Sizing and Cost Minimization of Standalone Hybrid WT/PV/Biomass/Pump-Hydro Storage-Based Energy Systems

Fahd A. Alturki * and Emad Mahrous Awwad *

Abstract: In this study, a standalone hybrid wind turbine (WT)/photovoltaic (PV)/biomass/pump-hydro-storage energy system was designed and optimized based on technical, economic, and environmental parameters to provide the load demand with an objective function of minimum cost of energy (COE). The constraints of the proposed approach are the loss of power supply probability, and the excess energy fraction. The proposed approach allows the combination of different sources of energy to provide the best configuration of the hybrid system. Therefore, the proposed system was optimized and compared with a WT/PV/biomass/battery storage-based hybrid energy system. This study proposes three different optimization algorithms for sizing and minimizing the COE, including the whale optimization algorithm (WOA), firefly algorithm (FF) and particle swarm optimization (PSO) and the optimization procedure was executed using MATLAB software. The outcomes of these algorithms are contrasted to select the most effective, and the one providing the minimum COE is chosen based on statistical analysis. The results indicate that the proposed hybrid WT/PV/biomass/pump-hydro storage energy system is environmentally and economically practical. Meanwhile, the outcomes demonstrated the technical feasibility of a pump-hydro energy storage system in expanding the penetration of renewable energy sources compared to other existing systems. The COE of the pumped-hydro storage hybrid system was found to be lower (0.215 $/kWh) than that with batteries storage hybrid system (0.254 $/kWh) which was determined using WOA at the same load demand.

Keywords: renewable energy; emission mitigation; optimization; energy management; pump-hydro storage; microgrid

1. Introduction

Recently, electricity requirements have been increasing significantly due to rapid technological development and large population growth [1–3]. Currently, there is significant progress in renewable energy systems worldwide due the steady decrease in accessibility to traditional energy reserves, the need to secure reliable and sustainable energy sources, and the global target to reduce CO₂ emissions by 50–80% by 2050 to mitigate the global environmental crises [4]. However, using sustainable energy resources alone cannot guarantee continuous energy supply due to their unpredictability and heavy dependence on environmental conditions as well as load variation. Thus, research has been recently focusing on hybrid energy systems-based renewable and conventional energy resources [5–7]. The microgrid is a modern concept that can reduce the cost of generating energy and reduce carbon emissions per year [8,9]. This is a prudent policy that not only reduces operating costs but also supports the ever-increasing advancement of renewable sources [10]. In this way, various renewable energy sources like wind turbine (WT), photovoltaic (PV), biomass units, hydropower units, help a lot in achieving this goal. Moreover, the storage batteries are always an inevitable part of microgrid due to the high volatility of the units [11,12]. In high-permeation frameworks, energy storage units must be used to compensate for unpredictable resources. Storage batteries are the most common type of electrical
energy storage devices. However, the mechanism of energy storage in batteries affects their performance, cost, and lifetime as it is based on electrochemical reactions. Compared to other energy storage devices, batteries have the disadvantages of short cycle life and lifetime, high capital cost, significant effects on the environment [13]. Furthermore, significant efforts are required for the transport and removal of batteries to and from high regions. Subsequently, mechanical storage systems, such as pumped-storage hydropower, could be a better option in remote areas where water is accessible compared to battery storage. Pumped-storage hydropower for standalone power generation facilities has been developed to improve the sustainability of low-carbon energy systems. Its main advantages include shorter re-compensation periods, faster response to load variations, longer lifetime, and lower maintenance cost compared to other systems [14–16].

1.1. Literature Survey

Sizing and optimization should be conducted before the installation of hybrid renewable energy systems (HRES) [17]. This is performed to obtain a general understanding of the system, e.g., the capacity of individual framework segments required to realize the load demand. Thus, sizing and optimization play an important role in the decision-making process for capital investment. In this regard, Kusakana et al. [18] executed a techno-economic study on the application of a standalone hydrokinetic hybrid system with pumped-storage hydropower in a remote area. The results confirmed the viability of the proposed framework. Ma et al. [19] reported that a photovoltaic (PV)/wind/pumped-storage hydropower system was more economically viable than a PV/wind/battery system. Rathore and Patidar [20] investigated a PV/wind/pumped-storage hydropower-based off-grid system for a remote community and determined that a pumped-storage hydropower-based system was both economically and environmentally better than battery-based storage systems. A study by Neubauer and Pesaran [21] demonstrated the effect of batteries on the total cost of the system [9]. The results indicated a deterministic count to confine the entire structure cost while accomplishing the pile necessities of the system. For more details about the storage options; Table 1 introduces the techno-economic characteristics of various storage options [22–24].

