Integration of Electric Vehicles in the Distribution Network: A Review of PV Based Electric Vehicle Modelling

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Abstract: Electric vehicles (EVs) are one of a prominent solution for the sustainability issues needing dire attention like global warming, depleting fossil fuel reserves, and greenhouse gas (GHG) emissions. Conversely, EVs are shown to emit higher emissions (measured from source to tailpipe) for the fossil fuel-based countries, which necessitates renewable energy sources (RES) for maximizing EV benefits. EVs can also act as a storage system, to mitigate the challenges associated with RES and to provide the grid with ancillary services, such as voltage regulation, frequency regulation, spinning reserve, etc. For extracting maximum benefits from EVs and minimizing the associated impact on the distribution network, modelling optimal integration of EVs in the network is required. This paper focuses on reviewing the state-of-the-art literature on the modelling of grid-connected EV-PV (photovoltaics) system. Further, the paper evaluates the uncertainty modelling methods associated with various parameters related to the grid-connected EV-PV system. Finally, the review is concluded with a summary of potential research directions in this area. The paper presents an evaluation of different modelling components of grid-connected EV-PV system to facilitate readers in modelling such system for researching EV-PV integration in the distribution network.

Keywords: plug-in electric vehicle; energy management system; renewable energy; vehicle-to-grid

1. Introduction

The issues like global warming, depleting fossil fuel reserves, and greenhouse gas (GHG) emissions need dire attention for ensuring a sustainable future. Because the transportation sector is one of the largest contributors to the rising harmful emissions, the electrification of transportation is seen as a promising solution for this problem. Electric vehicle (EV) technology has existed for more than a century peaking commercially around 1900. However, due to the easy availability of fossil fuels, advancements in internal combustion (IC) technology, and simplicity in the use of IC engines, EVs were put on hold and limited to golf carts and delivery vehicles. Figure 1 shows the progression timeline of the EVs. The dependency on petroleum imports for transportation purposes is also reduced by electrification of transportation, thereby increasing energy security. However, the adoption rate of EVs remains slow owing to factors, such as high initial cost, battery degradation, inadequate charging infrastructure, range anxiety, etc. [1]. Various policies and incentives are made available by governments around the world to promote the uptake of EV and to prevent these barriers from realizing a complete shift to electrified transportation. As per the report “Global EV outlook” of the International Energy Agency, the total number of EVs are projected to reach 130 million by 2030 [2].
However, high penetration of EVs also poses distribution network quality issues, particularly network congestion, three-phase voltage imbalance and off-nominal frequency problems. The EVs are a mobile single-phase load so they can be randomly plugged in at any one of three phases within distribution networks, leading to a scenario that electrical components in one particular phase, such as power supply cable, overhead line or transformer may be heavily loaded while the rest of two phases are not. The unbalanced three-phase loading may lead to a series of negative impact on power quality issue: Transformer failures, equipment loss-of-life, relay misfunction, etc. Moreover, as EVs are highly spatial and temporally uncertain, handling EVs as additional loads while maintaining the reliability and security of the grid is difficult. The coincidence of timing between EV home charging and residential load peaks leads to additional system peaks. Moreover, multiple EV chargers in a neighbourhood can introduce significant harmonics, thereby reducing power quality [3]. Therefore, the integration of substantial EV penetration in the distribution networks is a significant area of interest in the research and engineering community, especially optimally controlling EV charging to minimise the impact of the above-described issues.

Another significant contributor to harmful emissions is the power industry, particularly fossil fuel-based power generation. Renewable energy sources (RES), such as wind and solar are increasingly adopted to mitigate the power industry emissions. The variable nature of RES which depends on the weather, time, location, etc. creates voltage stability and reliability issues for the power grid requiring integration of Energy Storage System (ESS). Also, there may not be sufficient demand requirement during the period of high RES generation, which leads to the under-utilisation of average generated capacity. Using ESS with RES can result in its effective utilisation as ESS can store energy when demand is low and supply back when demand is high. Apart from using ESS, application of demand-side management techniques like load shifting, time of use pricing, and demand bidding can also solve the aforementioned problems associated with RES although the impact of these techniques is limited compared to ESS [4,5].

