Active Control of Drive Chain Torsional Vibration for DFIG-Based Wind Turbine

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Abstract: Due to the fast electric control of the doubly-fed induction generator (DFIG) when experiencing power grid disturbance or turbulent wind, the flexible drive chain of the wind turbine (WT) generates long-term torsional vibration, which shortens the service life of the drive chain. The torsional vibration causes fatigue damage of the gearbox and affects power generation. In this paper, a two-channel active damping control measure is proposed. The strategy forms a new WT electromagnetic torque reference value through two channels: one is a proportion integration differentiation (PID) damping term with frequency difference, which is used to reduce torsional vibration caused by frequency difference between fan and shafting; the other adopts the torsional vibration angle ($\theta_s$) as the feedback signal, and an additional damping term is formed by bandpass filter (BPF) and trap filter (BRF). The strategy can increase the electromagnetic torque and suppress the torsional vibration of the drive chain. Finally, modeling and simulation using MATLAB/Simulink show that the method can effectively suppress the torsional vibration of the drive chain without affecting power generation.

Keywords: torsional vibration; active control strategy; drive chain; electromagnetic torque; wind power generation; doubly-fed induction generator; wind turbine

1. Introduction

Wind power generation has been growing rapidly throughout the world in recent years, and the doubly-fed induction generator (DFIG) has become a mainstream wind turbine (WT) [1]. Due to the harsh environment of the WT and severe impact load, the failure rate of the WT is higher than other industrial fields; one of the serious problems is torsional vibration on the WT shaft [2]. Torsional vibration can cause significant stresses and fatigue loss of gearbox. In addition, torsional vibration of the mechanical components can be transmitted to electrical power oscillations, leading to potential resonances between WT and the power system. In severe cases, the WT will be damaged and lead to grid faults [3]. It can be seen that torsional vibration of the drive chain not only directly affects the safe operation of the WT, but also the stability of the network system. Therefore, reducing torsional vibration of the drive chain is particularly important and urgent.

In recent years, some scholars have done some research on control of the WT drive chain. Among other things, researchers studied the following: control of the DFIG by controlling the active and reactive power [4,5]; the control strategy under the grid fault of WT [6–8]; suppression of the torsional vibration by controlling the mechanical torque of the drive chain through pitch angle [9–12]; control of torsional vibration based on Small-Signal Analysis [13]; electromechanical oscillation damping [14]; and using the variable pitch system and converter as actuators to reduce the dynamic load of the WT to suppress torsional vibration of drive chain [15]. Although these methods have played a certain role in...
increasing damping and reducing torsional vibration, most of the research was on cases of grid faults or mechanical torque, and involve little about long-term low-amplitude and low-frequency torsional vibration of the drive chain during normal operation of the grid.

Based on the work of predecessors, this paper proposes a novel active control strategy to reduce the torsional vibration of the drive chain during normal operation of power grid. Since the inertia of the generator is much smaller than that of the WT, the dynamic change of the electromagnetic torque is more likely to cause severe vibration of the drive chain than the aerodynamic torque. Therefore, controlling the electromagnetic torque is the key to reducing torsional vibration of the drive chain and improving the reliability of the WT. In this paper, a two-channel active damping control measure is proposed, achieving the purpose of suppressing torsional vibration of the drive chain under the premise of ensuring the output power of the unit is stable.

2. Modeling of Wind Turbine

2.1. Structure of Wind Turbine

The drive chain of the doubly-fed WT studied in this paper is mainly composed of wind wheel, pitch control system, spindle front bearing, low speed shaft, gearbox, high speed shaft, generator, etc. (as shown in Figure 1). The mechanical energy absorbed by the wind wheel is transmitted to the gearbox through the low-speed shaft, and the high-speed shaft connects the high-speed output terminal of the gearbox with the generator. At the same time, the drive chain transfers the load to the tower barrel through the chassis and yaw system.

