New Models Used to Determine the Dioxins Total Amount and Toxicity (TEQ) in Atmospheric Emissions from Thermal Processes

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Abstract: In order to reduce the calculation effort during the simulation of the emission of polychlorinated dibenzo-p-dioxins and furans (PCDD/F) during municipal solid waste incineration, minimizing the number of simulated components is mandatory. For this purpose, two new multilinear regression models capable of determining the dioxins total amount and toxicity of an atmospheric emission have been adjusted based on previously published ones. The new source of data used (almost 200 PCDD/F analyses) provides a wider range of application to the models, increasing also the diversity of the emission sources, from industrial and laboratory scale thermal processes. Only three of the 17 toxic congeners (1,2,3,6,7,8-HxCDD, 2,3,7,8-TCDF and OCDF), whose formation was found to be linearly independent, were necessary as inputs for the models. All model parameters have been statistically validated and their confidence intervals have been calculated using the Bootstrap method. The resulting coefficients of determination ($R^2$) for the models are 0.9711 ± 0.0056 and 0.9583 ± 0.0085; its root mean square errors (RMSE) are 0.2115 and 0.2424, and its mean absolute errors (MAE) are 0.1541 and 0.1733 respectively.

Keywords: PCDD/F; dioxins formation; MSW incineration; linear regression model; estimation of toxicity; congener profile

1. Introduction

In several countries of the eurozone, municipal solid waste (MSW) generation has constantly increased since the 90s, so its management is a critical environmental issue that society must solve at a future time. The European Commission collects data about the techniques used to it, such as recycling, landfilling, composting, and incineration [1]. Despite the fact that European institutions and many authors consider landfilling as more demanding than MSW incineration [2], other environmental questions, like polychlorinated dibenzo-p-dioxins and dibenzofurans (PCDD/F) atmospheric emissions during combustion processes should be considered [3,4]. Each PCDD/F molecule can contain up to...
eight chlorine atoms in eight different places on the molecule. This combination of number of chlorines and places results in an extensive family of molecules, where each molecule is called a congener.

Combustion processes emit PCDD/Fs as a mixture of up to 210 congeners, of which only 10 dioxins and 7 furans are considered to be toxic and thus most frequently analysed. In order to evaluate the impact of atmospheric emissions, the most common approach is to calculate the amount of toxic equivalents (TEQs) according to NATO/CCMS (North Atlantic Treaty Organization/Committee on the Challenges of Modern Society) [5]. This criterion uses toxic equivalency factors (TEFs) that proportionally modify the amount of each congener considering the most toxic one (2,3,7,8-TCDD) as the reference (unity factor). Despite the fact that TEFs have been questioned [6,7] and updated [8], the International Toxicity Equivalency Factors (I-TEFs) [9] prevail internationally, since most regulations for atmospheric emissions refer to them [10].

Despite the fact that the emission of PCDD/F has been related to industrial processes and human activity, some authors highlight the contribution of forest fires to the total emission of PCDD/Fs [11]. Several studies have been published on the formation of PCDD/F during the combustion of biomass and e-waste [12], demolition and construction wood [13], viscoelastic memory foam [14], furniture [15] and many other different residues. A publication addressing the emissions of a cement production plant [16] determined that, focusing on the distribution of the congeners of their samples, no big differences were observed among their emissions despite the fuel used in the kiln. The formation of PCDD/Fs from MSW incineration showed a strong interdependence with phenols, chlorinated benzenes and other precursors [17]. This interaction was used to suggest a model for the formation of dioxins’ precursors during thermal processes of degradation with the purpose of establishing an on-line measurement instrument [18].

Extensive investigations and reviews related to the formation of PCDD/F during combustion processes have been published [3,19]. However, despite the gigantic attempts, the governing mechanism and the parameters involved such as activity rates still remain uncertain [18]. Once the equilibrium constants of the PCDD/F formation reactions were calculated, it was found that those thermodynamic parameters strongly promote its generation [20–23]. Besides, the distribution of congeners calculated using the equilibrium constants is not consistent with the experimental one [24]. This evidence indicates that other formation mechanisms, along with gas phase reactions, should contribute to PCDD/F formation. Besides, the experimental PCDD/Fs emission values are considerably below the calculated emission values using the thermodynamic equilibrium constants; thus, the thermodynamic equilibrium is never reached. This fact suggests that kinetic mechanisms control the formation of PCDD/F, rather than thermodynamic ones.

