New Method for Shallow and Deep Trap Distribution Analysis in Oil Impregnated Insulation Paper Based on the Space Charge Detrapping

Jian Hao 1,*, Runhao Zou 1, Ruijin Liao 1, Lijun Yang 1 and Qiang Liao 2

1 The State Key Laboratory of Power Transmission Equipment & System Security and New Technology, Chongqing University, Chongqing 400044, China; 20161101041@cqu.edu.cn (R.Z.); rjliao@cqu.edu.cn (R.L.); yljcqu@cqu.edu.cn (L.Y.)
2 College of Power Engineering, Chongqing University, Chongqing 400044, China; lqzx@cqu.edu.cn
* Correspondence: haojian2016@cqu.edu.cn; Tel.: +86-182-2301-0926

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Abstract: Space charge has close relation with the trap distribution in the insulation material. The phenomenon of charges trapping and detrapping has attracted significant attention in recent years. Space charge and trap parameters are effective parameters for assessing the ageing condition of the insulation material qualitatively. In this paper, a new method for calculating trap distribution based on the double exponential fitting analysis of charge decay process and its application on characterizing the trap distribution of oil impregnated insulation paper was investigated. When compared with the common first order exponential fitting analysis method, the improved dual-level trap method could obtain the energy level range and density of both shallow traps and deep traps, simultaneously. Space charge decay process analysis of the insulation paper immersed with new oil and aged oil shows that the improved trap distribution calculation method can distinguish the physical defects and chemical defects. The trap density shows an increasing trend with the oil ageing, especially for the deep traps mainly related to chemical defects. The greater the energy could be filled by the traps, the larger amount of charges could be trapped, especially under higher electric field strength. The deep trap energy level and trap density could be used to characterize ageing. When one evaluates the ageing condition of oil-paper insulation using trap distribution parameters, the influence of oil performance should not be ignored.

Keywords: space charge; trap distribution; oil impregnated insulation paper; charge detrapping; electrical field; oil ageing

1. Introduction

Oil-paper insulation has been widely applied in power transformers. It is reported that the space charge has great effect on the insulation property of the oil-paper insulation in convert transformer [1–5]. Space charge means the excess electric charge over a region of space, rather than distinct point-like charges [6,7]. Space charge could severely distort the local electrical field, which causes the material degradation or leads to the insulation breakdown [1–3]. Besides, oil-paper insulation gradually degrades under the combined stresses of thermal, electrical, and chemical during transformer routine operation [8–10]. The polar and conductive ageing by-products would lead to the obvious injection phenomenon of space charge [8–10]. It is found that the space charge injection and accumulation in oil-paper insulation is strongly dependent on its ageing condition [11–15]. Space charge may be an ageing condition indicator for the oil-paper insulation [1,8–10]. Ageing could introduce defects (physical and chemical) and lead to the rise of localised states in the material. The localised states is named trap [16,17]. Space charge are determined by the trap distribution [1,16–19], which is related
to defect in material [20–23]. Therefore, understanding the trap distribution effect on the dynamic behavior of space charge is very important.

Many researches about the trap distribution characteristics for polyethylene and insulation paper have been conducted [1,16–18,22–25]. The space charge measurement which is non-destructive is the current popular technology for trap distribution analysis. In [16,17], trap energy level and the trap density of the low density polyethylene (LDPE) and gamma irradiated LDPE were analyzed by a trapping-detrapping model for the shallow and deep trap. It is found that trap parameter changes could reflect the LDPE ageing. Tang, Hao et al. estimated the trap distribution in oil impregnated insulation paper based on the first-order exponential fitting analysis of the charge decay [1,24,25]. The trap energy level and trap density could be calculated using the space charge detrapping parameters. Wei calculated the trap parameters of oil impregnated insulation paper with different ageing condition based on the dual-level trap model [19]. Results show that the trap density increases when the sample being thermally or electrically aged.

For the dual-level trap model, the faster charges and slower charges have been taken into account [16,18,19]. The values of trap energy level and trap density for shallow or deep trap could be obtained. However, the trap energy level and density of shallow trap or deep trap only has one value. This is not fully consistent with the actual situation that shallow or deep traps in material exist within a wide range of energy levels [16]. For the trap energy distribution calculation method based on the first-order exponential fitting analysis of charge decay, the range of trap energy and its density could be obtained [24,25]. However, the first-order exponential fitting did not consider that the charges escape from the shallow traps is faster than that of the deep traps, which leads to the shallow trap’s and deep trap’s energy level and density could not be distinguished. In addition, there are a lot of studies on the ageing state evaluation of LDPE using trap parameters [16,18,26,27]. Unlike the LDPE, the use of trap parameters to assess the ageing condition of oil-paper insulation is very rare [1]. To evaluate the ageing state of oil-paper insulation using trap parameters, which is mainly to characterize the state of oil impregnated insulation paper [28–31], it is needed to consider the influence of oil properties on the trap parameters, which is not considered in the previous publication [1,9,10,19,24,25].