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Mechanical Storage</th>
<th>Chemical Storage</th>
<th>Electrical Storage</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Pump Storage</td>
<td>Flywheel</td>
<td>Compressed Air</td>
</tr>
<tr>
<td>Energy density (Wh/kg)</td>
<td>0.5–1.5</td>
<td>10–30</td>
<td>30–60</td>
</tr>
<tr>
<td>Power density (W/kg)</td>
<td>40–60</td>
<td>400–1500</td>
<td>20,000</td>
</tr>
<tr>
<td>Lifetime (yr)</td>
<td>40–60</td>
<td>1–15</td>
<td>20–60</td>
</tr>
<tr>
<td>Energy efficiency (%)</td>
<td>65–87</td>
<td>85–95</td>
<td>90–95</td>
</tr>
<tr>
<td>Discharge time</td>
<td>1–24 h</td>
<td>ms–15 min</td>
<td>1–24 h</td>
</tr>
<tr>
<td>Technological development</td>
<td>Mature</td>
<td>Commercial</td>
<td>Developed</td>
</tr>
<tr>
<td>Capital cost ($/kW)</td>
<td>600–2000</td>
<td>250–350</td>
<td>400–800</td>
</tr>
</tbody>
</table>

Meta-heuristic based approaches are generally classified into swarm and evolutionary-based intelligence approaches. Evolutionary based approaches mimic the origins of advancement in nature, on which numerous developmental approaches in the literature are based [25–28]. In this regard, the authors in [25] have minimized a PV/pump-hydropower-based power generation system for remote areas using a genetic algorithm (GA) and reported its economic feasibility to reliably satisfy demand requirements. Shabani and Mahmoudimehr [26] investigated a PV/pumped-storage hydropower configuration using a GA with different PV-tracking techniques and the results were compared to those of a PV/battery configuration. The results indicated that the total cost of the PV/battery configuration is 76% higher than that of the PV/pumped-storage hydropower configuration. Stoppato et al. [27] have minimized the cost of energy (COE) of a PV/pumped-storage
hydropower system for providing electricity demand and drinking water to rural areas in Nigeria using particle swarm optimization (PSO). The authors in [28] have optimized a PV/wind/pumped-storage hydropower-based energy system for a remote cite using PSO. The results indicated that a PV/wind/pumped-storage hydropower system has the lowest COE out of all studied configurations.

The intelligence-based swarm algorithms are based on the behavior of a lot of creatures [29–35]. In the firefly algorithm (FF) and whale optimization algorithm (WOA), the boundaries to be regulated through the optimization process are less than those with GA and PSO [36]. This gives FF and WOA more potential and is prevalent in solving optimization problems [37]. FF, WOA, and PSO algorithms have been selected in this paper for their superiority in solving complex optimization problems. FF and WOA are examples of meta-heuristic-based optimization techniques. FF is recognized as a non-algorithmic particular parameter. WOA does not require initial values for mutation and is suitable for handling discrete and ceaseless factors that cannot find the nearby optima [38]. Generally, PSO is regularly widely utilized in research due to its higher probability and productivity in determining the global optima. However, in complex optimization problems, PSO may suffer from unsteady convergence and becoming trapped in a local minimum. A summary of some recent studies on various hybrid systems based pump-hydro storage is introduced in Table 2.

Table 2. Pump-hydro storage-based hybrid energy systems.

<table>
<thead>
<tr>
<th>Pump-Hydro Storage Based Hybrid Systems</th>
<th>Standalone/On-Grid</th>
<th>Optimizer</th>
<th>Evaluation Criteria</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>PV/Wind/Pump-hydro</td>
<td>Standalone</td>
<td>Demand Response</td>
<td>Cost analysis, Excess Energy (EE)</td>
<td>[39]</td>
</tr>
<tr>
<td>PV/Wind/Pump-hydro</td>
<td>Standalone</td>
<td>HOMER</td>
<td>COE, Net Present Cost (NPC), emissions, Renewable Penetration (RP)</td>
<td>[40]</td>
</tr>
<tr>
<td>PV/Wind/Diesel/Pump-hydro/Fuel Cell (FC)/Battery</td>
<td>Standalone</td>
<td>HOMER</td>
<td>COE, NPC, emissions, EE, RP</td>
<td>[41]</td>
</tr>
<tr>
<td>Wind/Pump-hydro</td>
<td>Standalone</td>
<td>GA</td>
<td>COE, reliability</td>
<td>[42]</td>
</tr>
<tr>
<td>PV/Wind/Pump-hydro</td>
<td>Standalone</td>
<td>GA</td>
<td>COE, reliability</td>
<td>[25]</td>
</tr>
<tr>
<td>PV/Wind/Pump-hydro</td>
<td>Standalone</td>
<td>GA, HOMER</td>
<td>Sensitivity analysis, COE, reliability</td>
<td>[44]</td>
</tr>
<tr>
<td>PV/Wind/Pump-hydro</td>
<td>Standalone</td>
<td>PSO, GA, Simulated Annealing</td>
<td>COE, reliability</td>
<td>[39]</td>
</tr>
<tr>
<td>PV/Wind/Pump-hydro</td>
<td>Standalone</td>
<td>Fmincon</td>
<td>Cost analysis</td>
<td>[45]</td>
</tr>
<tr>
<td>PV/Diesel/Pump-hydro</td>
<td>Standalone</td>
<td>Fmincon</td>
<td>Cost analysis</td>
<td>[46]</td>
</tr>
<tr>
<td>Wind/Pump-hydro</td>
<td>On-grid</td>
<td>Evolutionary Algorithm</td>
<td>NPC, PP</td>
<td>[47]</td>
</tr>
<tr>
<td>PV/Wind/Battery/Pump-hydro</td>
<td>On-grid</td>
<td>Non-Dominated Sorting GA</td>
<td>Cost analysis, CO₂ emissions</td>
<td>[48]</td>
</tr>
<tr>
<td>PV/Wind/Pump-hydro</td>
<td>On-grid</td>
<td>Direct Multi-Search</td>
<td>Cost analysis, CO₂ emissions, RP</td>
<td>[49]</td>
</tr>
</tbody>
</table>