The relevance of the kinetic mechanisms reinforces the suggestion that the formation of the PCDD/Fs congeners is interdependent [25], which should lead to a correlation between the amounts of the different congeners produced. This interdependence between the less-chlorinated PCDD/Fs congeners and the TEQ has been modelled [26]; as well as the correlation between TEQ and PCDD/Fs precursors like tri/tetra-chlorobenzene [27], or naphthalene, fluorene, and phenanthrene [28].

The main goal of the present research is to develop a simulation model of a MSW incineration facility and estimate the PCDD/Fs atmospheric emissions on it. A critical consideration during the optimization of the model is reducing the number of simulated chemical species. Specifically, the objective of this study is to update and refine two previously published models [29] in order to increase the scale and the sources of data: From only industrial processes, to both industrial and laboratory thermal decomposition processes. These models are capable of determining the dioxins total amount and toxicity of an atmospheric emission using only the amount of three congeners as regressors. Data on PCDD/Fs atmospheric emission of similar combustion processes are available, containing both concentration and TEQ for all the 17 toxic studied congeners.

As in every statistical analysis, it is also necessary to limit the interval of confidence of the parameters of the models. In this study, in order to evaluate the statistical inference, we used the Bootstrap method, which applies computing power to a fundamental reasoning based on asking “What
would happen if we applied this method many times?" Statistical inference is based on the sampling distributions of sample statistics. The Bootstrap method allows to find the sample distribution, at least approximately, from just one sample [30]. The main steps of this procedure are the following: (a) Resampling: The sampling population is determined using multiple random samples from the population, which are the same size as the original random sample. In order to ensure that, sampling with replacement is performed. This means that, after choosing an observation from the population, it is returned to the population before drawing the next observation, so all observations can be repeated in each sample [31]. (b) Distribution: Depending on the distribution of all the sampling populations, the method of determining values for the estimations will differ [32,33].

In this case, we expect to achieve a normal distribution to associate the values of the parameters of the models to the average of all the observations, its standard error to the standard deviation, and the limits of the interval of confidence to the percentiles 2.5 and 97.5.

2. Experimental

2.1. Data Sources

In our previous work, a set of 130 PCDD/F analyses from IQS-URL Environmental Laboratory were used. The whole analytical method, including sampling, extraction and purification operations for determining the total amount of each PCDD/F congener, was carried out in line with UNE EN 1948:2007 [34]. The data were used to identify the linear dependence between the 17 toxic congeners of PCDD/Fs during their formation. As a result, two models able to determine the total PCDD/F amount and the TEQ of a sample using only the amount of three congeners were adjusted. This dataset, using the decimal logarithm of the values, was named as $X_{\text{OLD}}$ matrix (130 × 17) since it was used in a previous publication [29].

A new set of 64 analyses was obtained from the “Waste, Energy, Environment and Nanotechnology research group (WEEN)” from the University of Alicante, which also contained information about the amounts of all the toxic PCDD/F congeners from their experimental research related to thermal decomposition processes of several kinds of wastes. Within this set, all the PCDD/F concentrations were higher than the limit of quantification (LOQ), trying to reduce all possible interferences due to its uncertainty. The set of values used consists of the decimal logarithm of the amounts of each congener. The interaction between the dataset and the regression line was not excessive in any case. This interaction is studied following the Hat Matrix criterion, considering that its influence should be lower than $3p/n$, where $p$ is the number of regressors and $n$ is the number of samples [35]. This set was named as $X_{\text{NEW}}$ matrix (64 × 17). From this set, a subset was defined discarding the analyses whose values of total PCDD/F amount or TEQ were outside the range of the $X_{\text{OLD}}$ set. This subset, comprising all new data within the range of $X_{\text{OLD}}$ set, was named as $X_{\text{NEW,INT}}$ (28 × 17).

2.2. Methodology

The data set called $X_{\text{NEW}}$ has been used to evaluate the linear dependence between all congeners using the variance inflation factors (VIFs). This methodology has been explained in a previous publication [29]. It is expected that the more independent congeners are similar for both datasets, $X_{\text{NEW}}$ and $X_{\text{OLD}}$. If so, this process is repeated considering all datasets as a unique one.

