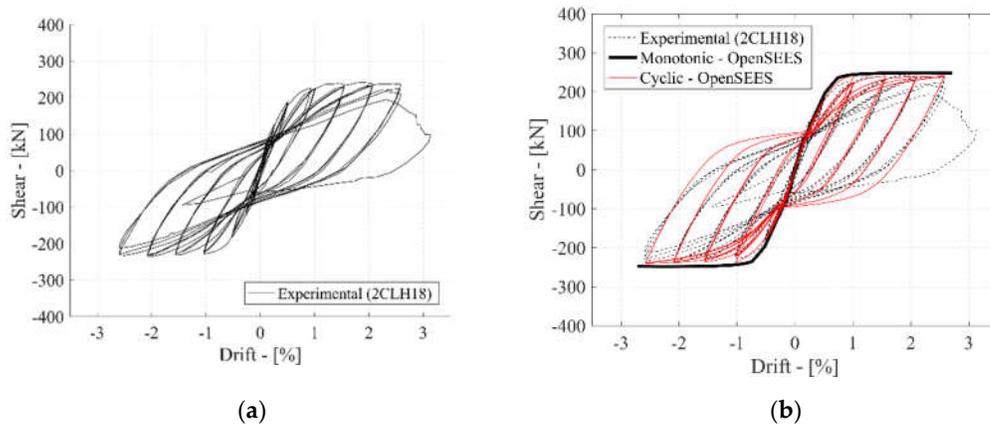
In Figures 12b and 13b the numerical analysis has been compared with the experimental one. In the numerical model the cracked stiffness of the shear spring,  $K_{S,cracked}$  has been set equal to the one of the uncracked one,  $K_{S,uncracked}$ , following. Therefore, the black dash line of Figure 4, as given by Equation (3).

It is clear from the experimental curve that the shear degradation starts at a drift value of about  $(\Delta s/L)_{exp} = 0.01$  and displacement of about  $\Delta s_{exp} = 30.4 \text{ mm}$  (square mark in Figure 13a).

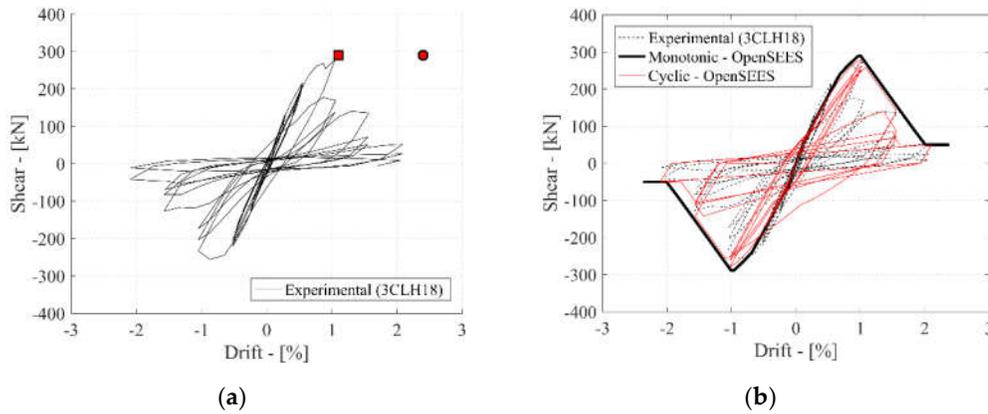
Using Equation (17) is possible to calculate the drift ratio and displacement at shear degradation that are  $(\Delta s/L)_{calc} = 0.024$  and  $\Delta s_{calc} = 71.4 \text{ mm}$ , respectively (circle mark in Figure 13a).

From the comparison between the experimental and calculate results (Figure 13b) is clear that the drift capacity model of expressed by Equation (17), in this case, gives a value much higher in term of drift ratio and displacement at shear failure than the one experienced experimentally.

Since the Limit Curve model is based on this empirical equation to define the shear limit surface theoretically it could not work correctly. Therefore, we decided to evaluate from the experimentation the values that should be used in the numerical analysis, in order to better approximate with OpenSEES the experimental curve. The values of the specimens failing in shear are reported in Table 2.



**Figure 12.** Specimen 2CLH18: (a) Experimental behaviour. (b) Comparison of numerical cyclic response with experimental results.



**Figure 13.** Specimen 3CLH18: (a) Experimental behaviour. The square and circle marks represent respectively the experimental (Table 2) and calculated (Equation (17)) initiation of shear degradation. (b) Comparison of numerical cyclic response with experimental results.