1.2. Motivation and Contributions

This paper essentially focuses on assessing the technical, economic, and environmental aspects of the pump-hydro storage when used in hybrid PV/Wind/biomass system to satisfy an isolated community’s load requirement. In other words, it formulates and identifies the best system configuration for optimal techno-economic feasibility with high reliability by using locally available sustainable resources, such as, solar energy, biomass, wind and pump-hydro options. A comparative analysis of battery (lead-acid battery) and pump-hydro storage options for a hybrid system to meet a similar dynamic load profile is also conducted. Finally, sensitivity analysis is carried out to assess the impact of the
variability in the input hardware costs and discount rates on the net present cost (NPC) and COE.

Three algorithms including FF, WOA, and PSO algorithms have been selected in this paper for their superiority in solving complex optimization problems. The algorithms are utilized to minimize the size of a hybrid WT/PV/biomass/pump-hydro storage system with a condition of satisfying the load demand with the minimum COE [50–54]. One of the objectives of the present work is to compare between these algorithms and select the best one in terms of accuracy and convergence speed. The constraints of the proposed approach are loss of power supply probability ($LPSP$), maximum ($LPSP_{max}$) and the excess energy fraction, minimum ($EFF_{min}$) [55,56]. The major contributions of this study are as follows:

- Proposing an effective approach based MATLAB software and using FF, WOA, and PSO algorithms that can minimize the size of the system in intelligent and operative manner.
- Setting the simulation paradigm that determines the operation of the HRES which comprises of WT/PV/pump-hydro storage/biomass.
- Investigating and analysing different hybrid systems including WT/PV/biomass/pump-hydro storage and WT/PV/biomass/battery storage systems.
- Proposing an effective management framework that handles the power management between the HRES components.
- Implementing a detailed comparative analysis, combined with sensitivity assessment of the economic and environmental indicators for the different HRES configurations.
- Highlighting the economic feasibility and environmental benefits of the proposed hybrid WT/PV/biomass/pump-hydro storage, the suitability and need for the implementation of hybrid energy projects in standalone areas of Saudi Arabia.

The remaining sections of the paper are arranged as follows: Section 2 introduces the modeling of the systems components; in Section 3, the system energy balance is explained. The proposed optimization algorithms are presented in Section 4. The simulation framework and its parameters and the simulation results are presented and discussed in Section 5. In Section 6, the conclusion is provided.

2. Design of the Proposed System Elements

Figure 1 shows a schematic diagram of the hybrid WT/PV/biomass power system integrated with a pumped-storage hydropower unit, illustrating the system parameters and power dispatch directions. A direct current (DC) load bus was linked to the PV system, wind turbine, and biomass system. The alternative current (AC) bus is linked with both load and the pumped-storage hydropower system. The pumped-storage hydropower unit can fill in as a bulk store application [57]. There are two tanks in this unit, i.e., the upper and lower tanks, which are used to store water for the storage of extra energy during off-rush hours and to exhaust the energy stored in the water back during rush hours, respectively [58]. The tank capacity depends on the value and storage time. The efficiency of these systems is typically within 80–85%, and hence, these systems are more efficient for energy storage compared to batteries. Furthermore, these storage systems exhibit long lifetime, high reliability, and low operation and maintenance costs (OMC) [59]. The pumped-storage hydropower systems use the lower and upper tanks. The pumped-storage hydropower systems are used for feeding the deficit of the output energy from PV, wind, and biomass energy by evacuating the water, which was previously pumped in case of energy surplus in the system, from the upper tank. The WT/PV/pumped-storage hydropower/biomass HRES performance depends on each sub-system performance [60–62]. Thus, to obtain the optimal performance of each power source, each one is presented and discussed separately in the following sections.
2.1. Modeling of Wind Generator System

The total wind power \( P_{wt} \) is given in terms of the total swept area \( A_w \), the efficiency of WT generator and corresponding converter \( \eta_w \) and the output power from wind generator \( P_w \), and can be estimated as follows [63]:

\[
P_{wt} = P_w A_w \eta_w
\]  

\[P_w = \begin{cases} 
P_r & V_r < V < V_{c0} \\ aV^3 - bP_r & V_{ci} < V < V_r \\ 0 & V_{co} < V \text{ and } V < V_r
\end{cases}
\]  

where \( P_r \) and \( V_r \) are the rated power and rated speed of WT, respectively. \( V_{ci} \) and \( V_{co} \) are the cut-in and cut-out wind speeds, respectively. \( a \) and \( b \) are coefficients and given as follows [64,65]:

\[
a = \frac{P_r}{(V_r^3 - V_{ci}^3)} \quad b = \frac{V_{ci}^3}{(V_r^3 - V_{ci}^3)}
\]