Large-scale integration of RES requires an increased size (or capacity) of ESS. Hence, it leads to a significant capital requirement, especially due to the high per-unit cost of ESS. As we are already moving towards electric vehicles to combat GHG emissions and these EVs essentially run on the batteries, the EVs can also act as a dynamic natured ESS, due to the vehicle-to-grid (V2G) feature, in which EVs deliver energy stored in their batteries back to the grid [6]. Additionally, EVs spend a considerable amount of time (22 h) in parked conditions [7], so they can be suitably used as ESS without creating inconvenience (e.g., range anxiety issues) for users. However, battery degradation is still an issue which can be offset by giving incentives to users/aggregators to participate in V2G. As the battery capacity of each EV is minuscule compared to grid load requirements, an aggregation of EVs is generally required to provide the grid with the backup power. Apart from storing surplus energy generated by RES, EVs can also provide the grid with additional ancillary services, such as voltage regulation, frequency regulation, spinning reserve, etc. EVs can also participate in energy trading.
An overview of EV modelling techniques is presented in References [16–18] with an emphasis on particularly PV, focusing on the modelling of control methods or EV loads. Also, a detailed review of power generation is based on fossil fuels [9]. However, using RES to charge the EVs could result in participation in V2G. However, most of the energy markets around the world require a minimum capacity to participate, which would require an aggregator of a large number of EVs. To counteract this, more research is being done on transactive or peer-to-peer (P2P) trading mechanisms [8].

Moreover, the emission benefits of electrified transportation cannot be maximised if the source of EV charging is based on non-renewable sources. In fact, EVs are shown to emit higher emissions, measured from well to wheel, i.e., source to the tailpipe for the countries whose primary source of power generation is based on fossil fuels [9]. However, using RES to charge the EVs could result in reducing GHG emissions, as shown in Reference [10], where 50,000 EVs charged from a mix of wind and PV energy sources resulted in 400 Mtons less emissions per year.

Based on these factors, this paper presents a general framework for designing a grid-connected EV-PV system. Several papers have also reviewed the different aspects of the interaction of EV-PV system and distribution network in the literature. References [11–14] discuss charging EVs using PV generation with a focus on control architectures and algorithms, and economic framework. The impact of the charging infrastructure of EV on the grid in terms of power quality is reviewed in Reference [15]. An overview of EV modelling techniques is presented in References [16–18] with an emphasis on modelling methods for EV loads and charging stations.

These review papers study the limited aspects of the interaction of grid-connected EV with RES, particularly PV, focusing on the modelling of control methods or EV loads. Also, a detailed review of modelling the uncertainties present in the grid-connected EV-PV system is not present in the literature to the knowledge of the authors. Therefore, this paper presents a comprehensive review of all aspects of modelling a grid-connected EV-PV system viz., control architectures, charging algorithms, and uncertainty analysis. This paper aims to provide an evaluation of these aspects to enable the researchers to model a grid-connected EV-PV system for carrying out impact or implementation studies of EV integration into the distribution system. The grid is represented by a distribution network as EV and PV both are on the distribution side. Throughout the paper, EV-PV system is considered as a single entity (limited to the times when connected to the grid for charging or vehicle-to-grid), and the PV is considered as a complementary energy source to charge EVs other than the grid. Figure 2 shows the analytical framework of the modelling aspects of grid-connected EV-PV system.

Figure 2. An analytical framework for grid-connected EV-PV (photovoltaics) interaction.
The organisation of the paper is as follows: Section 2 provides an overview of the modes of EV integration with the grid. Section 3 discusses the control architectures of connecting EVs to the grid. Section 4 describes the state-of-the-art literature of smart charging algorithms of grid-connected EV-PV system. Section 5 reviews the uncertainty analysis methods for EV demand, PV generation, and load distribution. The suggestions for future research with concluding remarks are presented in Section 6.

2. EV Interaction with the Distribution Network

Figure 3 shows a general representation of an EV connected to the electrical grid. The technology which allows the bidirectional flow of energy between EV and grid is known as vehicle-to-grid (V2G). It is achieved by the integration of Information and Communication Technologies (ICT) with the EV charging system. The modelling research of EV interaction with the distribution network has transitioned from unidirectional mode in the initial stage to bidirectional mode in the current stage [6,7].

With the increasing level of EV penetration, the associated technical issues, e.g., system imbalance, decreased stability, and power quality, as well as increased system cost, are becoming more prominent, due to additional energy and power demand. The unidirectional approach, i.e., G2V mode, has been extensively studied in the literature in the form of topics like smart charging [19], safety [20], and control features [21]. The focus of these studies is on minimizing the charging cost [22] or minimizing the impact on the distribution system [23,24].