**Table 2.** Experimental values needed for the calibration of the shear spring (Figure 4).

Rectangular Section					
Reference	Specimen	$\Delta_s/L$ (---)	$K_{s,deg}$ (kN/mm)	$V_s$ (kN)	$V_{res}$ (kN)
Lynn A.C. (2001) [31]	3CLH18	0.0100	-7.5	277.0	50.0
	3SLH18	0.0077	-4.4	270.0	48.7
	2SLH18	0.0088	-6.2	231.6	—
	3CMH18	0.0100	-12.4	324.4	94.3
	3CMD12	0.0085	-4.1	355.8	—
Saatcioglu, Ozcebe [32]e	U1	0.044	-2.8	273.0	70.0
	U2	0.021	-6.0	280.0	90.0
	U3	0.044	-3.7	255.0	—
Hollow Rectangular Section					
Reference	Specimen	$\Delta_s/L$ (---)	$K_{s,deg}$ (kN/mm)	$V_s$ (kN)	$V_{res}$ (kN)
Calvi et al. [33]	T250	0.022	-8.9	217.2	47.9
	T500A	0.010	-6.3	209.0	—
	T500B	0.022	-7.8	228.0	—
	T750	0.020	—	257.9	—

**5. Conclusions**

This paper presents a finite element model for assessing the nonlinear behavior of RC bridge piers under combined axial, shear, and bending moment. The model explicitly takes into account the response caused by the shear capacity deterioration due to the interaction with flexural deformation. This important effect has been introduced through the incorporation of a zero-length shear spring in series with a flexural column element and a rotational slip spring.

A phenomenological curve for the shear response has been proposed and calibrated, realistically capturing the monotonic and cyclic response of columns, including the pinching, the stiffness softening, and the strength deterioration due to deformations and cyclic load reversals. A good agreement between the numerical prediction and experimental data can be observed.

**Author Contributions:** All authors substantially contributed to this work. A.R. and A.P. were the scientific principal investigators of the research, and were responsible of conceptualization of activities and the development of investigations. D.L. and G.F. makes substantial contributions to the investigation with particular

regard to the software. C.N. and B.B. supervised all the research and revised the results. All authors have read and agreed to the published version of the manuscript.

**Funding:** This research was funded by ReLUIIS/DPC within the framework of the 2014–2018 and of the 2019–2021 Research Projects.

**Acknowledgments:** The authors would like to thank the anonymous referees for their valuable comments and suggestions.

**Conflicts of Interest:** The authors declare no conflict of interest.

## References

1. Nuti, C.; Rasulo, A.; Vanzi, I. Seismic assessment of utility systems: Application to water, electric power and transportation networks. In Proceedings of the Safety, Reliability and Risk Analysis: Theory, Methods and Applications Proceedings of the Joint ESREL and SRA-Europe Conference, Valencia, Spain, 22–25 September 2008; Volume 3, pp. 2519–2529.
2. Nuti, C.; Rasulo, A.; Vanzi, I. Seismic safety of network structures and infrastructures. *Struct. Infrastruct. Eng.* **2010**, *6*, 95–110, doi:10.1080/15732470802663813.
3. Rasulo, A.; Testa, C.; Borzi, B. Seismic risk analysis at urban scale in Italy. *Lect. Notes Comput. Sci.* **2015**, *9157*, 403–414. DOI: 10.1007/978-3-319-21470-2\_29
4. Rasulo, A.; Fortuna, M.A.; Borzi, B. Seismic risk analysis at urban scale in Italy. *Lect. Notes Comput. Sci.* **2016**, *9788*, 198–213. DOI: 10.1007/978-3-319-42111-7\_16
5. Lavorato, D.; Pelle, A.; Fiorentino, G.; Nuti, C.; Rasulo, A. A nonlinear material model of corroded rebars for seismic response of bridges, COMPDYN 2019. In Proceedings of the 7th ECOMAS Thematic Conference on Computational Methods in Structural Dynamics and Earthquake Engineering, Crete Island, Greece, 24–26 June 2019.
6. Lavorato, D.; Fiorentino, G.; Pelle, A.; Rasulo, A.; Bergami, A.V.; Briseghella, B.; Nuti, C. A corrosion model for the interpretation of cyclic behavior of reinforced concrete sections. *Struct. Concr.* **2019**, doi:10.1002/suco.201900232.
7. Lynn, A.C.; Moehle, J.P.; Mahin, S.A.; Holmes, W.T. Seismic evaluation of existing reinforced concrete building columns. *Earthq. Spectra* **1996**, *12*, 715–739.
8. Priestley, M.J.N.; Seible, F.; Verma, R.; Xiao, Y. Seismic shear strength of reinforced concrete columns. In *Structural Systems Research Project Report No. SSRP 93/06*; University of California: San Diego, CA, USA, 1993.
9. Sezen, H.; Moehle, J.P. Shear strength model for lightly reinforced concrete columns. *J. Struct. Eng.* **2004**, *130*, 1692–1703.
10. Filippou, F.C.; D’Ambrisi, A.; Issa, A. Nonlinear static and dynamic analysis of reinforced concrete subassemblages. In *Earthquake Engineering Research Center Report No. UCB/EERC-92/08*; University of California: Berkeley, CA, USA, 1992.
11. Cassese, P.; De Risi, M.T.; Verderame, G.M. A degrading shear strength model for RC columns with hollow circular cross-section. *Int. J. Civ. Eng.* **2019**, *17*, 1241–1259.
12. Cassese, P.; De Risi, M.T.; Verderame, G.M. A modelling approach for existing shear-critical RC bridge piers with hollow rectangular cross section under lateral loads. *Bull. Earthq. Eng.* **2019**, *17*, 237–270.
13. Guedes, J.; Pinto, A.V. A numerical model for shear dominated bridge piers. In Proceedings of the Second Italy–Japan Workshop on Seismic Design and Retrofit of Bridges, Rome, Italy, 27–28 February, 1997.
14. Ranzo, G.; Petrangeli, M. A fibre finite beam element with section shear modelling for seismic analysis of RC structures. *J. Earthq. Eng.* **1998**, *2*, 443–473.
15. Petrangeli, M. Fiber element for cyclic bending and shear of RC structures. II: verification. *J. Eng. Mech.* **1999**, *125*, 1002–1009.
16. Marini, A.; Spacone, E. Analysis of reinforced concrete elements including shear effects. *ACI Struct. J.* **2006**, *103*, 645–655.
17. Ceresa, P.; Petrini, L.; Pinho, R.; Sousa, R. A fibre flexure-shear model for seismic analysis of RC-framed structures. *Earthq. Eng. Struct. Dyn.* **2009**, *38*, 565–586.
18. McKenna, F.; Fenves, G.L.; Scott, M.H.; Jeremic, B. *Open System for Earthquake Engineering Simulation (OpenSEES)*; University of California: Berkeley, CA, USA, 2000.