The data subset called $X_{\text{NEW,INT}}$ has been used to check two linear models that determine the total PCDD/F amount and the TEQ of an atmospheric emission using only the amount of three PCDD/Fs congeners. For this purpose, a graph was constructed whose ordinates were the total amount or TEQ from the analysis and whose abscissae were the amount or TEQ determined by the model. In the best-case scenario, it was supposed to obtain a correlation with a strong linear trend, with its slope equal to one and its intercept equal to zero.

Once the multicollinearity was studied and the previous models were checked using $X_{\text{NEW,INT}}$, a new linear regression was performed using $X_{\text{NEW}}$ and $X_{\text{OLD}}$ together. The methodology used to
adjust a model to data, where the total dioxins’ amount was a linear combination of the independent congeners, was Ordinary Least Squares [36].

\[
C_{TOT} = b_0' + \sum_{j=1}^{k} b'_j C_j
\] (1)

Since the total concentration of PCDD/F cannot be used to determine the toxicity, another linear regression was conducted directly between the amount of each linearly independent congener and the TEQ.

\[
T_{TOT} = b_0 + \sum_{j=1}^{k} b_j C_j
\] (2)

where \(C_j\) was the amount of each congener \(j\), \(C_{TOT}\) was the total PCDD/F amount in the sample, \(T_{TOT}\) was the total TEQ of the sample, \(b_0'\) or \(b_0\) were the intercepts of the linear adjustment, and \(b'_j\) or \(b_j\) were the parameters of the models related to each regressor (where \(k\) is the number linearly independent regressors).

Evaluation of the accuracy of the models is checked by making a graph where the ordinate is the total amount or TEQ from the dataset, and the abscissa is the calculated amount or TEQ using model 1 and model 2, respectively.

Model 1 and model 2 are directly conditioned by the datasets used in their adjustment. In order to quantify how the ability of the models to predict the total amount or the toxicity will vary depending on the dataset used, the resampling Bootstrapping method was used.

This method randomly determines which particular analyses from the sets \(X_{NEW}\) and \(X_{OLD}\) are used to adjust the models. Since the total amount of analyses will remain constant, some analyses may be used more than once in each adjustment. This process is iterated a large number of times (3000 iterations in this case) and all the parameters of each fit are collected in order to determine the confidence interval of the regression parameters. The value of the parameter of the model is equalled to the average of that parameter through all the iterations, and the standard error of that parameter is associated to its standard deviation. The confidence intervals are determined using the percentiles related to the selected statistical significance (95% in this case).

2.3. Software

All calculations and plots have been performed using Microsoft Excel 2013, Version 15.0.5093.1001 by Microsoft Corporation, Redmond, Washington, EUA; R Version 3.3.2 (2016-10-31) by The R Foundation for Statistical Computing, and R Package Rcmdr Version: 2.3.2 (2017-01-02) by Fox (2016).

3. Results

3.1. Multicollinearity and VIFs

Table 1 shows the results of the multicollinearity study. The left half side of the table reflects the VIFs and the associated value of \(R^2\) of the 17 congeners from both datasets \(X_{OLD}\) and \(X_{NEW}\). The right half side of the table, which is used for comparison purposes only, reflects the same parameters but only using \(X_{OLD}\) [29].

Considering the \(X_{OLD}\) dataset, the formation of the congeners 2,3,7,8-TCDF, OCDF and 1,2,3,6,7,8-HxCDD was determined as linearly independent since its \(R^2\) value, which is related to its VIF value following \(VIF_i = 1/(1 - R_i^2)\), is significantly below 0.90. \(R^2\) value related to OCDD is 0.89 but it is not significantly below 0.90 and is to be treated as linearly independent.

Considering the \(X_{OLD} + X_{NEW}\) dataset, it can be observed that all VIFs are lower. This may be caused by the fact that the \(X_{OLD}\) dataset comes from industrial processes and \(X_{NEW}\) dataset comes from laboratory scale and experimental research. Despite these lower values, it is noticeable that
the seven more independent congeners are the same in both datasets, although in a different order, as shown in Table 1. This fact reflects that the correlation between the formation of all 17 congeners is similar enough in both datasets, even considering the differences that may occur between industrial processes and laboratory scale processes.

Since this similar behaviour has been demonstrated, combining both datasets cannot be considered as arbitrary. Thus, congeners 2,3,7,8-TCDF, OCDF and 1,2,3,6,7,8-HxCDD are still considered as the ones linearly independent.

Table 1. Results for VIFs of each congener calculated sequentially, discarding the most linearly dependent congener after each iteration. The left half shows the results for both datasets mixed together (X_{OLD} + X_{NEW}) and the right half shows the results from X_{OLD} as a comparison [29].

