A New Model for Environmental Assessment of the Comminution Process in the Chain of Biomass Energy Processing †

Weronika Kruszelnicka

Department of Technical Systems Engineering, Faculty of Mechanical Engineering, University of Science and Technology in Bydgoszcz, 85-796 Bydgoszcz, Poland; weronika.kruszelnicka@utp.edu.pl

† This paper is an extended version of article presented at the 6th Scientific Conference Renewable Energy Systems, Engineering, Technology, Innovation ICoRES 2019, to be published in E3S Web of Conferences.

Abstract: Acquiring energy contained in biomass requires its prior appropriate preparation. These treatments require some energy inputs, which significantly affect the reduction of the energy and the environmental balance in the entire life cycle of the biomass energy processing chain. In connection with the above, the aim of this work is to develop a methodology for the environmental assessment of biomass grinding in the processing chain for energy purposes. The research problem is formulated as follows: Is it possible to provide an assessment model that takes into account the environmental inputs and benefits of the grinding process of biomass intended for further energy use (for example, combustion)? How do the control variables of the grinding machine affect the environmental process evaluation? In response to these research problems, an original, carbon dioxide emission assessment index of the biomass grinding process was developed. The model was verified by assessing the process of rice and maize grinding on a real object—a five-disc mill—with various speed settings of the grinding disc. It was found that the carbon dioxide emission assessment model developed provides the possibility of comparing grinding processes and identifying the grinding process with a better CO\textsubscript{2} emission balance, where its values depend on the control parameters of the mill.

Keywords: disc-mill; efficiency; carbon dioxide; rice; corn; grinding

1. Introduction

Grinding processes are one of the most commonly used preparatory processes for energy carriers (fossil and alternative) intended for combustion and co-combustion [1,2] and biofuel production [3–5]. These biomass forms may include plant-based lignocellulose waste [6,7], sewage waste [8,9], and animal-based meat processing waste [10]. To enhance the utilization of these biomass forms for direct combustion [11,12] or as a biorefinery feedstock [1,7], size reduction approaches typically constitute a significant pre-treatment step that must be undertaken [13]. This is because size reduction operations serve to enhance accessibility to the stored carbon present in biomass. Such size reduction is predominantly carried out on cylindrical mills, drum mills, ball mills, hammer mills, and disc mills [13,14]. Hammer and disc mills yield the best results in terms of the grinding product quality, energy consumption, and efficiency [1,13]. The main goals of grinding granular biomass, as well as other energy materials (e.g., coal, wood), include the reduction of dimensions, the release of substances contained in the material structure, and an increase in the material-specific surface area so that the energy contained in its structure can be released faster [15–18]. In order to maximize the potential of ground raw materials, energy consumption during grinding (processing) should be as low as
possible [19]. Unfortunately, mills and grinders currently in use are still characterized by high energy consumption and low efficiency [15,20]. Undertaking research, creating structural and technological solutions aimed at improving the energy and environmental efficiency of grinding systems, is significant. The key element is the implementation of eco-innovative systems, starting with assessment at the design stage with the use of a multi-criteria analysis, as one example [21,22]. Criteria for the selection of grinding technology and the assessment of its operation should clearly indicate solutions that meet the assumptions of sustainable development [23–25].

Assessment criteria that refer to the concept of environmental efficiency can be interpreted as the efficiency of innovative and environmental actions and the consequences of the environmental impact of machines, devices, and engineering equipment [26]. The concept of a product assessment based on the so-called eco-efficiency and related indexes is becoming more and more popular [26,27]. The major assumption of eco-efficiency is to work out a technological solution with the best cost-to-benefit ratio while maintaining a reduction of the environmental impacts [27,28]. Huppes and Ishikawa [29] proposed four indexes to be used for the assessment of a technology’s (Table S1) environmental productivity (Table S1, Equation (1)), environmental intensity of production (Table S1, Equation (2)), environmental improvement cost (Table S1, Equation (3)) and environmental cost-effectiveness (Table S1, Equation (4)) which is a combination of the relations between the environmental indexes and the economic results. LCA (life cycle assessment) is a method for assessing environmental impacts [30]. LCC (life cycle costing) is used for assessing economic efficiency [31] and PSIA product impact social assessment is a method used for assessing social impacts [32]. LCA and LCC methods for assessing the grinding process constitute just one of many other elements to be used to assess technological biomass processing in its entirety, either for energy or food production purposes [30,33–36]. MFA (material flow analysis) is another assessment method that focuses on the flow of material between particular stages of the technological process [37]. Knowledge of the quantitative demand for materials in the manufacturing process is also used by the MAIA (material intensity analysis), which is based primarily on determining MIPS (material input per service unit index) (Table S1, Equation (5)), which defines the amount of natural resources needed to manufacture a product or provide a service [38]. X factor, defined as the ratio of the eco-efficiency of the product under assessment to that of the reference product, described in [39], can also be used for eco-efficiency assessment (Table S1, Equation (6)). X factor makes it possible to determine how far the manufactured product is from the performance level of the reference product. It allows one to compare different manufacturing variants of the same product on the basis of the ratio of the product being assessed to the reference product’s eco-efficiency level (Table S1, Equation (6)). Tahara et al. [40] have proposed the ICEICE (integrated CO2 efficiency index for company evaluation) including indirect and direct CO2 emissions in combination with economic effects and total CO2 efficiency, direct CO2 efficiency, and indirect CO2 efficiency calculated on the basis of indexes (Table S1, Equations (7)–(9)). Bennet et al. [41] have developed an optimization tool—Eco Compass—which can be used to support decision making processes in business to meet the demand according to sustainable development assumptions. Kasner [42] has proposed an integrated life cycle index (Table S1, Equation (10)) to determine efficiency in obtaining benefits from technological costs involved in the entire life cycle, which includes manufacturing costs, operational costs, and post-use management costs. This index takes advantage of data regarding the environmental impact obtained with the use of LCA [43]. The indexes and criteria presented herein can successfully be adapted for evaluation of the grinding process through appropriate modeling. Eco-efficiency models developed for technology make it possible to compare the technologies under consideration (products) in a scalar form and select a technology that is best in terms of productivity, the economy, and the environment [44].