19. Menegotto, M.; Pinto, P.E. Method of analysis of cyclically loaded RC plane frames including changes in geometry and non-elastic behavior of elements under normal force and bending. *International Association for Bridge and Structural Engineering* **1973**, *11*, 15–22.
20. Popovics, S. A numerical approach to the complete stress-strain curve of concrete. *Cem. Concr. Res.* **1973**, *3*, 583–599.
21. Mander, J.B.; Priestley, M.J.; Park, R. Theoretical stress-strain model for confined concrete. *J. Struct. Eng.* **1988**, *114*, 1804–1826.
22. Eligehausen, R.; Bertero, V.V.; Popov, E.P. Local bond stress-slip relationships of deformed bars under generalized excitations: Tests and analytical model. In *Report No EERC.*; Earthquake Engineering Research Center, University of California: Berkeley, CA, USA, 1983; pp. 1–169.
23. Sezen, H.; Setzler, E.J. Reinforcement slip in reinforced concrete columns. *ACI Struct. J.* **2008**, *105*, 280.
24. CEB-FIB. *Model Code 2010-Final Draft*; The International Federation for Structural Concrete (FIB CEB-FIP): Lausanne, Switzerland, 2010.
25. Elwood, K.J. Shake Table Tests and Analytical Studies on the Gravity Load Collapse of Reinforced Concrete Frames. Level of Ph.D. Thesis, University of California, Berkeley, CA, USA, January 2002.
26. Elwood, K.J.; Eberhard, M.O. Effective Stiffness of Reinforced Concrete Columns. In Research Digest No 2006-1. *ACI Structural Journal* **2009**, *106*, 476–484.
27. Park, R.; Paulay, T. *Reinforced Concrete Structures*; John Wiley & Sons: Hoboken, NJ, USA, 1975.
28. Biskinis, D.E.; Roupakias, G.K.; Fardis, M.N. Degradation of Shear Strength of Reinforced Concrete Members with Inelastic Cyclic Displacements. *ACI Struct. J.* **2004**, *101*, 773–783.
29. Elwood, K.J.; Moehle, J.P. Drift Capacity of Reinforced Concrete Columns with Light Transverse Reinforcement. *Earthq. Spectra* **2005**, *21*, 71–89.
30. Kowalsky, M.J.; Priestley, M.J.N. Improved Analytical Model for Shear Strength of Circular Reinforced Concrete Columns in Seismic Regions. *ACI Struct. J.* **2000**, *97*, 388–396.
31. Lynn, A. Seismic Evaluation of Existing Reinforced Concrete Building Column. Ph.D. Thesis, University of California at Berkeley, Berkeley, CA, USA, 2001.
32. Saatcioglu, M.; Ozcebe, G. Response of reinforced concrete columns to simulated seismic loading. *Struct. J.* **1989**, *86*, 3–12.
33. Calvi, G.M.; Pavese, A.; Rasulo, A.; Bolognini, D. Experimental and numerical studies on the seismic response of R.C. hollow bridge piers. *Bull. Earthq. Eng.* **2005**, *3*, 267–297.



© 2020 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (<http://creativecommons.org/licenses/by/4.0/>).