2.2. Photovoltaic (PV) Energy Source Modeling

The output power from the PV system \( P_{pv} \) is estimated in terms of PV area \( A_{pv} \), PV system efficiency \( \eta_{pv} \) and tilted solar radiation \( I_T \) as follows [66–68]:

\[
P_{pv} = I_T A_{pv} \eta_{pv}
\]

2.3. Modelling of Pump-Hydro Storage System

In this study, surplus power from the PV, biomass and wind systems are used to drive the pump set to lift water from the lower basin of the waterfall to the upper tank [69]. The power required to operate the pump set is calculated as follows:

\[
P_p = \frac{Q_p \rho g h}{\eta_p}
\]

where \( \eta_p \) is the pumping system efficiency, the water mass density is \( \rho_w \) in (kg/m\(^3\)), the water volume’s flow rate is \( Q_p \) in (m\(^3\)/s), the effective water head is \( h \) in (m), and the acceleration of gravity is \( g \) in (m/s\(^2\)) [70].
2.4. Biomass Generator Modelling

The biomass system is utilized as a backup source during deficit time, in which the output power of the PV and WT is unable to fulfill the demand requirements [71]. The amount of power provided by the gasifier generator is estimated as follows:

$$ P_{bio}(t) = \text{Feedstock}(t) \times HHV \times 27.78 \times 10^{-5} \times \eta_g $$

(6)

where, $27.78 \times 10^{-5}$ is units conversion operator from kJ to kWh. The presented model estimates the $HHV$ as per the biomass' compound creation as follows [72]:

$$ HHV = 3.55C_2 - 232C - 2230H + 51.2C \times H + 131N + 20,600 $$

The gasifier operates at maximum load ratio ($G_{max} = 80\%$) and minimum load ratio ($G_{min} = 30\%$) of its estimated capacity to ensure no operation at lower demands. The output power of the generator ($G_{output}$) can be estimated as follows:

$$ G_{output} = \begin{cases} 0 & P_{bio} < G_{min} \\ G_{max} & P_{bio} > G_{max} \\ P_{bio} & G_{max} < P_{bio} < G_{min} \end{cases} $$

(7)

$E_{bio}$ is the yield yearly energy and can be calculated as follows:

$$ E_{bio} = \sum_{t=0}^{t=8760} N_{gen} G_{output} \times t $$

(8)

2.5. Cost of Energy (COE) Modeling

The COE is used here for cost estimation which is estimated as follows [73,74]:

$$ \text{COE} = \frac{\text{Total present value (TPV)} \times \text{Capital recovery factor (CRF)}}{\text{Annual load demand (ALD)}} $$

(9)

$$ CRF = \frac{r(1+r)^T}{(1+r)^T - 1} $$

(10)

$$ TPV = IC + OMC + RC - PSV $$

(11)

where, $T$ is the lifetime of the system in years, $r$ is net interest rate [75]. $IC$ is initial capital cost and $OMC$ is operation and maintenance cost of the HRES segments, respectively. $OMC$ involved in hydro-pumped storage can be calculated as follows [76]:

$$ OMC = OMC_0 \left( \frac{1+i}{r-i} \right)^T \left( 1 - \left( \frac{1+i}{1+r} \right)^T \right) \quad r \neq i $$

(12)

$$ OMC = OMC_0 \times T \quad r = i $$

(13)

$OMC$ in the case of HRES is the main system cost, as fuel cost free and is written as follows:

$$ C_{o&m} = C_{pv,den}t_{pv} + C_{wt,den}t_{wt} + C_{bio,den}t_{bio} + C_{hydro,den}t_{hydro} + C_{pump,den}t_{pump} $$

(14)

where, $C_{pv,den}$, $C_{wt,den}$, $C_{bio,den}$, $C_{hydro,den}$, $C_{pump,den}$ are $OMC$ of PV, WT, bio generator, hydro, and pumping set; per time, $t_{pv}$, $t_{wt}$, $t_{bio}$, $t_{hydro}$, $t_{pump}$, respectively.

The replacement cost of the HRES elements is $RC$ as follows [77]:

$$ RC = \sum_{j=1}^{N_{rep}} \left( C_{RC} \times C_U \times \left( \frac{1+i}{1+r} \right)^{T_j/(N_{rep}+1)} \right) $$

(15)
where, $C_{RC}$ is the replacement units capacity, $C_{U}$ is the replacement units cost, and $N_{rep}$ is the no. of replacements units during $T$, and $i$ is the replacement units inflation rate [78]. The present value of scrap is $PSV$ which is estimated as follows [79]:

$$PSV = \sum_{j=1}^{N_{rep}+1} SV \left( \frac{1 + i}{1 + r} \right)^{T_j/(N_{rep}+1)}$$  \hspace{1cm} (16)

2.6. Reliability Criteria

The reliability constraint is an important factor in designing and optimization of HRES, which is represented as significant to $LPSP$ and $EEF$ as follows.