However, in the bidirectional mode, EV is not only the load for the grid, but also a distributed generation and storage. The initial idea was to use EV battery to store energy and send it back to the grid in peak period, known as peak load shaving [6]. Reference [25] presents a review of peak shaving strategies using demand-side management, energy storage systems, and electric vehicles. Table 1 illustrates the characteristic differences between the unidirectional and bidirectional modes. As an individual EV has a small battery capacity, a major challenge is the synchronisation of a large number of EVs charging/discharging operation required for them to be an effective storage system. Also, the limited uptake of EV did not quite make this idea of using EV in the bidirectional mode mainstream. Research later indicated that the application of bidirectional V2G in the ancillary market: Spinning reserve and voltage control is much more important than peak load reduction. Spinning reserve is the extra generation that can be made readily available, and it is paid for the availability along with
the time it is called for deployment (compared to peak load shaving), which makes deployment of EV in ancillary service provision very economically favourable. Moreover, in terms of frequency of deployment, the voltage regulation is needed more than 300 times per day compared to the need for peak load shaving, which is only a few hundred hours per year [26].

<table>
<thead>
<tr>
<th>Features</th>
<th>Unidirectional</th>
<th>Bidirectional</th>
</tr>
</thead>
<tbody>
<tr>
<td>Power flow</td>
<td>Grid-to-vehicle (G2V)</td>
<td>G2V and vehicle-to-grid (V2G)</td>
</tr>
<tr>
<td>Infrastructure</td>
<td>Communication</td>
<td>Communication, bidirectional charger</td>
</tr>
<tr>
<td>Cost</td>
<td>Low</td>
<td>High</td>
</tr>
<tr>
<td>Complexity</td>
<td>Low</td>
<td>High</td>
</tr>
<tr>
<td>Services</td>
<td>Load profile management, Frequency regulation [27]</td>
<td>Backup power support, frequency regulation, voltage regulation, active power support [28]</td>
</tr>
<tr>
<td></td>
<td>Overloading prevention, load levelling, profit maximisation, emission minimisation [29]</td>
<td>Overloading prevention, profit maximisation, emission minimisation, renewable energy sources (RES) integration, voltage profile improvement, harmonic filtering [30], load levelling, power loss reduction [31]</td>
</tr>
<tr>
<td>Advantages</td>
<td>Limited services</td>
<td>Battery degradation, high complexity, and cost, social barriers</td>
</tr>
<tr>
<td>Disadvantages</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Initially, V2G involved only energy transfer from EVs to the distribution system. However, with the advancement in technology, two new energy transfer modes (V2H and V2V) are added. Therefore, the bi-directional energy transfer from EV can now be classified into:

- Vehicle-to-grid (V2G): Energy transfer from EV to the distribution network.
- Vehicle-to-home/building (V2H/V2B): Energy transfer from EV to home/building.
- Vehicle-to-vehicle (V2V): Energy transfer from one EV to another EV.

3. Modelling of Grid-Connected EV-PV System

The sustainability of EV depends on the source of charging. All forms of EVs, i.e., plug-in electric vehicle (PEV), hybrid electric vehicle (HEV), or plug-in hybrid electric vehicle (PHEV), have lower emissions if the energy supplied for charging is based on clean fuel, such as renewable sources. However, contrary to popular belief if the EVs are charged from fossil fuel or gas-based generation, the emissions are significant and not zero. The RES, i.e., PV, wind, tidal, geothermal, or hydro, are excellent options to power electric vehicles. Moreover, the following reasons make PV an admirable source to charge the EVs:

- The cost of PV has been dropping continuously and is currently less than $1/W_p [32].
- PV is highly accessible, i.e., PV modules are generally installed on the building rooftops and carparks, close to EV locations.
- PV modules do not require maintenance and are also noise-free.
- EVs can store the surplus generated solar energy, thereby eliminating the need for battery systems [33,34].
Figure 4 shows a general framework for designing a smart charging system for integrating EV-PV system into the grid. As the focus of this review paper is on modelling aspect of the grid-connected EV-PV system, this section will provide an overview of the modelling of control approaches with subsequent sections reviewing about charging models/algorithms and uncertainty.

![Figure 4. A general outline for modelling a grid-connected EV-PV charging system.](image)

The control architectures for grid-connected EVs (with or without PVs) can be categorised into the following three methodologies:

- **Centralised scheduling;**
- **Decentralised scheduling;**
- **Price-varying scheduling.**

In centralised scheduling method, EV aggregator plays a crucial role in integrating EV with the grid. Initially, each EV sends the necessary charging related information to the aggregator. After which aggregator computes the optimal charging strategy and participates in the energy trading through bidding, which is verified by grid system operators. The general objective functions in centralised type scheduling are charging cost minimisation [35], line power loss minimisation [36], aggregator profit maximisation [37,38], voltage regulation [39] and frequency regulation [40]. Due to the aggregation of many EVs, this method is very good for providing backup power and ancillary services. However, in the centralised method, EV users have to relinquish the charging process control to centralised authority. Other drawbacks of this approach are high dependency on the control centre and large communication bandwidth.