Only a few works address the environmental assessment of the grinding process exclusively in terms of ecology [45–49]. In many works, specific energy consumption and fragmentation degree have been indicated as two basic criteria for the assessment of this process [50–53]. Flizikowski et al. [45] proposed an environmental efficiency index to assess the grinding process defined as a ratio of CO2 emissions produced by grinding to the biomass energy use for outlays in the form of emissions of
equivalent CO₂ in the process of grinding (Table S2, Equation (1)). Mroziński et al. [46] showed an
index of environmental non-destructivity defined as a ratio of equivalent CO₂ emissions to electric
energy consistent with this equivalent (Table S2, Equation (2)). Kruszelnicka et al. [48] discussed a
material energy efficiency index, which refers to indirect emissions involved in the process of energy
different materials (Table S2, Equation (3)). In other studies [47,49], Kruszelnicka proposed a
sustainable emissivity index for the environmental assessment of grinding, which also refers to indirect
emissions involved in grinding (Table S2, Equation (4)), making it possible to optimize the grinder disc
process parameter settings.

In view of the above, the aim of the work is to develop a methodology for the carbon dioxide
emission assessment of biomass grinding in the processing chain for energy purposes. The research
problem is formulated as follows: Is it possible to create an assessment model that takes into account
the environmental inputs and benefits of the grinding process of biomass intended for further energy
use (for example combustion)? How do the control variables (the angular velocity of the cutting edges
of working elements) of the grinding machine affect the carbon dioxide emissions of the process [54]?
To obtain an answer to the research problem, a model was developed for the carbon dioxide emission
assessment of the grinding process, including the relations between the benefits from energy biomass
grinding and the environment-related costs used for grinding. Verification of the model was carried
out on a real object—a five-disc mill. Dependences between the angular speed settings of the grinding
discs and the values of the proposed assessment model were identified to indicate parameters that
provide the assessment index with the best values. A mathematical model of the proposed sustainable
CO₂ emissions indicator, the test stands and the experiment conditions are described in Section 2.
Section 3 contains the results and a discussion. The discussion has been summarized and the most
important conclusions are included in Section 4.

2. Materials and Methods

2.1. Model of a Sustainable CO₂ Emissions Index

The proposed model of a sustainable CO₂ emissions index is based on the assumption of
environmental assessment models of the grinding process (Table S2, Equations (1) and (2)) presented
in [45,46]. Equivalent CO₂ emissions in the grinding process are closely related to its energy
consumption [45–49]. Considering a system whose aim is to reduce the process, product, machine,
and environmental impacts (e.g., by eliminating CO₂) while maintaining its higher efficiency and
providing a high-quality product as well as energy efficiency, the integrated energy purpose of product
(for example, combustion) sustainable CO₂ emissions index can be expressed as [54,55]

\[ W_{ZCO₂} = \frac{\Delta B_{CO₂}}{N_{CO₂}} \]  

(1)

where

\( \Delta B_{CO₂} \) — environmental benefits—change in CO₂ emissions,

\( N_{CO₂} \) — environmental costs of grinding—energy consumption.

The one factor influencing the positive change in carbon dioxide balance can be described as CO₂
emissions, for example, from the burnt ground energy biomass \( X_{BCO₂} \), because biomass is a renewable
fuel, which during the growth phase, absorbs an amount of carbon dioxide equal to the emissions from
its energy use [56]. Additionally, in industrial emission monitoring systems, CO₂ emission indexes
from biomass are treated as zero [57]. These should be reduced by equivalent CO₂ emissions related to
energy consumption in the grinding process \( X_{RCO₂} \) in accordance with the equation on environmental
benefits [54]:

\[ \Delta B_{CO₂} = X_{BCO₂} - X_{RCO₂} \]  

(2)

where
$X_{BCO_2}$—CO$_2$ emissions from the energy use (for example, combustion) of ground biomass, kgCO$_2$eq.

$X_{RCO_2}$—the amount of CO$_2$ emissions associated with the use of electricity in the grinding process, kgCO$_2$eq.

The results of previous research show that the energy properties of biomass (especially its digestibility, exergy) change depending on the degree of fineness (post-grinding particle size) \[46,55,58\]; therefore, it was accepted that emissions from the combustion of ground biomass $X_{BCO_2}$ are expressed as the sum of emissions from the combustion of biomass divided into size classes, according to the equation \[54\]:

$$X_{BCO_2} = m_B \cdot \sum (J_{ACO_2} \cdot W_{Bi} \cdot q_i)$$  \hspace{1cm} (3)

where

$m_B$—mass of ground biomass, kg,

$J_{ACO_2}$—unit CO$_2$ emissions for the $i$-th size class of biomass, kg·kWh$^{-1}$,

$W_{Bi}$—calorific value of the $i$-th size class of biomass, kWh·kg$^{-1}$,

$q_i$—mass share of the $i$-th size class of biomass.

The emissions involved in electricity consumption during grinding are described as follows \[54\]:

$$X_{RCO_2} = E_{cM} \cdot J_{KCO_2}$$  \hspace{1cm} (4)

where

$E_{cM}$—total energy consumption of the grinding machine during the grinding of a mass of biomass $m_B$, kWh,

$J_{KCO_2}$—emissions of carbon dioxide for the production of electric energy from coal, kgCO$_2$eq·kWh$^{-1}$.

In this case, environmental costs were assumed as total energy consumption $E_{cM}$ for biomass grinding. Taking into account the above and Dependencies (3) and (4), the sustainable CO$_2$ emissions index will take the form \[54\]:

$$W_{ZCO_2} = (X_{BCO_2} - X_{RCO_2}) / E_{cM} = (m_B \cdot \sum (J_{ACO_2} \cdot W_{Bi} \cdot q_i) - E_{cM} \cdot J_{KCO_2}) / E_{cM}$$  \hspace{1cm} (5)

Knowing that the mass of the ground biomass $m_B$ is related to grinding efficiency $Q$:

$$Q = \frac{m_B}{t} \Rightarrow m_B = Q \cdot t$$  \hspace{1cm} (6)

$Q$—grinding efficiency, kg·h$^{-1}$,

$t$—time, h,

and that the energy used in the grinding process $E_{cM}$ is equal to

$$E_{cM} = \sum P_i \cdot t = P_c \cdot t$$  \hspace{1cm} (7)

where

$P_i$—power on the $i$-th grinding element,

$P_c$—total power of the grinder.

Then Equation (5) assumes the following form:

$$W_{ZCO_2} = (Q \cdot t \cdot \sum (J_{ACO_2} \cdot W_{Bi} \cdot q_i) - P_c \cdot t \cdot J_{KCO_2}) / P_c \cdot t$$  \hspace{1cm} (8)
which after being reduced by time $t$, gives

$$W_{ZCO^2} = \frac{(Q \sum (JACO^2 \cdot W_{Bi} \cdot q_i) - P_c \cdot JKCO^2)}{P_c}$$  \hspace{1cm} (9)$$

In this way, Equation (9), including the most important characteristics of the grinding process, that is, efficiency, the power of the grinding unit, and the product degree of fineness, is provided. Both the power and the product degree of fineness depend on the angular speeds of rotating elements. In the case of multi-disc grinders, this concerns the angular speeds of the grinding discs. Thus, it can be supposed that the values of the sustainable emissivity index will also depend on the angular speeds of the discs, which have been verified in this study.