![Diagram of Structure of Wind Turbine](image)

**Figure 1.** Diagram of Structure of Wind Turbine.

2.2. Modeling of the Wind Wheel

The mathematical relation for the mechanical power extraction from the wind can be expressed as follows [16,17]:

\[
P_m = \frac{1}{2} C_p(\lambda, \beta) \rho \pi R^2 V^3
\]

(1)

\[
T_t = \frac{P_m}{\omega_m} = \frac{1}{2} A \rho V^2 C_p(\lambda, \beta) \frac{R}{\lambda}
\]

(2)

where \(P_m\) is the mechanical power (W) from the wind, \(T_t\) is the mechanical torque (N·m), \(\rho\) is the air density (kg/m³), \(A\) is the swept area by the WT rotor (m²), \(R\) is the blade radius (m), \(V\) is the wind speed (m/s), and \(C_p\) is the power coefficient (or performance coefficient), tip speed ratio is \(\lambda (\omega_m R/V)\), and blade pitch angle is \(\beta\) (deg), \(\omega_m\) is the angular speed of the WT (rad/s). The \(C_p\) curves [18] were calculated for different tip speed ratio (\(\lambda\)) and different blade pitch angle (\(\beta\)). The \(C_p - \lambda\) curves are shown in Figure 2.
The power coefficient \( C_p \) indicates how efficiently the conversion of wind power to rotational mechanical power is performed by the WT. The Betz limit is the maximum theoretic value reached by the power coefficient which is 0.59 for three blades horizontal axis WT (a more complete discussion can be find in [18]). The \( C_p \) curves are obtained experimentally by the manufactures following international rules.

In more generic analysis, the Equations (3) and (4) can be used to model the dynamics of the \( C_p \). The values of \( C_1-C_9 \) presented in Table 1 were suggested by Slootweg to represent the aerodynamics of a modern WT [19].

\[
C_p(\lambda, \beta) = C_1 \left( \frac{C_2 \lambda - C_3 \beta - C_4 \beta^3 C_5 - C_6}{\lambda + C_3 \beta} \right) e^{-\frac{C_7}{\lambda^3 + 1}} \tag{3}
\]

\[
\lambda_i = \frac{1}{\lambda + C_3 \beta - \frac{C_8}{\beta^3 + 1}} \tag{4}
\]

<table>
<thead>
<tr>
<th>( C_1 )</th>
<th>( C_2 )</th>
<th>( C_3 )</th>
<th>( C_4 )</th>
<th>( C_5 )</th>
<th>( C_6 )</th>
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<td>13.2</td>
<td>18.4</td>
<td>-0.02</td>
<td>-0.003</td>
</tr>
</tbody>
</table>

2.3. Drive Train Modeling

The impeller and generator rotor of a doubly fed WT are usually connected by a gearbox. Due to the existence of the gearbox, the flexibility of the entire shafting system is increased. In this paper, a two-mass model is used to simulate the flexible drive train system of a WT, which can accurately reflect torsional vibration of the drive chain. The two mass block shafting model equates impeller and hub as one mass block, and generator and gearbox as one mass block; the basic principle diagram is shown in Figure 3.

![Figure 3. Drive chain model block diagram.](image)
The WT low-speed shaft is converted to the high-speed side of the generator rotor by the gearbox, and the variables and parameters are still expressed by the symbols before the conversion. The mathematical model of the two-mass drive chain motion equation is as follows [20]:

\[
\begin{align*}
J_t \frac{d \omega_t}{dt} &= T_t - (k_g \theta_s + D_s (\omega_t - \omega_g)) \\
J_g \frac{d \omega_g}{dt} &= (k_g \theta_g + D_g (\omega_t - \omega_g)) - T_e
\end{align*}
\]

where \( J_t, J_g \) are the inertia of the impeller and the generator rotor (including the gearbox); \( \omega_t \) and \( \omega_g \) are angular velocity of impeller and generator rotor; \( T_t \) and \( T_e \) are mechanical torque and electromagnetic torque of WT; \( \theta_s \) is the torsion angle of the drive chain; \( D_s \) and \( K_s \) are damping coefficient and stiffness coefficient of drive chain, respectively.