<table>
<thead>
<tr>
<th>R²</th>
<th>VIF</th>
<th>Congener</th>
<th>Number</th>
<th>Number</th>
<th>Congener</th>
<th>VIF</th>
<th>R²</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.9875</td>
<td>80.2</td>
<td>1,2,3,6,7,8-HxCDF</td>
<td>5</td>
<td>5</td>
<td>1,2,3,6,7,8-HxCDF</td>
<td>639.3</td>
<td>0.9984</td>
</tr>
<tr>
<td>0.9850</td>
<td>66.9</td>
<td>1,2,3,7,8-PeCDF</td>
<td>2</td>
<td>12</td>
<td>1,2,3,7,8-PeCDD</td>
<td>423.2</td>
<td>0.9976</td>
</tr>
<tr>
<td>0.9745</td>
<td>39.2</td>
<td>1,2,3,4,7,8-HxCDD</td>
<td>13</td>
<td>16</td>
<td>1,2,3,4,6,7,8-HpCDD</td>
<td>315.2</td>
<td>0.9968</td>
</tr>
<tr>
<td>0.9720</td>
<td>35.7</td>
<td>1,2,3,4,7,8-HxCDF</td>
<td>4</td>
<td>3</td>
<td>2,3,4,7,8-PeCDF</td>
<td>168.0</td>
<td>0.9940</td>
</tr>
<tr>
<td>0.9682</td>
<td>31.5</td>
<td>1,2,3,4,6,7,8-HpCDD</td>
<td>16</td>
<td>4</td>
<td>1,2,3,4,7,8-HxCDF</td>
<td>141.0</td>
<td>0.9929</td>
</tr>
<tr>
<td>0.9636</td>
<td>27.5</td>
<td>1,2,3,4,6,7,8-HpCDF</td>
<td>8</td>
<td>15</td>
<td>1,2,3,7,8,9-HxCDD</td>
<td>121.9</td>
<td>0.9918</td>
</tr>
<tr>
<td>0.9625</td>
<td>26.7</td>
<td>2,3,4,7,8-PeCDF</td>
<td>3</td>
<td>9</td>
<td>1,2,3,4,7,8,9-HpCDF</td>
<td>99.6</td>
<td>0.9900</td>
</tr>
<tr>
<td>0.9584</td>
<td>24.0</td>
<td>1,2,3,4,7,8,9-HpCDF</td>
<td>9</td>
<td>2</td>
<td>1,2,3,7,8-PeCDF</td>
<td>81.1</td>
<td>0.9877</td>
</tr>
<tr>
<td>0.9564</td>
<td>22.9</td>
<td>1,2,3,7,8-PeCDD</td>
<td>12</td>
<td>8</td>
<td>1,2,3,4,6,7,8-HpCDD</td>
<td>64.5</td>
<td>0.9845</td>
</tr>
<tr>
<td>0.9477</td>
<td>19.1</td>
<td>1,2,3,7,8,9-HxCDD</td>
<td>15</td>
<td>13</td>
<td>1,2,3,4,7,8-HxCDD</td>
<td>52.8</td>
<td>0.9811</td>
</tr>
<tr>
<td>0.9364</td>
<td>15.7</td>
<td>2,3,4,6,7,8-HxCDF</td>
<td>6</td>
<td>6</td>
<td>2,3,4,6,7,8-HxCDF</td>
<td>31.8</td>
<td>0.9686</td>
</tr>
<tr>
<td>0.9111</td>
<td>11.2</td>
<td>OCDF</td>
<td>10</td>
<td>7</td>
<td>1,2,3,7,8,9-HxCDF</td>
<td>14.1</td>
<td>0.9289</td>
</tr>
<tr>
<td>0.8839</td>
<td>8.6</td>
<td>1,2,3,6,7,8-HxCDD</td>
<td>14</td>
<td>11</td>
<td>2,3,7,8-TCDD</td>
<td>10.8</td>
<td>0.9073</td>
</tr>
<tr>
<td>0.8039</td>
<td>5.1</td>
<td>1,2,3,7,8,9-HxCDF</td>
<td>7</td>
<td>17</td>
<td>OCDD</td>
<td>9.3</td>
<td>0.8925</td>
</tr>
<tr>
<td>0.7823</td>
<td>4.6</td>
<td>2,3,7,8-TCDF</td>
<td>1</td>
<td>14</td>
<td>1,2,3,6,7,8-HxCDD</td>
<td>5.2</td>
<td>0.8876</td>
</tr>
<tr>
<td>0.7834</td>
<td>4.6</td>
<td>2,3,7,8-TCDD</td>
<td>11</td>
<td>10</td>
<td>OCDF</td>
<td>3.4</td>
<td>0.7096</td>
</tr>
<tr>
<td>0.5803</td>
<td>2.2</td>
<td>OCDD</td>
<td>17</td>
<td>1</td>
<td>2,3,7,8-TCDF</td>
<td>2.4</td>
<td>0.5857</td>
</tr>
</tbody>
</table>