For the machine idle gear, when $E_{cM} > 0$ and $m_B = 0$, the quantity of emissions from groundmass is equal to 0, which yields:

$$W_{ZCO^2(min)} = (-P_c \cdot JKCO^2)/P_c = -JKCO^2$$  \hspace{1cm} (10)$$

Thus, the lowest value of emissions that can be assumed by the sustainable indicator is emissions equal to unit emissions from electrical energy produced from coal (Figure 1).

The level of emissions of CO$_2$eq from fossil fuels to be sustained by emissions from alternative fuels occurs at $W_{ZCO^2} = 0$ (Figure 1), that is, when

$$Q \sum (JACO^2 \cdot W_{Bi} \cdot q_i) - P_c \cdot JKCO^2 = 0$$  \hspace{1cm} (11)$$

$$Q \sum (JACO^2 \cdot W_{Bi} \cdot q_i) = P_c \cdot JKCO^2$$  \hspace{1cm} (12)$$

In order to reach energy sustainability (with an assumption that the mass to be ground will be used for the production of electrical energy to power the grinder), the value of electric energy produced from the combustion of biomass $E_B$ should be at least equal to that used in the grinding process:

$$E_{cM} = E_B$$  \hspace{1cm} (13)$$

The level of energy obtained from combusted biomass is

$$E_B = Q \cdot t \cdot k_3 \sum W_{Bi} \cdot q_i$$  \hspace{1cm} (14)$$

where:

$W_{ZCO^2}$ values, when $E_B > E_{cM}$

$W_{ZCO^2}$ values, when $X_{BCO^2} > X_{RCO^2}$

Figure 1. Graphic interpretation of the sustainable CO$_2$ emissions index.
$W_{B_{\text{min}}}$—minimal calorific value from the set of values of the $i$-th biomass fractions $W_{Bi}$, $k_k = 0.4$—co-generation coefficient [59].

Substituting Equations (7) and (14) for Equation (13) yields:

$$P_c = Q_k \sum W_{Bi}q_i$$

(15)

In an associated production of electric energy from heat energy obtained from biomass combustion, unit emissions (per 1 kWh$_e$ of generated electric energy) $I_{ACO_{2e}}$ is expressed in the following way:

$$I_{ACO_{2e}} = I_{ACO_{2}}/k_k$$

(16)

hence, the value of the sustainable CO$_2$ emissions index for sustainable $W_{ZCO_{2(e)}}$ is

$$W_{ZCO_{2(e)}} = (Q_k \sum W_{Bi}q_i/J_{ACO_{2e}} - Q_k \cdot k_k \cdot J_{KCO_{2}} \sum W_{Bi}q_i)/Q_k \sum W_{Bi}q_i$$

(17)

after reduction it is

$$W_{ZCO_{2(e)}} = \sum W_{Bi}q_i/J_{ACO_{2}}/\sum W_{Bi}q_i - J_{KCO_{2}}$$

(18)

and considering Equation (16):

$$W_{ZCO_{2(e)}} = (\sum W_{Bi}q_i/J_{ACO_{2e}}/k_k)/\sum W_{Bi}q_i - J_{KCO_{2}}$$

(19)

The minimal value of the sustainable CO$_2$ emissions index occurs for energy sustainability when 100% ($q_i = 1$) of the grinding product (combusted biomass) is the fraction with the lowest unit CO$_2$ emissions, thus yielding:

$$W_{ZCO_{2(min)}} = (W_{B(JACO_{2min})}/J_{ACO_{2min}}/k_k)/W_{B(JACO_{2min})}/q_i - J_{KCO_{2}}$$

(20)

Considering that $q_i = 1$, Equation (20) takes the form:

$$W_{ZCO_{2(min)}} = W_{B(JACO_{2min})}/J_{ACO_{2min}}/k_k - W_{B(JACO_{2min})}/J_{KCO_{2}}$$

(21)

and being reduced:

$$W_{ZCO_{2(min)}} = J_{ACO_{2min}}/k_k - J_{KCO_{2}}$$

(22)

Equation (22) implies that

- if $J_{ACO_{2min}}/k_k > J_{KCO_{2}}$ then $W_{ZCO_{2(min)}} > 0$;
- if $J_{ACO_{2min}}/k_k < J_{KCO_{2}}$ then $W_{ZCO_{2(min)}} < 0$.

2.2. Conditions of Experimental Model Verification

Verification of the model of the sustainable CO$_2$ emissions index involved carrying out an experiment with the use of a real object. Tests were performed in the following order:

1. Choice and preparation of the test stand;
2. Choice and preparation of the biomass to be tested;
3. Determination of grinding conditions and the tests program;
4. Comminution of the biomass while monitoring functional characteristics of grinding;
5. Determination of calorific values and emission values for given biomass fractions after comminution;
6. Calculation of the value of the sustainable CO$_2$ emissions index;
7. Analysis of the relations between the emissions index and the angular speed of the working elements cutting edges.
2.2.1. Test Stand

A mathematical model of the sustainable CO₂ emissions index for the grinding process in the biomass processing chain has been developed to be implemented in a self-regulating control grinding system. The tests were conducted for a five-disc mill drive. The test stand consisted of a grinding unit (of a five-disc grinder) equipped with modules to control and monitor the functional characteristics of the mill control unit and the feed system. Figure 2 shows a view of the test stand.