Simplified (5) can obtain (6):

\[
\frac{J_t J_g}{J_t + J_g} \frac{d^2 \theta_s}{dt^2} + D_s \frac{d \theta_s}{dt} + K_s \theta_s = \frac{J_g T_t + J_t T_e}{J_t + J_g}
\]

Equation (6) is the differential equation of motion of the drive chain system, which can establish the state space equation of the drive chain based on the lumped mass method [20]:

\[
\begin{bmatrix}
\frac{d^2 \theta_s}{dt^2} \\
\frac{d \theta_s}{dt} \\
\frac{d \omega_s}{dt}
\end{bmatrix} =
\begin{bmatrix}
-(J_t + J_g) D_s & -J_g K_s & 0 \\
J_g & -J_g K_s & 0 \\
0 & 0 & -T_e
\end{bmatrix}
\begin{bmatrix}
\frac{d \theta_s}{dt} \\
\frac{d \omega_s}{dt}
\end{bmatrix} +
\begin{bmatrix}
\frac{1}{J_t} \\
\frac{1}{J_g}
\end{bmatrix}
\begin{bmatrix}
T_t \\
T_e
\end{bmatrix}
\]

(7)

In the Equations (7) and (8), the \( T_e \) is used as the control input, the \( T_t \) of the wind wheel is regarded as the disturbance input.

2.4. Dynamic Model of the DFIG

The generator stator of the doubly-fed WT is directly connected to the grid, and the generator rotor is connected to the grid through the back-to-back converter [21] (as shown in Figure 4). The mathematical model of doubly-fed generator in two-phase rotation coordinate system (d-q frame) is studied and oriented the stator flux [22] (\( \phi_{ad} = \phi_s, \phi_{aq} = \phi_i, \phi_{dq} = 0, \phi_{dq} = 0 \)).

The classical electrical equations of the DFIG in the Park frame are addressed in [23], Lennart [23] and Tapia [24] given as follows:

\[
\begin{align*}
\frac{d \phi_{sd}}{dt} &= V_{sd} - R_s i_{sd} + \varphi_{sq} \omega_s \\
\frac{d \phi_{sq}}{dt} &= V_{sq} - R_s i_{sq} + \varphi_{iq} \omega_s \\
\frac{d \phi_{rd}}{dt} &= V_{rd} - R_r i_{rd} + \varphi_{rq} \omega_r \\
\frac{d \phi_{rq}}{dt} &= V_{rq} - R_r i_{rq} + \varphi_{dq} \omega_r
\end{align*}
\]

(9)

where the stator and rotor angular velocities are linked by the following relation:

\[
\omega_r = \omega_s - \omega
\]

(10)

\( V_{sd} - V_{sq} \) and \( V_{rd} - V_{rq} \) are the stator and rotor d-q axes voltages, respectively; \( R_s \) and \( R_r \) are the stator and rotor phase resistances, respectively.
where \( L_s = L_f + L_m, L_r = L_f + M^2 L_m \).

The stator and rotor flux can be expressed as follows:

\[
\begin{align*}
\varphi_{sd} &= L_s i_{sd} + M i_{rd} \\
\varphi_{sq} &= L_s i_{sq} + M i_{rq} \\
\varphi_{rd} &= L_r i_{rd} + M i_{sd} \\
\varphi_{rq} &= L_r i_{rq} + M i_{sq}
\end{align*}
\]  

(11)

where \( L_s = L_f + L_m, L_r = L_f + M^2 L_m \).