In the present paper, firstly, the trapped charges and charge decay behaviors of the oil-paper insulation sample with new and aged oil were measured by the pulsed electroacoustic (PEA) method. Secondly, an improved method for calculation of the shallow and deep trap distribution in oil impregnated insulation paper based on the double exponential kinetic analysis of charge detrapping was proposed. The trap distribution calculated using the improved method and common method were compared in detail. At last, the relationship between the trapped charges and the trap distribution parameters was analyzed. The new method could improve the accuracy in estimating the trap parameters for the oil-paper insulation.

2. Experiments

The PEA principle can be seen in literatures [1–3,10,13,14], as shown in Figure 1a [1]. When considering the oil-paper insulation is commonly used as multi-layer, in this experiment, oil-paper insulation samples with three layers immersed in new and aged oil were measured, respectively. The acidity of the new oil is 0.023 mgKOH/g, while the aged oil is 0.43 mgKOH/g. The sample preparation and testing process could be seen in our previous publication [31]. The samples were stressed at different dc electric field strength (20 kV/mm, 30 kV/mm, and 40 kV/mm) at 15 °C for 1 h (Al: cathode, Semiconducting polymer: anode). Space charge behaviors under the “voltage-off” and the “decay” condition were analyzed.
3. Experimental Results and Discussions

3.1. Charges Trapped in the Samples

Traps can capture charges injected or generated in the material under the effect of electrical field [18,32]. The amount of charges that are trapped in shallow and deep traps attributes to the trap distribution [18,32]. In order to establish the relationship between the trapped charges and the trap parameters, the volts-off measurement mainly presents the characteristics of trapped charges was analyzed, as presented in Figure 2. The distribution behavior of the charges trapped in the sample with new and aged oil is similar. Homo-charges injection occurs in both samples. A lot of negative charges trapped in the vicinity of the cathode, and a lot of positive charges trapped in the vicinity of the anode. There are obvious positive charges trapped at the paper-paper interface. In Figure 2, what is more important is that the density of the trapped charges in both samples increase with the electric field strength enhanced, which indicates that the filling rate of the charges in the traps is higher under the higher electrical field strength.
Figure 2. Space charges trapped in the oil impregnated insulation paper with new and aged oil under DC 20 kV/mm, 30 kV/mm, and 40 kV/mm. (a) sample with new oil (20 kV/mm); (b) sample with new oil (30 kV/mm); (c) sample with new oil (40 kV/mm); (d) sample with aged oil (20 kV/mm); (e) sample with aged oil (30 kV/mm); (f) sample with aged oil (40 kV/mm).

The trapped charges amount in the sample was calculated using the Equation (1) presented in [1,13,16,24,25]. \( \rho(x, t) \) means the charge density, \( S \) is electrode area, and \( d \) is sample thickness.

\[
Q(t) = \int_0^d |\rho(x, t)| S dx
\]  

(1)

The total amount of trapped charges in the oil impregnated insulation paper with new and aged oil under volt-off condition is shown in Figure 3a,b, whether it is sample with new oil or aged oil, the total amount of charges trapped increases with enhanced electric field strength. For the sample immersed with new oil, the physical and chemical defects is limited, the traps could be fully filled when the voltage applied only for a while (Figure 3a). Thus, the amount of charges trapped in the sample shows a little increasing trend at first and then reaches saturation quickly with the voltage applied under 20 kV/mm, 30 kV/mm and 40 kV/mm, respectively. However, for the sample with aged oil, new physical and chemical defects were generated, which leads to the amount of trapped charges increases gradually, and it tends to attain a saturation value finally (Figure 3b). The saturation amount of trapped charges in the sample with aged oil is significantly larger than that in the sample with new oil under each applied electric filed. From Figure 3 it could be deduced that the saturation amount of trapped charges, and its increasing trend could reflect the changes in the material, which is related to the microscopic trap distribution.