2.6.1. Loss of Power Supply Probability ($LPSP$)

$LPSP$ value is limited between 0 and 1, where one means that the load is rejected and 0 indicates that the demand is constantly is fulfilled. $LPSP$ is expressed as follows:

$$LPSP = \frac{\sum_{t=1}^{T} P_{deficit}(t) \cdot \Delta t}{\sum_{t=1}^{T} P_{demand}(t) \cdot \Delta t}, \hspace{1cm} T = 8760 \text{ and } \Delta t = 1. \hspace{1cm} (17)$$

2.6.2. Excess Energy Fraction ($EEF$)

$EEF$ can be estimated as follows:

$$EEF = \frac{\sum_{t=1}^{T} \text{wasted energy}(t) \cdot \Delta t}{\sum_{t=1}^{T} E_{pv}(t) \cdot \Delta t + \sum_{t=1}^{T} E_{wt}(t) \cdot \Delta t + \sum_{t=1}^{T} E_{bio}(t) \cdot \Delta t}, \hspace{1cm} T = 8760 \text{ and } \Delta t = 1. \hspace{1cm} (18)$$

2.7. CO$_2$ Emission and Its Footprints for Society

Emissions adversely affect the environment and human health, so it is necessary to search for a hybrid energy system that reduces these emissions [80]. In this regard, a method for calculating CO$_2$ emission is defined in this section. Moreover, the emissions from the hybrid WT/PV/biomass/pump-hydro storage system and the hybrid WT/PV/biomass/battery storage system are compared in the results section. The estimation of CO$_2$ is performed in significance to the electricity exhaustion per kW, with electricity emission operator of 0.81. The total system emission of CO$_2$ is estimated as follows:

$$\text{CO}_2 \text{ emission per day} = \text{Emission factor} \cdot \text{Use of electricity (kW)} \hspace{1cm} (19)$$

2.8. Inverter Modelling

Alternating current (AC) and direct current (DC) buses were linked through the inverter. In this study the required capacity of the inverter is estimated based on the flow of energy from the DC to AC. The output power ($P_{out}$) is determined in terms of input power ($P_{in}$) and inverter efficiency ($\eta_{inv}$ ~ 95%) as follows [79]:

$$P_{out} = P_{in} \eta_{inv} \hspace{1cm} (20)$$

2.9. Meteorological Data and Load Profile

The proposed algorithms were applied for the system’s size optimization to feed the load demand at a specific site in Saudi Arabia, located at latitude and longitude of 29°49.794′ N and 39°34.362′ E, respectively. Real load data have been utilized to estimate the load profile of the site under study as shown in Figure 2. The hourly metrological data obtained from the National Aeronautics and Space Administration (NASA) database for wind speed, solar radiation and ambient temperature has been utilized. MATLAB software, version R2018b is used to perform the simulation and obtain the results. Figure 3 presents the dataset containing wind speed data per hour, Figure 4 shows the solar insolation data per hour and Figure 5 shows the ambient temperature. The quantity of biomass raw
materials available at the study site was assumed to be one ton/day with 20 dollars/ton. Table 3 shows the financial characteristics of the system elements [81,82]. This table introduces the present cost of each component which includes initial capital cost, operation and maintenance cost and replacement cost within the lifetime of the system in years.

![Figure 2. The load profile of the site under study.](image)

![Figure 3. Hourly wind speed data per year.](image)

![Figure 4. Hourly insolation profile data per year.](image)
3. Energy Balance Operations of the Proposed System

Optimizing a system’s size requires a comprehensive analysis of the HRES elements, load at the selected site, technical and economic characteristics of the hardware components, and an appropriate dispatch strategy. The power management algorithm or dispatch strategy has substantial effects on the optimal sizing of the hybrid system, and consequently, on the post optimization performance indicators. The dispatch of the HRES is determined based on the yield energy of the PV, WT and biomass generators contrast with the accounts of the load demand \( E_D, \text{kWh} \). If the yield energy of the PV, WT and biomass generators is lower than load demand, some water from the upper tank must be released to fulfill the load and vice versa.

3.1. Energy Balance

The energy balance \( E_B, \text{kWh} \) of the system is preceded as follows:

\[
E_B = E_{pv} + E_{wt} + E_{bio} - E_D
\]  

The upper tank is assumed to have a length of \( (a, \text{m}) \), a width of \( (b, \text{m}) \), and a height of \( (h_2, \text{m}) \), then has a cube shape \( (V, \text{m}^3) \) which has a volume of stockpiled water as follows:

\[
V = abh_2
\]  

The water volume set aside in the gracefully at whatever point in the year is resolved as follows:

\[
\text{If } V_{\text{max}} - V_{(t-1)} < V_{\text{min}} \text{Then } V_{(t)} = V_{(t-1)} - Q_{\text{dis}}^{(t)} + Q_{\text{pump}}^{(t)}
\]

\[
V_{(t)} = \min\left(V_{(t-1)}, V_{\text{max}}\right) - Q_{\text{dis}}^{(t)} + Q_{\text{pump}}^{(t)}
\]

The maximum and minimum limits of the water storage in the tank are \( V_{\text{max}} \) and \( V_{\text{min}} \), respectively. During the deficit time of energy, the water capacity which should be released
from the tank to fulfill the load demand is \( Q_{\text{dis}}^{(t)} \). \( Q_{\text{pump}}^{(t)} \) is the pumped water capacity during the surplus time of energy. While executing the energy balance process, the level of water is fluctuating with time, and then the essential level of the pump-hydro system is:

\[
h_{\text{add}} = \frac{V_{(t-1)}}{\text{area}} = \frac{V_{(t-1)}}{ab}
\]