3.2. Testing Previous Models Using X_{NEW,INT}

Two previous models capable of determining the dioxins total amount and toxicity (TEQ) of an atmospheric emission based on the concentration of 1,2,3,6,7,8-HxCDD, OCDF and 2,3,7,8-TCDF which have been tested with the dataset X_{NEW,INT}. As explained above, this dataset comprises a number of 28 new PCDD/F analyses from laboratory experiments whose total amount and TEQ fall within the range of the X_{OLD} set. Figure 1 shows the interrelationship between the calculated dioxins total amount and TEQ using previous models 1 and 2 and the values from dataset X_{NEW,INT}. In these graphs, it is worth mentioning that the linear trend is still strong, even acknowledging that the slope is not close to 1 and the intercept is not close to zero. This fact suggests that a new adjustment of the model may be needed.
null hypothesis (H0) supposes that the tested congener and the total PCDD/F amount are not interdependent at all (H0: Parameter \(b_j = 0\)). Since the evaluation of p-values gave extremely low values, all of the parameters of model 1’ can be considered as significantly different to zero. This fact and the high value of R\(^2\) are enough to validate model 1’ for Equation (1).

### Table 2. Parameters and statistic data for the readjusted models: model 1’ for predicting PCDD/F amounts (pg) and model 2’ for TEQ values (pg I-TEQ).

<table>
<thead>
<tr>
<th>Model</th>
<th>Variable</th>
<th>Parameters</th>
<th>(b_{14})</th>
<th>(b_{10})</th>
<th>(b_1)</th>
<th>(b_0)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1’</td>
<td>n = 194</td>
<td>Value</td>
<td>0.351</td>
<td>0.389</td>
<td>0.225</td>
<td>1.560</td>
</tr>
<tr>
<td></td>
<td>R(^2) = 0.9705</td>
<td>Std. error</td>
<td>0.0258</td>
<td>0.0207</td>
<td>0.0216</td>
<td>0.0309</td>
</tr>
<tr>
<td></td>
<td></td>
<td>p-value for (H_0 : b_j = 0)</td>
<td>&lt;0.0000</td>
<td>&lt;0.0000</td>
<td>&lt;0.0000</td>
<td>&lt;0.0000</td>
</tr>
<tr>
<td>2’</td>
<td>n = 194</td>
<td>Value</td>
<td>0.349</td>
<td>0.182</td>
<td>0.378</td>
<td>0.762</td>
</tr>
<tr>
<td></td>
<td>R(^2) = 0.9575</td>
<td>Std. error</td>
<td>0.0295</td>
<td>0.0237</td>
<td>0.0247</td>
<td>0.0354</td>
</tr>
<tr>
<td></td>
<td></td>
<td>p-value for (H_0 : b_j = 0)</td>
<td>&lt;0.0000</td>
<td>&lt;0.0000</td>
<td>&lt;0.0000</td>
<td>&lt;0.0000</td>
</tr>
</tbody>
</table>

The same method was replicated to adjust model 2’ based on Equation (2), where the TEQ was a linear combination of the amount of 2,3,7,8-TCDF, OCDF and 1,2,3,6,7,8-HxCDD. The results for this model 2’, using datasets \(X_{\text{OLD}}\) and \(X_{\text{NEW}}\), are shown in Table 2. The value of R\(^2\) for model 2’ was 0.9575, and the Adjusted R\(^2\) was 0.9570. Following the same criteria as for model 1’, the possibility of overfitting is discarded since both R\(^2\) and Adjusted R\(^2\) are almost equal.