![Figure 2. Test stand for monitoring the process of multi-disc grinding](image)

The main elements of the grinder include the housing, body, working chamber, hopper, product reception basket, and grinding unit. The grinding unit includes five discs powered by five electric motors which make it possible to control and monitor the grinding characteristics independently for each disc. Table 1 provides the most important structural characteristics of the grinder discs.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Disc 1</th>
<th>Disc 2</th>
<th>Disc 3</th>
<th>Disc 4</th>
<th>Disc 5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Disc diameter (D_n) (mm)</td>
<td>274</td>
<td>274</td>
<td>274</td>
<td>274</td>
<td>274</td>
</tr>
<tr>
<td>Number of holes (l_n) (psc.)</td>
<td>14</td>
<td>22</td>
<td>27</td>
<td>33</td>
<td>39</td>
</tr>
<tr>
<td>Diameter of holes (d_n) (mm)</td>
<td>30</td>
<td>23</td>
<td>21</td>
<td>17.5</td>
<td>17.5</td>
</tr>
<tr>
<td>Radius of hole arrangement in a row 1 (mm)</td>
<td>85</td>
<td>82.4</td>
<td>79.5</td>
<td>79.5</td>
<td>82</td>
</tr>
<tr>
<td>Radius of hole arrangement in a row 2 (mm)</td>
<td>101.5</td>
<td>107.4</td>
<td>95.5</td>
<td>99.5</td>
<td>102</td>
</tr>
<tr>
<td>Radius of hole arrangement in a row 3 (mm)</td>
<td>-</td>
<td>-</td>
<td>110.5</td>
<td>114.5</td>
<td>117</td>
</tr>
</tbody>
</table>

2.2.2. Comminuted Biomass

The study involved samples of corn and rice grains that were not suitable for food or animal feed uses. Corn is widely used in the energy sector, especially in biogas production. In Canada, it has also been used for direct combustion in special stoves [60,61]. Rice, as the plant with the greatest cultivation area, has great potential to be used for energy production. It is most commonly used in the form of briquettes [62]. Both comminuted grains can be a good substitute for coal, considering their relatively high heating values [61,63–65].

Before grinding, the moisture of the grains was assessed on a MAC 210/NP moisture balance (RADWAG, Radom, Poland) on the basis of the sample mass difference before and after drying, in accordance with the weighing method given in ISO norm 1446 [66,67]. The moisture of the rice grains was \(13.47\% \pm 0.02\%\), while for corn it was \(12.68\% \pm 0.02\%\), and the average dimension \(D_{80}\) of
the grains was determined on the basis of granulometric analysis carried out in accordance with ISO norm 13322-2:2006 [68], by means of a CAMSIZER device (Retsch Technology GmbH, Haan, Germany), where the results were 2.14 ± 0.02 mm and 8.15 ± 0.02 mm, respectively. Before the grinding process, grains were subjected to prior initial drying. The rice used in the study was deprived of its husk, while the corn was separated from the cobs. Before being burned, pellets were made from ground material that was divided into appropriate dimensional fractions.

2.2.3. Comminution Process Conditions

Emissivity assessment was carried out for a five-disc mill, for the comminution of two grainy materials: rice and corn. In each case, 1 kg of the material was used; both power intake and torques that occurred on particular discs were recorded. Data were recorded every 5 s. Grinding efficiency was determined according to Equation (6). The biomass granulometric content after grinding was determined by means of a CAMSIZER device (Retsch Technology GmbH, Haan, Germany), according to ISO norm 13322-2:2006 [68]. The material was delivered by means of a slide feeder with a fixed input equal to 112 kg·h⁻¹. The angular speeds of the discs were accepted as process variables in order to find out their impact on the sustainable CO₂ emissions index. Summary ΔS∆ω change in the angular speed on all the discs, starting with the minimal level, that is, from 20 rad·s⁻¹, was accepted as the variable of the analysis of the relations between the emissions index values and the angular speed.

The experiment plan included five different test programs (PB) and angular speed settings depending on the manner of the speed growth Δω (Table 2), accepted according to [49]. Angular speed settings were repeatedly changed in the range from 20 to 100 rad·s⁻¹ with a certain gradient Δω (Table 2). Next, the values of the proposed sustainable CO₂ emissions index were determined for each configuration.

<table>
<thead>
<tr>
<th>Test Program</th>
<th>Configuration No.</th>
<th>SΔω rad·s⁻¹</th>
<th>Δω rad·s⁻¹</th>
<th>ω₁ rad·s⁻¹</th>
<th>ω₂ rad·s⁻¹</th>
<th>ω₃ rad·s⁻¹</th>
<th>ω₄ rad·s⁻¹</th>
<th>ω₅ rad·s⁻¹</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>1</td>
<td>50</td>
<td>5</td>
<td>20</td>
<td>25</td>
<td>35</td>
<td>40</td>
<td></td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>100</td>
<td>10</td>
<td>20</td>
<td>30</td>
<td>40</td>
<td>50</td>
<td>60</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>150</td>
<td>15</td>
<td>20</td>
<td>35</td>
<td>50</td>
<td>65</td>
<td>80</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>200</td>
<td>20</td>
<td>20</td>
<td>40</td>
<td>60</td>
<td>80</td>
<td>100</td>
</tr>
<tr>
<td>II</td>
<td>1</td>
<td>200</td>
<td>20</td>
<td>100</td>
<td>80</td>
<td>60</td>
<td>40</td>
<td>20</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>150</td>
<td>15</td>
<td>80</td>
<td>65</td>
<td>50</td>
<td>35</td>
<td>20</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>100</td>
<td>10</td>
<td>60</td>
<td>50</td>
<td>40</td>
<td>30</td>
<td>20</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>50</td>
<td>5</td>
<td>40</td>
<td>35</td>
<td>30</td>
<td>25</td>
<td>20</td>
</tr>
<tr>
<td>III</td>
<td>1</td>
<td>40</td>
<td>20</td>
<td>20</td>
<td>40</td>
<td>20</td>
<td>40</td>
<td>20</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>85</td>
<td>20</td>
<td>45</td>
<td>25</td>
<td>45</td>
<td>25</td>
<td>45</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>225</td>
<td>25</td>
<td>75</td>
<td>50</td>
<td>75</td>
<td>50</td>
<td>75</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>360</td>
<td>20</td>
<td>100</td>
<td>80</td>
<td>100</td>
<td>80</td>
<td>100</td>
</tr>
<tr>
<td>IV</td>
<td>1</td>
<td>40</td>
<td>20</td>
<td>20</td>
<td>40</td>
<td>20</td>
<td>40</td>
<td>20</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>80</td>
<td>40</td>
<td>20</td>
<td>60</td>
<td>20</td>
<td>60</td>
<td>20</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>120</td>
<td>60</td>
<td>20</td>
<td>80</td>
<td>20</td>
<td>80</td>
<td>20</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>160</td>
<td>80</td>
<td>20</td>
<td>100</td>
<td>20</td>
<td>100</td>
<td>20</td>
</tr>
<tr>
<td>V</td>
<td>1</td>
<td>240</td>
<td>80</td>
<td>100</td>
<td>20</td>
<td>100</td>
<td>20</td>
<td>100</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>280</td>
<td>60</td>
<td>100</td>
<td>40</td>
<td>100</td>
<td>40</td>
<td>100</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>320</td>
<td>40</td>
<td>100</td>
<td>60</td>
<td>100</td>
<td>60</td>
<td>100</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>360</td>
<td>20</td>
<td>100</td>
<td>80</td>
<td>100</td>
<td>80</td>
<td>100</td>
</tr>
</tbody>
</table>