In decentralised scheduling method, individual EVs are controlled directly instead of through a central control unit. Firstly, EV aggregator formulates a bidding strategy based on EV load demand data collected or forecasted in a given period. Then, the bids are submitted to the central grid operator and cleared in the energy market the same as in centralised scheduling. After the bids are approved, and an agreement is done with the grid operator, the aggregator broadcasts the charging prices to individual EV users. Based on the price and convenience, users decide whether to charge/discharge their EVs in a given period. The advantage of this type of scheduling is that the infrastructure is simple and of low cost. However, due to a random number of EVs guaranteed to be available at a given time, this method’s capability of the provision of backup power and ancillary services is low. Also, privacy and security issues are there. The general objective function in decentralised type scheduling is mainly charging cost minimisation [41–43]. Other objectives are RES integration [44], load profile levelling [45], voltage regulation [46] and frequency regulation [47].
The price-varying scheduling has the same structure as decentralised scheduling, however, the charging behaviours of EVs are directly affected by varying electricity pricing. Instead of two-way communication, i.e., price and power schedule information exchanged in decentralised scheduling, here the only price is communicated to EVs. Reference [48] discusses the feasibility of using time-of-use (TOU) based pricing for EV energy management. Reference [49] presents a socially optimal pricing system between EV aggregators and utility. Reference [50] introduces a smart EV energy management algorithm that takes dynamic factors, such as user participation and load variation into account.

Figure 5 presents an overview of the comparison between the scheduling strategies discussed above [51]. Even though the price-varying scheduling is overall less complex, it is less attractive for commercial entities to participate in V2G, due to the high cost of computation on their side. Hence, the focus of research is generally more on centralised and decentralised scheduling strategies.

![Figure 5. An overview of scheduling strategies in V2G mode [51].](image)

The grid-connected EV-PV systems are designed based on spatial configuration requirements, i.e., for homes or office use etc. Generally, in the literature, four space-based levels are used: Residential (individual house), non-residential (commercial/workplaces), public charging stations and inter-territory region. Due to the large size of EV loads, which almost doubles the electricity consumption of a household, it is reasonable to provide another energy source (like PV) [52]. Nevertheless, it appears through the literature that while coupling EV with PV inside households can be beneficial, the benefits are bounded by the EV utilisation for mobility. Most of the EVs are usually away from home during the day, and therefore, cannot benefit from maximal PV generation. It is reasonable to assume that usually, EVs will be at non-residential places (commercial/workplaces) during this day period when peak PV generation happens. So, EVs will be either at residential or non-residential areas. Therefore, the focus of this paper is only on the modelling of residential and non-residential (commercial/workplace) EV-PV system. The PV based EV charging stations are not yet economically feasible, due to the marginal cost associated with PV generation and the cost of energy storage systems [53]. Reference [54] is one example of the limited literature available on standalone PV based EV charging stations.
4. EV Smart Charging Using PV and Grid

Multiple studies have explored the advantages of a PV based EV charging system. Reference [55] demonstrates the advantage of using PV to charge the EV and show that it allows for greater penetration of both PV and EV. EVs can also mitigate the negative effects of excess PV generation [56]. Reference [57] presents a case study of Columbus, USA, in which it is demonstrated that charging EV from the PV is more economical and produces less CO\textsubscript{2} footprint than charging EV from the grid. A case study presented in Reference [58] compares charging of EVs through the modes: Only grid, only PV with battery storage and grid integrated PV and finds that the grid integrated PV performs better economically compared to the other two systems. In Reference [59], the authors discuss the application of PV energy and EV as an energy storage system to mitigate the peak loading in the grid. These studies demonstrate the advantages of PV based EV charging over grid EV charging. There is a vast amount of literature on different charging algorithms or achieving different economic, technical, or social objectives related to PV based EV charging. Table 2 provides a summary of key smart charging related works for the grid-connected EV-PV system.

The optimisation model type depends on the problem formulation. Generally, the convex type problems (linear, mixed-integer, quadratic) can achieve optimal solutions with a low computational cost. For non-convex problems, meta-heuristic type optimisation methods (Genetic Algorithm, Particle Swarm Optimisation) are useful to achieve a near-optimal solution with a low computational burden. The rule-based algorithm or heuristic type optimisation methods can produce good enough solutions for random instantaneous events (e.g., plugging/unplugging of EVs, PV power variation) with little data and computational power requirements. The focus of the literature is generally on residential or office PV based EV charging system, not on commercial applications, due to less complexity in analysis and modular integration in the distribution system. Moreover, almost all the smart charging research focuses on the specific aspects of optimizing the EV integration into grid, e.g., slow/fast charging, market participation, ancillary services. For emulating the real-life implementation, a comprehensive system with multiple aspects is required. Reference [60,61] are some early stages work on a comprehensive system combining multiple aspects which are usually studied in isolation.