Figure 2 shows the relationship between the dioxins amount or TEQ, determined with models 1’ and 2’, respectively, and the results from the chemical analysis provided by the laboratory.
The results of the bootstrapping are shown in Table 4. The values of the percentile 2.5 and 97.5 represent the limits of the interval of confidence of 95%. The results of the bootstrapping are shown in Table 4.

Comparing the values of the parameters determined in Table 2 with the interval of confidence determined in Table 4, it is noticeable that all of them are in the interval of confidence and also close to the average value.

Regarding the values of $R^2$ and its low standard error it can be concluded that the percent of variability expressed through model 1' and model 2' is very stable to changes in the used dataset. The accuracy of the models has also been evaluated calculating the mean absolute error and the root mean squared error. Mean absolute error (MAE) values were 0.1541 and 0.1733 for model 1' and model 2', respectively. Root mean square error (RMSE) values were 0.2115 and 0.2424.

### Table 3. Parameters for the testing of the readjusted model linear regressions.

<table>
<thead>
<tr>
<th>Model</th>
<th>1'</th>
<th>2'</th>
</tr>
</thead>
<tbody>
<tr>
<td>Regression Parameters</td>
<td>Slope</td>
<td>Intercept</td>
</tr>
<tr>
<td>Value</td>
<td>1.000</td>
<td>0.000</td>
</tr>
<tr>
<td>Std. Error</td>
<td>0.0126</td>
<td>0.0482</td>
</tr>
<tr>
<td>p-value for $H_0$ : Intercept = 0</td>
<td>-</td>
<td>1.0000</td>
</tr>
<tr>
<td>p-value for $H_0$ : Slope = 1</td>
<td>1.0000</td>
<td>-</td>
</tr>
</tbody>
</table>

### 3.4. Validating Model 1' and Model 2' Using Bootstrapping

Once models 1' and 2' are adjusted, the confidence intervals of their parameters are determined by an iterative resampling method with replacement. The resulting values obtained using the bootstrap method follow a normal (Gaussian) distribution. Hence, the value of each parameter used to define model 1' and model 2' will be equalled to the average of the values collected through 3000 iterations. The values of the percentiles 2.5 and 97.5 represent the limits of the interval of confidence of 95%. The results of the bootstrapping are shown in Table 4.

Comparing the values of the parameters determined in Table 2 with the interval of confidence determined in Table 4, it is noticeable that all of them are in the interval of confidence and also close to the average value.

Regarding the values of $R^2$ and its low standard error it can be concluded that the percent of variability expressed through model 1' and model 2' is very stable to changes in the used dataset. The accuracy of the models has also been evaluated calculating the mean absolute error and the root mean squared error. Mean absolute error (MAE) values were 0.1541 and 0.1733 for model 1' and model 2', respectively. Root mean square error (RMSE) values were 0.2115 and 0.2424.
Table 4. Bootstrapping method results.

<table>
<thead>
<tr>
<th>Model</th>
<th>Variable</th>
<th>( R^2 )</th>
<th>( b_{14} )</th>
<th>( b_{10} )</th>
<th>( b_1 )</th>
<th>( b_0 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>1’</td>
<td>Average</td>
<td>0.9711</td>
<td>0.354</td>
<td>0.386</td>
<td>0.225</td>
<td>1.560</td>
</tr>
<tr>
<td></td>
<td>Std. Error</td>
<td>0.0056</td>
<td>0.0387</td>
<td>0.0285</td>
<td>0.0316</td>
<td>0.0423</td>
</tr>
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<td></td>
<td>Percentile 2.5</td>
<td>0.9587</td>
<td>0.274</td>
<td>0.327</td>
<td>0.166</td>
<td>1.480</td>
</tr>
<tr>
<td></td>
<td>Percentile 97.5</td>
<td>0.9812</td>
<td>0.429</td>
<td>0.439</td>
<td>0.290</td>
<td>1.640</td>
</tr>
<tr>
<td>2’</td>
<td>Average</td>
<td>0.9583</td>
<td>0.350</td>
<td>0.180</td>
<td>0.379</td>
<td>0.759</td>
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<tr>
<td></td>
<td>Std. Error</td>
<td>0.0085</td>
<td>0.0364</td>
<td>0.0286</td>
<td>0.0356</td>
<td>0.0518</td>
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<td></td>
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<td>0.124</td>
<td>0.307</td>
<td>0.656</td>
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<td>Percentile 97.5</td>
<td>0.9734</td>
<td>0.421</td>
<td>0.237</td>
<td>0.447</td>
<td>0.862</td>
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</table>