2.2.4. Determination of Calorific and Emissions Values for Given Biomass Fractions after Comminution

Rice and corn grains were comminuted and divided into dimensional fractions with the use of steel sieves (Table 3). The division was made by means of a sieve shaker Analysette 3 PRO (Fritsch GmbH,
Idar-Oberstein, Germany) in accordance with DIN norm 66165 [69]. After the division into fractions, a pellet maker was used to prepare pellets. Next, 1.5 kg samples were combusted in a pellet Greńsk furnace of the EG-Pellet type (GREN sp. z o.o., Pszczyna, Poland). CO₂ emissions measurements were performed by means of a dedicated exhaust fumes analyzer ULTRAMAT 23 (Siemens AG, Nürnberg, Germany) for approximately 10 min for each sample. The analyzer measures the content of carbon dioxide (CO₂), carbon monoxide (CO), nitrogen oxide (NO), sulfur dioxide (SO₂), and dioxide (O₂) in the exhaust emissions.

### Table 3. Dimensions of rice and corn fractions used for pellets.

<table>
<thead>
<tr>
<th>Fraction Dimension (µm)</th>
<th>Rice</th>
<th>Corn</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0–630</td>
<td>630–1250</td>
</tr>
</tbody>
</table>

Calorific values of the pellets prepared from the ground biomass with dimensions presented in Table 3 were determined in earlier tests whose results can be found in the authors’ other publications [55].

2.2.5. Analytical Methods

Tools for statistical analysis available in MS Excel (Microsoft, Redmond, Washington, USA) and Statistica (TIBCO Software Inc., Palo Alto, CA, USA) were used to analyze the results. Basic descriptive statistics of sustainable emissivity were determined. Relations between angular speeds of the grinder discs and emissivity were examined using correlation analysis with Spearman’s method and the analysis of regression and the adequacy of the proposed models. The significance level was accepted as $p < 0.05$.

3. Results and Discussion

3.1. Input Variables of the Sustainable CO₂ Emissions Model

The following assumptions and limitations were adopted for this study:

- CO₂ emissions involved in the production of electric energy from coal is 0.812 kgCO₂·kWh⁻¹ [70].
- In the emissions analysis of this paper, only emissions from the grinding and energy-use processes were considered. Emissions relating to the pelletization process were excluded. The analysis was limited to energy use in the form of pellet combustion. No other methods were considered, such as gasification, fermentation, or digestion.

3.1.1. Power Consumption

The power input on each disc of the five-disc grinder was recorded during the experiment. Figure 3 shows the grinder’s total power input for each configuration of the five testing programs (Table 2).

An increase in the angular speed of the multi-disc grinder was caused by power consumption growth (Figure 3). It can also be noted that the highest power input was found for high-speed disc settings (setting no. 4 from PB III and setting no. 4 from PB V) and lowest for low angular speeds (setting no. 1 from PB III and setting no. 1 from PB IV). The power input for all the settings was higher for corn grinding. The power requirement during corn grinding is higher than that during rice grinding, and this results from the strength properties of both types of grains, which largely depend on their physical properties, e.g., humidity and internal structure [71]. The forces used to destroy the corn grain should be higher than those used to permanently deform the rice grain, which translates into a higher resistance to the movement of the working elements of the crusher (cutting discs) and results in an increased power requirement in the case of corn grinding [47]. The above statements result from
the different internal structures of the grains examined—differences in the structure of the endosperm and tegument (the ground rice was deprived of its husk) [72–74].

![Figure 3. Total power input of a five-disc grinder for the analyzed angular speed settings of working discs.](image)

3.1.2. Grinding Efficiency

Figure 4 shows the results of monitoring the grinding process efficiency for each configuration of the disc angular speed setting according to five research programs (Table 2). Grinding efficiency increased along with an increase in the disc angular speeds (Figure 4). It can also be seen that the highest efficiency was found for the disc high angular speed settings (setting no. 4 from PB III and setting no. 4 from PB V).

![Figure 4. Grinding efficiency for the analyzed settings of the disc angular speeds.](image)

3.1.3. Granulometric Content of Biomaterial after Grinding

Knowledge of the percentage share of the accepted dimensional fractions of biomass is needed to determine the values of the sustainable CO₂ emissions index. For this purpose, a granulometric
analysis of the ground material was performed with the use of a CAMSIZER device (Retsch Technology GmbH, Haan, Germany). Table 4 shows the results of this analysis for particular settings of the disc angular speed for rice and corn. The results show that the fraction percentage share was different for each disc angular speed setting configuration.

Table 4. Granulometric content of biomaterial after grinding for the analyzed disc angular speed settings.

<table>
<thead>
<tr>
<th>Config</th>
<th>Rice</th>
<th>Corn</th>
</tr>
</thead>
<tbody>
<tr>
<td>I 1</td>
<td>9.4</td>
<td>29.3</td>
</tr>
<tr>
<td>I 2</td>
<td>3.4</td>
<td>13.8</td>
</tr>
<tr>
<td>I 3</td>
<td>6.9</td>
<td>21.0</td>
</tr>
<tr>
<td>I 4</td>
<td>5.8</td>
<td>18.4</td>
</tr>
<tr>
<td>II 1</td>
<td>5.8</td>
<td>18.4</td>
</tr>
<tr>
<td>II 2</td>
<td>2.9</td>
<td>12.7</td>
</tr>
<tr>
<td>II 3</td>
<td>2.3</td>
<td>10.1</td>
</tr>
<tr>
<td>II 4</td>
<td>0.9</td>
<td>6.4</td>
</tr>
<tr>
<td>III 1</td>
<td>1.7</td>
<td>9.0</td>
</tr>
<tr>
<td>III 2</td>
<td>2.8</td>
<td>11.7</td>
</tr>
<tr>
<td>III 3</td>
<td>8.9</td>
<td>22.5</td>
</tr>
<tr>
<td>III 4</td>
<td>13.3</td>
<td>35.0</td>
</tr>
<tr>
<td>IV 1</td>
<td>1.7</td>
<td>9.0</td>
</tr>
<tr>
<td>IV 2</td>
<td>2.4</td>
<td>13.7</td>
</tr>
<tr>
<td>IV 3</td>
<td>6.3</td>
<td>23.4</td>
</tr>
<tr>
<td>IV 4</td>
<td>8.4</td>
<td>28.1</td>
</tr>
<tr>
<td>V 1</td>
<td>7.0</td>
<td>27.3</td>
</tr>
<tr>
<td>V 2</td>
<td>9.4</td>
<td>27.2</td>
</tr>
<tr>
<td>V 3</td>
<td>12.4</td>
<td>30.8</td>
</tr>
<tr>
<td>V 4</td>
<td>13.3</td>
<td>35.0</td>
</tr>
</tbody>
</table>

3.1.4. Unit Emissions Index $J_{ACO_2}$ for the $i$-th Dimensional Fraction

A unit CO$_2$ emissions index for a given biomass fraction was determined on the basis of the analysis of the CO$_2$ content in exhaust emissions. The values of the unit $J_{ACO_2}$ index are presented in Table 5. It can be noticed that CO$_2$ emissions increased along with an increase in the size of the particles of the biomass, which was used for the preparation of pellets.

