A Risk Assessment Model of Coalbed Methane Development Based on the Matter-Element Extension Method

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Abstract: Coalbed methane development represents a complex system engineering operation that involves complex technology, many links, long cycles, and various risks. If risks are not controlled in a timely and effective manner, project operators may easily cause different levels of casualties, resource waste and property loss. To evaluate the risk status of coalbed methane development projects, this paper constructs a coalbed methane development risk assessment index system that consists of six first grade indexes and 45 second grade indexes. The weight of each index is calculated based on the structure entropy weight method. Then, a theoretical model for risk assessments of coalbed methane development is established based on the matter-element extension method. Finally, the model is applied to analyze a coalbed methane development project in the southern Qinshui Basin of China. The results show that the overall risk level of the coalbed methane development project is Grade II, indicating that the overall risk of the project is small, but the local risk of the project needs to be rectified in time. The assessment results are consistent with the actual operation of the project, indicating that the established risk assessment model has good applicability and effectiveness.

Keywords: coalbed methane development; risk assessment; structural entropy weight method; matter-element extension method

1. Introduction

With the rapid development of the global economy and the continuous advancement of urbanization, national dependence on black fossil energy, such as coal and oil, has increased. However, this increased dependence has caused excessive emissions to the atmosphere of toxic and harmful substances, such as carbon dioxide, sulfur dioxide, carbon monoxide and soot. These problems have caused environmental pollution problems, such as greenhouse effects, acid rain and haze, which have seriously affected the quality of life and health of residents. The above situation has received the attention of many actors, including the Chinese government. To achieve a balance between economic development and environmental protection, China’s energy use structure is changing to a pattern of “high efficiency, low energy consumption, low pollution and low emissions” under the leadership of the government [1].

In this context, coalbed methane (CBM) has become a prominent resource. CBM is mainly composed of methane that is stored in coal seams, adsorbed on the surface of coal matrix particles, partially free in coal pores or dissolved in coal seam water hydrocarbon gas. It is an associated mineral resource of coal and unconventional natural gas, and it is also a clean and high-quality energy source. China is a large coal mining country that experiences frequent gas explosions [2]. Since 1949,
126 severe gas explosion accidents (defined as killing 30 or more people in one accident) have occurred, and 7,502 people have died [3]. These accidents have not only caused serious casualties and property losses, but have also had a serious negative impact on society [4,5]. The development of CBM can not only improve environmental pollution [6], but also fundamentally reduce the methane content in the coal seam, which is beneficial to reducing the occurrence of coal mine gas explosions [7–9]. These advantages have driven CBM development as a component of the new energy industry and ushered it into a golden development period [1]. However, CBM development represents a complex system engineering operation that involves complex technology, many links, long cycles, and various risks. CBM development is highly susceptible to various risks, such as economic, legal, technological, and management risks, and risk control failure can result in casualties, resource waste and property losses. To avoid these risks and promote the steady development of the CBM industry, it is necessary to first understand and perceive the risks throughout the life cycle of CBM development via risk assessment research.

At present, achievements have been made in the research on CBM development risk assessment. Roadifer et al. [10] evaluated the future trends and risks of CBM development and identified the key factors affecting CBM reserves and productivity by combining experimental and mathematical-statistical methods. Senthi et al. [11] used Monte Carlo simulations and the hypercube model to evaluate the economic risks faced by the CBM industry. Chen et al. [12] also used the Monte Carlo simulation method to establish a risk transformation process model of the main uncertain factors in the CBM economy. Zhang et al. [13] determined the optimal index weights using the optimized combination entropy method and the triangular fuzzy number method and established a CBM development potential assessment model. Acquah-Andoh et al. [14] explored the best schemes for optimizing a company’s revenue share for CBM development contracts based on factor analysis, discounted cash flow and parameter sensitivity analysis and found that the best scheme can distribute the economic risks of CBM development between governments and contractors. Luo et al. [15] used the net present value method to evaluate the economics of CBM production in China and found that the CBM price, productivity and operating costs are the three main factors affecting the economic feasibility of CBM development. Mares et al. [16] found that the uncertainty of adsorption capacity and desorption capacity were two important factors affecting the commercial development of CBM development, and their study provides a reference for the economic risk assessment of CBM development. Mu et al. [17] believed that three aspects are of great significance for avoiding CBM development risks: Pre-evaluation of CBM development, geological and gas reservoir engineering research and engineering technological innovation. Kirchgessner et al. [18] believed that safety and environmental factors also affect the economic benefits of CBM recovery. Su et al. [19] improved the discounted cash flow method by performing a hierarchical differentiation evaluation, staged evaluation and dynamic evaluation. It is also believed that production has the greatest impact on the economics of CBM development.

In summary, although scholars have made some achievements in the research on CBM development risks, the following shortcomings are observed:

(1). Most studies focus on economic risk factor analyses of the national CBM industry. At present, risk assessment research for CBM development projects has not provided a reference for investors, insurance companies and CBM development operators.

(2). Although several researchers have studied the risk of CBM development projects, the research depth was insufficient because the studies only determined the weight of the CBM risk assessment indicators. These studies used the weights to identify the main risk factors of CBM development, but failed to quantitatively measure the overall risk levels of CBM development projects and calculate the membership degree of each bottom index.

(3). In terms of the construction of the indicator system, the above studies lack a systematic and comprehensive indicator selection process and did not cover the life cycle of CBM development, including geological exploration, drilling, gathering, and market applications. Therefore, the research results have a certain one-sidedness.
To fill the above gaps and achieve a reasonable assessment of the risk status of coalbed methane development projects, this paper will construct a risk assessment model for coalbed methane development. First, this paper seeks to construct a complete risk assessment index system for CBM development, including the laws, regulations and policies, resource characteristics, engineering technology and organizational management, according to the risk characteristics involved in the life cycle of CBM development.

Second, to scientifically determine the weight of each index, the weight calculation method should be chosen reasonably. The AHP, Delphi method and expert experience are commonly used methods to determine the index weights in risk assessment, and the AHP is the most widely used method [20]. However, the disadvantage of AHP is that if the index system contains a large number of indexes, it will greatly increase the workload of experts, which affects the acquisition of the judgment matrix, and thus, affects the accuracy of the weight calculation. Compared with the AHP, the structure entropy weight method (SEWM) can reduce a large amount of the computational workload and obtain more accurate results in the case of a large number of indexes. The SEWM combined the methods of subjective and objective assignments, as well as qualitative and quantitative analysis [21]. The main steps of the SEWM include: (1) Collecting experts’ comments and forming the typical order; (2) analyzing the blind degree (uncertainty) of indexes; (3) normalized treatment of indexes; and (4) determining the index weight of each layer. Please refer to Section 2.2 for the specific calculation process.

Third, scientifically assess the risk of CBM development, and the assessment method should be rationally selected. The risk assessment method in this paper is based on the matter-element extension method (MEEM). Because MEEM is a method for multi-index comprehensive assessment and mainly based on the extrinsic matter-element model, extension set and correlation function theory [22], the method can judge the membership level of things according to different characteristics of the elements and less data and can avoid the randomness and subjectivity of the evaluation process to a certain extent. It is a combination of qualitative and quantitative methods. At present, this method has achieved good results in risk assessment in many fields, such as oil exploitation [23], tailings pond [24], and building fire [25]. The main steps of the MEEM include the following: (1) Determining the classical domains, joint domains, and matter elements; (2) calculating the correlation degrees; (3) assessing multi-level extension; and (4) classifying risk. Please refer to Section 2.3 for the specific calculation process. Finally, this paper will conduct a case study to verify the feasibility of the risk assessment model.

The main contents of this paper include the following parts: Section 1 introduces the research significance, research purposes, literature review and current deficiencies in the field of coalbed methane development risk research. Section 2 introduces the research steps of the article, constructs the risk assessment index system of coalbed methane development, introduces the calculation steps of the structural entropy weight method and uses this method to calculate the index weight, and then introduces the calculation process of the matter-element extension method. Section 3 conducts a case study to verify the validity of the evaluation model. Section 4 analyses and discusses the assessment results. Section 5 summarizes the conclusions of the article.

2. Methodology

This study follows four steps: (1) The key risk factors involved in the life cycle of CBM development were identified through literature analysis, field investigation, legal norm inquiry and expert consultations. Thus, the risk assessment index system of CBM development was determined; (2) The SEWM was used to determine the weight of each index; (3) Based on the MEEM, a theoretical model of risk assessment was constructed. The risk classification rules were determined; (4) A case study was implemented. The main research steps involved in this paper are shown in Figure 1.
Figure 1. Steps of the present study. CBM, coalbed methane.

The four steps are described as follows:

Step 1: Build a targeted risk assessment index system for CBM development. First, the status quo of risk assessment and the key influencing risk factors of CBM development were achieved through on-site investigation, reading relevant literature and visiting the insurance company and a third-party risk assessment institution. On this basis, a preliminary risk assessment index system was established. Some experts from consulting organizations, management departments, and research institutions engaged in CBM development were invited to evaluate the preliminary index system. According to the experts’ suggestions, this system mainly focused on the risks involved in geological resource exploration, drilling and drainage, gathering and transportation and market operations. Six main aspects, namely, laws and policies, resource characteristics, engineering technology, economic operation, organization and management, and safety and emergency protection, were covered. Finally, the first-level indexes were refined to the second-level indexes; thus, the risk assessment index system used in the CBM development was established.

Step 2: After the index system was determined, an index weight was assigned to all indexes in each layer. However, using the traditional analytic hierarchy process (AHP) method to assign the index weights would greatly increase the experts’ workload. Therefore, this paper introduced a new method, the SEWM, to assign the index weights. This method combines the methods of subjective and objective assignments via qualitative and quantitative analyses. The detailed principles and application method of the SEWM will be explained in Section 2.2.1.

Step 3: For quantitative risk assessment, this paper established a theoretical model of risk assessment based on the MEEM. The model covers four parts: (1) Determining classical domains,
sections, and matter elements; (2) calculating correlation degrees; (3) assessing multi-level extension; and (4) classifying risk. The detailed calculation steps will be described in Section 2.3.

Step 4: Case study. A CBM development project in the southern part of the Qinshui Basin in China was chosen for the case study to verify the feasibility of the assessment system.

2.1. Construction of the CBM Development Risk Assessment Index System

2.1.1. Principle

To reflect the risks of CBM development accurately and objectively, the scientific basis, guidance, operability, systematic process, comparability and comprehensiveness were considered to establish the index system in this paper.

2.1.2. Construction of Index System

Life cycle theory has been widely used in many fields, such as economics [26], environmental research [27], and management research [28]. The basic meaning of the life cycle can be understood as the whole process from “cradle to grave”. For a product, the life cycle is the process of returning to nature from nature, which includes not only raw material collection and processing, but also the product storage, transportation and sales. According to the above definition, this paper divides the life cycle of CBM development into three main stages: Resource exploration, resource exploitation, and gathering and market operation. The risk characteristics of these three stages were analyzed, and the risk factors were summarized into the following six categories: (1) Risks of laws, regulations and policies; (2) risks of resource characteristics; (3) risks of engineering and technology; (4) risks of economic operations; (5) risks of organization and management; and (6) risks of safety and emergency protection.

