Methods for Determining Mold Development and Condensation on the Surface of Building Barriers

Aleksander Starakiewicz, Przemysław Miąsik, Joanna Krasoń and Lech Lichołai *

Department of Building Engineering, Rzeszów University of Technology, ul. Poznańska 2, 35-959 Rzeszów, Poland; olekstar@prz.edu.pl (A.S.); pmiasik@prz.edu.pl (P.M.); jkras@prz.edu.pl (J.K.)

* Correspondence: Lech.Lichołai@prz.edu.pl; Tel.: +48-17-8651327

Received: 6 December 2019; Accepted: 25 December 2019; Published: 30 December 2019

Abstract: The article presents four equivalent methods for checking mold growth on the surface of building barriers and checking water vapor condensation on their surface. Each method applies to two parallel phenomena that may occur on a building barrier. The first method is to calculate and compare temperature factors. In the second method, the characteristic humidity in the room is calculated and compared. The third method is to calculate and compare the characteristic temperatures in the room. The fourth method is based on the calculation and comparison of characteristic water vapor pressures. Three boundary conditions are presented for each method and phenomenon: when a given phenomenon can occur, when it begins or ends, and when it does not occur. The presented methods systematize the approach to the problem of mold development and surface condensation. The presented calculation results relate to the selected building barrier functioning in specific indoor and outdoor climate conditions. The calculation results confirm the compliance of the presented methods in identifying the phenomenon of mold growth or condensation on the surface of the barrier. A graphical interpretation of the results for each method with periods of occurrence or absence of a given phenomenon is also presented.

Keywords: mold development; surface condensation; building barriers; calculation methods

1. Introduction

The development of mold and/or condensation on the surface of building barriers are physical phenomena that occur in various types of buildings, mainly on their internal surfaces. These phenomena are harmful to the functioning of building barriers, but also to residents or users due to mold fungi growing on their surface [1]. They cause the formation of disease entities such as allergies and allergic reactions in humans and animals, and the occurrence of a specific smell.

These phenomena occurred very sporadically in the past; nowadays they are quite common in buildings for various reasons [2–4]. In the current period, when buildings with a higher number of sealed off areas and thermal insulation of external barriers are erected (more comfortable barriers due to the higher temperature of their internal surfaces), these phenomena appear more often and are even more disturbing [5].

The reasons for these phenomena have been described in the article on alternative methods of determining mold risk [5]. These include: external climate [6], construction [7], geometry, technology, and quality of the barrier [8,9], and the internal microclimate [10,11]. In addition, the way the rooms are used, the arrangement of the furniture and their installation can affect surface condensation and mold growth on the interior surfaces of the walls. In the article [12] an analysis of thermal conditions occurring around built-in furniture in living rooms was carried out. The analysis covered both the summer and winter periods, because during these periods there was a phenomenon of condensation and mold on the internal surfaces of the walls from the construction side. The results confirm that the...
Impact of mold on the internal surface of the walls is influenced by the way the residents use the rooms, as well as the lack of adequate ventilation between the wall surface and furniture. Increasing the temperature of the inner wall surface above 16 °C would reduce the risk of condensation on this surface [12]. In general terms, it comes down to the relationship that occurs between the parameters of the internal microclimate affecting the barrier and temperatures on the surface of the barrier. If mold growth occurs on the barrier surface and the standard parameters of the internal microclimate are maintained, the reason for this phenomenon is usually on the side of the building barrier. The opposite situation may occur when the barrier has standard parameter. The reason then is usually on the side of the internal microclimate. It is often difficult to indicate one cause, as the occurrence of mold growth can be caused by both the building barrier and the internal microclimate. In any case of mold, corrective actions must be taken to eliminate the cause. When the problem of condensation appears in the barrier, various solutions should be applied to repair or modify the structure of the barrier [8,13], at the same time stabilizing the temperature of the internal surface of the barrier, and additives may be applied to modify this barrier [14,15]. Such solutions will also improve the indoor climate, reducing room temperature fluctuations.

Over the past decades, the approach to the design of building barriers has changed in terms of avoiding surface condensation. The standard requirements are also changing, which, due to the need to reduce CO₂ emissions to the atmosphere, require newly designed buildings to be more airtight and have better thermal insulation. At the same time, there are still older facilities that do not meet the requirements for new facilities. That is why (with a similar method of use) older buildings function differently due to the lower insulation of external barriers and windows which are not well sealed, as opposed to new buildings with high insulation of external barriers and very well-sealed windows.

In older buildings, a frequent cause of condensation was the thermal bridges at the junctions of the external walls with the horizontal structural elements of the building [16,17].

Currently, the problem is among others, the risk of condensation forming on the outer surface of the window. The authors in article [18] linked the increase in condensation on the external surface to the increase in the insulation of these windows and climate change. To reduce the formation of condensation, additional shading elements on the windows directed towards the sky have been proposed, which would limit the condensation of water vapor on the external surface of the glazing in the morning. In the article [19], the authors attempted to determine the rate of surface condensation on cold glazed surfaces of building elements. The tests were carried out in a full-sized test chamber, using imaging techniques to analyze the appearance and increase of surface condensation on glazed surfaces.

The type of window frame used has an additional effect on the formation of condensation and mold. Appropriate use of profile types will reduce the risk of the above problem. In the article [20], the authors, using computer simulations, compared different types of window frames to assess the risk of surface condensation on the example of double-sliding double-glazed windows.

The thermoplastic spacer with its size optimization and the insulation cover inserted into the window frame and window frame size were evaluated. The biggest impact on reducing the risk of condensation is the introduction of a spacer with a smaller area with an enlarged air gap between the panes and an increase in the size of the window frame. Both of these elements favorably increase the temperature in the areas where the glazing joins the frame.

The problem of mold growth and surface condensation appears periodically, often in buildings after retrofitting of external barriers. This condition is worrying because these phenomena, instead of disappearing completely, actually get worse in some cases. The task to be considered is the adoption of such a method of checking the functioning of the heat and humidity processes of the barrier as to allow a reliable assessment of the possibility of surface condensation and mold growth on the surface of the building component under certain climatic conditions and of the internal microclimate.

To analyze the above problem, various methods can now be used, such as computational [18], experimental [8,19], and computer simulations [21–23].
Currently, according to PN-EN ISO 13788 [24], to check the development of mold on the surface of a building barrier, one method is defined and acceptable, while there are no other alternative methods in this area. The method given in the standard [24] boils down to a comparison of two temperature factors: the temperature factor \( f_{Rsi} \) resulting from the insulation of the barrier (its construction), and the factor \( f_{Rsi,max} \) resulting from the humidity conditions prevailing in the room in the so-called critical month. In order to meet the design condition (to eliminate the risk of mold growth), the minimum thermal insulation of the barrier \( R_{T,min} \) or the maximum value of the heat transfer coefficient \( U_{max} \) need to be calculated. In practice, this involves the need to modernize the barrier, which in turn leads to the generation of costs for the task.

Considering the above, an attempt was made to compare different conditions for mold development and surface condensation and to define when a given phenomenon occurs, when it starts and when it does not occur. Then, for each condition of the occurrence of the relevant phenomenon, what is to be done to eliminate it is given, and calculation algorithms for how to implement it are given. Presented, among others, is the applicable standard condition related to the \( f_{Rsi} \) parameter, the calculation of internal humidity \( \varphi_i \), humidity of the beginning of condensation \( \varphi_i,con \), the permissible humidity in the room \( \varphi_i,max \), with observance of the standard condition to avoid mold growth, the external temperature eliminating condensation \( \Theta_{e,con} \), and the minimum thermal insulation of the barrier eliminating condensation \( U_{con} \).