<table>
<thead>
<tr>
<th>References</th>
<th>Objectives</th>
<th>Optimisation Model</th>
<th>Software/Implementation</th>
<th>Key Findings</th>
</tr>
</thead>
<tbody>
<tr>
<td>[62]</td>
<td>Peak shaving and valley filling</td>
<td>Linear programming</td>
<td>MATLAB</td>
<td>The effectiveness of the proposed algorithm is dependent on a high number of available parking spots.</td>
</tr>
<tr>
<td>[35]</td>
<td>Maximizing profit and PV utilisation</td>
<td>Mixed Integer Linear programming</td>
<td>GAMS</td>
<td>Due to battery degradation cost, V2G is not economically feasible unless high PV production is present</td>
</tr>
<tr>
<td>[63]</td>
<td>Minimizing system cost</td>
<td>Mixed Integer Linear programming</td>
<td>CPLEX</td>
<td>Smart charging can result in saving of operational cost for charging and PV usage for the parking lot owner</td>
</tr>
<tr>
<td>[64]</td>
<td>Minimizing charging cost</td>
<td>Fuzzy logic</td>
<td>MATLAB</td>
<td>The algorithm is not optimisation based so targets several objectives: Reduction in charging cost and system losses, improvement in voltage profile.</td>
</tr>
</tbody>
</table>
Table 2. Cont.

<table>
<thead>
<tr>
<th>References</th>
<th>Objectives</th>
<th>Optimisation Model</th>
<th>Software/Implementation</th>
<th>Key Findings</th>
</tr>
</thead>
<tbody>
<tr>
<td>[65]</td>
<td>Maximizing PV utilisation</td>
<td>Metaheuristic</td>
<td>MATLAB</td>
<td>The proposed heuristic algorithm achieves desired objectives with low computational cost and without forecasting of uncertain variables.</td>
</tr>
<tr>
<td>[66]</td>
<td>Maximizing EV aggregator benefits</td>
<td>Hybrid MPC</td>
<td></td>
<td>The proposed algorithm achieves near-optimal solution of EV charge scheduling problem with better efficiency than standard MPC</td>
</tr>
<tr>
<td>[67]</td>
<td>Maximizing PV utilisation and reducing EV charging impact</td>
<td>Linear programming</td>
<td>Case study: New South Wales distribution system</td>
<td>The proposed strategy controls the charging/discharging profile of EVs to match with the shape of the PV output to achieve desired objectives.</td>
</tr>
<tr>
<td>[68]</td>
<td>Minimizing charging cost</td>
<td>Mixed Integer Linear programming</td>
<td>Case study: Korea</td>
<td>The proposed algorithm does not consider selling excess power and demonstrates charging cost savings compared to uncoordinated charging</td>
</tr>
<tr>
<td>[61]</td>
<td>Minimizing system cost</td>
<td>Mixed Integer Linear programming</td>
<td>Microsoft Solver Foundation</td>
<td>A comprehensive system to achieve one optimal charging profile will result in a larger net benefit compared to individual applications.</td>
</tr>
<tr>
<td>[69]</td>
<td>Minimizing charging cost</td>
<td>Convex programming</td>
<td>MATLAB</td>
<td>ESS can significantly reduce charging cost and bi-directional V2H is cheaper than H2V</td>
</tr>
<tr>
<td>[70]</td>
<td>Maximizing profit and ESS life</td>
<td>Non-linear programming</td>
<td>GAMS</td>
<td>Considering only revenue maximisation will result in an adverse effect on ESS life</td>
</tr>
<tr>
<td>[71]</td>
<td>Maximizing PV utilisation</td>
<td>Linear programming</td>
<td>Case study: LomboXnet</td>
<td>Proposed algorithm increases PV self-consumption and reduces peak demand by half</td>
</tr>
<tr>
<td>[72]</td>
<td>Minimizing charging cost</td>
<td>Rule-based algorithm</td>
<td>MATLAB</td>
<td>Rule-based charging is superior to conventional charging for less charging cost and reduced grid loading</td>
</tr>
<tr>
<td>[73]</td>
<td>Maximizing PV utilisation</td>
<td>Rule-based algorithm</td>
<td>MATLAB</td>
<td>V2B can be an effective strategy if initial capital costs and electricity price are fitting</td>
</tr>
<tr>
<td>[74]</td>
<td>Minimizing peak demand</td>
<td>MPC</td>
<td>MATLAB</td>
<td>EV scheduling can reduce both the magnitude and frequency of peak loading</td>
</tr>
<tr>
<td>[75]</td>
<td>Peak shaving and valley filling</td>
<td>Quadratic programming</td>
<td>MATLAB</td>
<td>Net load variation was lower in case of low PV power-sharing and vice-versa</td>
</tr>
</tbody>
</table>

V2H, vehicle-to-home; H2V, home-to-vehicle; V2B, vehicle-to-building; MPC, model predictive control.