Where \( i_{sd} - i_{sq} \) and \( i_{rd} - i_{rq} \) are the stator and rotor \( d-q \) axes currents, respectively; \( \varphi_{sd} - \varphi_{sq} \) and \( \varphi_{rd} - \varphi_{rq} \) are the stator and rotor \( d-q \) axes fluxes, respectively; \( L_s, L_m, \) and \( L_r \) are the stator, magnetizing, and rotor inductances, respectively; \( \varphi_s \) and \( \varphi_r \) are damping, respectively; The stator and rotor active and reactive powers are given, respectively, by Equations (12) and (13):

\[
\begin{align*}
P_s &= \frac{3}{2} (V_{sd} i_{sd} + V_{sq} i_{sq}) \\
Q_s &= \frac{3}{2} (V_{sq} i_{sd} - V_{sd} i_{sq})
\end{align*}
\]  

(12)

\[
\begin{align*}
P_r &= \frac{3}{2} (V_{rd} i_{rd} + V_{rq} i_{rq}) \\
Q_r &= \frac{3}{2} (V_{rq} i_{rd} - V_{rd} i_{rq})
\end{align*}
\]  

(13)

In the rotating field reference frame, the \( d-q \) orientation has to be synchronized with the stator flux [25] (see in Figure 5):

The electromagnetic torque is given by [26, 27]:

\[
T_e = \frac{3}{2} \frac{M}{L_s} (i_{rd} \varphi_{sq} - i_{rq} \varphi_{sd})
\]  

(14)

where \( T_e \) is electromagnetic torque; and \( p \) is number of poles. Basic equation of motion control systems is expressed as [28].

\[
f \frac{d\omega_m}{dt} + D \omega_m + K \theta_m = T_e - T_m
\]  

(15)

with

\[
\frac{d\theta_m}{dt} = \omega_m
\]

where \( J \) is the mechanical moment of inertia (kg \( \cdot \) m\(^2\)) ; \( \omega_m \) and \( \theta_m \) are the mechanical angular speed of rotor (rad/s) and mechanical angle of rotor (rad), respectively; \( T_e \) and \( T_m \) are the electromagnetic torque (N-m) and load torque (N-m), respectively; \( D \) and \( K \) are the resistance torque damping coefficient and torsional elastic torque coefficient, respectively.
with proportion integration differentiation (PID) [29] control, the torsion angle ($\theta_t$) is used as the feedback signal to increase the electromagnetic torque through the torsional load controller, and achieve the purpose of suppressing the torsional vibration under the premise of ensuring the output power of the unit is stable.

3. Active Control Approach

This paper proposed a new control strategy of torsional vibration during normal operation of the power grid. Based on proportion integration differentiation (PID) [29] control, the torsion angle ($\theta_t$) is used as the feedback signal to increase the electromagnetic torque through the torsional load controller, and achieve the purpose of suppressing the torsional vibration under the premise of ensuring the output power of the unit is stable.

3.1. Characteristic Analysis of Torsional Vibration

According to the two-mass block model of the drive chain shown in Equation (5), the motion equation of the impeller relative to the angular displacement $\theta_s$ of the generator rotor can be obtained in [30]:

$$\frac{d^2 \theta_s}{dt^2} + D_s \left( \frac{1}{J_t} + \frac{1}{J_g} \right) \frac{d \theta_s}{dt} + K_s \left( \frac{1}{J_t} + \frac{1}{J_g} \right) \theta_s = \frac{T_n}{J_t} + \frac{T_e}{J_g}$$  \hspace{1cm} (17)

The above formula shows that $\theta_s$ moves in the form of second-order oscillation. The poles of the equation of motion are as follows:

$$\lambda_{1,2} = -\xi \omega_n \pm j \omega_\xi$$

where, $\omega_n = \sqrt{K_s \left( \frac{1}{J_t} + \frac{1}{J_g} \right)}$ is the natural oscillation frequency of drive chain, $\xi = \frac{D_s}{2 \sqrt{K_s} \sqrt{\left( \frac{1}{J_t} + \frac{1}{J_g} \right)}}$ is the damping ratio of the drive chain, $\omega_\xi = \omega_n \sqrt{1 - \xi^2}$ is the actual oscillation frequency after considering the system damping. It can be seen that the actual torsional vibration frequency of the drive chain is closely related to the parameters $D_s, K_s, J_t, J_g$ of the system.
Through Formula (17), the transfer function with \( T_t \) and \( T_e \) as input variables can be further derived, as shown in Formula (18) and (19).