2. Materials and Methods

2.1. Methods for Preventing Mold Growth on Building Barriers

Determining the phenomenon of mold development on a building barrier will be presented for four different methods:

- the first method (M1) involves the procedure for determining the temperature factors \( f_{Rsi} \) and \( f_{Rsi,max} \);
- the second method (M2) consists of comparing the relative humidity of air \( \varphi_i,max \) and \( \varphi_i \);
- the third method (M3) uses the comparison of barrier temperatures \( \Theta_{si} \) and \( \Theta_{si,min} \);
- the fourth method (M4) consists of comparing the air vapor pressures \( p_{i,max} \) and \( p_i \).

For each of the methods, a design condition was formulated to avoid mold growth on the building barrier.

2.1.1. M1—Avoiding Mold Growth on the Basis of Determining the Minimum Allowable Temperature Factor \( f_{Rsi,min} \): Procedure According to PN-EN ISO 13788 [24]

According to this method, in order to avoid mold growth, the relative humidity of the surface should not exceed 0.8 of the actual water vapor pressure in the room for several days [24]. When calculating the risk of mold growth using the standard method, monthly average values (temperature, humidity, etc.) should be used.

For each month of the year:

1. Define the average monthly value of the outside air temperature \( \Theta_e \).
2. Define the outside air humidity: the average monthly water vapor pressure can be calculated using the equations:

\[
p_e = \varphi_e \cdot p_{sat} \left( \Theta_e \right)
\]

\( p_e \)—average monthly water vapor pressure;
\( \varphi_e \)—average monthly relative humidity of air;
\( p_{sat} \)—pressure of water vapor at saturation;
\( \Theta_e \)—average monthly value of the outside air temperature
3. Determine the indoor air temperature $\Theta_i$ (according to the purpose of the room according to national standards)

4. Calculate the partial pressure of water vapor in the room $p_i$ on the basis of $\Delta p$ or take the relative humidity in the air-conditioned room as constant, taking into account the correction for the safety margin:

   Based on the internal humidity class (from 1 to 5):

   $$p_{i,ISO} = p_e + \Delta p \cdot 1.1$$

   $\Delta p$-excess internal water vapor pressure (according to Annex A [24])

   Based on relative humidity in the room ($\varphi_i$):

   $$p_{i,ISO} = (\varphi_i + 0.05) \cdot p_{sat}(\Theta_i)$$

   $\varphi_i$-assumed average monthly value of relative humidity of the indoor air

5. Calculate the minimum permissible pressure of saturated water vapor on the barrier surface $p_{sat}(\Theta_{si})$ (corresponding to the surface temperature, $\Theta_{si}$). The maximum permissible relative humidity on the surface is assumed $\varphi_{si} = 0.8$:

   $$p_{sat}(\Theta_{si}) = \frac{p_{i,ISO}}{0.8}$$

6. Determination of the minimum permissible barrier surface temperature $\Theta_{si,min}$ (based on $p_{sat}(\Theta_{si})$):

   $$p_{sat}(\Theta_{si}) \rightarrow \text{ISO}[24] - \text{AnnexE} \rightarrow \Theta_{si,min}$$

7. Calculation of the minimum allowable temperature factor $f_{Rsi,min}$:

   $$f_{Rsi,min} = \frac{\Theta_{si,min} - \Theta_e}{\Theta_i - \Theta_e}$$

8. Determination of the critical month and $f_{Rsi,max}$ ($f_{Rsi,max}$ is the highest value of $f_{Rsi,min}$ from 12 months).

9. Design condition:

   $$f_{Rsi} > f_{Rsi,max}$$

   $$f_{Rsi} = \frac{U^{-1} - R_{si}}{U^{-1}} = \frac{1}{U} - R_{si} = \frac{R_T - R_{si}}{R_T}$$

   $R_T$—thermal resistance of barrier;

   $R_{si}$—heat transfer resistance on the internal surface.

10. If the design condition is not met, we calculate the minimum thermal insulation of the barrier $R_{T,min}$, or maximum value of the heat transfer coefficient $U_{max}$:

    $$f_{Rsi,max} = \frac{R_{T,min} - R_{si}}{R_{T,min}} \rightarrow R_{T,min} = \frac{R_{si}}{1 - f_{Rsi,max}}$$

    $$f_{Rsi,max} = \frac{1}{U_{max}} - R_{si} \rightarrow U_{max} = \frac{1 - f_{Rsi,max}}{R_{si}}$$

   Based on the design condition, it is possible to determine the difference between temperature factors in the following months of the year: $\Delta f_R = f_{Rsi} - f_{Rsi,min}$. A positive value ($\Delta f_R > 0$) means no risk
of mold growth but also shows a reserve of safe barrier function. However, a negative value ($\Delta f_R < 0$) means a threat of mold growth and shows the depth of this phenomenon in the critical month and other months.

2.1.2. M2—Avoiding Mold Growth on the Basis of Determining the Permissible Humidity in the Room $\varphi_{i,max}$

If there is a risk of mold growth, it is also important to answer the question: “what is the permissible humidity in the room $\varphi_{i,max}$, so that there is no mold growth on the wall surface and that the standard condition is observed”. According to the standard procedure, if the design condition is not met, the minimum thermal insulation of the barrier or the maximum value of the heat transfer coefficient (Equations (8) and (9)) needs to be calculated. This is a one-way procedure because it gives the user no alternative. It boils down to increasing the thermal insulation of the barrier, that is, carrying out retrofitting. This means that mold development will be eliminated only after these construction works have been carried out. This treatment requires time, an appropriate period of the year to carry it out, permission to perform (historic buildings) and considerable funding. However, the user expects to eliminate this phenomenon as soon as possible, recommendations for use and financial estimates. The following method gives this possibility.

Consider the situation when condensation begins (or ends) on the wall surface, it is possible to write it with the following equation:

$$\Theta_{con} = \Theta_{si} = \Theta_{dp,con}$$

(10)

This means that when the condensation start (end) temperature $\Theta_{con}$ occurs, the surface temperature of barrier $\Theta_{si}$ and the air dew point temperature $\Theta_{dp,con}$ are equal. Of these three quantities, the easiest way is to determine the surface temperature of barrier $\Theta_{si}$. It is calculated using the temperature factor $f_{Rsi}$ or the heat transfer coefficient $U$. The temperature factor of the barrier $f_{Rsi}$ is given by the formula:

$$f_{Rsi} = \frac{\Theta_{si} - \Theta_e}{\Theta_i - \Theta_e}$$

(11)

By transforming Equation (11) and taking into account Equation (10), it is possible to determine the temperature of the barrier surface at which the condensation process begins:

$$\Theta_{si} = f_{Rsi} (\Theta_i - \Theta_e) + \Theta_e = \Theta_{con} = \Theta_{dp,con}$$

(12)

Using the heat transfer coefficient $U$, you can calculate the surface temperature of the barrier at which the condensation process begins using the equation:

$$\Theta_{si} = \Theta_i - U(\Theta_i - \Theta_e) - f_{Rsi} = \Theta_{con} = \Theta_{dp,con}$$

(13)