Second, these six types of risks are used as first grade indexes, which are then refined to second grade indexes through an on-site investigation and a literature review [10–13,15–19,29–37] and related laws and regulations. The laws and regulations include the “Mineral Resources Law of the People’s Republic of China” [38], “Coalbed Methane Industry Policy” [39], “Safety Production Law of the People’s Republic of China” [40], and “Hazardous Chemicals Safety Management Regulations” [41]. Third, the index system was revised through expert consultation. Finally, the assessment index system of CBM development risk was determined (Figure 2), and it consisted of six first grade indexes and 45 second grade indexes. For a detailed index analysis, please refer to Appendix A.
2.2. Determination of Index Weights

To accurately calculate the weight of each index, a reasonable weight calculation method should be selected. The AHP, Delphi method and expert experience are commonly used methods to determine the index weights in risk assessment, and the AHP is the most widely used method [20]. Because many indexes are included in the proposed index system, the use of the AHP to determine the index weight would entail a large workload, which would not be conducive to acquiring the judgement matrix. Therefore, this paper introduced the SEWM to determine the index weight of the CBM development risk assessment system. The SEWM combines subjective and objective assignment methods, as well as qualitative and quantitative analyses. This method can reduce the calculation workload and achieve higher accuracy, especially for the many indexes in the CBM development risk assessment system.

2.2.1. Principle of the SEWM

The basic idea of the SEWM is to analyze the indexes of the assessment system and the interrelationship between them and then to classify the indexes into independent hierarchical grades. The execution steps are as follows.

(1). Collection of experts’ comments

Several experts were invited to complete the questionnaire form (Table 1) in accordance with the procedure and requirements of the Delphi method [42]. The experts ranked the importance of each index independently according to their own knowledge and experience. The indexes were ranked from high to low according to their importance; for example, mark “1” represented “most important”, mark “2” represented “more important”, mark “3” represented “important”, and so on. Some indexes could be recognized as equally important, and the final rank of the indexes could be discussed by the experts.
Table 1. Collection of experts’ comments.

<table>
<thead>
<tr>
<th>Index1</th>
<th>Index2</th>
<th>Index3</th>
<th>Index4</th>
<th>Index5</th>
<th>...</th>
</tr>
</thead>
<tbody>
<tr>
<td>Expert1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Expert2</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Expert3</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Expert4</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>...</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

(2). Blind degree (uncertainty) analysis

The potential deviation and uncertainty of the experts’ comments on the index ranks might arise, due to noisy data. To eliminate noisy data and reduce uncertainty, the qualitative judgement conclusion from the experts should be statistically analyzed and addressed. To reduce the uncertainty of the experts’ ranking, the entropy value was calculated by the entropy theory. The execution steps are shown below [21,43].

Supposing that \(k\) experts were invited to take the questionnaire survey, then \(k\) questionnaire forms would be returned, and every form would be recognized as an index set and marked as \(R=\{r_1, r_2, ..., r_l\}\); where \(r_i\) refers to the expert ranking array denoted by \(\{a_{i1}, a_{i2}, ..., a_{in}\}\) (\(i=1, 2, ..., k\)) and \(a_{i1}, a_{i2}, ..., a_{in}\) can be any natural number from \(\{1, 2, ..., n\}\). As previously mentioned, “1” represents the highest level of importance. The index sort matrix obtained from the \(k\) table is shown as matrix \(A\).

\[
A = \begin{bmatrix}
a_{11} & a_{12} & a_{13} & \cdots & a_{1n} \\
a_{21} & a_{22} & a_{23} & \cdots & a_{2n} \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
a_{k1} & a_{k2} & a_{k3} & \cdots & a_{kn}
\end{bmatrix}
\] (1)

where \(a_{ij}\) represents the \(i\)th expert’s evaluation of the \(j\)th index.

The qualitative ranking result could be transformed into quantitative results by a membership function, which can be defined as follows:

\[
\chi(I) = \lambda p_n(I) \ln p_n(I),
\] (2)

where \(p_n(I) = \frac{m-I}{m-1}\), \(\lambda = \frac{1}{\ln(m-1)}\), which can be input into Equation (2):

\[
\chi(I) = \frac{1}{\ln(m-1)} \left(\frac{m-I}{m-1}\right) \ln \left(\frac{m-I}{m-1}\right).
\] (3)

Dividing both sides by \((m-I)/(m-1)\), assume that \(1-\chi(I)/(m-1)/(m-1)\approx\mu(I)\). Then,

\[
\mu(I) = \frac{\ln(m-I)}{\ln(m-1)}.
\] (4)

where \(I\) is defined as the qualitative ranking number of a certain index evaluated by an expert. For example, a set of qualitative ranking numbers 5, 2, 3, 4, 1 for the five indexes \(r_1, r_2, r_3, r_4, r_5\) was evaluated by one expert. Thus, index \(r_5\) was the most important, because \(I = 1\). \(M\) is the transformation parameter and defined as \(m = j + 2\), and \(j\) is the number of indexes.

The qualitative ranking number \(I\) is input into Equation (4) to obtain the quantitative transformation value of \(b_{ij}\). \(B_{ij} = \mu(a_{ij})\) is the membership degree of the qualitative ranking number \(I\), and the matrix \(B = (b_{ij})_{n,n}\) is defined as the membership degree matrix. A new parameter, average understanding degree \(b_{ij}\), was introduced to present the consistency degree of the evaluation of index \(r_j\) by \(k\) experts; its calculation is as follows:

\[
b_{ij} = \frac{b_{1j} + b_{2j} + \cdots + b_{kj}}{k}.
\] (5)

Blind understanding degree \(\sigma_{ij}\) is defined as the uncertainty of the evaluation of index \(r_j\) by \(k\) experts,
\[ \sigma_j = \left[ \max(b_{j1}, b_{j2}, \ldots, b_{jk}) - b_j \right] + \left[ b_j - \min(b_{j1}, b_{j2}, \ldots, b_{jk}) \right] / 2. \]  

\[ \text{The global understanding degree } X_j \text{ is defined as the degree of the evaluation of every index } r_j \text{ by all } k \text{ experts invited,} \]

\[ X_j = b_j (1 - \sigma_j). \]  

2. Normalized treatment

To obtain the weight of index \( r_j \), Equation (7) needs further normalized treatment,

\[ a_j = X_j / \sum_{j=1}^{k} X_j. \]

Obviously, \( a_j > 0 \) and \( \sum_{j=1}^{k} a_j = 1 \). The \( a = (a_1, a_2, \ldots, a_k) \) was expressed as the weight vector of the index set \( R = (r_1, r_2, \ldots, r_k) \).

2.2.2. Calculation of the Index Weight

In this study, a total of 12 experts who have worked in the CBM development industry for a long time, including three experts in CBM resource exploration, three experts in CBM mining technology, two experts in coal economy, two experts in energy policy, and two managers of CBM development enterprises. To more comprehensively formulate risk assessment criteria from multiple perspectives, the experts were randomly divided into four groups, each with three persons. In this way, the diverse understandings of various research fields could be fully explored, and different knowledge and experience could be used to perform a qualitative evaluation of each assessment index.

The weight determination of the indexes in the first grade was taken as an example:

(1). The rank results from the four groups of experts were collected in Table 2:

<table>
<thead>
<tr>
<th>Index ( r_1 )</th>
<th>Index ( r_2 )</th>
<th>Index ( r_3 )</th>
<th>Index ( r_4 )</th>
<th>Index ( r_5 )</th>
<th>Index ( r_6 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Group A</td>
<td>4</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>6</td>
</tr>
<tr>
<td>Group B</td>
<td>3</td>
<td>1</td>
<td>1</td>
<td>2</td>
<td>5</td>
</tr>
<tr>
<td>Group C</td>
<td>3</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>5</td>
</tr>
<tr>
<td>Group D</td>
<td>4</td>
<td>2</td>
<td>1</td>
<td>3</td>
<td>6</td>
</tr>
</tbody>
</table>

(2). The obtained rank matrix \( A \):

\[ A = \begin{bmatrix}
4 & 1 & 2 & 3 & 6 & 5 \\
3 & 1 & 1 & 2 & 5 & 4 \\
3 & 1 & 2 & 3 & 5 & 4 \\
4 & 2 & 1 & 3 & 6 & 5
\end{bmatrix} \]

(3). The calculated membership matrix \( B \) was based on Equation (4) and rank matrix \( A \), and \( m \) was set as 8.

\[ B = \begin{bmatrix}
0.712 & 1.000 & 0.921 & 0.827 & 0.356 & 0.565 \\
0.827 & 1.000 & 1.000 & 0.921 & 0.565 & 0.712 \\
0.827 & 1.000 & 0.921 & 0.827 & 0.565 & 0.712 \\
0.712 & 0.921 & 1.000 & 0.827 & 0.356 & 0.565
\end{bmatrix} \]

(4). The average degree of understanding of a particular dimension from all experts:

\[ b_j = \frac{b_{j1} + b_{j2} + b_{j3} + b_{j4}}{4} = (0.770, 0.980, 0.960, 0.851, 0.460, 0.638). \]

(5). Based on the previous results and Equations (5) and (6), the blind understanding degree \( \sigma_j \) for the indexes from all experts could be obtained. Then, the evaluation vector \( X \) could be calculated according to the blind understanding degree \( \sigma_j \) and Equation (7). Finally, the weight of each index could be achieved by the normalized treatment method. The calculated result of each
parameter is shown in Table 3. Similarly, the weight distribution of the second grade indexes can be obtained by refining. The index distribution is shown in Table 4. The detailed calculation processes are shown in Appendix B (Table A2.-A7.).

Table 3. Weight distribution of the first grade index.

<table>
<thead>
<tr>
<th></th>
<th>Index $r_1$</th>
<th>Index $r_2$</th>
<th>Index $r_3$</th>
<th>Index $r_4$</th>
<th>Index $r_5$</th>
<th>Index $r_6$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Group A</td>
<td>4</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>6</td>
<td>5</td>
</tr>
<tr>
<td>Group B</td>
<td>3</td>
<td>1</td>
<td>1</td>
<td>2</td>
<td>5</td>
<td>4</td>
</tr>
<tr>
<td>Group C</td>
<td>3</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>5</td>
<td>4</td>
</tr>
<tr>
<td>Group D</td>
<td>4</td>
<td>2</td>
<td>1</td>
<td>3</td>
<td>6</td>
<td>5</td>
</tr>
<tr>
<td>Average cognition degree $b_j$</td>
<td>0.770</td>
<td>0.980</td>
<td>0.960</td>
<td>0.851</td>
<td>0.460</td>
<td>0.638</td>
</tr>
<tr>
<td>$b_{max}$</td>
<td>0.827</td>
<td>1.000</td>
<td>1.000</td>
<td>0.921</td>
<td>0.565</td>
<td>0.712</td>
</tr>
<tr>
<td>$b_{max} - b_j$</td>
<td>0.057</td>
<td>0.020</td>
<td>0.040</td>
<td>0.070</td>
<td>0.104</td>
<td>0.074</td>
</tr>
<tr>
<td>$b_{min}$</td>
<td>0.712</td>
<td>0.921</td>
<td>0.921</td>
<td>0.827</td>
<td>0.356</td>
<td>0.565</td>
</tr>
<tr>
<td>$b_j - b_{min}$</td>
<td>0.057</td>
<td>0.059</td>
<td>0.040</td>
<td>0.023</td>
<td>0.104</td>
<td>0.074</td>
</tr>
<tr>
<td>$\sigma_j$</td>
<td>0.057</td>
<td>0.040</td>
<td>0.040</td>
<td>0.047</td>
<td>0.104</td>
<td>0.074</td>
</tr>
<tr>
<td>1-$\sigma_j$</td>
<td>0.943</td>
<td>0.960</td>
<td>0.960</td>
<td>0.953</td>
<td>0.896</td>
<td>0.926</td>
</tr>
<tr>
<td>$X_j$</td>
<td>0.726</td>
<td>0.941</td>
<td>0.922</td>
<td>0.811</td>
<td>0.412</td>
<td>0.591</td>
</tr>
<tr>
<td>Weight</td>
<td>0.165</td>
<td>0.214</td>
<td>0.209</td>
<td>0.184</td>
<td>0.094</td>
<td>0.134</td>
</tr>
</tbody>
</table>
Table 4. Index weights and actual scores.