\[
\frac{\theta_s(s)}{T_t(s)} = \frac{1}{J_t s^2 + 2\xi\omega_n s + \omega_n^2}
\]

\[
\frac{\theta_s(s)}{T_e(s)} = \frac{1}{J_g s^2 + 2\xi\omega_n s + \omega_n^2}
\]

Based on the transfer functions shown in Equations (18) and (19), the frequency domain characteristics of the drive chain from \( T_t \) and \( T_e \) to \( \theta_s \) can be obtained (as shown in Figure 6). It can be seen that whether the input quantity is electromagnetic torque disturbance or mechanical torque disturbance, the amplitude gain of the drive chain near the resonance frequency is very high, that is, both inputs can excite the drive chain torsional vibration. Meanwhile, it also can be seen the magnitude of the drive chain system with electromagnetic torque as input at the resonance frequency is larger than the mechanical torque, so the disturbance of electromagnetic torque will cause more serious torsional vibration.

![Bode Diagram](image)

**Figure 6.** Frequency domain characteristics of \( \frac{\theta_s(s)}{T_t(s)} \) and \( \frac{\theta_s(s)}{T_e(s)} \).

### 3.2. Control Principle of Drive Chain

On the basis of PID control, adding a torque feedback loop connected by a bandpass filter (BPF) and a trap filter (BRF) achieves two-channel active damping control, additional torques \( T_{\text{damp}1} \) and \( T_{\text{damp}2} \) are added near the natural vibration frequency of the drive chain. The main function of BPF is to produce ripple torque. The BRF is mainly to avoid the multi-section traversing frequency of wind wheel speed, such as 3P, 6P, and other frequencies. After the PID control, the deviation of the system is quickly and accurately eliminated, and the set value is restored, which makes the oscillation and deviation of the system smaller.

In the torsional vibration control of WT drive chain, the change of generator’s torque will have a great influence on its speed and output power. If the change of generator’s torque is too large, it may cause the instability of the system. So the \( T_{\text{damp}1} \) and \( T_{\text{damp}2} \) should be limited to a certain range, and then superimposed on the original torque reference value. Based on this principle, combined with the state space equation given in (7), the drive chain damping control strategy is shown in Figure 7.
Figure 7. Block Diagram of Drive Chain Damping Control.

It can be seen that the torque reference $T_e^*$ contains three parts, as shown in the following equation:

$$T_e^* = T_{gen}^* + T_{damp1} + T_{damp2}$$  (20)

$T_{gen}^*$ is the given value of the torque control, $T_{damp1}$ and $T_{damp2}$ are the compensation electromagnetic torque. The $T_{damp1}$ is obtained by series connection of a BPF and a BRF. The $T_{damp2}$ is obtained by PID. The transfer functions between a BPF and a BRF are as follows:

$$G_{BPF}(s) = \frac{K_2\zeta_f\omega s(1 + \tau s)}{s^2 + 2\zeta_f\omega s + a^2}$$  (21)

$$G_{BRF}(s) = \frac{K(s^2 + \omega^2)}{s^2 + 2\zeta\omega s + \omega^2}$$  (22)

In the formula, $K$ is the control gain, $\zeta_f$ is the filter damping ratio, and $\omega$ is the center frequency. Sometimes, in order to compensate for the time lag in the design of the control system, a differential calculus $(1 + \tau s)$ is added to the BPF, but the time constant $\tau$ is usually close to 0.

$$K = \left(\frac{\zeta_{tot}}{\zeta} - 1\right)\sqrt{\frac{1}{J_t} + \frac{1}{J_g}}$$  (23)

where

$$\zeta = \frac{D_s}{2\sqrt{K_g}} \sqrt{\frac{1}{J_t} + \frac{1}{J_g}}$$

In the formula, $\zeta$ (0.25 in paper) and $\zeta_{tot}$ are the inherent damping ratio of the drive chain system and the damping ratio after increasing the damping control, respectively.