The stochastic behaviour of the PV generation is a major disadvantage for EV charging. The approach of a smart charging algorithm is to provide flexibility in EV charging to account for the uncertainty in PV generation. Reference [71] has shown that smart charging, along with the V2G technology, increases PV self-consumption and reduces peak demand. Reference [76] varies the EV charging power with time to match with the generated PV power and achieves the condition of maximum PV utilisation. Another way to counteract uncertainty is the sequential charging in which the total number of EVs charging at constant power is varied dynamically so that the net charging power follows the PV generation, as seen in Reference [77]. Reference [78] considers multiple cases to show the superiority of sequential charging over concurrent charging in terms of PV utilisation under stochastic conditions. However, due to no associated time constraints, it is not feasible for workplace charging.

5. Uncertainty Modelling

This section reviews the methods for modelling the uncertainties present with the various input parameters for the EV-PV grid integrated system. Three input factors are of main interest: EV charging demand, PV generation, and Electrical load distribution. The tables in respective sections summarise the techniques used to model the uncertainties present. The remarks show the comparative analyses of these techniques in terms of system size, computational cost, and accuracy.
5.1. EV Charging Demand

The uncertainties in EV charging demand are due to multiple factors, e.g., user behaviour, charging infrastructure, and operational parameters. Table 3 presents an overview of various uncertainty methods for modelling EV load demand in terms of application and associated drawbacks. Generally, Monte Carlo and Probability distribution based modelling method is common practice in the literature. However, due to computational cost and accuracy issues associated with them, respectively, more advanced methods like Markov chain and Information gap decision theory are used for specific applications. A hybrid approach of combining methods is also used to minimise the associated drawbacks.

Table 3. Overview of uncertainty modelling methods for EV load demand.

<table>
<thead>
<tr>
<th>Method</th>
<th>Remarks</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>Scenario reduction</td>
<td>• Simple and less computationally intensive</td>
<td>[79,80]</td>
</tr>
<tr>
<td></td>
<td>• Approximate uncertainty modelling, accuracy depends on the amount of historical data available</td>
<td></td>
</tr>
<tr>
<td>Monte Carlo simulation</td>
<td>• High accuracy, but also computationally intensive</td>
<td>[19,81]</td>
</tr>
<tr>
<td></td>
<td>• Accuracy depends on the amount of historical data available</td>
<td></td>
</tr>
<tr>
<td>Fuzzy logic</td>
<td>• Historical data not required</td>
<td>[82,83]</td>
</tr>
<tr>
<td></td>
<td>• Accuracy depends on rule settings which are based on researcher experience</td>
<td></td>
</tr>
<tr>
<td>Hybrid Monte Carlo-fuzzy</td>
<td>• High accuracy, but also computationally intensive</td>
<td>[84]</td>
</tr>
<tr>
<td></td>
<td>• Can model both temporal and spatial uncertainty</td>
<td></td>
</tr>
<tr>
<td>Artificial Neural Network</td>
<td>• Accuracy depends on input dataset quality</td>
<td>[37,85]</td>
</tr>
<tr>
<td></td>
<td>• Considers the correlation between forecasted and observed data</td>
<td></td>
</tr>
<tr>
<td>Markov chain</td>
<td>• Very high accuracy with moderate computational cost</td>
<td>[86]</td>
</tr>
<tr>
<td></td>
<td>• Performance depends on input data dimension</td>
<td></td>
</tr>
<tr>
<td>Probability distribution</td>
<td>• Very simple, but also less accurate</td>
<td>[87,88]</td>
</tr>
<tr>
<td>fitting</td>
<td>• Low computationally intensive however difficult to employ with non-linear problems</td>
<td>[89,90]</td>
</tr>
<tr>
<td>Robust optimisation</td>
<td>• Not flexible, i.e., give a single solution which might be infeasible</td>
<td></td>
</tr>
<tr>
<td>Information gap decision theory</td>
<td>• Useful for dealing with severe uncertainties</td>
<td>[91,92]</td>
</tr>
<tr>
<td></td>
<td>• Complex implementation</td>
<td></td>
</tr>
</tbody>
</table>

Figure 6 shows the various input parameters for the uncertainty modelling of EV load demand. The parameters related to time (e.g., arrival, departure, travel, service) and charging power demand required are common in all the three modes of charging: Individual, residential, and commercial, while others are specific to the application. The uncertainties in the parameters involving human factors, i.e., travel/arrival/departure time and pattern are difficult to describe accurately, and also the literature is quite scarce on the effect of human learning capability on EV charging demand. Reference [44] is an example of paucity of research on the practical effect of human factors on EV charging.
5.2. PV Generation