<table>
<thead>
<tr>
<th>First Grade Indexes (ri)</th>
<th>Weight (ωi)</th>
<th>Second Grade Indexes (rik)</th>
<th>Weight (ωik)</th>
<th>Total Score</th>
<th>Actual Score (vik)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Laws, regulations and policies (r1)</td>
<td>0.165</td>
<td>Mineral rights and gas rights conflict (r11)</td>
<td>0.226</td>
<td>100</td>
<td>91</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Major licenses and approvals (r12)</td>
<td>0.235</td>
<td>100</td>
<td>88</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Foreign cooperation franchise (r13)</td>
<td>0.113</td>
<td>100</td>
<td>48</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Government financial subsidies (r14)</td>
<td>0.188</td>
<td>100</td>
<td>83</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Resource tax reform (r15)</td>
<td>0.118</td>
<td>100</td>
<td>48</td>
</tr>
<tr>
<td></td>
<td></td>
<td>New energy policy (r16)</td>
<td>0.120</td>
<td>100</td>
<td>84</td>
</tr>
<tr>
<td>Resource characteristics (r2)</td>
<td>0.214</td>
<td>Gas content (r21)</td>
<td>0.160</td>
<td>100</td>
<td>79</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Permeability (r22)</td>
<td>0.173</td>
<td>100</td>
<td>82</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Reservoir pressure (r23)</td>
<td>0.160</td>
<td>100</td>
<td>89</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Porosity (r24)</td>
<td>0.124</td>
<td>100</td>
<td>76</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Hydrogeological conditions (r25)</td>
<td>0.124</td>
<td>100</td>
<td>86</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Coal seam area (r26)</td>
<td>0.075</td>
<td>100</td>
<td>74</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Coal seam thickness (r27)</td>
<td>0.075</td>
<td>100</td>
<td>81</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Buried depth (r28)</td>
<td>0.118</td>
<td>100</td>
<td>87</td>
</tr>
<tr>
<td>Engineering technology (r3)</td>
<td>0.209</td>
<td>Geological evaluation technique (r31)</td>
<td>0.170</td>
<td>100</td>
<td>86</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Extraction technology (r32)</td>
<td>0.158</td>
<td>100</td>
<td>74</td>
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<tr>
<td></td>
<td></td>
<td>Development process technology (r33)</td>
<td>0.134</td>
<td>100</td>
<td>77</td>
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<tr>
<td></td>
<td></td>
<td>Gas gathering technology (r34)</td>
<td>0.121</td>
<td>100</td>
<td>82</td>
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<tr>
<td></td>
<td></td>
<td>Treatment technology (r35)</td>
<td>0.111</td>
<td>100</td>
<td>81</td>
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<tr>
<td></td>
<td></td>
<td>Transportation technology (r36)</td>
<td>0.073</td>
<td>100</td>
<td>68</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Dynamic monitoring and analysis (r37)</td>
<td>0.098</td>
<td>100</td>
<td>78</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Drainage system (r38)</td>
<td>0.136</td>
<td>100</td>
<td>75</td>
</tr>
<tr>
<td>Economic operation (r4)</td>
<td>0.184</td>
<td>CBM price fluctuation (r41)</td>
<td>0.087</td>
<td>100</td>
<td>83</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Project cost (r42)</td>
<td>0.147</td>
<td>100</td>
<td>78</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Return on investment (r43)</td>
<td>0.134</td>
<td>100</td>
<td>76</td>
</tr>
<tr>
<td></td>
<td></td>
<td>CBM production (r44)</td>
<td>0.145</td>
<td>100</td>
<td>72</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Macroeconomics (r45)</td>
<td>0.086</td>
<td>100</td>
<td>84</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Funds recovery (r46)</td>
<td>0.104</td>
<td>100</td>
<td>86</td>
</tr>
<tr>
<td></td>
<td></td>
<td>External market resources (r47)</td>
<td>0.086</td>
<td>100</td>
<td>56</td>
</tr>
<tr>
<td></td>
<td></td>
<td>External network resources (r48)</td>
<td>0.057</td>
<td>100</td>
<td>82</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Market demand (r49)</td>
<td>0.135</td>
<td>100</td>
<td>78</td>
</tr>
<tr>
<td>Organizational management (r5)</td>
<td>0.094</td>
<td>Organizational structure adaptability (r51)</td>
<td>0.270</td>
<td>100</td>
<td>85</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Management coordination and communication (r52)</td>
<td>0.181</td>
<td>100</td>
<td>79</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Process management (r53)</td>
<td>0.205</td>
<td>100</td>
<td>73</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Organizational management quality (r54)</td>
<td>0.115</td>
<td>100</td>
<td>82</td>
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<tr>
<td></td>
<td></td>
<td>Resource allocation capability (r55)</td>
<td>0.229</td>
<td>100</td>
<td>74</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Safety technology and equipment (r56)</td>
<td>0.151</td>
<td>100</td>
<td>75</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Hidden danger investigation and treatment (r57)</td>
<td>0.133</td>
<td>100</td>
<td>78</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Safety training and education (r58)</td>
<td>0.133</td>
<td>100</td>
<td>76</td>
</tr>
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<td></td>
<td>Safety culture (r59)</td>
<td>0.062</td>
<td>100</td>
<td>72</td>
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<td></td>
<td></td>
<td>Safety investment (r60)</td>
<td>0.141</td>
<td>100</td>
<td>72</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Emergency plan (r61)</td>
<td>0.098</td>
<td>100</td>
<td>74</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Emergency drill frequency (r62)</td>
<td>0.088</td>
<td>100</td>
<td>54</td>
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<tr>
<td></td>
<td></td>
<td>Emergency supplies reserve (r63)</td>
<td>0.095</td>
<td>100</td>
<td>63</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Emergency rescue team (r64)</td>
<td>0.100</td>
<td>100</td>
<td>76</td>
</tr>
</tbody>
</table>

2.3. Assessment Model Construction

The goal of the MEEM is to use the degree of association of the extension set to determine the assessment level of the matter element feature. The MEEM is a method for comprehensive multi-index assessments, and it is mainly based on the extrinsic matter-element model, extension set and correlation function theory [22]. This method can judge the subordinate level of items according to their different characteristics with low data requirements and can avoid the randomness and subjectivity of the evaluation process to a certain extent. The MEEM combines qualitative and quantitative analyses and has achieved good results in risk assessment in many fields, such as oil exploitation [23], tailings pond [24], and building fire [25]. Based on the above advantages, this method is applied to research CBM development risk assessments.

The MEEM includes the following steps [44,45]: (1) According to the development of things and relevant reference materials, the characteristics of things are analyzed, the things are divided into several grades according to certain rules, the numerical range of each level is clarified, and a multi-index MEEM is established; (2) Using the correlation function to calculate the degree of association between the things to be evaluated and each assessment level; (3) Things have the highest degree of relevance to one of the levels, indicating that they are most consistent with that level. Next, the calculation process of the CBM development risk assessment model will be described in detail.

2.3.1. Determination of the Classical Domain, Joint Domain and Matter-Element Evaluation
The matter element uses the ordered triplet \( M = \{ C, R, V \} \) as the basic element to describe things, where \( C \) is the name of the thing, \( R \) is the name of the feature, and \( V \) is the value taken by \( C \) for \( R \) [25].

(1) Determining the classical domain \( M_j \)

Let \( M_j \) be the classic domain of matter-element \( M \):

\[
M_j = (U_j, R, V_j) = \begin{pmatrix}
U_j & r_1 & (a_{j1}, b_{j1}) \\
& r_2 & (a_{j2}, b_{j2}) \\
& & \vdots \\
& & (a_{ji}, b_{ji})
\end{pmatrix},
\]

where \( U_j \) is the \( j \)th risk level in the risk level domain \( U \), \( V_j \) is the range of assessment index set \( R \) about the risk level \( U_j \), and \( a_{ji} \) and \( b_{ji} \) are the lower and upper limits of the index \( r \) at the \( j \)th risk level, respectively.

(2) Determining the joint domain \( M_c \)

Let \( M_c \) be the joint domain of matter-element \( M \):

\[
M_c = (U, R, V_c) = \begin{pmatrix}
U & r_1 & (a_{c1}, b_{c1}) \\
& r_2 & (a_{c2}, b_{c2}) \\
& & \vdots \\
& & (a_{ci}, b_{ci})
\end{pmatrix},
\]

where \( V_c \) is the range of evaluation index set \( R \) about the risk level domain \( U \), and \( a_{ci} \) and \( b_{ci} \) are the lower and upper limits of the index \( r \) at all risk levels, respectively.

(3) Determining the matter-element evaluation \( M_i \)

Let \( M_i \) be the matter-element evaluation of matter-element \( M \):

\[
M_i = (\oplus, \otimes, V_i) = \begin{pmatrix}
S_j & r_{i1} & v_{i1} \\
& r_{i2} & v_{i2} \\
& & \vdots \\
& & (r_{ip}, v_{ip})
\end{pmatrix},
\]

where \( S_j \) is the \( i \)th first grade index to be evaluated, \( R_i = \{ r_{i1}, r_{i2}, \ldots, r_{ip} \} \) is the second grade assessment index set for \( S_j \), \( r_{ip} \) is the \( p \)th second grade assessment index of the \( i \)th first grade index, and \( V_i \) is the value of the second grade index \( R_i \) for \( S_j \).

2.3.2. Calculating the Correlation Degree

By introducing the concept of distance in classical mathematics, the correlation function of the second grade index \( r_{ik} \) of the CBM development risk assessment on the risk level \( U_j \) is established. Therefore, the correlation degree \( K_j(r_{ik}) \) of the \( k \)th second grade index in the \( i \)th first grade index with respect to the risk level \( U_j \) is determined.

\[
K_j(r_{ik}) = \begin{cases}
\rho(v_{ik}, V_j) & \rho(v_{ik}, V_j) \neq 0 \\
\frac{\rho(v_{ik}, V_j) - \rho(v_{ik}, V_j) \rho(v_{ik}, V_j)}{\rho(v_{ik}, V_j) - 1} & \rho(v_{ik}, V_j) = 0
\end{cases},
\]

where \( \rho(v_{ik}, V_j) = \frac{v_{ik} - \frac{a_{ik} + b_{ik}}{2}}{\frac{b_{ik} - a_{ik}}{2}} \) and \( \rho(v_{ik}, V_j) = \frac{v_{ik} - \frac{a_{ik} + b_{ik}}{2}}{\frac{b_{ik} - a_{ik}}{2}} \) are the lower and upper limits of the index \( r \) at all risk levels, respectively, and \( v_{ik} \) is the expert score for the second grade index \( r_{ik} \).