Figure 3. Trapped charges amount in the sample with new and aged oil under volt-off condition. (a) charges amount in sample with new oil; (b) charges amount in sample with aged oil.
3.2. Charges Decay Process

Trapped charges can release from the traps by photon assisted detrapping, thermal detrapping impact ionization, and tunneling [16,32]. Charge detrapping process of the insulation paper immersed with new and aged oil is presented in Figure 4. It is obvious that the charge density of the charges that are trapped near to the cathode increases with the voltage and the oil deterioration degree increased. The trapped charges dissipates quickly. Most of the trapped charges diminish away from the sample after being removed voltage 30 min.

Figure 4. Space charge detrapping process for insulation paper immersed with new and aged oil under DC 20 kV/mm, 30 kV/mm, and 40 kV/mm. (a) space charge detrapping process for insulation paper immersed with new oil (20 kV/mm); (b) space charge detrapping process for insulation paper immersed with new oil (30 kV/mm); (c) space charge detrapping process for insulation paper immersed with new oil (40 kV/mm); (d) space charge detrapping process for insulation paper immersed with aged oil (20 kV/mm); (e) space charge detrapping process for insulation paper immersed with aged oil (30 kV/mm); (f) space charge detrapping process for insulation paper immersed with aged oil (40 kV/mm).

As depicted in publication [1,3,16,17], charges trapped in deep traps usually dissipate slowly, while charges that are trapped in shallow traps escape from the traps very shortly. Figure 5 shows the dissipation law of the trapped charges in the sample with new oil and aged oil. The higher the applied electric filed strength, the more charges trapped in the samples, which leads to the higher initial decay value of the total charge. In addition, it is clearly that the sample with aged oil has higher initial amount of trapped charges than that of the sample with new oil. For the sample with new oil, it is $3.46 \times 10^{-8}$ C for 20 kV/mm, $5.08 \times 10^{-8}$ C for 30 kV/mm, and $5.65 \times 10^{-8}$ C for 40 kV/mm. For the sample with aged oil, it is $7.23 \times 10^{-8}$ C for 20 kV/mm, $10.8 \times 10^{-8}$ C for 30 kV/mm, and $17.4 \times 10^{-8}$ C for
40 kV/mm. It is noteworthy that for both sample the amount of charges shows a significant decrease in the initial time of the voltage being removed, and then followed by a slow decay. This corresponds to the release of fast charges and slow charges, respectively.

![Graph showing charge detrapping process](image)

**Figure 5.** Charge detrapping process in oil impregnated insulation paper with new and aged oil after being applied DC electrical field 20 kV/mm, 30 kV/mm, and 40 kV/mm for 1 h. (a) sample with new oil; (b) sample with aged oil.

### 4. Improved Method for Trap Distribution Analysis


The common trap distribution calculation method based on the first-order exponential fitting analysis of charge decay is described in [24,25,32]. The charge density decreases according to an exponential law, as shown in Equation (2). In Equation (2), $\sigma$ and $A$ means the equivalent surface charge density and the initial surface charge density, respectively. $\tau$ and $t$ is the time constant and decay time for trapped charges dissipation. The current density $|j(t)|$, including the decay time constant could be calculated by Equation (3). The current density is $|j(t)|$, and the average charge centroid is $\rho'$, 120 pm. $L$ means the sample thickness.

$$\sigma = A \times e^{-t/\tau}$$

$$|j(t)| = \frac{\rho' A}{L} e^{-t/\tau}$$

The trap energy level $E_t$, the trap density $N(E_t)$, and the current density $|j(t)|$ follows Equations (4) and (5). Where $\nu$ means electron vibration frequency, $3 \times 10^{12}$ s$^{-1}$. $K$ means Boltzmann’s constant, $8.568 \times 10^{-5}$ eV/K. $T$ is the absolute temperature, $K$. $f_0(E_t)$ is 1/2, which means the trap’s original occupation rate. $e$ is the electron charge, $1.6 \times 10^{-19}$ C.

$$E_t = KT \ln(\nu t)$$

$$|j(t)| = \frac{e L K T}{2 \tau} \frac{f_0(E_t)}{f_0(0)} N(E_t)$$

If $\eta_1 = \frac{e L K T}{2 \tau} f_0(0)$, $\eta_2 = \frac{\rho' A}{L}$, $\eta_1$ and $\eta_2$ are constant, then

$$N(E_t) = \frac{\eta_2}{\eta_1} \frac{t}{\tau} e^{-t/\tau}$$
Equation (6) presents that the trap density \( N(E_t) \) at trap energy level \( E_t \) could be calculated as long as the values of \( A \) and \( \tau \) being obtained by analysis the charge detrapping behavior measured by PEA equipment, as shown in Figure 6.