Based on the calculated septum temperature $\Theta_{si}$, we determine the condensation pressure $p_{i,con}$ (equal to the saturated water vapor pressure related to the septum surface temperature) [2]:

$$\Theta_{si} \rightarrow (\text{ISO}[24]) \rightarrow p_{i,con} = p_{sat}(\Theta_{si})$$

(14)

To prevent mold growth, the permissible water vapor pressure in the room, $p_{i,ISO}$ can be 80% of the pressure specified in the formula (14):

$$p_{i,ISO} = 0.8 \cdot p_{i,con}$$

(15)

The moisture reserve assumed by ISO [24] due to the heterogeneity of humidity in the room is: 5% relative humidity $\varphi_i$ or 10% moisture increase $\Delta p$. The permissible relative humidity of the air in
the room $\varphi_{i,\text{max}}$ for a case of 5% moisture, we will determine from the relationship analogous to that in Equation (3):

$$p_{i,\text{ISO}} = (\varphi_{i,\text{max}} + 0.05) \cdot p_{\text{sat}}(\Theta_i)$$  \hfill (16)

Because we know how to calculate $p_{i,\text{ISO}}$, comparing Equations (15) and (16) we get:

$$0.8p_{i,\text{con}} = (\varphi_{i,\text{max}} + 0.05) \cdot p_{\text{sat}}(\Theta_i)$$  \hfill (17)

After transforming Equation (17) we get:

$$\varphi_{i,\text{max}} = \frac{0.8p_{i,\text{con}}}{p_{\text{sat}}(\Theta_i)} - 0.05$$  \hfill (18)

However, the permissible relative humidity of the air in the room $\varphi_{i,\text{max}}$, for a case of 10% moisture increase, we determine from the equation:

$$\varphi_{i,\text{max}} = p_{i,\text{max}} \cdot p_{\text{sat}}(\Theta_i) = p_e + \Delta p_{\text{max}}$$  \hfill (19)

In order for mold not to develop, the permissible increase in humidity in the room $\Delta p_{\text{max}}$, we determine as in Equation (2):

$$p_{i,\text{ISO}} = (p_e + 1.1 \cdot \Delta p_{\text{max}})$$  \hfill (20)

substituting Equation (15) for $p_{i,\text{ISO}}$, we get:

$$0.8p_{i,\text{con}} = (p_e + 1.1 \cdot \Delta p_{\text{max}})$$  \hfill (21)

after conversion:

$$\Delta p_{\text{max}} = \frac{0.8p_{i,\text{con}} - p_e}{1.1}$$  \hfill (22)

The final formula for the permissible humidity in the room $\varphi_{i,\text{max}}$ is obtained after inserting $\Delta p_{\text{max}}$ (Equation (22)) in Equation (19):

$$\varphi_{i,\text{max}} = \frac{p_e + \Delta p_{\text{max}}}{p_{\text{sat}}(\Theta_i)} = \frac{0.8p_{i,\text{con}} + 0.1p_e}{1.1p_{\text{sat}}(\Theta_i)}$$  \hfill (23)

Based on the air parameters used in the calculations, it is possible to determine the actual water vapor pressure in the following months:

$$p_i = p_e + \Delta p$$  \hfill (24)

The relative humidity of the air in the room in the following months will be calculated:

$$\varphi_i = \frac{p_i}{p_{\text{sat}}(\Theta_i)}$$  \hfill (25)

Using the relative humidity of the air, the design condition to avoid mold would be:

$$\varphi_{i,\text{max}} > \varphi_i$$  \hfill (26)

Based on this design condition, it is possible to determine the difference between relative humidity of air in the following months of the year:

$$\Delta \varphi(m) = \varphi_{i,\text{max}}(m) - \varphi_i(m)$$  \hfill (27)

$m$-month considered.
A positive value ($\Delta \phi (m) > 0$) means no risk of mold growth (meeting the design condition) and informs about the value of safe relative humidity in the room. The negative value ($\Delta \phi (m) < 0$), on the other hand, means that there is a risk of mold growth and informs about what value the maximum humidity has exceeded. If there is a risk of mold growth, we have information not only about the critical month but also about other months in which this threat occurs.

2.1.3. M3—Avoiding Mold Growth on the Basis of Characteristic Temperatures

Another physical quantity that it is possible to use when checking the condition to avoid mold growth on the surface of the barrier is temperature. Based on the knowledge of the barrier surface temperature $\Theta_{si}$ and the minimum permissible barrier surface temperature $\Theta_{si,min}$, it is possible to formulate a design condition to avoid mold growth:

$$\Theta_{si} > \Theta_{si,min}$$  \hfill (28)

The barrier surface temperature ($\Theta_{si}$) is calculated from Equation (13):

$$\Theta_{si} = \Theta_i - U \cdot (\Theta_i - \Theta_e) \cdot R_{si}$$  \hfill (29)

The minimum allowable barrier surface temperature $\Theta_{si,min}$ will be determined on the basis of the standard procedure given in points 1–6 (Equations (1)–(4b)). If the design condition is not met, we calculate the maximum value of the heat transfer coefficient $U_{max}$. This factor is derived from the minimum surface temperature of the barrier and results from the conversion of the modified Equation (29):

$$\Theta_{si,min} = \Theta_i - U_{max} \cdot (\Theta_i - \Theta_e) \cdot R_{si}$$  \hfill (30)

$$U_{max} = \frac{\Theta_i - \Theta_{si,min}}{(\Theta_i - \Theta_e) \cdot R_{si}}$$  \hfill (31)

Based on this design condition, it is possible to determine the difference between temperatures on the barrier surface in the following months of the year:

$$\Delta \Theta_i(m) = \Theta_{si}(m) - \Theta_{si,min}(m)$$  \hfill (32)

A positive value ($\Delta \Theta_i(m) > 0$) means no risk of mold growth (meeting the design condition) and informs about the value of a safe surface temperature reserve. However, a negative value ($\Delta \Theta_i(m) < 0$) means a threat of mold growth and informs how many degrees the temperature of the barrier is lower in the critical month and in other months in which this threat occurs.

From the point of view of the operation of the building, it is important to note the value of the outside air temperature $\Theta_{e,min}$ at which mold growth will begin on the barrier surface. To determine it, Equation (29) needs to be modified and then converted.

$$\Theta_{si,min} = \Theta_i - U \cdot (\Theta_i - \Theta_{e,min}) \cdot R_{si}$$  \hfill (33)

$$\Theta_{e,min} = \Theta_i - \frac{\Theta_i - \Theta_{si,min}}{U \cdot R_{si}}$$  \hfill (34)

The value of this temperature is important for the user because it informs when there may be a risk of mold growth on the surface of the barrier. Knowing the course of temperatures in winter, it is possible to estimate the approximate time or period of occurrence of this phenomenon.