A PV module converts energy from the sun into electrical form depending upon the incident radiation on the module surface. This incident solar radiation is highly variable and depends on various geographical and metrological factors. The common variables used in uncertainty modelling of PV generation are solar irradiance, sky type index (clear, cloudy, sunny), module and air temperature, wind speed, and humidity. Table 4 shows a summary of commonly used uncertainty modelling methods for PV generation. The commonly practiced methods are Point estimation, Monte Carlo, Scenario based analysis, and statistical methods (Autoregressive Moving Average). These methods are less complex and work well with small system size. However, for bigger PV systems, Rolling Horizon approach and Kernel Density are more suitable. Generative Adversarial Network (GAN) is the latest uncertainty modelling method based on a machine learning approach.
Table 4. Overview of common uncertainty modelling methods for PV.

<table>
<thead>
<tr>
<th>Method</th>
<th>Remarks</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>Point estimation</td>
<td>• Computationally intensive with more input variables</td>
<td>[93]</td>
</tr>
<tr>
<td>Bootstrap</td>
<td>• Simple and low computational cost</td>
<td>[94]</td>
</tr>
<tr>
<td></td>
<td>• High accuracy</td>
<td></td>
</tr>
<tr>
<td>Monte Carlo simulation</td>
<td>• High accuracy, but also computationally intensive</td>
<td>[95]</td>
</tr>
<tr>
<td>Mean-Variance estimation</td>
<td>• Based on the assumption that uncertainty is normally distributed</td>
<td>[96]</td>
</tr>
<tr>
<td></td>
<td>• Simple, but less accurate for practical cases</td>
<td></td>
</tr>
<tr>
<td>Two stage scheduling</td>
<td>• Upper level deals with global adjustment and lower with local adjustment</td>
<td>[97]</td>
</tr>
<tr>
<td></td>
<td>• Simple, flexible and accurate</td>
<td></td>
</tr>
<tr>
<td>Scenario based analysis</td>
<td>• Very commonly used method with a high degree of accuracy</td>
<td>[98]</td>
</tr>
<tr>
<td></td>
<td>• Accuracy depends upon the scenario generation technique</td>
<td></td>
</tr>
<tr>
<td>Kernel Density estimation</td>
<td>• Needs to analyse a large amount of historical data</td>
<td>[99]</td>
</tr>
<tr>
<td>Autoregressive Moving Average</td>
<td>• Accuracy depends on historical time-series dataset</td>
<td>[35]</td>
</tr>
<tr>
<td></td>
<td>• Needs a lot of historical data and analysis</td>
<td></td>
</tr>
<tr>
<td>Probability distribution fitting</td>
<td>• Very simple, but also less accurate</td>
<td>[100]</td>
</tr>
<tr>
<td>Rolling Horizon approach</td>
<td>• Effective for large scale system with moderate computational cost</td>
<td>[101]</td>
</tr>
<tr>
<td>Generative Adversarial network</td>
<td>• Very new and highly accurate scenario based method</td>
<td>[102]</td>
</tr>
</tbody>
</table>

References [103,104] describes the implementation details of various forecasting techniques for PV power generation. More details about uncertainty modelling for the RES systems can be found in References [105–108]. The literature of PV based uncertainty modelling is scarce as the cumulative effect of PV power on the system is small compared to other uncertain variables (load, EV demand).

The most common method to mitigate the PV uncertainty is using an external battery storage system, i.e., different from the EV batteries [109]. The excess PV generation, usually in the afternoon, is stored in the battery pack and used to charge the EVs when PV generation is inadequate. Reference [110] compares three different algorithms for finding the best operation characteristics for the battery storage and finds that using a sigmoid function-based discharging algorithm, while charging EVs during the night and storing PV excess is the best approach. However, these studies do not consider the optimal sizing of the external battery storage system as it is a quite expensive component. Apart from mitigating PV uncertainty, the external battery storage system also minimises the impact of EV demand uncertainty parameters constrained by time.

5.3. Electrical Load Demand

The consumption of electricity is highly spatially and temporally uncertain, varying between different load sources, seasons, and the time of day. The main factors for introducing uncertainty in load sources are user behaviours, climatic conditions, and electrical equipment variation [111]. Table 5 shows an overview of various common methods used for modelling uncertainty in electrical loads. Readers can refer to [105,108,111–113] for implementation details of these and other methods used to model uncertainties present in electrical load. The convolution and cumulant based techniques are
traditional methods popular in the late nineties’ era. However, with the scaling of computational cost with system size, the point estimation became a more popular method. Monte Carlo and Scenario based analysis are also fairly common in the literature.