3.5. Comparison with Previous Models

As shown in the previous sections, models 1’ and 2’ proposed in the present work can satisfactorily determine the total PCCD/F amount and TEQ from thermal processes based on the amount of only three congeners as an input. Compared to our previously published models [29], the current ones have a wider range of application, with increased number and sources of data. The dataset used to adjust the new models comprised 194 analyses \((X_{\text{OLD}} + X_{\text{NEW}})\), as opposed to the 130 used in our previous work \((X_{\text{OLD}})\), which represents an increase of almost 50% in the number of considered sources. In addition, the new dataset included data not only from industrial processes, but also from laboratory thermal decomposition experiments, broadening the scope of application of the models.

Considering that all 194 analyses come from thermal decompositions from plenty of different industrial and laboratory-scale processes, our models 1’ and 2’ can be considered suitable for combustion processes overall. This assumption increases the range of application of our first models considerably.

In the same way as in the previously published models, their main limitation to calculate the total PCDD/F amount or TEQ is that the values of the amounts of the three congeners must be above the LOQ.

Many other models have been proposed, based on the interdependence between the concentration of mono- to tri-chlorinated dibenzo-\(p\)-dioxins and TEQ or the total concentration [26], with lower values for the coefficient of determination. The P-values of many of these models that use low chlorinated PCDD/Fs as regressors also reflect that the correlations may be determined by chance. Furthermore, the use of mono- to tri-chlorinated dibenzo-\(p\)-dioxins as a regressor is not as favourable as the use of some of the 17 toxic congeners, since the low-chlorinated PCDD/F congeners frequently are not analysed nor controlled by the legislation. The coefficient of determination of another model that determines the correlation between PAHs and PCDD/Fs was 0.62, while the value of the same parameter considering the multiple regression analysis with naphthalene, fluorene and phenanthrene as regressors was 0.85 [28]. This correlation between PAHs and PCDD/Fs has also been considered as obvious in emissions produced by the co-incineration of MSW and coal, modifying the S/Cl ratio [37]. Our new models 1’ and 2’ are still more accurate than other correlations used to estimate the PCDD/Fs concentration on-line, based on the concentration of precursors like trichlorobenzene and tetrachlorobenzene, whose coefficients of determination were around 0.89 [27].

Despite a multilinear model has been able to estimate the total amount and toxicity properly, these models could be improved in the future fitting a neural network model. The next step in our investigation is to use these new models to determine a kinetic model able to estimate the emission of PCDD/Fs from process parameters such as temperature, oxygen ratio, pressure, etc. The main advantage of using these new models is that only the formation of three congeners has to be determined to be able to estimate the total emission. Once this kinetic model is determined it can be used to optimize the process of municipal solid waste incineration and reduce the emission of PCDD/Fs.
4. Conclusions

Two previous models that estimate the total PCDD/F amount and toxicity (TEQ) based on the amounts of 1,2,3,6,7,8-HxCDD, OCDF and 2,3,7,8-TCDF have been tested using new analyses from laboratory runs.

The use of these models verifies the existence of a strong linear trend, despite the value of the slope being significantly different to 1 and the value of the intercept being significantly different to 0 when applied to the new data.

The multicollinearity of the 130 analyses used to determine those previous models has been compared to the multicollinearity of 64 new analyses, producing very similar results. It has been assumed that for the dataset of all the 194 analyses, the same congeners can be considered as linearly independent.

Those two models have been readjusted with the 194 analyses using multiple linear regression. The new models have been validated examining the residual analysis of the regression and also checking the validity of the slope and the intercept with its associated p-value.

The intervals of confidence of the parameters of the models have been calculated using Bootstrapping method. It has been demonstrated that the percent of variability expressed through model 1′ and model 2′ is very stable to changes in the used dataset.

The accuracy of the models has also been evaluated calculating the mean absolute error and the root mean squared error. MAE values were 0.1541 and 0.1733 and RMSE values were 0.2115 and 0.2424 for model 1′ and model 2′.

Thanks to the readjustment of the models with more analyses, the current ones present a wider scope of application, with an increase in the scale and the sources of data, modelling combustion processes overall.

These new models are now ready to be used to simplify a kinetic model that estimates the formation of PCDD/Fs during municipal solid waste incineration. This kinetic model will only need to estimate the formation of three congeners instead of 17, which will decrease the calculation effort when using it.

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References


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