2.1.4. M4—Avoiding Mold Growth on the Basis of Determining the Characteristic Water Vapor Pressure

Another physical quantity that is possible to use when checking the condition to avoid mold growth on the surface of the barrier is the water vapor pressure. Based on the knowledge of the actual
water vapor pressure $p_i$ and the maximum allowable water vapor pressure $p_{i,\text{max}}$, it is possible to formulate a design condition to avoid mold growth:

$$p_{i,\text{max}} > p_i$$  \hspace{1cm} (35)

The maximum allowable vapor pressure $p_{i,\text{max}}$ is calculated from the equation below, in which the maximum moisture increase $\Delta p_{\text{max}}$ was determined in Equation (22):

$$p_{i,\text{max}} = p_e + \Delta p_{\text{max}} = \frac{0.8p_{i,\text{con}} + 0.1p_e}{1.1}$$  \hspace{1cm} (36a)

If the relative humidity of the room air is determined $\varphi_i$ then the maximum permissible vapor pressure $p_{i,\text{max}}$ is calculated from the equation:

$$p_{i,\text{max}} = 0.8p_{i,\text{con}} - 0.05p_{\text{sat}}(\Theta_i)$$  \hspace{1cm} (36b)

However, the actual water vapor pressure $p_i$ will be determined from Equation (24).

Tables 1 and 2 for various physical quantities summarize the conditions that must be met for mold growth, its absence or the beginning (end) to occur on the building barrier.

**Table 1. Conditions for mold growth on the surface of a building barrier.**

<table>
<thead>
<tr>
<th>No.</th>
<th>Mold Growth</th>
<th>Beginning (End) of Mold Growth</th>
<th>Design Condition (No Mold Development)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>$f_{R,Rsi} &lt; f_{R,Rsi,\text{min}}$</td>
<td>$f_{R,Rsi} = f_{R,Rsi,\text{min}}$</td>
<td>$f_{R,Rsi} &gt; f_{R,Rsi,\text{min}}$</td>
</tr>
<tr>
<td>2.</td>
<td>$\varphi_{i,\text{max}} &lt; \varphi_i$</td>
<td>$\varphi_{i,\text{max}} = \varphi_i$</td>
<td>$\varphi_{i,\text{max}} &gt; \varphi_i$</td>
</tr>
<tr>
<td>3.</td>
<td>$\Theta_{si} &lt; \Theta_{si,\text{min}}$</td>
<td>$\Theta_{si} = \Theta_{si,\text{min}}$</td>
<td>$\Theta_{si} &gt; \Theta_{si,\text{min}}$</td>
</tr>
<tr>
<td>4.</td>
<td>$p_{i,\text{max}} &lt; p_i$</td>
<td>$p_{i,\text{max}} = p_i$</td>
<td>$p_{i,\text{max}} &gt; p_i$</td>
</tr>
</tbody>
</table>

**Table 2. Conditions for mold growth on the surface of a building barrier in the form of a parameter difference ($\Delta$).**

<table>
<thead>
<tr>
<th>No.</th>
<th>Mold Growth</th>
<th>Beginning (End) of Mold Growth</th>
<th>Design Condition (No Mold Development)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>$\Delta f_R = (f_{R,i} - f_{R,Rsi,\text{min}}) &lt; 0$</td>
<td>$\Delta f_R = 0$</td>
<td>$\Delta f_R = (f_{R,i} - f_{R,Rsi,\text{min}}) &gt; 0$</td>
</tr>
<tr>
<td>2.</td>
<td>$\Delta \varphi = (\varphi_{i,\text{max}} - \varphi_i) &lt; 0$</td>
<td>$\Delta \varphi = 0$</td>
<td>$\Delta \varphi = (\varphi_{i,\text{max}} - \varphi_i) &gt; 0$</td>
</tr>
<tr>
<td>3.</td>
<td>$\Delta \Theta = (\Theta_{si} - \Theta_{si,\text{min}}) &lt; 0$</td>
<td>$\Delta \Theta = 0$</td>
<td>$\Delta \Theta = (\Theta_{si} - \Theta_{si,\text{min}}) &gt; 0$</td>
</tr>
<tr>
<td>4.</td>
<td>$\Delta p = (p_{i,\text{max}} - p_i) &lt; 0$</td>
<td>$\Delta p = 0$</td>
<td>$\Delta p = (p_{i,\text{max}} - p_i) &gt; 0$</td>
</tr>
</tbody>
</table>

2.2. Methods for Checking the Presence of Water Vapor Condensation on Building Barriers

The determination of the phenomenon of water vapor condensation on a building barrier will be presented for four different methods.

- method 1 (M1$_{\text{con}}$) based on a comparison of temperature factors $f_{R,i}$ and $f_{R,dp}$;
- method 2 (M2$_{\text{con}}$) based on comparison of relative humidity $\varphi_{i,\text{con}}$ and $\varphi_i$;
- method 3 (M3$_{\text{con}}$) involving the comparison of the barrier temperature $\Theta_{si}$ and the air dew point temperature $\Theta_{dp}$ and
- method 4 (M4$_{\text{con}}$) based on comparing the water vapor pressure of $p_{i,\text{con}}$ and $p_i$.

A design condition has been formulated for each method to avoid condensation on the building barrier.
2.2.1. M1\textsubscript{con}—Avoiding Condensation on the Basis of Determining the Air Dew Point Temperature Factor $f_{Rdp}$

The procedure for checking the condensation of water vapor on a building barrier is based on a comparison of two temperature factors. The temperature factor $f_{Rsi}$ resulting from the insulation (construction) of the barrier and the factor $f_{Rdp}$ resulting from humidity conditions in the room. To avoid condensation, the air dew point temperature should not exceed the room surface temperature. On this basis, it is possible to formulate a design condition to avoid surface condensation:

$$f_{Rsi} > f_{Rdp} \quad (37)$$

The temperature factor $f_{Rsi}$ can be determined on the basis of the known value of the heat transfer coefficient (U) according to formula (7) or the known value of the barrier surface temperature $\Theta_{si}$ according to formula (11). The barrier surface temperature is calculated according to formula (13). The temperature factor $f_{Rdp}$ is calculated on the basis of the dew point temperature $\Theta_{dp}$ according to the formula:

$$f_{Rdp} = \frac{\Theta_{dp} - \Theta_e}{\Theta_i - \Theta_e} \quad (38)$$

The dew point of the air in the room $\Theta_{dp}$ is determined on the basis of the actual water vapor pressure in the room $p_i$:

$$p_i = p_{sat}(\Theta_{dp}) \rightarrow (ISO[24] - Annex E) \rightarrow \Theta_{dp} \quad (39)$$

The actual water vapor pressure in room $p_i$ shall be determined on the basis of pressure increase $\Delta p$ according to formula (24) or on the basis of relative humidity in room $\phi_i$ according to the following formula:

$$p_i = \phi_i \cdot p_{sat}(\Theta_i) \quad (40)$$

2.2.2. M2\textsubscript{con}—Avoiding Condensation on the Basis of Determining Condensation Humidity $\phi_{i,con}$

To avoid condensation on the surface of the barrier, condensation humidity $\phi_{i,con}$ understood as relative humidity of the surface should not exceed the actual pressure of the water vapor in the room. The design condition to avoid surface condensation can be formulated as follows:

$$\phi_{i,con} > \phi_i \quad (41)$$

The humidity of the condensation in the room in the following months will be calculated from the formula:

$$\phi_{i,con} = \frac{p_{i,con}}{p_{sat}(\Theta_i)} \quad (42)$$

The condensation pressure will be determined according to the formula (29), the surface temperature of the barrier $\Theta_{si}$:

$$\Theta_{si} \rightarrow (ISO[24] - Annex E) \rightarrow p_{sat}(\Theta_{dp}) = p_{i,con} \quad (43)$$