Table 5. Overview of common uncertainty modelling methods for electrical load demand.

<table>
<thead>
<tr>
<th>Method</th>
<th>Remarks</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>Point estimation</td>
<td>• Does not require complete knowledge about the system, but computationally intensive with more input variables</td>
<td>[114,115]</td>
</tr>
<tr>
<td></td>
<td>• Two-point is the simplest and three-point is most efficient</td>
<td></td>
</tr>
<tr>
<td>Monte Carlo simulation</td>
<td>• High accuracy, but also computationally intensive</td>
<td>[116,117]</td>
</tr>
<tr>
<td></td>
<td>• Different sampling techniques reduce the computational burden</td>
<td></td>
</tr>
<tr>
<td>Fuzzy logic</td>
<td>• Less computationally intensive and robust in nature</td>
<td>[118]</td>
</tr>
<tr>
<td></td>
<td>• Vital parameters are decided by the researcher based on experience</td>
<td></td>
</tr>
<tr>
<td>Scenario based analysis</td>
<td>• Very commonly used method with a high degree of accuracy</td>
<td>[119]</td>
</tr>
<tr>
<td></td>
<td>• Accuracy depends upon the scenario generation technique</td>
<td></td>
</tr>
<tr>
<td>Autoregressive Moving Average</td>
<td>• Accuracy depends on historical time-series dataset</td>
<td>[85,120]</td>
</tr>
<tr>
<td></td>
<td>• Needs a lot of historical data and analysis</td>
<td></td>
</tr>
<tr>
<td>Convolution based</td>
<td>• Traditional analytical method with low computation efficiency</td>
<td>[121,122]</td>
</tr>
<tr>
<td></td>
<td>• Applicable to linear systems with independent inputs</td>
<td></td>
</tr>
<tr>
<td>Probability distribution fitting</td>
<td>• Very simple, but also less accurate</td>
<td>[88,123]</td>
</tr>
<tr>
<td>Cumulant based</td>
<td>• Traditional analytical method with high computation efficiency</td>
<td>[124]</td>
</tr>
<tr>
<td></td>
<td>• Accuracy decreases with higher order systems</td>
<td></td>
</tr>
</tbody>
</table>

6. Conclusions and Future Research Suggestions

Electric vehicles and renewable energy-based generation are a promising solution to rising GHG emissions. Further, EVs can act as a dynamic energy storage system through the technology of V2G, thereby, facilitating RES integration in the smart grid. Also, well to wheel emissions from EVs depend upon the charging source. Therefore, RES based EV charging is desired for the overall reduction in emissions and getting the best of both technologies. Thus, this research area is quite popular and needs further exploration for worldwide implementation. This paper presents a state-of-the-art comprehensive review of the modelling of grid-connected EV-PV charging systems. A general framework of designing the grid-connected EV-PV system is described along with a focus on smart charging algorithms. The modelling techniques for associated uncertainties with the grid-connected EV-PV system, i.e., EV demand, electrical load, and PV generation are also intensely reviewed. The study reveals that although the research in this area is plentiful, few gaps need to be investigated. Some future research directions are suggested as following:

- Smart charging algorithms

The EV charging models need to be more comprehensive in nature, i.e., multiple charging powers, charging station and battery-swapping station, and wholesale market trading and ancillary services provisions, in order to more accurately and realistically model the practical implementation. More studies with respect to finding the optimal trade-offs between computational burden and performance should be made.
• P2P V2G power transfer

There is a need for more research on peer-to-peer or transactive type charging systems as this encourages all types (big, small, etc.) EV aggregators to trade energy with one another instead of only sizeable aggregator participating in central energy trading. Another advantage is that transactive trading can operate independently of direct influence from the grid so that the price signal from the central power station may not affect the performance of the transactive trading the way it influences the scheduling and trading of energy in existing systems.

• Uncertainty analysis

The focus of future research should be on finding more realistic forecasting and uncertainty analysis techniques that optimally balance simplicity and performance. Also, more advancement is needed in the modelling of challenging variables like human behaviour, etc. Further, almost all the current research focuses on improving PV forecasting accuracy rather than addressing uncertainties associated with PV generation.

• PV based EV charging stations

With PV based EV charging being a viable solution for emission issues, more research is needed on the commercial aspects, e.g., solar charging stations as current research focus more on residential EV-PV systems. The impact analysis and interaction with the distribution system needs to be studied in detail.

• Price-varying scheduling

Because of easy implementation and effectiveness for managing charging load in peak-valley times, price-varying scheduling is very attractive to aggregators. Therefore, more research is required for charging models based on price response and price elasticity.

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