![Figure 6. Trap distribution calculation based on the charge decay process.](image)

### 4.2. Improved Method for Trap Distribution Analysis Using Charge Detrapping Process

There are majorly two types of trap with different energy level, namely shallow trap and deep trap. Charges decay faster from shallow traps than that from deep traps [16, 17, 32], therefore, the first-order exponential decay expression of charge detrapping shown above should be changed to double exponential decay expression, as shown in Table 1. In the following, the trap distribution of oil impregnated insulation paper based on the first-order exponential fitting analysis (common method) and the double exponential fitting analysis (improved method) is compared.

<table>
<thead>
<tr>
<th>Common Method: First Order Exponential Fitting Analysis</th>
<th>Improved Method: Double Exponential Fitting Analysis</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \sigma = A \times e^{-t/\tau} )</td>
<td>( \sigma = \sigma_{\text{fast}} + \sigma_{\text{slow}} = A_{\text{fast}} \times e^{-t/\tau} + A_{\text{slow}} \times e^{-t/\tau} )</td>
</tr>
<tr>
<td>(</td>
<td>j(t)</td>
</tr>
<tr>
<td>( E_t = kT \ln(vt) )</td>
<td>( E_{t-\text{fast}} = kT \ln(vt), E_{t-\text{slow}} = kT \ln(vt) )</td>
</tr>
<tr>
<td>(</td>
<td>j(t)</td>
</tr>
<tr>
<td>( \eta_1 = \frac{e^{LKT}}{2} f_0(E_t) )</td>
<td>( \eta_{1-\text{fast}} = \frac{e^{LKT}}{2} f_0(E_{t-\text{fast}}), \eta_{1-\text{slow}} = \frac{e^{LKT}}{2} f_0(E_{t-\text{slow}}) )</td>
</tr>
<tr>
<td>( \eta_2 = \frac{\epsilon \sigma L}{e} )</td>
<td>( \eta_{2-\text{fast}} = \frac{\epsilon \sigma L}{e}, \eta_{2-\text{slow}} = \frac{\epsilon \sigma L}{e} )</td>
</tr>
<tr>
<td>( N(E_t) = \frac{n_1}{\eta_1} e^{-t/\tau} )</td>
<td>( N(E_{t-\text{fast}}) = \frac{n_1}{\eta_{1-\text{fast}}} e^{-t/\tau}, N(E_{t-\text{slow}}) = \frac{n_1}{\eta_{1-\text{slow}}} e^{-t/\tau} )</td>
</tr>
</tbody>
</table>

Table 1. The calculation equation of the trap distribution using common method and the improved method.
4.3. Comparison Analysis of the Charge Detrapping Process Using the Improved Method and Common Method

The charge detrapping process presented in Figure 5 was fitted using the first order exponential expression and double order exponential expression, respectively, as shown in Figure 7. The first order exponential fitting equations and the double order exponential fitting equations are shown in Tables 2 and 3. As shown in Figure 7a,c and Table 2, the fitting curves obtained by the first order exponential fitting expression fit well with the measured data. However, in the middle and late stages of charge decay, some measured data deviate from the fitting curve. While for the fitting curves obtained by double order exponential fitting expression shown in Figure 7b,d and Table 3 is in good agreement with the measured data, especially in the middle and late stages of charge decay. This presents that the double order exponential fitting analysis accords with the law of charge dissipation, which includes the fast charge and slow charge. When compared with the common method, the improved method is more suitable for the kinetic analysis of charge detrapping.

![Figure 7](image-url)

**Figure 7.** Common and improved method for fitting analysis of charge detrapping for oil impregnated insulation paper with new oil and aged oil being applied DC electrical field 20 kV/mm, 30 kV/mm, and 40 kV/mm for 1 h. (a) common method: sample with new oil; (b) improved method: sample with new oil; (c) common method: sample with aged oil; (d) improved method: sample with aged oil.

The higher the applied electric filed strength, the more charges trapped in the samples (Figure 3), which also leads to the higher initial decay value of total charge, as shown in Figure 7a. The initial decay value of total charge increases as electrical field strength. The total trapped charge decay shows a fast decay initially and follows a much slower change. This fact approves the two trapping levels approximation used in our analysis. The charge detrapping expression based on the first order exponential fitting analysis for oil impregnated insulation paper with new oil shown in Table 2 present that the decay constant time decreases with increasing of the electric filed strength. It is 922.66 s for the
20 kV/mm, 683.25 s for the 30 kV/mm, and 577.41 s for the 40 kV/mm. The faster decay rate of the charges may lead to the less values of total charge in the decay process, although the samples applied higher electric filed having a higher decay value of total charge.

Table 2. The charge detrapping expression based on the first order exponential fitting analysis for oil impregnated insulation paper with new and aged oil.