The relative humidity of the air in the room in the following months will be calculated according to the formula (25). The actual water vapor pressure in room $p_i$ in this formula is determined on the basis of the pressure increase $\Delta p$ according to formula (24) or on the basis of relative humidity in the room $\phi_i$ according to formula (40).
2.2.3. M3\textsubscript{con}—Avoiding Condensation on the Basis of Characteristic Temperatures

Based on the knowledge of the barrier surface temperature $\Theta_{si}$ and the air dew point temperature in the room $\Theta_{dp}$, it is possible to formulate a design condition to avoid surface condensation:

$$\Theta_{si} > \Theta_{dp}$$ (44)

The barrier surface temperature $\Theta_{si}$ in the following months will be calculated from Equation (29). However, the air dew point temperature in the room $\Theta_{dp}$ in subsequent months will be determined according to the relationship (39) on the basis of the actual water vapor pressure in the room $p_i$ determined according to formulas (24 or 40). Based on this design condition, it is possible to determine the difference between the temperature at the barrier surface and the air dew point temperature in the following months of the year:

$$\Delta\Theta(m) = \Theta_{si}(m) - \Theta_{dp}(m)$$ (45)

A positive value of $\Delta\Theta(m) > 0$ means no surface condensation (meeting the design condition) and informs about the value of the safe surface temperature reserve. However, a negative value of $\Delta\Theta(m) < 0$ means surface condensation and informs how many degrees the barrier temperature is lower in the months in which this threat occurs.

2.2.4. M4\textsubscript{con}—Avoiding Condensation on the Basis of Determining the Characteristic Water Vapor Pressure

Based on the knowledge of the actual water vapor pressure $p_i$ and the water vapor condensation pressure on the surface of the barrier $p_{i,con}$, it is possible to formulate a design condition to avoid condensation:

$$p_{i,con} > p_i$$ (46)

The water vapor condensation pressure on the barrier surface $p_{i,con}$ in the following months will be calculated from Equation (43) on the basis of the barrier surface temperature $\Theta_{si}$ calculated according to formula (29). However, the actual water vapor pressure in the room ($p_i$) in the following months will be determined according to the formula (24 or 40). Based on this design condition, it is possible to determine the difference between the water vapor condensation pressure on the barrier surface and the air vapor pressure in the following months of the year:

$$\Delta p(m) = p_{i,con}(m) - p_i(m)$$ (47)

A positive value ($\Delta p(m) > 0$) means no surface condensation (fulfillment of the design condition) and indicates the value of a safe pressure reserve. The negative value ($\Delta p(m) < 0$), on the other hand, means surface condensation and informs about the value of exceeded pressure.

In Tables 3 and 4 different physical quantities summarize the conditions that must be met in order for the phenomenon of surface condensation on a building barrier: to occur, to have its beginning (end) or not occurring (lack of condensation).

<table>
<thead>
<tr>
<th>No.</th>
<th>A Condition of Occurrence of Condensation</th>
<th>Beginning (End) of Condensation</th>
<th>Design Condition (No Condensation)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>$f_{RSi} &lt; f_{RDp}$</td>
<td>$f_{RSi} = f_{RDp}$</td>
<td>$f_{RSi} &gt; f_{RDp}$</td>
</tr>
<tr>
<td>2.</td>
<td>$p_{i,con} &lt; p_i$</td>
<td>$p_{i,con} = p_i$</td>
<td>$p_{i,con} &gt; p_i$</td>
</tr>
<tr>
<td>3.</td>
<td>$\Theta_{si} &lt; \Theta_{dp}$</td>
<td>$\Theta_{si} = \Theta_{dp}$</td>
<td>$\Theta_{si} &gt; \Theta_{dp}$</td>
</tr>
<tr>
<td>4.</td>
<td>$p_{i,con} &lt; p_i$</td>
<td>$p_{i,con} = p_i$</td>
<td>$p_{i,con} &gt; p_i$</td>
</tr>
</tbody>
</table>

Table 3. Conditions for the occurrence of surface condensation on a building barrier.
Table 4. Conditions for the occurrence of surface condensation on a building barrier in the form of a difference of parameters ($\Delta$).

<table>
<thead>
<tr>
<th>No.</th>
<th>A Condition of Occurrence of Condensation</th>
<th>Beginning (End) of Condensation</th>
<th>Design Condition (No Condensation)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>$\Delta f_{R\text{con}} = (f_{R\text{si}} - f_{R\text{dp}}) &lt; 0$</td>
<td>$\Delta f_{R\text{con}} = 0$</td>
<td>$\Delta f_{R\text{con}} = (f_{R\text{si}} - f_{R\text{dp}}) &gt; 0$</td>
</tr>
<tr>
<td>2.</td>
<td>$\Delta \phi_{\text{con}} = (\phi_{i,\text{con}} - \phi_i) &lt; 0$</td>
<td>$\Delta \phi_{\text{con}} = 0$</td>
<td>$\Delta \phi_{\text{con}} = (\phi_{i,\text{con}} - \phi_i) &gt; 0$</td>
</tr>
<tr>
<td>3.</td>
<td>$\Delta \Theta_{\text{con}} = (\Theta_{si} - \Theta_{dp}) &lt; 0$</td>
<td>$\Delta \Theta_{\text{con}} = 0$</td>
<td>$\Delta \Theta_{\text{con}} = (\Theta_{si} - \Theta_{dp}) &gt; 0$</td>
</tr>
<tr>
<td>4.</td>
<td>$\Delta p_{\text{con}} = (p_{i,\text{con}} - p_i) &lt; 0$</td>
<td>$\Delta p_{\text{con}} = 0$</td>
<td>$\Delta p_{\text{con}} = (p_{i,\text{con}} - p_i) &gt; 0$</td>
</tr>
</tbody>
</table>

3. Results and Discussion

For the verification of the presented calculation methods for mold development and surface condensation, the following data was adopted: outdoor air temperature, $\Theta_e$, and relative humidity of the outdoor air $\phi_e$, according to the Rzeszów-Jasionka meteorological station [25], indoor air temperature $\Theta_i = 20^\circ\text{C}$, moisture increase in a room for the 4th class of internal humidity $\Delta p = 10.8$ hPa [24], external wall (50 cm thick made of solid brick) with a heat transfer coefficient $U = 1.20$ W/(m$^2$K); heat transfer resistance on the internal surface of the barrier $R_{si} = 0.25$ (m$^2$K)/W [24]. Data for calculations are presented in Table 5.

Table 5. Parameters of external and internal climate and building barrier.