2.3.3. Multi-Level Extension Assessment
(1) Primary assessment
Calculate the correlation matrix \( K(ri) \) of the first indexes for each risk level:

\[
K(ri) = (\omega_i^1, \omega_i^2, \ldots, \omega_i^p) k_1(ri), k_2(ri), \ldots, k_m(ri) = (k_j(ri)) \quad (13)
\]

where \( \omega_i = (\omega_i) \) is the weight vector of the second grade indexes, and the calculation method is shown in Formulas (1)~(8); and \( K(ri) = (k_j(ri)) \) is the correlation degree matrix of the second grade indexes for each risk level.

(2) Secondary assessment
Determine the correlation degree matrix \( K(S) \) of the CBM development safety for each risk level.

\[
K(S) = (\omega_1, \omega_2, \ldots, \omega_j) k_1(r_1), k_2(r_1), \ldots, k_m(r_1) = (k_j(S)) \quad (14)
\]

where \( \omega = (\omega) \) is the weight vector of the first grade indexes, and the calculation method is shown in formulas (1)~(8); \( a^\otimes K(ri) = (k(ri)) \) is the correlation degree matrix of the first grade indexes for each risk level.

(3) Determining the risk level
According to the principle of maximum membership degree, the risk level corresponding to the maximum correlation degree in the correlation degree matrix \( K(S) \) of the CBM development for each risk level is the risk level of the assessment object. That is, when \( \max k_j(S) = k_j(S) \), with \( j = (1, 2, 3 \ldots n) \), the risk level of the assessment object is at level \( j \).

2.3.4. Risk Classification
To scientifically measure the risk of CBM development and ensure the systematic nature and accuracy of the assessment results, this paper divides the risk level of CBM development into five grades according to the actual CBM development situation and the risk classification rules in the literature [25,46], as shown in Table 5. Notably, when the established risk assessment model has been tested by a large number of empirical tests, the risk classification criteria can be corrected by data feedback to make the criteria more sensitive.

<table>
<thead>
<tr>
<th>Risk Level</th>
<th>Score Range</th>
<th>Basic Characteristics</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>(85, 100]</td>
<td>System operation condition is very good, risk is very low</td>
</tr>
<tr>
<td>II</td>
<td>(70, 85]</td>
<td>System operation condition is good, risk is lower</td>
</tr>
<tr>
<td>III</td>
<td>(50, 70]</td>
<td>System operation condition is mediocre, risk is mediocre</td>
</tr>
<tr>
<td>IV</td>
<td>(25, 50]</td>
<td>System operation condition is poor, risk is higher</td>
</tr>
<tr>
<td>V</td>
<td>[0, 25]</td>
<td>System operation condition is very poor, risk is very high</td>
</tr>
</tbody>
</table>

3. Case Study
The southern part of the Qinshui Basin is one of the earliest areas for CBM exploration and development in China, and it has also attracted the most investment and research in CBM exploration and development in China [47]. The CBM storage conditions in this area are stable and have good development potential [48,49]. As a key breakthrough area for CBM exploration and development, many experts have carried out exploration and research work here, leading to the accumulation of a wealth of test and production data [50]. The experts have a deeper understanding of the characteristics of reservoir CBM accumulation, reservoir geological conditions and gas layer distribution. Therefore, this paper takes a CBM development project in this area as the research object and invited 5 experts, including 1 CBM exploration expert, 2 CBM mining technical experts, 1 energy
policy expert and 1 project manager, to participate. Based on the engineering practice data of the project, the experts anonymously scored the actual operation status of each second grade index. The total score for each index is 100. In this paper, the actual scores of the second grade indexes of the CBM development project are obtained by calculating the average value, as shown in Table 4.

3.1. Determination of the Classical Domain, Joint Domain and Matter-Element Evaluation

Take the first grade index laws, regulations and policies \((r_1)\) as an example to establish the matter-element \(M\) and determine its classical domain \(M_c\), joint domain \(M_j\) and matter-element evaluation \(M\). Similarly, classical domains, joint domains and matter-element evaluations of other first grade indexes can be obtained.

(1) Determining the classical domain \(M_c\)
The classical domains for each risk level are determined by Formula (9):

\[
M_I = \begin{pmatrix}
(U_1) & r_{11} (85,100) \\
 & r_{12} (85,100) \\
 & r_{13} (85,100) \\
 & r_{14} (85,100) \\
 & r_{15} (85,100) \\
 & r_{16} (85,100)
\end{pmatrix}
= \begin{pmatrix}
(U_2) & r_{11} (70,85) \\
 & r_{12} (70,85) \\
 & r_{13} (70,85) \\
 & r_{14} (70,85) \\
 & r_{15} (70,85) \\
 & r_{16} (70,85)
\end{pmatrix}
\]

\[
M_{III} = \begin{pmatrix}
(U_3) & r_{11} (50,70) \\
 & r_{12} (50,70) \\
 & r_{13} (50,70) \\
 & r_{14} (50,70) \\
 & r_{15} (50,70) \\
 & r_{16} (50,70)
\end{pmatrix}
\]

\[
M_{IV} = \begin{pmatrix}
(U_4) & r_{11} (25,50) \\
 & r_{12} (25,50) \\
 & r_{13} (25,50) \\
 & r_{14} (25,50) \\
 & r_{15} (25,50) \\
 & r_{16} (25,50)
\end{pmatrix}
\]

\[
M_{V} = \begin{pmatrix}
(U_5) & r_{11} (0.25) \\
 & r_{12} (0.25) \\
 & r_{13} (0.25) \\
 & r_{14} (0.25) \\
 & r_{15} (0.25) \\
 & r_{16} (0.25)
\end{pmatrix}
\]

(2) Determining the joint domain \(M_j\)
The joint domain \(M_j\) is determined by Formula (10):

\[
M_j = \begin{pmatrix}
(U) & r_{11} (100,0) \\
 & r_{12} (100,0) \\
 & r_{13} (100,0) \\
 & r_{14} (100,0) \\
 & r_{15} (100,0) \\
 & r_{16} (100,0)
\end{pmatrix}
\]

(3) Determining the matter-element evaluation \(M_i\)
The matter-element evaluation \(M_i\) of indexes \(r_i\) is determined by Formula (11):

\[
M_i = \begin{pmatrix}
S_1 & r_{11} & v_{11} \\
 & r_{12} & v_{12} \\
 & \vdots & \vdots \\
 & r_{1p} & v_{1p}
\end{pmatrix}
= \begin{pmatrix}
R_1 & r_{11} & 91 \\
 & r_{12} & 88 \\
 & r_{13} & 48 \\
 & r_{14} & 83 \\
 & r_{15} & 86 \\
 & r_{16} & 84
\end{pmatrix}
\]
3.2. Calculating the Correlation Degree

Taking the correlation degree of the second grade index \( r_{i1} \) of the first grade index \( r_i \) as an example, the calculation steps of the correlation degrees of the second grade indexes are obtained by Formula (12),

\[
\rho(v_{i1}, V_4) = \frac{|91 - (0 + 100)/2| - (100 - 0)/2 = -9; \\
\rho(v_{i1}, V_5) = \frac{|91 - (25 + 50)/2| - (50 - 25)/2 = 41; \\
\rho(v_{i1}, V_6) = \frac{|91 - (0 + 100)/2| - (100 - 0)/2 = -9; \\
k_1(r_{i1}) = \rho(v_{i1}, V_4)/[ \rho(v_{i1}, V_1) - \rho(v_{i1}, V_6) ] = -9/(-9 + 6) = 2; \\
k_2(r_{i1}) = \rho(v_{i1}, V_5)/[ \rho(v_{i1}, V_1) - \rho(v_{i1}, V_5) ] = 41/(-9 - 21) = -0.7; \\
k_3(r_{i1}) = \rho(v_{i1}, V_6)/[ \rho(v_{i1}, V_1) - \rho(v_{i1}, V_6) ] = 66/(-9 - 66) = 0.88; \\
\]

Similarly, the correlation degrees of the second grade indexes under other first grade indexes can be calculated. The calculation results are shown in Table 6. The calculation process is shown in Appendix C.

<table>
<thead>
<tr>
<th>First Grade Indexes</th>
<th>Second Grade Indexes</th>
<th>Relevance of Second Grade Indexes</th>
<th>Risk Level</th>
</tr>
</thead>
<tbody>
<tr>
<td>Safety and emergency protection</td>
<td>( r_{i1} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Organizational management</td>
<td>( r_{i1} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Management coordination and communication</td>
<td>( r_{i1} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Process management</td>
<td>( r_{i1} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Organizational management quality</td>
<td>( r_{i1} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Resource allocation capability</td>
<td>( r_{i1} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Safety and emergency protection</td>
<td>( r_{i1} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Hidden danger investigation and treatment</td>
<td>( r_{i1} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Safety training and education</td>
<td>( r_{i1} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Safety culture</td>
<td>( r_{i1} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Safety investment</td>
<td>( r_{i1} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Emergency plan</td>
<td>( r_{i1} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Emergency drill frequency</td>
<td>( r_{i1} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Emergency supplies reserve</td>
<td>( r_{i1} )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Emergency rescue team</td>
<td>( r_{i1} )</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 6. The relevance of second grade indexes.
3.3. Multi-Level Extension Assessment

(1) Primary assessment
Taking the first grade index \( r_1 \) as an example, the correlation degree matrix \( K(r_1) \) is determined according to the weight calculation result in Table 4 and Formula (13).

\[
K(r_1) = (\omega_1, \omega_1, \omega_1, \omega_1, \omega_1) (k(r_1)) =
\begin{bmatrix}
2.000 & -0.400 & -0.700 & -0.820 & -0.880 \\
0.333 & -0.200 & 0.600 & -0.760 & -0.840 \\
-0.435 & -0.314 & -0.040 & 0.043 & -0.324 \\
-0.105 & 0.133 & -0.433 & -0.660 & -0.773 \\
0.077 & -0.067 & -0.533 & -0.720 & -0.813 \\
-0.059 & 0.067 & -0.467 & -0.680 & -0.787
\end{bmatrix}
\]

\[
= (0.463, -0.148, -0.504, -0.650, -0.769)
\]

In the same way, the correlation degree matrixes of other first grade indexes are calculated. The detailed calculation processes are shown in Appendix B.

\[
K(r_2) = (-0.006, 0.105, -0.411, -0.647, -0.765)
\]

\[
K(r_3) = (-0.204, 0.200, -0.260, -0.540, -0.694)
\]

\[
K(r_4) = (-0.188, 0.163, -0.286, -0.572, -0.714)
\]

\[
K(r_5) = (-0.295, 0.114, -0.103, -0.414, -0.610)
\]

(2) Secondary assessment
According to formula (14), the comprehensive correlation degree matrix of the research object for each risk level is determined.

\[
K(S) = (\omega_1, \omega_2, \omega_3, \omega_4, \omega_5, \omega_6) K(r_1) =
\begin{bmatrix}
0.463 & -0.148 & -0.504 & -0.650 & -0.769 \\
-0.006 & 0.105 & -0.411 & -0.647 & -0.765 \\
-0.075 & 0.205 & -0.276 & -0.566 & -0.711 \\
-0.204 & 0.200 & -0.260 & -0.540 & -0.694 \\
-0.188 & 0.163 & -0.286 & -0.572 & -0.714 \\
-0.295 & 0.114 & -0.103 & -0.414 & -0.610
\end{bmatrix}
\]

\[
= (-0.035, 0.108, -0.317, -0.573, -0.716)
\]

(3) Determining the risk level
According to the principle of maximum membership degree, the risk level corresponding to the maximum correlation degree in correlation degree matrix \( K(S) \) of CBM development for each risk level is the risk level of the assessment object. Because \( \max_k(S) = 0.108 = K(S) \), the risk level of the CBM development project is Grade II.