<table>
<thead>
<tr>
<th>E(kV/mm)</th>
<th>Fitting Equation $Q_0(t)$ ($10^{-8}$ C)</th>
<th>$\tau$ (s)</th>
<th>$R^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>new oil</td>
<td></td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>$Q_0(t) = 1.25 \times \exp(-t/922.66) + 1.25 \times \exp(-t/922.66) + 0.29$</td>
<td>922.66</td>
<td>0.99</td>
</tr>
<tr>
<td>30</td>
<td>$Q_0(t) = 1.48 \times \exp(-t/233.89) + 2.65 \times \exp(-t/1312.75) + 0.92$</td>
<td>233.89</td>
<td>0.99</td>
</tr>
<tr>
<td>40</td>
<td>$Q_0(t) = 2.15 \times \exp(-t/214.54) + 3.19 \times \exp(-t/1157.06) + 0.30$</td>
<td>214.54</td>
<td>0.99</td>
</tr>
<tr>
<td></td>
<td>aged oil</td>
<td></td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>$Q_0(t) = 2.18 \times \exp(-t/198.20) + 4.77 \times \exp(-t/1228.10) + 0.29$</td>
<td>198.20</td>
<td>0.99</td>
</tr>
<tr>
<td>30</td>
<td>$Q_0(t) = 4.14 \times \exp(-t/214.80) + 5.94 \times \exp(-t/1493.10) + 0.83$</td>
<td>214.80</td>
<td>0.99</td>
</tr>
<tr>
<td>40</td>
<td>$Q_0(t) = 4.10 \times \exp(-t/210.00) + 10.63 \times \exp(-t/1628.40) + 0.92$</td>
<td>210.00</td>
<td>1.00</td>
</tr>
</tbody>
</table>

Table 3. The charge detrapping expression based on the double order exponential fitting analysis for oil impregnated insulation paper with new and aged oil.

<table>
<thead>
<tr>
<th>E(kV/mm)</th>
<th>Fitting Equation $Q_0(t)$ ($10^{-8}$ C)</th>
<th>$\tau_{fast}$</th>
<th>$\tau_{slow}$</th>
<th>$R^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>new oil</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>$Q_0(t) = 2.18 \times \exp(-t/991.20) + 4.77 \times \exp(-t/1228.10) + 0.29$</td>
<td>991.20</td>
<td>1228.10</td>
<td>1.00</td>
</tr>
<tr>
<td>30</td>
<td>$Q_0(t) = 4.14 \times \exp(-t/214.80) + 5.94 \times \exp(-t/1493.10) + 0.83$</td>
<td>214.80</td>
<td>1493.10</td>
<td>1.00</td>
</tr>
<tr>
<td>40</td>
<td>$Q_0(t) = 4.10 \times \exp(-t/210.00) + 10.63 \times \exp(-t/1628.40) + 0.92$</td>
<td>210.00</td>
<td>1628.40</td>
<td>1.00</td>
</tr>
</tbody>
</table>

The charge detrapping expression based on the double order exponential fitting analysis for oil impregnated insulation paper with new oil shown in Table 3 presents that the sample applied 40 kV/mm for 1 h has a much faster decay rate, while there has a slower decay rate for the charges trapped in the deep traps. The faster charges detrapping from the shallow traps contributes more to the decay process due to that there is limited defects in the new sample. When the sample composed by aged oil, many chemical defects would be introduced into the sample, which contributes to deep traps. This leads to more charges be trapped in the sample and charges decay more slowly. Therefore, the less total charge under 40 kV/mm for the sample with new oil in the decay process attributes to limited trap in the new sample and faster decay rate for the charges trapped in shallow trap.

4.4. Comparison Analysis of the Trap Distribution Using the Improved Method and Common Method

The trap energy level and its density calculated using the common method and the improved method is presented in Figure 8. It can be seen that there is only one peak for the trap distribution obtained by the first order exponential fitting expression (Figure 8a,c), which only has one decay time constant for the charge detrapping process. Therefore, the shallow trap and the deep trap could not be distinguished. However, for the trap distribution calculated using the double order exponential fitting expression, there are two energy levels of trap distribution (Figure 8b,d). The shallow traps and deep traps could be particularly distinguished according to their peaks’ energy level.