<table>
<thead>
<tr>
<th>Month</th>
<th>$\Theta_e$ $^\circ\text{C}$</th>
<th>$p_{\text{sat,e}}$ hPa</th>
<th>$\phi_e$ %</th>
<th>$p_e$ hPa</th>
<th>$\Delta p$ hPa</th>
<th>$\Theta_i$ $^\circ\text{C}$</th>
<th>$p_{\text{sat,i}}$ hPa</th>
<th>$U$ W/(m$^2$K)</th>
<th>$R_{si}$ m$^2$K/W</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>–4.57</td>
<td>4.16</td>
<td>83.0</td>
<td>3.45</td>
<td>10.80</td>
<td>20</td>
<td>23.35</td>
<td>1.2</td>
<td>0.25</td>
</tr>
<tr>
<td>II</td>
<td>0.33</td>
<td>6.25</td>
<td>82.6</td>
<td>5.18</td>
<td>10.62</td>
<td>20</td>
<td>23.35</td>
<td>1.2</td>
<td>0.25</td>
</tr>
<tr>
<td>III</td>
<td>0.95</td>
<td>6.54</td>
<td>77.9</td>
<td>5.09</td>
<td>10.29</td>
<td>20</td>
<td>23.35</td>
<td>1.2</td>
<td>0.25</td>
</tr>
<tr>
<td>IV</td>
<td>8.00</td>
<td>10.72</td>
<td>74.6</td>
<td>7.99</td>
<td>6.48</td>
<td>20</td>
<td>23.35</td>
<td>1.2</td>
<td>0.25</td>
</tr>
<tr>
<td>V</td>
<td>12.51</td>
<td>14.49</td>
<td>74.4</td>
<td>10.78</td>
<td>4.04</td>
<td>20</td>
<td>23.35</td>
<td>1.2</td>
<td>0.25</td>
</tr>
<tr>
<td>VI</td>
<td>16.83</td>
<td>19.14</td>
<td>76.8</td>
<td>14.70</td>
<td>1.71</td>
<td>20</td>
<td>23.35</td>
<td>1.2</td>
<td>0.25</td>
</tr>
<tr>
<td>VII</td>
<td>16.87</td>
<td>19.19</td>
<td>78.0</td>
<td>14.97</td>
<td>1.69</td>
<td>20</td>
<td>23.35</td>
<td>1.2</td>
<td>0.25</td>
</tr>
<tr>
<td>VIII</td>
<td>17.65</td>
<td>20.16</td>
<td>79.0</td>
<td>15.93</td>
<td>1.27</td>
<td>20</td>
<td>23.35</td>
<td>1.2</td>
<td>0.25</td>
</tr>
<tr>
<td>IX</td>
<td>14.32</td>
<td>16.30</td>
<td>82.1</td>
<td>13.38</td>
<td>3.07</td>
<td>20</td>
<td>23.35</td>
<td>1.2</td>
<td>0.25</td>
</tr>
<tr>
<td>X</td>
<td>6.80</td>
<td>9.87</td>
<td>83.4</td>
<td>8.23</td>
<td>7.13</td>
<td>20</td>
<td>23.35</td>
<td>1.2</td>
<td>0.25</td>
</tr>
<tr>
<td>XI</td>
<td>2.03</td>
<td>7.07</td>
<td>86.2</td>
<td>6.09</td>
<td>9.70</td>
<td>20</td>
<td>23.35</td>
<td>1.2</td>
<td>0.25</td>
</tr>
<tr>
<td>XII</td>
<td>–1.23</td>
<td>5.51</td>
<td>85.6</td>
<td>4.72</td>
<td>10.80</td>
<td>20</td>
<td>23.35</td>
<td>1.2</td>
<td>0.25</td>
</tr>
</tbody>
</table>

To illustrate the boundary conditions of a given method for each of the two phenomena, all necessary parameters for the twelve consecutive months of the year were calculated and presented in Tables 6 and 7, respectively.

Table 6. Parameters for mold development characteristics for four methods.

<table>
<thead>
<tr>
<th>Month</th>
<th>$p_{\text{i,ISO}}$ hPa</th>
<th>$p_{\text{sat}}(\Theta_{si,\text{min}})$ hPa</th>
<th>$\Theta_{si,\text{min}}$ $^\circ\text{C}$</th>
<th>$f_{R\text{si,\text{min}}}$ –</th>
<th>$f_{R\text{si}}$ –</th>
<th>$\Theta_{si}$ $^\circ\text{C}$</th>
<th>$p_i$ hPa</th>
<th>$\phi_i$ %</th>
<th>$p_{i,\text{max}}$ hPa</th>
<th>$\phi_{i,\text{max}}$ %</th>
</tr>
</thead>
</table>
Table 7. Parameters for surface condensation characteristics for four methods.

<table>
<thead>
<tr>
<th>Month</th>
<th>( \Theta_{dp} ) °C</th>
<th>( f_{Rdp} ) –</th>
<th>( f_{RSi} ) –</th>
<th>( \Theta_{si} ) °C</th>
<th>( p_{i,con} ) hPa</th>
<th>( p_i ) hPa</th>
<th>( \varphi_i ) %</th>
<th>( \varphi_{i,con} ) %</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>12.25</td>
<td>0.685</td>
<td>0.70</td>
<td>12.6</td>
<td>14.60</td>
<td>14.25</td>
<td>61.1</td>
<td>62.5</td>
</tr>
<tr>
<td>II</td>
<td>13.83</td>
<td>0.686</td>
<td>0.70</td>
<td>14.1</td>
<td>16.07</td>
<td>15.80</td>
<td>67.7</td>
<td>68.8</td>
</tr>
<tr>
<td>III</td>
<td>13.42</td>
<td>0.654</td>
<td>0.70</td>
<td>14.3</td>
<td>16.26</td>
<td>15.38</td>
<td>65.9</td>
<td>69.7</td>
</tr>
<tr>
<td>IV</td>
<td>12.49</td>
<td>0.374</td>
<td>0.70</td>
<td>16.4</td>
<td>18.63</td>
<td>14.47</td>
<td>62.0</td>
<td>79.8</td>
</tr>
<tr>
<td>V</td>
<td>12.85</td>
<td>0.045</td>
<td>0.70</td>
<td>17.8</td>
<td>20.29</td>
<td>14.82</td>
<td>63.5</td>
<td>86.9</td>
</tr>
<tr>
<td>VI</td>
<td>14.41</td>
<td>–0.762</td>
<td>0.70</td>
<td>19.0</td>
<td>22.01</td>
<td>16.41</td>
<td>70.3</td>
<td>94.3</td>
</tr>
<tr>
<td>VII</td>
<td>14.65</td>
<td>–0.711</td>
<td>0.70</td>
<td>19.1</td>
<td>22.02</td>
<td>16.66</td>
<td>71.4</td>
<td>94.3</td>
</tr>
<tr>
<td>VIII</td>
<td>15.14</td>
<td>–1.069</td>
<td>0.70</td>
<td>19.3</td>
<td>22.35</td>
<td>17.20</td>
<td>73.7</td>
<td>95.7</td>
</tr>
<tr>
<td>IX</td>
<td>14.45</td>
<td>0.023</td>
<td>0.70</td>
<td>18.3</td>
<td>21.00</td>
<td>16.45</td>
<td>70.5</td>
<td>89.9</td>
</tr>
<tr>
<td>X</td>
<td>13.40</td>
<td>0.500</td>
<td>0.70</td>
<td>16.0</td>
<td>18.20</td>
<td>15.36</td>
<td>65.8</td>
<td>78.0</td>
</tr>
<tr>
<td>XI</td>
<td>13.82</td>
<td>0.656</td>
<td>0.70</td>
<td>14.6</td>
<td>16.61</td>
<td>15.80</td>
<td>67.7</td>
<td>71.1</td>
</tr>
<tr>
<td>XII</td>
<td>13.55</td>
<td>0.696</td>
<td>0.70</td>
<td>13.6</td>
<td>15.59</td>
<td>15.52</td>
<td>66.5</td>
<td>66.8</td>
</tr>
</tbody>
</table>

In the phenomenon of mold development, the characteristic parameters resulting from the insulation of the building barrier are: temperature factor of the barrier \( f_{RSi} \); barrier temperature \( \Theta_{si} \); maximum water vapor pressure in the room \( p_{i, max} \); maximum relative air humidity in the room \( \varphi_{i, max} \), while for the indoor microclimate it is: minimum permissible barrier temperature factor, \( f_{RSi, min} \); minimum permissible barrier temperature \( \Theta_{si, min} \); water vapor pressure in the room; relative air humidity in the room \( \varphi_i \) (Table 6).