4. Results and Discussion

(1). The correlation degree of comprehensive risk of the research object is 0.108, and the overall risk level of the CBM development project is judged to be Grade II according to the principle of maximum membership degree. This finding shows that the overall risk of the project is small and within an acceptable range, but the local risk of the project needs to be rectified in a timely manner.

(2). According to the calculation results of the correlation degree of the second grade indexes in Table 6, it is possible to determine the links with higher risks in the second grade indexes. The following is an analysis of the indexes with risk levels greater than Grade II.

(1) According to the investigation, the operators of the project did not obtain the right to cooperate with foreign countries, which indicates that the project cannot be assisted by foreign companies in terms of technology and management. Therefore, the project is at a higher risk in foreign cooperation franchises.

(2) The transportation technology of this project is relatively backwards, and mainly relies on tank trucks for CBM transportation, and there is no long-distance pipeline network for the system.
Therefore, the transportation technology risk of this project is high. It is recommended that the project operator regularly check the reliability of the tank truck equipment and conduct safety training for the tank truck driver.

(3) Because the project operators are affiliated with private enterprises, and the enterprises have been established only for a short period, a well-known corporate image or reputation in the CBM industry have not been established. For these reasons, the project’s external market resource risk is high.

(4) The project is not doing well in safety training and education. According to the survey, not all employees have participated in safety training, which will cause high risks to the daily operation of the project. CBM leakage and explosion accidents caused by human error are not uncommon; therefore, project operators should pay more attention to this aspect.

(5) The number of daily emergency drills of the project is not up to standard. During the investigation of the emergency drill record, it was found that the project conducted only one accident emergency drill every year, which did not meet the standards of China’s Safe Production Law stipulates that emergency drills be performed at least once every six months for firms involved in the production, filling, storage, supply and sales of flammable and explosive chemicals and the emergency plan is to be continuously improved in light of the actual situation. Therefore, to reduce the project risk, the project operators should add at least one more accident emergency drill every year.

(6) The project’s emergency supplies were not adequately prepared and did not include gas masks and explosion-proof emergency lights. The main component of CBM is methane, which is a flammable, explosive, toxic and corrosive gas. If a CBM leak accident occurs during the production process, rescue personnel are required to have a gas mask; otherwise, death, due to suffocation, is likely. Moreover, project operators should be equipped with a sufficient number of explosion-proof emergency lights. Other lighting equipment may cause methane explosion accidents, due to static electricity during use.

(7) The risks of other second grade indexes are very small, and their risk levels reached the first or second level. First, the risks of laws, regulations and policies faced by the project are minimal. The current new energy policies and financial subsidy policies are conducive to the development of the CBM industry. Second, there is no conflict between mining rights and air rights in the block where the project is located. In addition, the major licensing and approval procedures for the project are also complete. Third, the coal reservoirs in the block where the project is located have good porosity, high permeability, high gas content and gas saturation, which are conducive to the development of CBM. Finally, the economic operational risks of the project are also small. The project’s return on investment and CBM production are at a high level.

(8) In summary, the overall risk of the project is small and within an acceptable range, indicating that the project has development value. The assessment results are in good agreement with the actual operation of the project, indicating that the established risk assessment model is feasible and effective.

5. Conclusions

With the development of the CBM industry in various countries around the world, a mature and complete risk assessment system is needed to accurately determine the overall risk level and local risk weakness of CBM development projects. This paper provides a reference for government policy formulation, investor project feasibility analyses, insurance company insurance premium rate determination, and project operator risk perception improvement ability. This study fills the gap in the literature concerning the above requirements. The main contributions of this paper are as follows:

(1) Taking a CBM development project as the research object and considering the risk characteristics of exploration, mining, gathering and market application involved in the project life cycle, a CBM development risk assessment index system consisting of six first grade indexes and 45 second grade indexes is constructed.

(2) Based on the SEWM, the weights of the risk assessment indexes are calculated. Then, the MEEM
is used to construct the theoretical model of CBM development risk assessment.

3. A case study of a CBM development project in the southern Qinshui Basin of China was carried out using the established CBM development risk assessment model. The results show that the overall risk level of the CBM development project is Grade II, indicating that the overall risk of the project is small and within an acceptable range, although the local risk of the project needs to be rectified in a timely fashion. The assessment results are in good agreement with the actual operation of the project, indicating that the established risk assessment model has good applicability and effectiveness.

4. The study makes three contributions. First, the research results can help relevant government departments formulate policies to reduce the risks faced by the CBM industry. Second, this work can provide a reference for investors to evaluate the feasibility of CBM development projects and for insurance companies to determine the insurance rate of CBM development projects. Finally, the research results are also conducive to improving the risk awareness and risk perception of CBM project operators. Therefore, the accuracy of managers’ risk aversion decisions can be improved, and the waste of resources and property loss caused by the failure of risk management and control in the daily production process of the project can be reduced.

Author Contributions: Data curation, W.W.; Formal analysis, W.W., S.L. and Y.Z.; Methodology, W.W. and Y.Z.; Supervision, S.L.; Writing—original draft, W.W.; Writing—review and editing, Y.Z. and S.M.

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Conflicts of Interest: The authors declare no conflicts of interest.

Abbreviations

CBM Coalbed methane
SEWM Structure entropy weight method
MEEM Matter-element extension method
## Appendix A

### Table A1. Index analysis.

<table>
<thead>
<tr>
<th>First Grade Indexes (r)</th>
<th>Second Grade Indexes (r)</th>
<th>Index Analysis</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Laws, regulations and policies (r)</td>
<td>Mineral rights and gas rights conflict (r)</td>
<td>In China, coal mines are licensed by the State Ministry of Land and Resources and the Provincial Department of Land and Resources, while CBM is licensed by the Ministry of Land and Resources. However, there are often overlapping conflicts between CBM and coal at the level of hydrocarbon accumulation. In addition, China has not always made good distinctions between the block planning of coal mines and CBM. Therefore, in many blocks, there are both coal mining rights issued by the Provincial Department of Land and Resources and CBM mining rights granted by the State Ministry of Land and Resources. This type of conflict has caused many worries for investors.</td>
<td>Zhang et al. [29]</td>
</tr>
<tr>
<td></td>
<td>Major licenses and approvals (r)</td>
<td>CBM development also involves a number of major licensing and approval risks. Investors and companies should strictly inspect the exploration and mining licenses, safety production licenses and dangerous chemicals business licenses for CBM development projects. The absence of any of the above documents poses a significant risk to the operation of the project.</td>
<td>PRC [38]</td>
</tr>
<tr>
<td></td>
<td>Foreign cooperation franchise (r)</td>
<td>Foreign cooperation can make up for the shortage of funds for CBM projects and introduce advanced technology and management experience, thus promoting the development of CBM projects.</td>
<td>PRC [39]</td>
</tr>
<tr>
<td></td>
<td>Government financial subsidies (r)</td>
<td>Increasing financial subsidies can increase corporate liquidity, reduce production costs, and ease corporate investment pressures. Lowering or eliminating financial subsidies will increase competition in the CBM market and restrict the initial development of CBM enterprises.</td>
<td>Zhang et al. [13]</td>
</tr>
<tr>
<td></td>
<td>Resource tax reform (r)</td>
<td>Increasing the resource tax will increase the production cost of CBM enterprises, reduce the profit margin, and hinder the enthusiasm of enterprises. In contrast, reducing or cancelling unreasonable tax and fee systems and increasing tax incentives will incentivize CBM enterprises.</td>
<td>Zhang et al. [13]</td>
</tr>
<tr>
<td></td>
<td>New energy policy (r)</td>
<td>In the short run, CBM resources account for a certain proportion of China’s energy consumption. However, in the long run, with the development of new energy technologies, there will be inevitable changes in China’s energy structure, affecting the supply and demand of CBM. Therefore, the implementation of the national new energy policy may introduce risks to CBM development.</td>
<td>PRC [39]</td>
</tr>
<tr>
<td>Resource characteristics (r)</td>
<td>Gas content (r)</td>
<td>The gas content of CBM determines the critical desorption pressure. The higher the critical desorption pressure, the smaller the magnitude of the pressure reduction required for the CBM well. This also means that the earlier the CBM well starts to produce gas, the more methane gas can be desorbed by the coal seam. Therefore, insufficient CBM resources may pose risks to CBM development.</td>
<td>Roadifer et al. [10]</td>
</tr>
<tr>
<td></td>
<td>Permeability (r)</td>
<td>Permeability is the most critical factor in controlling the flow of CBM in coal reservoirs and the gas production of gas wells. It determines whether CBM can be successfully recovered. Therefore, permeability directly affects the economic benefits of CBM development, and low permeability of the coal seam may pose risks to the development of CBM.</td>
<td>Zhang et al. [12]</td>
</tr>
<tr>
<td></td>
<td>Reservoir pressure (r)</td>
<td>In the production process of CBM, a reasonable grasp of the trend of bottom hole flow pressure can reduce reservoir sensitivity, and thus, increase the production of CBM. Therefore, the size and distribution of coal reservoir pressure affect not only the enrichment of CBM, but also the production of CBM.</td>
<td>Zhang et al. [13]</td>
</tr>
<tr>
<td></td>
<td>Porosity (r)</td>
<td>Porosity is a key factor in determining the adsorption, permeability and strength properties of coal. By measuring the porosity and pressure of the CBM, the content of free CBM in the coal can be obtained. As a transport channel connecting the adsorption volume with the free surface, the pores also constitute the adsorption, diffusion and permeation system of CBM. Therefore, poor coal seam porosity may pose risks to CBM development.</td>
<td>Mares et al. [16]</td>
</tr>
<tr>
<td></td>
<td>Hydrogeological conditions (r)</td>
<td>The groundwater system controls the adsorption and accumulation of CBM through formation pressure. This gas control can cause the CBM to escape, and it can also conserve the CBM. In the development of CBM, CBM wells generally require a large amount of drainage and pressure reduction to produce gas. Therefore, regional hydrogeological conditions are the main factors determining the selection of well network, downhole equipment and dehydration process in the development of CBM. Therefore, unstable hydrogeological conditions may introduce risks to the development of CBM.</td>
<td>Lei et al. [31]</td>
</tr>
</tbody>
</table>
At the initial stage of the CBM development process, the coal seam area containing CBM is an important measure. In general, the larger the area of the gas-bearing coal seam, the higher the CBM content. Therefore, a poor coal seam area may pose risks to CBM development. Zhai et al. [32]

In the case of a certain degree of gas saturation, the thickness of the coal seam directly determines the amount of gas-bearing resources of the gas reservoir. The thicker the coal seam, the more abundant the CBM that converges into the wellbore and the higher the CBM production. Therefore, insufficient coal seam thickness may introduce risks to CBM development. Zhai et al. [32]