4. Simulation Results

In order to verify the active control strategy proposed in this paper, modeling and simulation for the drive chain of 1.5 MW doubly-fed WT in MATLAB/Simulink. The parameters of WT are shown in Table 2.

According to the two mass modeling given in chapter 2, the drive chain model is built. The drive chain specific parameters are shown in Table 3.
Table 2. Wind turbine parameters of 1.5 MW doubly-fed.

<table>
<thead>
<tr>
<th>Category</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Type of Wind Turbines</td>
<td>Doubly-fed wind turbine</td>
</tr>
<tr>
<td>Rated power</td>
<td>1.5 MW</td>
</tr>
<tr>
<td>Number of blades</td>
<td>3.0</td>
</tr>
<tr>
<td>Rated speed</td>
<td>18.0 r/min</td>
</tr>
<tr>
<td>Wind wheel diameter</td>
<td>70.0 m</td>
</tr>
<tr>
<td>Power regulation</td>
<td>Variable pitch angle and speed</td>
</tr>
<tr>
<td>Cutting into the wind</td>
<td>3.5 m/s</td>
</tr>
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<td>Cutting out the wind</td>
<td>25.0 m/s</td>
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<tr>
<td>Rated wind speed</td>
<td>16.0 m/s</td>
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Table 3. Drive chain parameters of 1.5 MW double-fed WT.

<table>
<thead>
<tr>
<th>Category</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wind wheel moment of inertia ($J_t$)</td>
<td>$4.45 \times 10^6$ kg·m²</td>
</tr>
<tr>
<td>Generator moment of inertia ($J_g$)</td>
<td>$8.45 \times 10^5$ kg·m²</td>
</tr>
<tr>
<td>Damping of drive chain ($D_s$)</td>
<td>$1.72 \times 10^5$ N·m/rad</td>
</tr>
<tr>
<td>Stiffness of drive chain ($K_s$)</td>
<td>$3.03 \times 10^8$ N·m/rad</td>
</tr>
</tbody>
</table>

According to the active control strategy introduced in chapter 3, the transfer functions of BPF and BRF are designed as follows:

$$G_{BPF} = \frac{6.16}{s^2 + 6.16s + 236.97}$$

$$G_{BRF} = \frac{s^2 + 29.89}{s^2 + 2.19s + 29.89}$$

(24)
(25)

According to (24) and (25), the corresponding Bode diagrams are obtained, as shown in Figure 8.

![Bode diagram](image)

Figure 8. Bode diagrams (a,b) are bandpass filter (BPF) and trap filter (BRF), respectively.

4.1. Simulation and Analysis under Constant Wind Speed (16 m/s)

Unless otherwise specified, all the simulations in this paper are carried out under the Per-unit value. At a constant wind speed (16 m/s), the simulation time is set to 6 s, the results are as follows in Figure 9.
Figure 9. Cont.
Figure 9. Simulation results under constant wind speed (16 m/s). (a) Wind speed ($\omega t$) 16 m/s; (b) Output mechanical torque on the shaft ($T_{\text{shaft}}$); (c) Torsion vibration angle ($\theta_s$); (d) Electromagnetic torque reference value ($T_{e}^*$); (e) The given value of the electromagnetic torque ($T_{\text{gen}}^*$); (f) Active power ($p$).

Under constant wind speed (16 m/s), the simulation results Figure 9a–c show that the effect of suppressing the torsional vibration of the drive chain is not obvious only with the PID, the strategy of combined control of PID and torsional load proposed in this paper has a good effect on suppressing the torsional vibration of the drive chain. Simulation results Figure 9d–f show that the simulation curves of $T_{\text{gen}}^*$ and active power are basically coincident with only PID regulation, and PID regulation and torsional load control are combined; it shows that the control strategy proposed in this paper can effectively suppress the torsional vibration of the drive chain without affecting the power output.