Table 5. Unit index $J_{ACO_2}$ of CO$_2$ emissions of the $i$-th fraction.

<table>
<thead>
<tr>
<th>Rice</th>
<th>Corn</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fraction Dimension (µm)</td>
<td>Unit Emissions Index (kg·kWh$^{-1}$)</td>
</tr>
<tr>
<td>0–630</td>
<td>0.0453</td>
</tr>
<tr>
<td>630–1250</td>
<td>0.0356</td>
</tr>
<tr>
<td>1250–2000</td>
<td>0.0745</td>
</tr>
<tr>
<td>&gt;2000</td>
<td>0.11428</td>
</tr>
</tbody>
</table>

3.1.5. Calorific Values

Calorific values for given dimensional fractions of biomass were accepted according to [55]. Table 6 shows the calorific values calculated into kWh·kg$^{-1}$.
Table 6. Calorific values of selected fractions of rice and corn calculated based on [55].

<table>
<thead>
<tr>
<th>Fraction Dimension (µm)</th>
<th>Calorific Value (kWh·kg⁻¹)</th>
<th>Fraction Dimension (µm)</th>
<th>Calorific Value (kWh·kg⁻¹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0–630</td>
<td>3.97</td>
<td>0–500</td>
<td>3.91</td>
</tr>
<tr>
<td>630–1250</td>
<td>3.93</td>
<td>60–1250</td>
<td>4.05</td>
</tr>
<tr>
<td>1250–2000</td>
<td>3.89</td>
<td>1250–2000</td>
<td>4.02</td>
</tr>
<tr>
<td>&gt;2000</td>
<td>3.85</td>
<td>&gt;2000</td>
<td>3.96</td>
</tr>
</tbody>
</table>

3.2. Carbon Dioxide Emissions Assessment of Grinding by Means of the Sustainable CO₂ Emissions Index

The grinding processes carried out in particular research programs were subjected to emissions assessment. For this purpose, the values of the sustainable CO₂ emissions index were determined for each case on the basis of both Equation (9) and the values of the variables obtained (Figures 3 and 4, and Tables 2–6). Figure 5 shows the results of the sustainable CO₂ emissions index calculation for the tested multi-disc grinder disc angular speed configurations and the two ground materials—rice and corn.

![Figure 5. Results of the sustainable CO₂ emissions index for each disc speed configuration.](image)

When analyzing the variability of the sustainable CO₂ emissions index, it should be noted that the desired condition is to reduce the energy consumption for grinding $E_{\text{dM}}$ and increase the environmental benefits $\Delta B_{\text{CO}_2}$, i.e., replacing CO₂ emissions from coal with CO₂ emissions from biomass combustion. In this case, the value of the proposed index should increase. When comparing the grinding processes, the more favorable in terms of emissions will be the one for which the sustainable CO₂ emissions index assumes higher values [54].

Based on the results, it was found that the best, in terms of emissivity, both for rice and corn grinding, were settings VI1 of the angular speed of the grinder discs (Figure 5). The least advantageous for rice grinding were settings V4, and for corn, settings IV4 (Figure 5). It was noticed that better emissivity results were obtained for the configuration in which the disc angular speed was low (for example, I1, II4, III1, IV1). The values of the sustainable emissions index were higher for rice grinding than for corn grinding in all the disc angular speed configurations, which was caused primarily by lower energy consumption during rice grinding and higher grinding efficiency. The values of the emissions index provided sufficient grounds to state that the emissions from electric energy used in the rice comminution process were sustainable or in fact higher than the emissions from coal.
from combustion of the comminuted biomass for all the analyzed disc angular speed settings because $W_{ZCO2} > W_{ZCO2(em)} = 0$ (Figures 5 and 6). In the case of corn grinding, two configurations (IV4 and V1) did not provide emissions sustainability ($W_{ZCO2} > W_{ZCO2(em)} = 0$).

![Figure 6](image_url)

**Figure 6.** Sustainable CO2 emissions index for rice grinding on a multi-disc grinder in a function of power input.

The minimal value of the sustainable emissions index CO2 $W_{ZCO2(min)}$, determined on the basis of Equation (10), was $-0.812$ kgCO2eq-kWh$^{-1}$ with the assumption that the electric energy used in the process of grinding was produced from coal (Figures 6 and 7). In the case of electric energy produced from natural gas, this would be $-0.201$ kgCO2eq-kWh$^{-1}$, from biogas: $-0.196$ kgCO2eq-kWh$^{-1}$, from diesel oil: $-0.276$ kgCO2eq-kWh$^{-1}$ [75].

![Figure 7](image_url)

**Figure 7.** Sustainable CO2 emissions index for corn grinding on a multi-disc grinder in a function of power consumption.
The dependences shown in Figures 6 and 7 indicate that there is no obvious correlation between power consumption and the sustainable CO\(_2\) emissions index when grinding corn, mainly due to the physico-mechanical properties of the corn grains that affect the grinding process. The influence of the working unit on the materials being ground and the mass flow phenomena in the grinding chamber are also crucial. The results obtained clearly show that the grinding process is different for both materials, which is influenced by differences in the physical and mechanical properties of both grains. In the case of corn, among other things, a greater unevenness of the grinding process (transient idling phases) was observed as a result of the material deposited in the grinding chamber as a consequence of the phenomenon of particle agglomeration, which was not observed in the case of rice. The balanced CO\(_2\) emission rate depends, apart from power consumption, on yield and the share of fractions of different particle sizes. The lack of an obvious relationship between power consumption and a balanced CO\(_2\) emission factor in maize grinding is due to the less clear relationship between power consumption (angular speeds of the grinding discs) and the yield and grain size composition of the grinding product than for rice. This, in turn, is also dictated by the difference in grain properties such as size. The ratio between grain size and disc gap is of particular importance for the yield and granulometric composition of the product. Rice grains are smaller so that they are crushed and drained through the inter-disc slots more quickly than larger maize grains, which must collide with the cutting edges of the shredder more times than rice grains before they leave the shredding chamber. The above-mentioned aspects make less regularity in the shredding of maize, resulting in a moderate relationship between power consumption and sustainable CO\(_2\) emissions.