The burial depth of coal seams is the main source of pressure. As the burial depth increases, the pressure will increase, which will increase the coalbed’s ability to adsorb methane. In addition, if the geological structural conditions change so that the burial depth of the coal seam changes, the pressure will be changed, thus, affecting the preservation of the CBM reservoir. Therefore, the burial depth of CBM may introduce risks to the development of CBM. Ge et al. [30]

Geological evaluation technique plays a key role in understanding the geological conditions of CBM resources and the law of hydrocarbon accumulation. Advanced geological resource evaluation technology can accurately detect the distribution and enrichment of CBM resources. Therefore, backward geological evaluation technology will introduce risks to the development of CBM. Mu et al. [17]

The extraction technology involves the adaptability of coal seams, which will directly affect the recovery and production of CBM wells. Moreover, the extraction technology and the drainage system should be coordinated; otherwise, reservoir ground stress and effective stress sensitivity damage will be caused, and the permeability will decrease. Therefore, backward mining technology may introduce risks to the development of CBM. Jie et al. [33]

The technology used in CBM development, the means for increasing production and the effect of increasing production vary across projects. At present, China’s CBM development process technology mainly uses fracturing stimulation technology, and the fracturing effect directly affects the production of CBM wells. Therefore, if the CBM development process is backward, it will introduce risks to the development of CBM. Jie et al. [33]

Gas gathering technology can effectively reduce the pressure of the gas production pipeline and the operating cost of the pipeline network and improve the operating efficiency and the development of CBM. Therefore, backward gas gathering process technology will increase operating costs and reduce operating efficiency, which will introduce risks to the development of CBM. Jie et al. [33]

The treatment technology can not only increase the methane content in the CBM, but also realize the compression or liquefaction of the CBM, thereby greatly increasing the storage and transportation volume of the CBM and driving the development of the CBM enterprises. Therefore, if the treatment technology is backward, the quality, reserves and transportation of CBM will be reduced, thus, introducing economic risks to CBM development. Jie et al. [33]

Transportation technology, among them, the tank truck transportation risk is greater because it involves more human error, and the delivery volume is much smaller than that of pipeline transportation. Transportation by long-distance pipeline network can reduce the potential for explosions caused by low-concentration CBM. Pipeline transportation technology can not only reduce the purification cost, but also greatly increase the transportation capacity of CBM. Therefore, backward transportation technology will also affect the development of CBM enterprises. Jie et al. [33]

Dynamic monitoring and analysis technology can observe and monitor the dynamic production of CBM exploration and development activities. This technology can determine the pressure distribution, connectivity of gas wells, and utilization of coal reservoirs. The technology can also guide production adjustment, which is conducive to improving the description accuracy of CBM reservoirs and the development of coal seams, thereby increasing the recovery rate of CBM. Therefore, the backwardness of dynamic monitoring and analysis technology will introduce risks to the development of CBM. Lyu et al. [34]

Unreasonable drainage systems often cause reservoir stress sensitivity damage. An unreasonable drainage system may significantly harm reservoir permeability. Too much damage may make it difficult or impossible to return the reservoir to the original state and may result in the CBM well not producing gas at all. Therefore, an unreasonable CBM drainage system may introduce risks to CBM development. Zhang et al. [12]

Unreasonable drainage systems often cause reservoir stress sensitivity damage. An unreasonable drainage system may significantly harm reservoir permeability. Too much damage may make it difficult or impossible to return the reservoir to the original state and may result in the CBM well not producing gas at all. Therefore, an unreasonable CBM drainage system may introduce risks to CBM development. Zhang et al. [12]

The price of CBM is a very sensitive factor that is greatly affected by the national energy development and resource policy adjustment and directly affects the economic benefits of CBM development. Therefore, fluctuations in the price of CBM will adversely affect the development of the CBM industry. Luo et al. [15]

High cost and low profit are the status quo of CBM development, which shows that if the project operator does not have a certain capital base, it will not be able to withstand the risks of CBM development. The level of mining costs also determines the level of profit. In recent years, although China's CBM demand and prices
have been rising, due to the increase in staff salaries and environmental compensation fees, the project mining costs have also increased, which has led to a growth rate of CBM development profit that is far less than the increase in CBM prices. Therefore, the project mining cost has become another important factor restricting the development of the CBM industry.

<table>
<thead>
<tr>
<th>Return on investment (r{o})</th>
<th>For CBM development enterprises, operating profit is the driving force for survival and development. If this driving force is lost, the solvency of the company will decline. Enterprises will fall into the predicament of production and development. Therefore, a low return on investment may introduce risks to CBM development.</th>
<th>Xia et al. [35]</th>
</tr>
</thead>
<tbody>
<tr>
<td>CBM production (r{o})</td>
<td>CBM production stability directly affects the daily operation of the project, which means that if the project's CBM production is unstable or insufficient, it will bring high economic risks to the company.</td>
<td>Su et al. [19]</td>
</tr>
<tr>
<td>Macroeconomics (r{o})</td>
<td>CBM development is closely related to the growth of the national economy. When the national economy develops slowly and even stagnates, the demand and price of CBM will fall. In addition, the risks brought about by the macroeconomic downturn to CBM development are reflected in interest rates, money supply and inflation. Therefore, the macroeconomic downturn may introduce risks to CBM development.</td>
<td>Senthi et al. [11]</td>
</tr>
<tr>
<td>Funds recovery (r{o})</td>
<td>Some CBM development companies do not know enough about the credit rating of customers in the credit sales process and blindly sell to them, which will result in a large number of receivables that cannot be recovered for a long time until they become bad debts. On the other hand, in China’s CBM development of current assets, the proportion of inventory is relatively large, and many enterprises are characterized by overstocking and inventory. Assets are occupied by debtors and stocks for a long time, making CBM development lack sufficient liquidity to reinvest or return debts due. The above situations will seriously affect the liquidity and safety of CBM development assets.</td>
<td>Xia et al. [35]</td>
</tr>
<tr>
<td>External market resources (r{o})</td>
<td>A typical feature of external market resources is market power, which refers to the influence and control of the market by economic entities. Market power refers to companies' ability to charge market prices to seek benefits and gain influence in the market and dominate stakeholder behavior. Market resources are expressed in various aspects, such as corporate image, goodwill and reputation. If the external market resources of the enterprise are poor, there may be risks to the development of CBM.</td>
<td>Zhang et al. [13]</td>
</tr>
<tr>
<td>External network resources (r{o})</td>
<td>External network resources mainly refer to the social relationships between enterprises and stakeholders. Many aspects of the CBM development process, such as access to funds, raw materials, production, sales promotion, and access to relevant policies, entail external relations. Relevant literature surveys have found that good external network resources can promote the development of a project. Conversely, the lack of such resources can introduce risks to CBM development.</td>
<td>Zhang et al. [13]</td>
</tr>
<tr>
<td>Market demand (r{o})</td>
<td>The market demand for clean energy is crucial to the development of the CBM industry. If the demand for clean energy is strong, it will be beneficial to the economic development of CBM development enterprises. If not, it will introduce risks to CBM development, due to the imbalance between supply and demand.</td>
<td>Chen et al. [12]</td>
</tr>
<tr>
<td>Organizational structure adaptability (r{o})</td>
<td>The organizational structure of the project determines not only how the strategic objectives and policies are established, but also the resource allocation efficiency of the project. The unreasonable organizational structure will increase the internal coordination cost of the enterprise, affect the efficiency and effectiveness of organizational decision-making, and reduce the efficiency of resource allocation. Therefore, an unreasonable organizational structure may introduce risks to the development of CBM.</td>
<td>Zhang et al. [13]</td>
</tr>
<tr>
<td>Organizational management (r{o})</td>
<td>Organizational management not only provides the mechanism and framework for the development and operation of CBM, but also arranges personnel and resources for project operation. Organizational disruption and management failure are the least noticeable potential risks to the project’s operations. It is also the root cause of the failure of the project management operational system.</td>
<td>Zhang et al. [13]</td>
</tr>
<tr>
<td>Management coordination and communication (r{o})</td>
<td>Due to the special nature of the workplace, the working surface needs to be constantly changing. Good coordination and communication within the organization not only ensure the smooth and efficient operation of the CBM development process, but also improve labor productivity and safe production management efficiency. Good coordination and communication skills can also maximize the overall efficiency of the project through effective systems, appropriate business complementarities, and good interpersonal relationships, thereby improving overall competitiveness. Conversely, if the company’s management coordination and communication skills are insufficient, it may introduce risks to CBM development.</td>
<td>Zhang et al. [13]</td>
</tr>
<tr>
<td>Process management (r{o})</td>
<td>In the process of production and operation, the CBM development project involves many departments, and the production process is very complicated. The project’s process management involves coordination between departments, reduction of operating costs and a guarantee of safe production. Therefore, inadequate process management may pose risks to CBM development.</td>
<td>Zhang et al. [12]</td>
</tr>
<tr>
<td>Organizational management fineness (r{o})</td>
<td>The main embodiment of the refined management of the CBM development process is the refined production method. It determines how to improve technology, eliminate waste, increase recovery rates, and efficiently use limited resources. Refined production methods are also an effective way to increase resources. Therefore, the lack of refined management of the CBM development process will introduce risks to CBM development.</td>
<td>Zhang et al. [13]</td>
</tr>
<tr>
<td>Resource allocation capability (r{o})</td>
<td>Resource allocation capability refers to maximizing the role of the resources a company owns and promoting the achievement of development goals. For CBM development projects, internal resources, such as CBM</td>
<td>Zhang et al. [12]</td>
</tr>
</tbody>
</table>
resources, financial resources and human resources, as well as external resources closely related to CBM development. How to use these resources reasonably and to their full potential without causing waste is an important issue that must be dealt with in the development of CBM. Therefore, an inefficient resource allocation capacity may introduce risks to CBM development.

In the process of CBM development, relevant technologies and equipment are required for effective safety protection. Compared with that in other countries, there is still a gap in the safety technology of CBM development in China, and the research and development of safety equipment are still far behind. Therefore, an inefficient resource allocation capacity may introduce risks to CBM development.

In the process of CBM development, relevant technologies and equipment are required for effective safety protection. Compared with that in other countries, there is still a gap in the safety technology of CBM development in China, and the research and development of safety equipment are still far behind. Therefore, an inefficient resource allocation capacity may introduce risks to CBM development.

Kirchgoessne et al. [18]

PRC [40]

PRC [40]

Henriqson et al. [36]

PRC [40]

Zhao et al. [37]

PRC [40]

PRC [41]

PRC [41]

PRC [41]
Appendix B

Table A2. Weight distribution of the second grade indexes of \( r_1 \).