(25)

When \( E_B < 0 \), the system works in the generating mode and the generated energy from the generator-turbine system is estimated as follows:

\[
E_{\text{H}}^{(t)} = \min \left[ \min \left( \frac{V_{(t-1)} - V_T}{3600}; Q_T \right) \eta_T \eta_{WP} (h_{\text{add}} + h_3); |E_B| \right]
\]

(26)

where, \( h_3 \) is the hydropower systems average head, \( Q_T \) is the turbine discharge water speed \( (\text{m}^3/\text{s}) \), \( \eta_{WP} \), and \( \eta_T \) are is the pipeline conveyance and generator efficiency, respectively. Thus, the water discharged volume over that period of time is calculated as follows:

\[
Q_{\text{dis}}^{(t)} = \frac{E_{\text{H}}^{(t)}}{\eta_T \eta_{WP} (h_{\text{add}} + h_3)}
\]

(27)

The deficit energy is determined as follows:

\[
E_{\text{def}}^{(t)} = \left| E_B^{(t)} + E_{\text{H}}^{(t)} \right|
\]

(28)

In case of \( E_B > 0 \), the share of surplus energy is utilized to pump water from lower tank to upper tank, the timely energy provided from PV, biomass and WT utilized by the pump system (pumping speed \( Q_P \, \text{m}^3/\text{s} \) and efficiency \( \eta_P \)) is estimated as follows:

\[
E_{\text{pump}}^{(t)} = \min \left[ \min \left( \frac{V_{\text{max}} - V_{(t-1)}}{3600}; Q_P \right) \eta_P \eta_{WP} (h_{\text{add}} + h_3); |E_B| \right]
\]

(29)

Thus, the timely pumped water capacity to the upper tank is estimated as follows:

\[
Q_{\text{pump}}^{(t)} = \frac{E_{\text{pump}}^{(t)}}{\eta_P \eta_{WP} (h_{\text{add}} + h_3)}
\]

(30)

3.2. Objective Function and Constraints

As previously mentioned, WOA, FF and PSO optimization techniques are applied to obtain the optimal solution of the sizing optimization problem of HRES within MATLAB pseudo codes. In each specific period of time, let it be an hour, as in this paper; the energy balance is performed between the generation elements in the system and the load in order to determine the correct energy flow. Hence, the objective function and constraints of the optimization problem are described as follows [83,84]:

The problem objective function is to minimize the system COE as follows:

\[
\text{Minimize} \quad \text{COE} \left\{ \text{COE}_{\text{pv}}, \text{COE}_{\text{wt}}, \text{COE}_{\text{hydo-pump}}, \text{COE}_{\text{bio}} \right\}
\]

(31)

The problem constraints are expressed as follows:

\[
0 \leq \text{LPSP} \leq \text{LPSP}_{\text{max}}
\]

(32)

\[
0 \leq \text{EEF} \leq \text{EEF}_{\text{max}}
\]

(33)

The simulation is performed for \( \text{LPSP}_{\text{max}} \) of 3%, and \( \text{EEF}_{\text{min}} \) of 14%.
4. Optimization Algorithms

As mentioned above, three different optimization algorithms have been utilized in this paper to carry out the sizing optimization process using MATLAB, where the following sections detail their operation:

4.1. Whale Optimization Algorithm (WOA)

The WOA is a novel nature-inspired metaheuristic optimization algorithm which invented by Mirjalili et al. [85]. Traditionally, WOA composed of encircling prey, searching for prey, bubble-net attacking model. The parameters of WOA are \((a_s)\) coefficient which linearly minimized from 2–0 in each iteration, \((r_s)\) coefficient is an arbitrary vector in \((0, 1)\) and \((A_s)\) coefficient within \((-1, 1)\). The pseudo-code of WOA is presented in Algorithm 1.

Algorithm 1 WOA

Whale population initialization \(X_s\)

1: Fitness estimation for all search agents:
2: \(X_s\) is optimal search agent
3: while \(t_i < \text{max-it}\)
4: for all search agent
5: Update \(a_s, A_s, d\) and \(p_s\)
6: if \(p_s < 0.5\) and \(A_s < 1\)
7: Update present search agent location
8: if \(A_s \geq 1\)
9: Choose an arbitrary search agent
10: end if
11: else if \(p_s \geq 0.5\)
12: Verify if any search agent exceeds the search space and add it
13: Fitness estimation for all search agents
14: Update \(X_s\) if other optimal solution exists
15: \(t_i = t_i + 1\)
16: end while
17: Return \(X_s\)

4.2. Firefly (FF) Algorithm

In particular, FF is developed using the social manners of fireflies and also a short and rhythmic light is emitted to alert and attract the new ones [86]. Light intensity \(\eta_u\) and light absorption coefficient \(k\) are the main FF parameters which have been described in detail in [87]. The pseudo-code of FF is shown in Algorithm 2.