The minimal value of the emissions index for energy sustainability \(W_{\text{CO}_2}^{(\text{emin})}\) for rice grinding was \(-0.699\) kgCO\(_2\)eq·kWh\(^{-1}\) (Figure 6), whereas for corn grinding, it was \(-0.690\) kgCO\(_2\)eq·kWh\(^{-1}\) (Figure 7). The value of the emissions index for energy sustainability \(W_{\text{CO}_2}^{(e)}\) for the analyzed configurations of the disc angular speed settings are marked with a grey line (Figures 6 and 7). The data show that the level of energy sustainability was exceeded for all the tested disc angular speed settings (Figures 6 and 7), that is, the energy produced from biomass combustion was higher than the energy used in the process of grinding (obtainment of the comminuted product).

### 3.3. Analysis of the Relations between the Values of the Sustainable CO\(_2\) Emissions Index and the Angular Speed of the Working Elements of the Cutting Edges

To determine the relations between the values of the sustainable CO\(_2\) emissions index and the variable speeds of the working discs, a statistical analysis of the variables was carried out. Table 7 presents the most important statistics that describe the variables and the results of the sustainable CO\(_2\) emissions index. Based on the skewness and kurtosis values, it was found that the distribution of the values of variables and the results of the sustainable CO\(_2\) emissions index differs from the normal distribution. Therefore, Spearman’s coefficient was used in the correlation analysis to describe monotonic relations between the variables.

<table>
<thead>
<tr>
<th>(W_{\text{CO}_2})</th>
<th>(R_p)</th>
<th>M</th>
<th>S</th>
<th>K</th>
<th>V</th>
<th>(\bar{x})</th>
<th>s</th>
<th>Min.</th>
<th>Max.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Corn</td>
<td>5.96</td>
<td>1.83</td>
<td>0.54</td>
<td>-0.53</td>
<td>76.31</td>
<td>2.42</td>
<td>1.84</td>
<td>-0.24</td>
<td>5.72</td>
</tr>
<tr>
<td>Rice</td>
<td>8.51</td>
<td>4.14</td>
<td>0.8</td>
<td>-0.08</td>
<td>50.73</td>
<td>4.82</td>
<td>2.45</td>
<td>1.93</td>
<td>10.44</td>
</tr>
</tbody>
</table>

\(S_{\Delta \omega}\) | 320 | 260 | 0.6 | -0.72 | 63.11 | 165.5 | 104.44 | 40 | 360 |
| \(\omega_1\) | 80 | 20 | 0.32 | -1.82 | 66.54 | 54.00 | 35.93 | 20 | 100 |
| \(\omega_2\) | 80 | 40 | 0.54 | -0.72 | 44.03 | 51.75 | 22.78 | 20 | 100 |
| \(\omega_3\) | 80 | 25 | 0.51 | -1.26 | 57.83 | 54.00 | 31.23 | 20 | 100 |
| \(\omega_4\) | 80 | 40 | 0.54 | -0.72 | 44.03 | 51.75 | 22.78 | 20 | 100 |
| \(\omega_5\) | 80 | 20 | 0.32 | -1.82 | 66.54 | 54.00 | 35.93 | 20 | 100 |

\(\bar{x}\)—mean value, \(s\)—standard deviation, M—median, Max—maximal value, Min—minima value, \(R_p\)—range, \(V\)—variability coefficient, S—skewness, K—kurtosis.
Correlation analysis using Spearman’s method revealed that the values of the sustainable CO\textsubscript{2} emissions index are negatively correlated with speed increase $S\Delta\omega$ (Table 8). For rice grinding, negative correlations between the sustainable CO\textsubscript{2} emissions index and the first, third, and fifth disc angular speeds were found as well as the summary increase in angular speeds $S\Delta\omega$. The results show that along with an increase in the multi-disc grinder angular speeds the values of the sustainable CO\textsubscript{2} emissions index decrease. This results, among others, from the dependence of power consumption and efficiency on angular speeds (of the rotating elements) as demonstrated in [25,47,76,77], which show that power consumption and efficiency increase along with an increase in grinder disc angular speeds, which, in the case of the sustainable CO\textsubscript{2} emissions index, means a decrease in its value.

**Table 8.** Analysis of sustainable CO\textsubscript{2} emissions index correlation with independent variables.

<table>
<thead>
<tr>
<th></th>
<th>$\omega_1$</th>
<th>$\omega_2$</th>
<th>$\omega_3$</th>
<th>$\omega_4$</th>
<th>$\omega_5$</th>
<th>$S\Delta\omega$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Corn</td>
<td>Rho Spearman's</td>
<td>-0.107</td>
<td>-0.258</td>
<td>-0.307</td>
<td>-0.557</td>
<td>-0.480</td>
</tr>
<tr>
<td></td>
<td>p-value</td>
<td>0.653</td>
<td>0.272</td>
<td>0.188</td>
<td>0.011</td>
<td>0.032</td>
</tr>
<tr>
<td>Rice</td>
<td>Rho Spearman's</td>
<td>-0.609*</td>
<td>-0.232</td>
<td>-0.855*</td>
<td>-0.434</td>
<td>-0.853*</td>
</tr>
<tr>
<td></td>
<td>p-value</td>
<td>0.004</td>
<td>0.325</td>
<td>0.000</td>
<td>0.056</td>
<td>0.000</td>
</tr>
</tbody>
</table>

* Significant correlations: Rho Spearman’s >0.6, p-value <0.05; $\omega_1$, $\omega_2$, $\omega_3$, $\omega_4$, $\omega_5$—disc angular speeds, rad s\textsuperscript{-1}; $S\Delta\omega$—summary increase in angular speeds, rad s\textsuperscript{-1}.

Multiple regression analysis was carried out for the analyzed variables of the rice grinding process using the backward stepwise method. A simple linear regression analysis was carried out for corn due to its correlation with $S\Delta\omega$ only. Table 9 shows the results of the regression analysis. The only model with significant coefficients for rice was a linear model of variable $S\Delta\omega$, which demonstrated a 74.6% variability of the sustainable emissions index. With regard to corn grinding, the linear model of variable $S\Delta\omega$ explained merely 32.7% of the sustainable emissions index.