<table>
<thead>
<tr>
<th>Group</th>
<th>Index ( r_{11} )</th>
<th>Index ( r_{12} )</th>
<th>Index ( r_{13} )</th>
<th>Index ( r_{14} )</th>
<th>Index ( r_{15} )</th>
<th>Index ( r_{16} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>1</td>
<td>2</td>
<td>6</td>
<td>3</td>
<td>5</td>
<td>4</td>
</tr>
<tr>
<td>B</td>
<td>2</td>
<td>1</td>
<td>5</td>
<td>4</td>
<td>3</td>
<td>6</td>
</tr>
<tr>
<td>C</td>
<td>2</td>
<td>1</td>
<td>5</td>
<td>3</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>D</td>
<td>2</td>
<td>1</td>
<td>4</td>
<td>3</td>
<td>6</td>
<td>5</td>
</tr>
</tbody>
</table>

\[ b_j \quad 0.941 \quad 0.980 \quad 0.549 \quad 0.798 \quad 0.615 \quad 0.586 \]

\[ b_{max} \quad 1.000 \quad 1.000 \quad 0.712 \quad 0.827 \quad 0.827 \quad 0.712 \]

\[ b_{max} - b_j \quad 0.059 \quad 0.020 \quad 0.163 \quad 0.029 \quad 0.212 \quad 0.126 \]

\[ b_{min} \quad 0.921 \quad 0.921 \quad 0.356 \quad 0.712 \quad 0.356 \quad 0.356 \]

\[ b_j - b_{min} \quad 0.020 \quad 0.059 \quad 0.193 \quad 0.086 \quad 0.259 \quad 0.230 \]

\[ \sigma_j \quad 0.040 \quad 0.040 \quad 0.178 \quad 0.058 \quad 0.236 \quad 0.178 \]

\[ 1 - \sigma_j \quad 0.961 \quad 0.961 \quad 0.822 \quad 0.712 \quad 0.765 \quad 0.822 \]

\[ X_j \quad 0.904 \quad 0.941 \quad 0.451 \quad 0.752 \quad 0.470 \quad 0.482 \]

Weight 0.226 0.235 0.113 0.188 0.118 0.120

The calculated membership matrix \( B_1 \) is based on Formula (4), and \( m \) is set as 8.

\[ B_1 = \begin{bmatrix} 1.000 & 0.921 & 0.356 & 0.827 & 0.565 & 0.712 \\ 0.921 & 1.000 & 0.565 & 0.712 & 0.827 & 0.356 \\ 0.921 & 1.000 & 0.565 & 0.827 & 0.712 & 0.712 \\ 0.921 & 1.000 & 0.712 & 0.827 & 0.356 & 0.565 \end{bmatrix} \]

Table A3. Weight distribution of the second grade indexes of \( r_2 \).

<table>
<thead>
<tr>
<th>Group</th>
<th>Index ( r_{21} )</th>
<th>Index ( r_{22} )</th>
<th>Index ( r_{23} )</th>
<th>Index ( r_{24} )</th>
<th>Index ( r_{25} )</th>
<th>Index ( r_{26} )</th>
<th>Index ( r_{27} )</th>
<th>Index ( r_{28} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>2</td>
<td>1</td>
<td>3</td>
<td>4</td>
<td>5</td>
<td>7</td>
<td>7</td>
<td>6</td>
</tr>
<tr>
<td>B</td>
<td>3</td>
<td>1</td>
<td>2</td>
<td>5</td>
<td>4</td>
<td>7</td>
<td>8</td>
<td>6</td>
</tr>
<tr>
<td>C</td>
<td>3</td>
<td>2</td>
<td>1</td>
<td>6</td>
<td>4</td>
<td>8</td>
<td>7</td>
<td>5</td>
</tr>
<tr>
<td>D</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>4</td>
<td>6</td>
<td>7</td>
<td>8</td>
<td>5</td>
</tr>
</tbody>
</table>

\[ b_j \quad 0.929 \quad 0.973 \quad 0.929 \quad 0.749 \quad 0.749 \quad 0.454 \quad 0.408 \quad 0.682 \]

\[ b_{max} \quad 1.000 \quad 1.000 \quad 1.000 \quad 0.815 \quad 0.815 \quad 0.500 \quad 0.500 \quad 0.732 \]

\[ b_{max} - b_j \quad 0.071 \quad 0.027 \quad 0.071 \quad 0.067 \quad 0.067 \quad 0.046 \quad 0.092 \quad 0.051 \]

\[ b_{min} \quad 0.886 \quad 0.946 \quad 0.886 \quad 0.631 \quad 0.631 \quad 0.315 \quad 0.315 \quad 0.631 \]

\[ b_j - b_{min} \quad 0.044 \quad 0.027 \quad 0.044 \quad 0.118 \quad 0.118 \quad 0.138 \quad 0.092 \quad 0.051 \]

\[ \sigma_j \quad 0.057 \quad 0.027 \quad 0.057 \quad 0.092 \quad 0.092 \quad 0.092 \quad 0.092 \quad 0.051 \]

\[ 1 - \sigma_j \quad 0.943 \quad 0.973 \quad 0.943 \quad 0.908 \quad 0.908 \quad 0.908 \quad 0.908 \quad 0.949 \]

\[ X_j \quad 0.876 \quad 0.947 \quad 0.876 \quad 0.680 \quad 0.680 \quad 0.412 \quad 0.370 \quad 0.647 \]

Weight 0.160 0.173 0.160 0.124 0.124 0.075 0.067 0.118

The calculated membership matrix \( B_2 \) is based on Formula (4), and \( m \) is set as 10.

\[ B_2 = \begin{bmatrix} 0.946 & 1.000 & 0.886 & 0.815 & 0.732 & 0.500 & 0.500 & 0.631 \\ 0.886 & 1.000 & 0.946 & 0.732 & 0.815 & 0.500 & 0.315 & 0.631 \\ 0.886 & 0.946 & 1.000 & 0.631 & 0.815 & 0.315 & 0.500 & 0.732 \\ 1.000 & 0.946 & 0.886 & 0.815 & 0.631 & 0.500 & 0.315 & 0.732 \end{bmatrix} \]
Table A4. Weight distribution of the second grade indexes of $r_3$.

<table>
<thead>
<tr>
<th>Group</th>
<th>Index $r_{31}$</th>
<th>Index $r_{32}$</th>
<th>Index $r_{33}$</th>
<th>Index $r_{34}$</th>
<th>Index $r_{35}$</th>
<th>Index $r_{36}$</th>
<th>Index $r_{37}$</th>
<th>Index $r_{38}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>1</td>
<td>2</td>
<td>4</td>
<td>5</td>
<td>3</td>
<td>7</td>
<td>6</td>
<td>4</td>
</tr>
<tr>
<td>B</td>
<td>1</td>
<td>3</td>
<td>2</td>
<td>6</td>
<td>4</td>
<td>8</td>
<td>7</td>
<td>5</td>
</tr>
<tr>
<td>C</td>
<td>2</td>
<td>1</td>
<td>3</td>
<td>4</td>
<td>7</td>
<td>6</td>
<td>5</td>
<td>3</td>
</tr>
<tr>
<td>D</td>
<td>1</td>
<td>2</td>
<td>5</td>
<td>4</td>
<td>3</td>
<td>7</td>
<td>6</td>
<td>3</td>
</tr>
</tbody>
</table>

$bj = 0.987$ $0.945$ $0.845$ $0.749$ $0.772$ $0.487$ $0.624$ $0.830$

$bj_{max} = 1.000$ $1.000$ $0.946$ $0.815$ $0.631$ $0.732$ $0.886$

$bj_{max} - bj = 0.013$ $0.055$ $0.101$ $0.067$ $0.114$ $0.144$ $0.109$ $0.056$

$bj_{min} = 0.946$ $0.886$ $0.732$ $0.631$ $0.315$ $0.500$ $0.732$ $0.732$

$bj - bj_{min} = 0.040$ $0.059$ $0.113$ $0.118$ $0.272$ $0.171$ $0.124$ $0.097$

$\sigma_j = 0.027$ $0.057$ $0.107$ $0.092$ $0.193$ $0.183$ $0.116$ $0.077$

$1 - \sigma_j = 0.972$ $0.943$ $0.893$ $0.908$ $0.807$ $0.842$ $0.884$ $0.923$

$X_j = 0.960$ $0.891$ $0.755$ $0.680$ $0.623$ $0.410$ $0.551$ $0.766$

Weight = 0.170 $0.158$ $0.134$ $0.121$ $0.111$ $0.073$ $0.098$ $0.136$

The calculated membership matrix $B_3$ is based on Formula (4), and $m$ is set as 10.

$$B_3 = \begin{bmatrix} 1.000 & 0.946 & 0.815 & 0.732 & 0.886 & 0.500 & 0.631 & 0.815 \\ 1.000 & 0.886 & 0.946 & 0.631 & 0.815 & 0.315 & 0.500 & 0.732 \\ 0.946 & 1.000 & 0.886 & 0.815 & 0.500 & 0.631 & 0.732 & 0.886 \\ 1.000 & 0.946 & 0.732 & 0.815 & 0.500 & 0.631 & 0.732 & 0.886 \end{bmatrix}$$

Table A5. Weight distribution of the second grade indexes of $r_4$.

<table>
<thead>
<tr>
<th>Group</th>
<th>Index $r_{41}$</th>
<th>Index $r_{42}$</th>
<th>Index $r_{43}$</th>
<th>Index $r_{44}$</th>
<th>Index $r_{45}$</th>
<th>Index $r_{46}$</th>
<th>Index $r_{47}$</th>
<th>Index $r_{48}$</th>
<th>Index $r_{49}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>8</td>
<td>2</td>
<td>4</td>
<td>3</td>
<td>7</td>
<td>5</td>
<td>6</td>
<td>9</td>
<td>1</td>
</tr>
<tr>
<td>B</td>
<td>6</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>8</td>
<td>7</td>
<td>4</td>
<td>5</td>
<td>1</td>
</tr>
<tr>
<td>C</td>
<td>5</td>
<td>1</td>
<td>3</td>
<td>2</td>
<td>4</td>
<td>6</td>
<td>7</td>
<td>8</td>
<td>2</td>
</tr>
<tr>
<td>D</td>
<td>7</td>
<td>3</td>
<td>4</td>
<td>2</td>
<td>6</td>
<td>5</td>
<td>8</td>
<td>9</td>
<td>1</td>
</tr>
</tbody>
</table>

$bj = 0.639$ $0.964$ $0.887$ $0.929$ $0.656$ $0.714$ $0.656$ $0.464$ $0.989$

$bj_{max} = 0.778$ $1.000$ $0.954$ $0.954$ $0.845$ $0.778$ $0.845$ $0.778$ $1.000$

$bj_{max} - bj = 0.139$ $0.036$ $0.067$ $0.026$ $0.189$ $0.064$ $0.189$ $0.314$ $0.011$

$bj_{min} = 0.477$ $0.903$ $0.845$ $0.903$ $0.477$ $0.602$ $0.477$ $0.301$ $0.954$

$bj_{min} - bj = 0.162$ $0.061$ $0.042$ $0.026$ $0.179$ $0.112$ $0.179$ $0.163$ $0.034$

$\sigma_j = 0.151$ $0.048$ $0.055$ $0.026$ $0.184$ $0.088$ $0.184$ $0.239$ $0.023$

$X_j = 0.543$ $0.918$ $0.838$ $0.905$ $0.535$ $0.651$ $0.535$ $0.354$ $0.966$

Weight = 0.087 $0.147$ $0.134$ $0.145$ $0.086$ $0.104$ $0.086$ $0.057$ $0.155$

The calculated membership matrix $B_4$ is based on Formula (4), and $m$ is set as 11.

$$B_4 = \begin{bmatrix} 0.477 & 0.954 & 0.845 & 0.903 & 0.602 & 0.778 & 0.699 & 0.301 & 1.000 \\ 0.699 & 1.000 & 0.954 & 0.903 & 0.477 & 0.602 & 0.845 & 0.778 & 1.000 \\ 0.778 & 1.000 & 0.903 & 0.954 & 0.845 & 0.699 & 0.602 & 0.477 & 0.954 \\ 0.602 & 0.903 & 0.845 & 0.954 & 0.699 & 0.778 & 0.477 & 0.301 & 1.000 \end{bmatrix}$$
### Table A6. Weight distribution of the second grade indexes of \( r_5 \).