For the trap distribution of sample with new oil calculated by the common method, the energy level is from 0.77 eV to 0.92 eV (Figure 8a). With the electric field strength increased from 20 kV/mm to 40 kV/mm, the maximum trap density increases from $1.29 \times 10^{12}$ m$^{-3} \cdot$eV$^{-1}$ to $8.36 \times 10^{13}$ m$^{-3} \cdot$eV$^{-1}$,
while the trap energy level corresponding to the maximum trap density decreases form 0.89 eV to 0.88 eV. For the trap distribution of sample with aged oil calculated by the common method, the energy level is from 0.77 eV to 0.92 eV (Figure 8c). The maximum trap density increases from $4.15 \times 10^{12} \text{ m}^{-3} \text{eV}^{-1}$ to $2.19 \times 10^{14} \text{ m}^{-3} \text{eV}^{-1}$ as the increasing of the electric field strength, and the trap energy level corresponding to the maximum trap density increases from 0.88 eV to 0.889 eV. In addition, the maximum trap density for the sample with aged oil is significantly higher than the sample with new oil. However, using the trap distribution obtained by the common method, it is difficult to know whether the increase in shallow trap or deep trap that is caused by oil ageing.

For the trap distribution of sample with new oil calculated by the common method, the energy level is more in line with the actual situation of trap distribution in material. While most shallow traps are distributed from 0.80 eV to 0.87 eV, and the trap energy level corresponding to the maximum shallow trap density peak is 0.85 eV, and the trap energy level corresponding to the maximum deep trap density peak is 0.90 eV. There exists a cross region in the range of the shallow trap and deep trap. Most shallow traps are distributed from 0.80 eV to 0.87 eV, while most deep traps are distributed from 0.85 eV to 0.92 eV. The peak being clearly separated. For the sample with new oil, the trap energy level corresponding to the maximum trap density increases from 0.88 eV to 0.889 eV. In addition, the maximum trap density of the sample with new oil is significantly higher than the sample with new oil. However, using the trap distribution obtained by the common method, it is difficult to know whether the increase in shallow trap or deep trap that is caused by oil ageing.

As shown in Figure 8b,d, for the trap distribution of sample with new oil and aged oil calculated by the improved method, it can be seen that the shallow trap density peak and the deep trap density peak being clearly separated. For the sample with new oil, the trap energy level corresponding to the maximum shallow trap density peak is 0.85 eV, and the trap energy level corresponding to the maximum deep trap density peak is 0.89 eV. For the sample with aged oil, the trap energy level corresponding to the maximum shallow trap density peak is 0.85 eV, and the trap energy level corresponding to the maximum deep trap density peak is 0.90 eV. There exists a cross region in the range of the shallow trap and deep trap. Most shallow traps are distributed from 0.80 eV to 0.87 eV,
while most deep traps are distributed from 0.85 eV to 0.92 eV. The phenomenon of cross region in trap energy level is more in line with the actual situation of trap distribution in material. What is more, the maximum trap density of the shallow traps and deep traps also increases with an enhanced electric field strength.

Traps is greatly affected by the physical and chemical defects [16,18,33,34]. Morphological structure changing would introduce physical defects in the material. Chemical defects usually introduced by photo-oxidation of the material [16,32]. It has been reported that the physical defects mainly depended on the shallow traps, while the chemical defects mainly depended on the deep traps [16,18,32]. Mineral oil ageing or deterioration is normally associated with oxidation, as shown in the following chemical reactions (1), (2), (3) [35–37]. Where RH: hydrocarbon compounds; R•, RO•, RO2•, H•: free radicals; ROOR: alkyl peroxide; ROOH: hydrogen peroxide. The ageing products are mainly the gaseous (CO, CO2, and volatile hydrocarbons), liquid (RCHO, R–CO–R, ROH, RCOOH, tars, and H2O) and sludge. From the chemical reactions (1), (2), (3), it can be seen clearly that oil thermal deterioration lowering the molecular weight and bring impurities to oil, especially acidic impurities [35–37]. Figure 8 clearly presents that the new method could describe the physical and chemical defects changes in the oil impregnated insulation paper. Though the trap energy level and trap density of the deep traps could be used as ageing markers, when one assessing the ageing condition of the oil-paper insulation by the trap parameters, the influence of oil performance should not be ignored due to the oil filter treatment during the transformer operation.

\[
\begin{align*}
(1) \quad & RH \rightarrow R• + H• \\
& \text{RH} + O_2 \rightarrow R• + HO_2• \\
& \text{RO2•} + H• \\
(2) \quad & \text{RO} \rightarrow \text{RO2•} \rightarrow \text{RH} \rightarrow \ldots \ldots \\
& \text{ROOH} \\
\end{align*}
\]