In the phenomenon of surface condensation, the characteristic parameters resulting from the insulation of a building barrier are: the temperature factor of the barrier \( f_{RSi} \); barrier temperature, \( \Theta_{si} \); condensation pressure of water vapor \( p_{i,con} \); condensation humidity in the room, \( \varphi_{i,con} \), while for the internal microclimate it is: barrier temperature factor \( f_{Rdp} \); dew point temperature \( \Theta_{dp} \); water vapor pressure in the room; relative air humidity in the room \( \varphi_i \) (Table 7).

By comparing the relevant parameters characterizing the building barrier with the parameters characterizing the internal microclimate, all boundary conditions for mold development listed in Tables 1 and 2 and for surface condensation given in Tables 3 and 4 were checked. Thus, the state of the phenomenon (its occurrence or absence) was determined and the results were presented in Tables 7 and 8 respectively.

Table 8. Parameters for determining the conditions of surface condensation and the state of the phenomenon for four methods.

<table>
<thead>
<tr>
<th>Month</th>
<th>( f_{RSi} )</th>
<th>( f_{Rdp} )</th>
<th>( \Delta f_{Rcon} )</th>
<th>( \varphi_{i,con} )</th>
<th>( \varphi_i )</th>
<th>( \Delta \varphi_{i,con} )</th>
<th>( \Theta_{si} ) °C</th>
<th>( \Theta_{dp} ) °C</th>
<th>( \Delta \Theta_{con} ) °C</th>
<th>( p_{i,con} ) hPa</th>
<th>( p_i ) hPa</th>
<th>( \Delta p ) hPa</th>
<th>Phenomenon</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>0.70</td>
<td>0.686</td>
<td>0.015</td>
<td>62.5</td>
<td>61.1</td>
<td>1.5</td>
<td>12.6</td>
<td>12.25</td>
<td>0.38</td>
<td>14.60</td>
<td>14.25</td>
<td>0.35</td>
<td>lack</td>
</tr>
<tr>
<td>II</td>
<td>0.70</td>
<td>0.686</td>
<td>0.014</td>
<td>68.8</td>
<td>67.7</td>
<td>1.2</td>
<td>14.1</td>
<td>13.83</td>
<td>0.27</td>
<td>16.07</td>
<td>15.80</td>
<td>0.27</td>
<td>lack</td>
</tr>
<tr>
<td>III</td>
<td>0.70</td>
<td>0.654</td>
<td>0.046</td>
<td>69.7</td>
<td>65.9</td>
<td>3.8</td>
<td>14.3</td>
<td>13.42</td>
<td>0.87</td>
<td>16.26</td>
<td>15.38</td>
<td>0.88</td>
<td>lack</td>
</tr>
<tr>
<td>IV</td>
<td>0.70</td>
<td>0.374</td>
<td>0.326</td>
<td>79.8</td>
<td>62.0</td>
<td>17.8</td>
<td>16.4</td>
<td>12.49</td>
<td>3.91</td>
<td>18.63</td>
<td>14.47</td>
<td>4.15</td>
<td>lack</td>
</tr>
<tr>
<td>V</td>
<td>0.70</td>
<td>0.045</td>
<td>0.655</td>
<td>86.9</td>
<td>63.5</td>
<td>23.4</td>
<td>17.8</td>
<td>12.85</td>
<td>4.90</td>
<td>20.29</td>
<td>14.82</td>
<td>5.47</td>
<td>lack</td>
</tr>
<tr>
<td>VI</td>
<td>0.70</td>
<td>–0.762</td>
<td>1.462</td>
<td>94.3</td>
<td>70.3</td>
<td>24.0</td>
<td>19.0</td>
<td>14.41</td>
<td>4.63</td>
<td>22.01</td>
<td>16.41</td>
<td>5.59</td>
<td>lack</td>
</tr>
<tr>
<td>VII</td>
<td>0.70</td>
<td>–0.711</td>
<td>1.411</td>
<td>94.3</td>
<td>71.4</td>
<td>23.0</td>
<td>19.1</td>
<td>14.65</td>
<td>4.42</td>
<td>22.02</td>
<td>16.66</td>
<td>5.36</td>
<td>lack</td>
</tr>
<tr>
<td>VIII</td>
<td>0.70</td>
<td>–1.069</td>
<td>1.769</td>
<td>95.7</td>
<td>73.7</td>
<td>22.1</td>
<td>19.3</td>
<td>15.14</td>
<td>4.16</td>
<td>22.35</td>
<td>17.20</td>
<td>5.15</td>
<td>lack</td>
</tr>
<tr>
<td>IX</td>
<td>0.70</td>
<td>0.023</td>
<td>0.677</td>
<td>89.9</td>
<td>70.5</td>
<td>19.5</td>
<td>18.3</td>
<td>14.45</td>
<td>3.85</td>
<td>21.00</td>
<td>16.45</td>
<td>4.55</td>
<td>lack</td>
</tr>
<tr>
<td>X</td>
<td>0.70</td>
<td>0.500</td>
<td>0.200</td>
<td>78.0</td>
<td>65.8</td>
<td>12.2</td>
<td>16.0</td>
<td>13.40</td>
<td>2.64</td>
<td>18.20</td>
<td>15.36</td>
<td>2.84</td>
<td>lack</td>
</tr>
<tr>
<td>XI</td>
<td>0.70</td>
<td>0.656</td>
<td>0.044</td>
<td>71.1</td>
<td>67.7</td>
<td>3.5</td>
<td>14.6</td>
<td>13.82</td>
<td>0.79</td>
<td>16.61</td>
<td>15.80</td>
<td>0.81</td>
<td>lack</td>
</tr>
<tr>
<td>XII</td>
<td>0.70</td>
<td>0.696</td>
<td>0.004</td>
<td>66.8</td>
<td>66.5</td>
<td>0.3</td>
<td>13.6</td>
<td>13.55</td>
<td>0.08</td>
<td>15.59</td>
<td>15.52</td>
<td>0.07</td>
<td>lack</td>
</tr>
</tbody>
</table>
3.1. Mold Growth on the Surface of the Barrier

Table 6 shows the calculated values of all necessary parameters to check mold growth for four methods in the twelve consecutive months of the year.

Table 9 presents the values of parameters necessary to check the boundary conditions of mold development for four methods in the twelve consecutive months of the year.

Table 9. Parameters for determining the boundary conditions for mold development and the state of the phenomenon for four methods - the bold font indicates negative values of the analyzed parameters at which the mold phenomenon occurs.