<table>
<thead>
<tr>
<th>Index</th>
<th>( r_{51} )</th>
<th>( r_{52} )</th>
<th>( r_{53} )</th>
<th>( r_{54} )</th>
<th>( r_{55} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Group A</td>
<td>1</td>
<td>3</td>
<td>4</td>
<td>5</td>
<td>2</td>
</tr>
<tr>
<td>Group B</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>4</td>
<td>2</td>
</tr>
<tr>
<td>Group C</td>
<td>2</td>
<td>4</td>
<td>1</td>
<td>5</td>
<td>3</td>
</tr>
<tr>
<td>Group D</td>
<td>1</td>
<td>4</td>
<td>2</td>
<td>5</td>
<td>3</td>
</tr>
</tbody>
</table>

| \( b_j \) | \( 0.975 \) | \( 0.725 \) | \( 0.821 \) | \( 0.443 \) | \( 0.836 \) |
| \( b_{\text{max}} \) | \( 1.000 \) | \( 0.898 \) | \( 0.898 \) | \( 0.613 \) | \( 0.898 \) |
| \( b_{\text{max}} - b_j \) | \( 0.025 \) | \( 0.174 \) | \( 0.077 \) | \( 0.170 \) | \( 0.062 \) |
| \( b_j - b_{\text{min}} \) | \( 0.076 \) | \( 0.111 \) | \( 0.208 \) | \( 0.057 \) | \( 0.062 \) |
| \( d_j \) | \( 0.051 \) | \( 0.143 \) | \( 0.143 \) | \( 0.113 \) | \( 0.062 \) |
| \( 1 - d_j \) | \( 0.949 \) | \( 0.857 \) | \( 0.857 \) | \( 0.887 \) | \( 0.938 \) |
| \( X_j \) | \( 0.925 \) | \( 0.621 \) | \( 0.704 \) | \( 0.393 \) | \( 0.784 \) |
| Weight | \( 0.270 \) | \( 0.181 \) | \( 0.205 \) | \( 0.115 \) | \( 0.229 \) |

The calculated membership matrix \( B_5 \) is based on Formula (4), and \( m \) is set as 7.

\[
B_5 = \begin{bmatrix}
1.000 & 0.774 & 0.613 & 0.387 & 0.898 \\
1.000 & 0.898 & 0.774 & 0.613 & 0.898 \\
0.898 & 0.613 & 1.000 & 0.387 & 0.774 \\
1.000 & 0.613 & 0.898 & 0.387 & 0.774
\end{bmatrix}
\]

### Table A7. Weight distribution of the second grade indexes of \( r_6 \).

<table>
<thead>
<tr>
<th>Index</th>
<th>( r_{61} )</th>
<th>( r_{62} )</th>
<th>( r_{63} )</th>
<th>( r_{64} )</th>
<th>( r_{65} )</th>
<th>( r_{66} )</th>
<th>( r_{67} )</th>
<th>( r_{68} )</th>
<th>( r_{69} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Group A</td>
<td>1</td>
<td>2</td>
<td>4</td>
<td>8</td>
<td>3</td>
<td>5</td>
<td>6</td>
<td>7</td>
<td>7</td>
</tr>
<tr>
<td>Group B</td>
<td>2</td>
<td>3</td>
<td>4</td>
<td>8</td>
<td>1</td>
<td>5</td>
<td>5</td>
<td>7</td>
<td>6</td>
</tr>
<tr>
<td>Group C</td>
<td>1</td>
<td>4</td>
<td>2</td>
<td>9</td>
<td>3</td>
<td>7</td>
<td>8</td>
<td>6</td>
<td>5</td>
</tr>
<tr>
<td>Group D</td>
<td>1</td>
<td>3</td>
<td>2</td>
<td>8</td>
<td>1</td>
<td>7</td>
<td>6</td>
<td>5</td>
<td>4</td>
</tr>
</tbody>
</table>

| \( b_j \) | \( 0.989 \) | \( 0.901 \) | \( 0.900 \) | \( 0.433 \) | \( 0.952 \) | \( 0.690 \) | \( 0.663 \) | \( 0.670 \) | \( 0.731 \) |
| \( b_{\text{max}} \) | \( 1.000 \) | \( 0.954 \) | \( 0.954 \) | \( 0.477 \) | \( 1.000 \) | \( 0.778 \) | \( 0.778 \) | \( 0.778 \) | \( 0.845 \) |
| \( b_{\text{max}} - b_j \) | \( 0.011 \) | \( 0.053 \) | \( 0.055 \) | \( 0.044 \) | \( 0.048 \) | \( 0.088 \) | \( 0.115 \) | \( 0.108 \) | \( 0.114 \) |
| \( b_j - b_{\text{min}} \) | \( 0.034 \) | \( 0.056 \) | \( 0.055 \) | \( 0.132 \) | \( 0.048 \) | \( 0.088 \) | \( 0.186 \) | \( 0.068 \) | \( 0.129 \) |
| \( d_j \) | \( 0.023 \) | \( 0.055 \) | \( 0.055 \) | \( 0.088 \) | \( 0.048 \) | \( 0.088 \) | \( 0.151 \) | \( 0.088 \) | \( 0.122 \) |
| \( 1 - d_j \) | \( 0.977 \) | \( 0.945 \) | \( 0.945 \) | \( 0.912 \) | \( 0.952 \) | \( 0.912 \) | \( 0.850 \) | \( 0.912 \) | \( 0.878 \) |
| \( X_j \) | \( 0.966 \) | \( 0.852 \) | \( 0.851 \) | \( 0.395 \) | \( 0.905 \) | \( 0.629 \) | \( 0.563 \) | \( 0.611 \) | \( 0.642 \) |
| Weight | \( 0.151 \) | \( 0.133 \) | \( 0.133 \) | \( 0.062 \) | \( 0.141 \) | \( 0.098 \) | \( 0.088 \) | \( 0.0953 \) | \( 0.100 \) |

The calculated membership matrix \( B_6 \) is based on Formula (4), and \( m \) is set as 11.

\[
B_6 = \begin{bmatrix}
1.000 & 0.954 & 0.845 & 0.477 & 0.903 & 0.778 & 0.699 & 0.602 & 0.602 \\
0.954 & 0.903 & 0.845 & 0.477 & 1.000 & 0.778 & 0.778 & 0.602 & 0.699 \\
1.000 & 0.845 & 0.954 & 0.301 & 0.903 & 0.602 & 0.477 & 0.602 & 0.602
\end{bmatrix}
\]

### Appendix C

(1) The correlation degree matrix of the first grade index \( r_2 \) is calculated as follows:

\[
K(r_2) = (\omega_{21}, \omega_{22}, \omega_{23}, \omega_{24}, \omega_{25}, \omega_{26}, \omega_{27}, \omega_{28}) (K(r_2)) =
\]
\[
K(r_3) = (\omega_{31}, \omega_{32}, \omega_{33}, \omega_{34}, \omega_{35}, \omega_{36}, \omega_{37}, \omega_{38}) (k(r_3)) = \begin{bmatrix}
-0.077 & -0.067 & -0.533 & -0.720 & -0.813 \\
-0.297 & 0.182 & -0.133 & -0.480 & -0.653 \\
-0.258 & 0.438 & -0.233 & -0.540 & -0.693 \\
-0.143 & 0.200 & -0.400 & -0.640 & -0.760 \\
-0.174 & 0.267 & -0.367 & -0.620 & -0.747 \\
-0.347 & -0.059 & 0.067 & -0.360 & -0.573 \\
-0.241 & 0.467 & -0.267 & -0.560 & -0.707 \\
-0.286 & 0.250 & -0.167 & -0.500 & -0.667
\end{bmatrix}
\]

= (-0.075, 0.205, -0.276, -0.566, -0.711);

(3) Correlation degree matrix of the first grade index \( r_4 \) is calculated as follows:
\[
K(r_4) = (\omega_{41}, \omega_{42}, \omega_{43}, \omega_{44}, \omega_{45}, \omega_{46}, \omega_{47}, \omega_{48}, \omega_{49}) (k(r_4)) = \begin{bmatrix}
-0.105 & 0.133 & -0.433 & -0.660 & -0.773 \\
-0.241 & 0.467 & -0.267 & -0.560 & -0.707 \\
-0.273 & 0.333 & -0.200 & -0.520 & -0.680 \\
-0.317 & 0.077 & -0.067 & -0.440 & -0.627 \\
0.087 & 0.147 & 0.134 & 0.145 & 0.086 & 0.104 & 0.086 & 0.057 & 0.155 \\
0.134 & 0.059 & 0.067 & -0.467 & -0.820 & -0.747 \\
0.143 & 0.143 & 0.200 & -0.400 & -0.640 & -0.760 \\
-0.241 & 0.467 & -0.267 & -0.560 & -0.707
\end{bmatrix}
\]

= (-0.204, 0.200, -0.260, -0.540, -0.694);

(4) Correlation degree matrix of the first grade index \( r_5 \) is calculated as follows:
\[
K(r_5) = (\omega_{51}, \omega_{52}, \omega_{53}, \omega_{54}, \omega_{55}) (k(r_5)) = \begin{bmatrix}
0.000 & 0.000 & -0.500 & -0.700 & -0.800 \\
-0.222 & 0.400 & -0.300 & -0.580 & -0.720 \\
0.308 & 0.125 & -0.100 & -0.460 & -0.640 \\
-0.142 & 0.200 & -0.400 & -0.640 & -0.760 \\
-0.297 & 0.182 & -0.133 & -0.480 & -0.653
\end{bmatrix}
\]

= (-0.188, 0.163, -0.286, -0.572, -0.714);

(5) Correlation degree matrix of the first grade index \( r_6 \) is calculated as follows:
\[
K(r_6) = (\omega_{61}, \omega_{62}, \omega_{63}, \omega_{64}, \omega_{65}, \omega_{66}, \omega_{67}, \omega_{68}, \omega_{69}) (k(r_6)) = \begin{bmatrix}
-0.286 & 0.250 & -0.167 & -0.500 & -0.667 \\
-0.241 & 0.467 & -0.267 & -0.560 & -0.707 \\
-0.397 & -0.241 & 0.158 & -0.120 & -0.413 \\
-0.317 & 0.077 & -0.067 & -0.440 & -0.627 \\
0.151 & 0.133 & 0.133 & 0.062 & 0.141 & 0.098 & 0.088 & 0.095 & 0.100 \\
-0.143 & -0.200 & 0.400 & -0.640 & -0.760 \\
-0.297 & 0.182 & -0.133 & -0.480 & -0.653 \\
-0.403 & -0.258 & 0.095 & -0.080 & -0.387 \\
-0.373 & -0.159 & 0.233 & -0.260 & -0.507 \\
-0.273 & 0.333 & -0.200 & -0.520 & -0.680
\end{bmatrix}
\]

= (-0.295, 0.114, -0.103, -0.414, -0.610)
References