4.2. Simulation and Analysis under Turbulent Wind

In the turbulent wind condition, the same simulation time is set to 6 s, and the simulation results are shown in Figure 10.

Under turbulent wind conditions, it can be seen from Figure 10a–c that the torsional vibration of the drive chain is also effectively suppressed and has similar control effects with constant wind speed, indicating the control strategy proposed in this paper also has good control effect under complex wind conditions and has universal applicability. It can be seen from Figure 10d–f that the simulation curves of electromagnetic torque and active power are basically coincident with only PID regulation, and PID regulation and torsional load control are combined. It shows that the control strategy proposed in this paper can effectively suppress the torsional vibration of the drive chain without affecting the power output.
Figure 10. Cont.
Figure 10. Simulation Results under Turbulent wind. (a) Turbulent wind; (b) Output mechanical torque on the shaft ($T_{\text{shaft}}$); (c) Torsion vibration angle ($\theta_\text{s}$); (d) The electromagnetic torque reference value ($T_e^*$); (e) The given value of the electromagnetic torque ($T_{\text{gen}}^*$); (f) Active power ($p$).

4.3. Under Constant Wind Speed (16 m/s) and Turbulent Wind

Under different wind speeds, in order to verify the control effect of the PID regulation and torsional load combined control strategy proposed in this paper, this section puts the simulation figure of constant wind speed (16 m/s) and turbulent wind in the same coordinate system, and simulation time is set to 6 s, as shown in Figure 11.

Figure 11a shows that the $T_{\text{shaft}}$ of the drive chain will be different under different wind conditions, but under the PID regulation and torsional load combined control strategy, the turbulent wind condition $T_{\text{shaft}}$ fluctuates near the constant wind condition. Figure 11b shows that the torsional vibration will be more serious in turbulent wind due to the uncertainty of the wind condition. However, under the PID regulation and torsional load combined control strategy, the turbulent wind condition $\theta_\text{s}$ fluctuates near the constant wind condition. Figure 11c shows that $T_e^*$ will be different due to different wind conditions, through the control strategy, the turbulent wind condition $T_e^*$ fluctuates near the constant wind condition. The constant wind condition only verifies the control performance of ideal conditions, and cannot be closer to reality, in order to be closer to the actual wind conditions under turbulence, the control strategy is verified. From the above results can be seen that the active control strategy proposed in this paper can effectively reduce the torsional vibration of drive chain under different wind conditions.
Figure 11. Simulation Results under constant wind speed and turbulent wind. (a) Output mechanical torque on the shaft \( T_{\text{shaft}} \); (b) Torsion vibration angle \( \theta_s \); (c) The electromagnetic torque reference value \( T_{e}^* \).

5. Conclusions

Aiming at a drive chain of a doubly fed WT with small damping and that is susceptible to torsional vibration load, a two-mass model of the drive chain is established. Through frequency domain analysis of the torsional vibration characteristics of the drive chain, it is found that the electromagnetic torque
disturbance can cause more serious torsional vibration of the drive chain than the mechanical torque. In order to reduce torsional vibration of the drive chain during the normal operation of the power grid, a torsional load controller based on BPF and BRF is designed with the \( \theta \) as feedback signal; combining PID and torsional load controller, a two-channel active damping control measure is proposed to suppress the torsional vibration of drive chain. The simulation results show that the control strategy proposed in this paper has better restraint effect on the torsional vibration of drive chain than with only PID, and the strategy has better adaptability when the input wind speed is uncertain, at the same time, it has no effect on the power output.

**Author Contributions:** M.L. designed the principles of the overall work and edited the final draft of paper; Z.L. realized MATLAB-based simulation and prepared the initial draft of paper; S.T. contributed significantly in writing the paper, Y.Z. and H.L. proposed some technical comments and edited the initial draft of paper.

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**Conflicts of Interest:** The authors declare no conflict of interest.

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