<table>
<thead>
<tr>
<th>Month</th>
<th>f&lt;sub&gt;Rsi&lt;/sub&gt;</th>
<th>f&lt;sub&gt;Rsi.min&lt;/sub&gt;</th>
<th>∆f&lt;sub&gt;R&lt;/sub&gt;</th>
<th>Θ&lt;sub&gt;i&lt;/sub&gt;</th>
<th>Θ&lt;sub&gt;i.min&lt;/sub&gt;</th>
<th>∆Θ</th>
<th>ϕ</th>
<th>∆ϕ</th>
<th>Θ</th>
<th>∆Θ</th>
<th>p</th>
<th>∆p</th>
<th>Phenomenon</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>0.70</td>
<td>0.871</td>
<td>-0.171</td>
<td>46.8</td>
<td>61.1</td>
<td>-14.2</td>
<td>12.6</td>
<td>16.8</td>
<td>-4.21</td>
<td>10.93</td>
<td>14.25</td>
<td>-3.32</td>
<td>mold</td>
</tr>
<tr>
<td>II</td>
<td>0.70</td>
<td>0.916</td>
<td>-0.216</td>
<td>52.1</td>
<td>67.7</td>
<td>-15.6</td>
<td>14.1</td>
<td>18.3</td>
<td>-4.24</td>
<td>12.16</td>
<td>15.80</td>
<td>-3.64</td>
<td>mold</td>
</tr>
<tr>
<td>III</td>
<td>0.70</td>
<td>0.890</td>
<td>-0.190</td>
<td>52.6</td>
<td>65.9</td>
<td>-13.2</td>
<td>14.3</td>
<td>17.9</td>
<td>-3.63</td>
<td>12.29</td>
<td>15.38</td>
<td>-3.09</td>
<td>mold</td>
</tr>
<tr>
<td>IV</td>
<td>0.70</td>
<td>0.718</td>
<td>-0.018</td>
<td>61.1</td>
<td>62.0</td>
<td>-0.9</td>
<td>16.4</td>
<td>16.6</td>
<td>-0.22</td>
<td>14.27</td>
<td>14.47</td>
<td>-0.20</td>
<td>mold</td>
</tr>
<tr>
<td>V</td>
<td>0.70</td>
<td>0.563</td>
<td>0.137</td>
<td>67.4</td>
<td>63.5</td>
<td>3.9</td>
<td>17.8</td>
<td>16.7</td>
<td>1.03</td>
<td>15.74</td>
<td>14.82</td>
<td>0.91</td>
<td>lack</td>
</tr>
<tr>
<td>VI</td>
<td>0.70</td>
<td>0.394</td>
<td>0.306</td>
<td>74.3</td>
<td>70.3</td>
<td>4.0</td>
<td>19.0</td>
<td>18.1</td>
<td>0.97</td>
<td>17.34</td>
<td>16.41</td>
<td>0.93</td>
<td>lack</td>
</tr>
<tr>
<td>VII</td>
<td>0.70</td>
<td>0.460</td>
<td>0.240</td>
<td>74.4</td>
<td>71.4</td>
<td>3.1</td>
<td>19.1</td>
<td>18.3</td>
<td>0.75</td>
<td>17.38</td>
<td>16.66</td>
<td>0.72</td>
<td>lack</td>
</tr>
<tr>
<td>VIII</td>
<td>0.70</td>
<td>0.478</td>
<td>0.222</td>
<td>75.8</td>
<td>73.7</td>
<td>2.2</td>
<td>19.3</td>
<td>18.8</td>
<td>0.52</td>
<td>17.70</td>
<td>17.20</td>
<td>0.50</td>
<td>lack</td>
</tr>
<tr>
<td>IX</td>
<td>0.70</td>
<td>0.691</td>
<td>0.009</td>
<td>70.6</td>
<td>70.5</td>
<td>0.2</td>
<td>18.3</td>
<td>18.2</td>
<td>0.05</td>
<td>16.49</td>
<td>16.45</td>
<td>0.04</td>
<td>lack</td>
</tr>
<tr>
<td>X</td>
<td>0.70</td>
<td>0.817</td>
<td>-0.117</td>
<td>59.9</td>
<td>65.8</td>
<td>-5.9</td>
<td>16.0</td>
<td>17.6</td>
<td>-1.54</td>
<td>13.99</td>
<td>15.36</td>
<td>-1.37</td>
<td>mold</td>
</tr>
<tr>
<td>XI</td>
<td>0.70</td>
<td>0.903</td>
<td>-0.203</td>
<td>54.1</td>
<td>67.7</td>
<td>-13.6</td>
<td>14.6</td>
<td>18.3</td>
<td>-3.64</td>
<td>12.63</td>
<td>15.80</td>
<td>-3.16</td>
<td>mold</td>
</tr>
<tr>
<td>XII</td>
<td>0.70</td>
<td>0.910</td>
<td>-0.210</td>
<td>50.4</td>
<td>66.5</td>
<td>-16.1</td>
<td>13.6</td>
<td>18.1</td>
<td>-4.46</td>
<td>11.77</td>
<td>15.52</td>
<td>-3.75</td>
<td>mold</td>
</tr>
</tbody>
</table>

A graphic interpretation of the characteristic parameters for four methods in the phenomenon of mold development is shown in Figure 1. The intersecting lines in the charts show the occurrence of the phenomenon of mold development.

Figure 1. Graphs of characteristic parameters in the phenomenon of mold development; (a) method M1; (b) method M2; (c) method M3; (d) method M4.
3.2. Condensation on the Surface of the Barrier

Table 7 shows the calculated values of all necessary parameters needed to check surface condensation for four methods in the twelve consecutive months of the year.

Table 8 presents the necessary parameters to check the surface condensation boundary conditions for four methods in the twelve consecutive months of the year.

A graphic interpretation of the characteristic parameters for the four methods in the phenomenon of surface condensation is shown in Figure 2. The non-intersecting lines in the charts show that there is no surface condensation.

![Figure 2. Characteristic graphs of parameters in the phenomenon of surface condensation.](image)

4. Conclusions

In the phenomenon of mold development and surface condensation, depending on the selected calculation method, parameter differences ($\Delta f_R; \Delta \varphi; \Delta \Theta; \Delta p$) having negative values show how much the given quantity has been exceeded, which is associated with the phenomenon of mold or condensation. However, in the case of positive values obtained, they show what given value a supply has in relation to the boundary value. The calculation methods presented allow for a comprehensive assessment of the risk of mold and condensation on the surface of building barriers. Methods not described in the standard (ISO [24]) are of particular importance here. The result of the standard method (in the case of a negative value of the $\Delta f_R$ coefficient) is the answer in the form of information about the need to retrofit the analyzed building barrier. In contrast, “non-standard” methods allow for a quantitative indication of the cause of the phenomenon (in the form of, for example, too high relative humidity in the room) and protection against the risk of mold and condensation by reducing this humidity in a specific period of time (in months in which the values $\Delta \varphi$ are negative). This approach to the problem may be of particular importance in buildings where, for various reasons, the retrofitting of barriers is not possible (e.g., in some historic buildings under conservation protection).
Author Contributions: Conceptualization, A.S.; Data curation, A.S.; Formal analysis, A.S., J.K. and P.M.; Funding acquisition, L.L.; Investigation, A.S.; Methodology, A.S., J.K. and P.M.; Project administration, L.L.; Resources, A.S., J.K. and P.M.; Supervision, L.L.; Validation, A.S., L.L., J.K. and P.M.; Visualization, A.S., J.K. and P.M.; Writing—original draft, A.S., J.K. and P.M.; Writing—review & editing, A.S., J.K. and P.M. All authors have read and agreed to the published version of the manuscript.

Funding: This research received no external funding.

Conflicts of Interest: The authors declare no conflict of interest. The funders had no role in the design of the study; in the collection, analyses, or interpretation of data; in the writing of the manuscript, or in the decision to publish the results.

References


© 2019 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (http://creativecommons.org/licenses/by/4.0/).