4.5. Effectiveness Verify of the Improved Method

In order to further verify of the improved method proposed in this paper, the space charge decay data published in [16,38] were extracted and analyzed using the new improved method, respectively. The decay charges amount changing with decay time for the fresh and aged oil impregnated insulation pressboard after being applied negative 25 kV/mm voltage for 4 h in [38] is shown in Figure 9a,b. The charge decay behavior was fitted using the common method (first order exponential fitting equation) and new method (double order exponential fitting equation). From Figure 9a, it can be seen that the initial and the last stage of the charge dissipation was not fitted very well using the common fitting method. However, this phenomenon could be eliminated by using the new method, as shown in Figure 9b. The fitting equations is shown in Table 4. The decay charges at initial and the last stage of the charge dissipation was fitted very well. The common fitting method regards the decay charge having the same motion behavior, while the new method (double order exponential fitting equation) includes the motion law of both the fast and slow charges, thus the new fitting method is more consistent with the reality of charge dissipation.

Figure 9c,d is the trap distribution calculated using the common method and the new method according to Table 1, respectively. The trap density for the aged pressboard is significantly higher than the fresh pressboard. However, it is difficult to know the increase degree of shallow trap or deep trap that is caused by ageing. In Figure 9d, it clearly shows the density of the shallow trap and deep trap
both increases for the aged pressboard compared with the fresh pressboard. The results shown in Figure 9 further verify the effectiveness of the improved method.

![Figure 9](image-url)

**Figure 9.** Charges decay and trap distribution analysis for the fresh and aged oil impregnated insulation pressboard sample applied negative 25 kV/mm voltage for 4 h (charges data was derived from [38]). (a) common method: charge decay analysis; (b) new method: charge decay analysis; (c) common method: charge decay analysis; (d) new method: charge decay analysis.

**Table 4.** The charge detrapping expression for the fresh and aged oil impregnated insulation pressboard sample applied negative 25 kV/mm voltage for 4 h (charges data was derived from [38]).

<table>
<thead>
<tr>
<th>Common Method</th>
<th>Fitting Equation ( Q_0(t) ) (10^{-8} C)</th>
<th>( \tau ) (s)</th>
<th>( R^2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>fresh pressboard</td>
<td>( Q_0(t) = 0.74 + 0.93 \times \exp(-t/2946) )</td>
<td>2946</td>
<td>0.91</td>
</tr>
<tr>
<td>aged pressboard</td>
<td>( Q_0(t) = 1.05 + 3.24 \times \exp(-t/222.2) )</td>
<td>222.2</td>
<td>0.95</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>New Method</th>
<th>Fitting Equation ( Q_0(t) ) (10^{-8} C)</th>
<th>( \tau_{fast} )</th>
<th>( \tau_{slow} )</th>
<th>( R^2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>fresh pressboard</td>
<td>( Q_0(t) = 0.34 \times \exp(-t/93.1) - 0.47 \times \exp(t/4660) + 1.99 )</td>
<td>93.1</td>
<td>4660</td>
<td>0.98</td>
</tr>
<tr>
<td>aged pressboard</td>
<td>( Q_0(t) = 6.05 \times \exp(-t/19.4) + 2.16 \times \exp(-t/437.1) + 0.94 )</td>
<td>19.4</td>
<td>437.1</td>
<td>0.99</td>
</tr>
</tbody>
</table>

The second verification case shown in Figure 10 analyzed the charges decay data for the LDPE sample after being applied 4 kV for 10 min (charges data was derived from [16]). There is a rapid decay for the charges at the initial dissipation stage, and then the charges dissipates much slowly. The pink line and the red line represent the fitting result using the common method and the new method, respectively. According to the measured data, it can be seen that red line is closer to the measured data, especially after the rapid decay stage. Therefore, the new method considering both the fast and slow charges have obvious advantages.
4.6. Relationship between Trapped Charges and Trap Distribution

Trap density changing with electric field strength for the sample with new and aged oil was analyzed, as shown in Figure 11. It is worth noting that the trap density of the shallow traps and deep traps both shows an increasing trend with the oil ageing (Figure 9b), especially for the deep traps. The maximum trap density of the deep trap for the sample with aged oil under 20 kV/mm, 30 kV/mm, and 40 kV/mm is $8.38 \times 10^{13} \text{ m}^{-3} \text{eV}^{-1}$, $1.04 \times 10^{14} \text{ m}^{-3} \text{eV}^{-1}$, and $1.86 \times 10^{14} \text{ m}^{-3} \text{eV}^{-1}$, respectively. While for the sample with new oil, the maximum trap density of the deep trap under 20 kV/mm, 30 kV/mm, and 40 kV/mm is only $2.20 \times 10^{13} \text{ m}^{-3} \text{eV}^{-1}$, $4.64 \times 10^{13} \text{ m}^{-3} \text{eV}^{-1}$, and $5.59 \times 10^{13} \text{ m}^{-3} \text{eV}^{-1}$. The maximum density of deep traps for sample with aged oil is 3.81, 2.24 and 3.33 times larger than the sample with new oil under 20 kV/mm, 30 kV/mm, and 40 kV/mm, respectively. However, the maximum density of shallow traps for sample with aged oil is 1.73, 2.80, and 1.92 times larger than that for the sample with new oil under 20 kV/mm, 30 kV/mm, and 40 kV/mm, respectively. Thus, it is obvious that using the improved trap distribution calculation method, it is easy to know the degree of increase in shallow trap or deep trap caused by oil ageing.