**Table 9.** Results of regression analysis for the sustainable CO\textsubscript{2} emissions index.

<table>
<thead>
<tr>
<th></th>
<th>Coefficients</th>
<th>t-stat.</th>
<th>p-Value *</th>
<th>F</th>
<th>Significance</th>
<th>R\textsuperscript{2}</th>
</tr>
</thead>
<tbody>
<tr>
<td>Corn</td>
<td>Constant</td>
<td>4.09</td>
<td>6.16</td>
<td>$8.08 \times 10^{-6}$</td>
<td>8.75</td>
<td>0.008</td>
</tr>
<tr>
<td></td>
<td>$S\Delta\omega$</td>
<td>-0.01</td>
<td>-2.96</td>
<td>0.008</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Rice</td>
<td>Constant</td>
<td>8.17</td>
<td>15.13</td>
<td>$1.11 \times 10^{-11}$</td>
<td>53.00</td>
<td>9.13 $\times 10^{-7}$</td>
</tr>
<tr>
<td></td>
<td>$S\Delta\omega$</td>
<td>-0.02</td>
<td>-7.28</td>
<td>9.13 $\times 10^{-7}$</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

$S\Delta\omega$—summary angular speed increase, * results $p > 0.5$ were accepted as significant.

Bearing in mind that linear models account for less than 80% of the variability of the sustainable emissions, the adequacy of nonlinear models was checked. The non-linear model which best described the changes in the sustainable emissions index of rice grinding on a five-disc grinder depending on the total increase in angular velocity on the discs $S\Delta\omega$ was an exponential model and its coefficient of determination was $R^2 = 0.889$ (Figure 8). For corn grinding, the best model was a logarithmic one (Figure 9). The dependencies provided indicate that the sustainable emissions index of grinding decreases along with an increase in the grinder disc angular speed.

The dependencies presented in Figures 8 and 9 can be used to determine the CO\textsubscript{2} emissions level predicted for the analyzed five-disc grinder, for the other materials and for emissivity control of the grinding process—establishing optimal values for the settings of the grinding process parameters (angular velocities), providing a reduction in CO\textsubscript{2} emissions from alternative fuels while decreasing energy use.
wood biomass. It can be used to compare the emissions parameters during the processing of materials different grinding process than in the case of rice, as described in Section 3.2. The index presented in this paper can be designated for other types of materials besides grain and wood biomass. It can be used to compare the emissions parameters during the processing of materials for energy purposes and to indicate the parameters of the grinding process that will ensure the highest possible increase in environmental benefits in the form of a change in CO₂ emissions per unit of grinding machine power. If other materials, e.g., lignocellulose biomass, are ground, it can be expected...
that the results would be different from those presented in this paper, which is of course related both to the different specificity of the grinding process itself and to the fact that the physico-mechanical properties of the cellulose materials differ significantly from those of grains used in this study.

4. Conclusions

The aim of the work—to develop a mathematical model of the sustainable CO\textsubscript{2} emissions index for the carbon dioxide emissions assessment of the biomass grinding process—was achieved. The methodology for evaluating the emissivity of grinding made it possible to provide a measurable assessment of the process with a focus on energy consumption and emissivity. An analysis of the sustainable CO\textsubscript{2} emissions index allows the authors to state that

- the sustainable CO\textsubscript{2} emissions index of rice and corn grinding on a five-disc mill, depending on the disc angular speed increase $S\Delta \omega$, can be described with high accuracy using a nonlinear model (Figures 8 and 9);
- it was observed that the sustainable CO\textsubscript{2} emissions index decreases with an increase in the value of $S\Delta \omega$;
- from the point of view of emissivity, it is better to grind at lower disc angular speeds;
- higher values of the emissions index were obtained for rice, and from the point of view of emissivity, rice is better than corn in energy applications.

The values of the sustainable CO\textsubscript{2} emissions index will vary depending on the source of energy fueling the grinding processes. The minimal value of the sustainable emissions index $W_{ZCO_{2}(\text{min})}$ was $-0.812$ kgCO\textsubscript{2}eq·kWh\textsuperscript{−1} with the assumption that the electric energy used in the process of grinding was produced from coal (Figures 6 and 7). In the case of electric energy produced from natural gas, it would be $-0.201$ kgCO\textsubscript{2}eq·kWh\textsuperscript{−1}, from biogas: $-0.196$ kgCO\textsubscript{2}eq·kWh\textsuperscript{−1}, from diesel oil: $-0.276$ kgCO\textsubscript{2}eq·kWh\textsuperscript{−1}. The best emissions balance would occur if the electricity fueling the grinding process came from a biogas plant. Different index values would also occur if biomass energy use from non-combustion methods were considered.

The index presented in this paper can be designated for other types of materials besides grain and wood biomass. It can be used to compare the emissions parameters during the processing of materials for energy purposes and to indicate the parameters of the grinding process, which would ensure the highest possible increase in environmental benefits in the form of a change in CO\textsubscript{2} emissions per unit of grinding machine power.

The model proposed in this study is dedicated strictly for industrial applications for real-time assessment of CO\textsubscript{2} emissions. The model implemented in the monitoring end control system of biomass pretreatment processes can, in a short time (using the input of real-time data from industrial sensors, counters, and meters), calculate the balance of emissions. This offers the possibility of indicating the best process parameters, for example, disc speed, which makes it possible to reduce the emissions of carbon dioxide from fossil fuels. In general, the proposed model can be part of an industrial control system because it is easy to calculate its values, depending on real-time data from sensors.

Supplementary Materials: The following are available online at http://www.mdpi.com/1996-1073/13/2/330/s1, Table S1: Eco efficiency indexes of technology presented in the literature, Table S2: Environmental assessment indexes for grinding according to the literature.

Author Contributions: The work was prepared entirely by the author Weronika Kruszelnicka. All authors have read and agreed to the published version of the manuscript.

Funding: Scientific work was financed by the budget resource for science in 2017–2021 as a research project under the “Diamentowy Grant” program.

Conflicts of Interest: The author declare no conflict of interest. The funders had no role in the design of the study; in the collection, analyses, or interpretation of the data, in the writing of the manuscript, or in the decision to publish the results.
References


61. Lizotte, P.-L.; Savoie, P.; De Champlain, A. Ash Content and Calorific Energy of Corn Stover Components in Eastern Canada. Energies 2015, 8, 4827–4838. [CrossRef]


73. Grefeuille, V.; Mabille, F.; Rousset, M.; Oury, F.-X.; Abecassis, J.; Lullien-Pellerin, V. Mechanical properties of outer layers from near-isogenic lines of common wheat differing in hardness. *J. Cereal Sci.* 2007, 45, 227–235. [CrossRef]


© 2020 by the author. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (http://creativecommons.org/licenses/by/4.0/).