Algorithm 2 FF

Whale population initialization \(X_s\)

1: Objective function \(f(x_a)\)
2: Generate FF primary population \(x_a, a=1,2,3, d\)
3: Light intensity \(\eta_u\) is executed via \(f(x_a)\)
4: Describe the light absorption coefficient, \(k\)
5: while \(t_i < \text{max-it}\)
6: for \(a = 1: d\) entire \(d\) FF
7: for \(b = 1: a\) entire \(d\) FF
8: if \(k_b \geq k_a\)
9: Move \(a^{th}\) firefly towards \(b\) in \(d\)-dimension by Levy flights
10: End if
11: Determine new solution and update \(\eta_u\)
12: End for \(b\)
13: End for \(a\)
14: Evaluate present best and rank fireflies
15: End while
16: Post-process visualization and result
4.3. Particle Swarm Optimization (PSO)

The PSO algorithm was first used with an initiated arbitrarily population that updates its positions using velocity vector. The latter consolidated the most appropriate global and individual positions. The contrast among the two positions is the global best resolution that demonstrates the best fitness value shown by individual particles. The parameters of PSO are, inertia weight \( w = 0.95 \), inertia weight damping ratio \( w_{\text{damp}} = 0.9 \), population size \( n = 100 \), personal learning coefficient \( c_1 = 2.01 \) and global learning coefficient \( c_2 = 1.92 \) [88–92]. Algorithm 3 shows the pseudo-code of PSO.

**Algorithm 3 PSO**

Function: PSO  
Input: Algorithm parameters, \( K_{\text{clusters}} \), Data\_count  
Output: S\_bestClustering  
Initialize a Population of particles with random positions and velocities, throught the input space  
**While ~StopCondition () do**  
**For each particle i do**  
\[ f_p = f(x_i) \]  
if \( f_p > \text{pbest} \) then  
\( \text{pbest}_i = f_p \)  
\( p_i = x_i \)  
End  
\[ g = \{ g | f(p_t) = \max (f(p_x), k \in N(x_i)) \} \]  
Update Velocity  
Update velocity  
End  
End

5. Simulation Results and Discussion

The qualification ascending from the lower and upper tanks is used in this assessment as \( h_3 = 100 \) m and the extra head is \( h_2 = 5 \) m. The upper tank has \( a = 600 \) m, length and \( b = 200 \) m, width. The pump and generator-turbine efficiencies are set at 90% and 85%, respectively. The greatest limit of the upper tank adds up to 375 MWh, which is comparable to 5 h of average load demand. The balance of energy over the period of study is shown in Figure 6.

![Figure 6. Energy balance over one year of study.](image-url)
In Figure 7, it is indicated that the majority of the total electricity demand (curve line) is met by power generated by PV and WT (85%) and the rest by the biomass generator (15%), with the pump-hydro system providing similar power patterns throughout the year.

**Figure 7.** Energy generations from different units of PV/WT/biomass/pump-hydro system.

Figure 8 presents the time series data for power input to the pump (Figure 8a) by excess energy generation from the PV, wind, biomass and power output from the water turbine while meeting the load demand (Figure 8b).

**Figure 8.** Cont.
Figure 8 presents the time series data for power input to the pump (Figure 8a) by excess energy generation from the PV, wind, biomass and power output from the water turbine while meeting the load demand (Figure 8b).

As mentioned before, this study was carried out using the hourly metrological data for one complete year, 8760 h. However, for a better understanding of the proposed approach; Figure 9 shows a certain 24 h simulation. This figure shows the power balance of the load demand ($P_L$), the total generated power ($P_{wt} + P_{pv} + P_{bio}$), and the pump power ($P_{pump}$) on a certain day.

The obtained optimal solution outcomes from the proposed optimization algorithms for the pump-hydro vs. battery-based hybrid systems are presented in Table 4. From Table 4, it can be seen that the COE of the PV/biomass/WT/pump-hydro hybrid system is lower than with PV/biomass/WT/battery hybrid system. Moreover, the global minimum has been obtained using the WOA algorithm.
Table 4. Summarized results for the pump-hydro vs. battery-based hybrid systems via the PSO, WOA and FF algorithms.

<table>
<thead>
<tr>
<th></th>
<th>PV/Biomass/WT/Pump-Hydro</th>
<th>PV/Biomass/WT/Battery</th>
</tr>
</thead>
<tbody>
<tr>
<td>LPSP (%)</td>
<td>1.92%</td>
<td>PSO 1.90%</td>
</tr>
<tr>
<td>F_{dump} (%)</td>
<td>5.94%</td>
<td>FF 10.51%</td>
</tr>
<tr>
<td>COE ($/kW)</td>
<td>0.215</td>
<td>PSO 0.225</td>
</tr>
<tr>
<td>CNPC ($)</td>
<td>491,957</td>
<td>FF 590,137</td>
</tr>
<tr>
<td>N_{PV}</td>
<td>11</td>
<td>PSO 12</td>
</tr>
<tr>
<td>N_{gen}</td>
<td>4</td>
<td>FF 3</td>
</tr>
<tr>
<td>N_{WT}</td>
<td>1</td>
<td>PSO 1</td>
</tr>
<tr>
<td>N_{bat}</td>
<td></td>
<td>FF 15</td>
</tr>
<tr>
<td>Pump-hydro</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

The iterations are numbered until the optimal solutions are obtained and the time consumed is considered as an important criterion for selecting any optimization algorithm. Figure 10 shows the convergence of PSO, WOA, and FF until obtain the optimal solution. As shown in Figure 10, WOA has realized the optimum solution faster than PSO and FF algorithms. Table 5 presents various indexes for statistical analysis to help in stability validation of WOA performance.