![Figure 10](image1.png) Charges decay analysis for the low density polyethylene (LDPE) sample applied 4 kV for 10 min (charges data was derived from [16]).

![Figure 11](image2.png) Trap density changing with electric field strength for the sample with new and aged oil. (a) common method; (b) improved method.

The saturation amount of trapped charges in both sample was extracted. The relationship between the saturation amount of the trapped charges and the trap parameters was analyzed. According to the common method for the trap distribution calculation, the total energy filled by the traps could
be calculated using the Equation (7). Where TNE is the total energy that is filled by the traps in the sample. $t$ means $t$ sample thickness. $S$ is the space charge testing area of the sample.

$$TNE = \int_{0}^{l} N_t \times E_t \times S\,dx$$  \hspace{1cm} (7)$$

According to the improved method for the trap distribution calculation, the total energy filled by the traps could be calculated using the equation defined below:

$$TNE = \int_{0}^{l} N_{t-\text{fast}} \times E_{t-\text{fast}} \times S\,dx + \int_{0}^{l} N_{t-\text{slow}} \times E_{t-\text{slow}} \times S\,dx$$  \hspace{1cm} (8)$$

As shown in Figure 12a,b, the greater the energy could be filled by the traps, the larger amount of charges could be trapped, especially under higher electric field strength. In addition, compared with the results shown in Figure 12a, the TNE values presented in Figure 12b calculated using the parameters obtained by the improved method which considers two types of trap has a better match with the saturation amount of trapped charges in both sample.

![Graphs showing relationship between trapped charges and total energy](image1)

**Figure 12.** Relationship between the trapped charges amount and the total energy filled by the traps obtained by common method and the improved method. (a) common method; (b) improved method.

5. Conclusions

An improved method for calculating trap distribution based on the double exponential fitting analysis of charge decay process and its application on characterizing the trap distribution of oil impregnated insulation paper was discussed in this paper. The following conclusions could be drawn.

1. The double exponential fitting analysis of charge decay includes the detrapping process of both fast charge and slow charge. Compared with the dual-level trap model and the common first order exponential fitting analysis method, the improved method is more suitable for the kinetic analysis of charge detrapping and trap distribution calculation. It could be able to obtain the energy level range and the density of shallow traps and deep traps simultaneously.

2. Using the improved trap distribution calculation method by double exponential fitting analysis of charge decay, it is not only can obtain the trap parameter changes caused by physical or chemical defects generated in material, but also can distinguish the shallow trap (physical defects) and deep trap (chemical defects). For oil impregnated insulation paper, the trap energy level and trap density representing deep traps is signal for ageing.
The trap density shows an increasing trend with the oil ageing, especially for the deep traps. The greater the energy that could be filled by the traps, the larger amount of charges could be trapped, especially under higher electric field strength. When one evaluating the ageing status of oil-paper insulation using trap parameters, the oil performance should not be ignored.

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Author Contributions: Jian Hao designed the experiments, improved the calculation method, did the space charge measurement and writing; Runhao Zou performed the space charge fitting; Ruijin Liao and Lijun Yang analyzed the data; Qiang Liao contributed discussion.

Conflicts of Interest: The authors declare no conflict of interest.

References
17. Liu, N.; Zhou, C.; Chen, G.; Xu, Y.; Cao, J.; Wang, H. Model to estimate the trapping parameters of cross-linked polyethylene cable peelings of different service years and their relationships with dc breakdown strengths. High Volt. 2016, 1, 95–105. [CrossRef]


29. Institute of Electrical and Electronics Engineers. IEEE Guide for Loading Mineral Oil Immersed Transformers; Institute of Electrical and Electronics Engineers: New York, NY, USA, 1996.


36. Sanghi, R. Chemistry behind the life of a transformer. Resonance 2003, 8, 17–23. [CrossRef]


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