![Figure 10. The convergence of the proposed optimization algorithms.](image)

Table 5. Statistical indexes for evaluating performance of the WOA algorithm.

<table>
<thead>
<tr>
<th>Index</th>
<th>Formula</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Relative error (RE)</td>
<td>( \frac{\sum_{i=1}^{n} (F_i - F_{\text{run}})}{F_{\text{run}}} )</td>
<td>0.022</td>
</tr>
<tr>
<td>Mean absolute error (MAN)</td>
<td>( \frac{\sum_{i=1}^{n}</td>
<td>F_i - F_{\text{run}}</td>
</tr>
<tr>
<td>Root mean square error (RMSE)</td>
<td>( \sqrt{\frac{\sum_{i=1}^{n} (F_i - F_{\text{run}})^2}{n}} )</td>
<td>0.023</td>
</tr>
<tr>
<td>Standard deviation (SD)</td>
<td>( \sqrt{\frac{\sum_{i=1}^{n} (F_i - \bar{F})^2}{n}} )</td>
<td>2.103%</td>
</tr>
<tr>
<td>Efficiency (EF)</td>
<td>( \frac{F_{\text{run}}}{F_{\text{gen}}} )</td>
<td>99.87%</td>
</tr>
</tbody>
</table>
The outcomes from Table 5 show that the WOA algorithm has an adequate root mean square error (RMSE). Besides, the SD approves that the proposed model-based WOA has palatable soundness. Table 6 shows the sensitivity analysis outcomes after several iterations of WOA algorithm. From Table 6, it is unmistakable that the proposed model is monetarily and ecologically achievable in correlation with other traditional models.

### Table 6. Sensitivity analysis outcomes of WOA.

<table>
<thead>
<tr>
<th>WOA Algorithm</th>
<th>Global</th>
<th>Best</th>
<th>Worst</th>
<th>Average</th>
<th>Median</th>
<th>SD</th>
<th>Suc. Rate</th>
<th>Average RE</th>
<th>MAV</th>
<th>RMSE</th>
<th>EF</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>2.7133</td>
<td>2.7133</td>
<td>2.709</td>
<td>2.716962</td>
<td>2.733</td>
<td>3.502</td>
<td>99%</td>
<td>0.16411</td>
<td>1.0396</td>
<td>3.0178</td>
<td>98.988</td>
</tr>
</tbody>
</table>

The environmental emissions from the hybrid WT/PV/biomass/pump-hydro storage system are substantially lower than with the hybrid WT/PV/biomass/battery storage system. It is noticeable that the hybrid WT/PV/biomass/pump-hydro storage system generates fewer CO$_2$ emissions (18,226 kg/year) than the hybrid WT/PV/biomass/battery storage system (24,125 kg/year). These results confirm the economic viability and environmental safety of using hybrid WT/PV/biomass/pump-hydro storage systems over hybrid WT/PV/biomass/battery storage systems.

### 6. Conclusions

In this study, a standalone hybrid wind turbine (WT)/photovoltaic (PV)/biomass/pump-hydro-storage energy system which satisfies the load demand of a certain remote community in Saudi Arabia is analyzed. The proposed system is compared with a standalone hybrid PV/WT/biomass/battery-storage energy system, in terms of costs, emissions and performance indicators. The operation of the proposed scheme depends on the hourly meteorological data of wind speed, radiation and temperature. PSO, WOA, and FF algorithm-based MATLAB have been utilized to minimize the system costs while fulfilling the load demand. The proposed computation ensured good execution, especially with the very large number of components. Also, the global minimum estimation of the objective function has been obtained quickly and in a concise range stood out from other optimization algorithms. The analyses presented in this research indicate the following conclusions:

- The PV/WT/biomass/pump-hydro-based optimized system is a profitable and environmentally viable option for satisfying electricity requirements compared to a PV/WT/biomass/battery storage-based optimized system.
- With growing electricity requirements, the proposed system could be implemented in isolated locations around the world as well.
- The comparison result showed that the WOA algorithm presents the best convergence among the studied algorithms until get the optimal solution.
- The feasibility study presented in this research can be used as a guideline for the installation of PV/WT/biomass/pump-hydro-based hybrid systems in the areas where the geographical location is favorable for the pump-hydro storage facility.
- The hybrid WT/PV/biomass/pump-hydro storage system generates fewer CO$_2$ emissions than the hybrid WT/PV/biomass/battery storage system.
- The proposed hybrid PV/WT/biomass/pump-hydro-based hybrid system would be ideal for a small community, health center, schools, small industry, and markets where grid connection is too expensive or practically impossible.
- The financial attractiveness and environmental sustainability of the proposed system are also aligned with the global energy economy and clean energy targets. These findings are likely to encourage local decision-makers and other stakeholders to grant and implement such projects in order to ensure an uninterrupted electricity supply for rural and often neglected communities.
Author Contributions: All authors contributed to the conception and design of the work, approved the final version of the manuscript and agreed to be accountable for all aspects of the work. All authors have read and agreed to the published version of the manuscript.

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