Abstract: High frequency surface wave radar (HFSWR) plays an important role in marine surveillance on account of its ability to provide wide-range early warning detection. However, vessel target track breakages are common in large-scale marine monitoring, which limits the continuous tracking ability of HFSWR. The following are the possible reasons for track fracture: highly maneuverable vessels, dense channels, target occlusion, strong clutter/interference, long sampling intervals, and low detection probabilities. To solve this problem, we propose a long-term continuous tracking method for multiple targets with stereoscopic HFSWR based on an interacting multiple model extended Kalman filter (IMMEKF) combined with an extreme learning machine (ELM). When the trajectory obtained by IMMEKF breaks, a new section of the track will start on the basis of the observation data. For multiple-target tracking, a number of broken tracks can be obtained by IMMEKF tracking. Then the ELM classifies the segments from the same vessel by extracting different features including average velocity, average curvature, ratio of the arc length to the chord length, and wavelet coefficient. Both the simulation and the field experiment results validate the method presented here, showing that this method can achieve long-term continuous tracking for multiple vessels, with an average correct track segment association rate of over 91.2%, which is better than the tracking performance of conventional algorithms, especially when the vessels are in dense channels and strong clutter/interference area.

Keywords: HFSWR; target tracking; interacting multiple model; extended Kalman filter; track association; extreme learning machine
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degree of association, and calculates the membership value of two tracks to determine whether the
track is associated or not. Bar-Shalom et al. [5] applied the fixed distance metric in the weighted
statistical method. Yeom et al. [6] presented a track segment association algorithm on the basis of
discrete optimization. Zhang et al. [7] stitched broken tracks by using an interacting multiple model
(IMM) estimator. Aybars et al. [8] calculated an association cost in order to associate tracks on
the basis of Mahalanobis distance. Zhu et al. [9] proposed a mixed integer nonlinear programming
(MINLP) model in the maximum likelihood rule. Ashraf et al. [10] presented a fuzzy correlation
approach on the basis of the fuzzy clustering means algorithm. Stubberud et al. [11] proposed a
straightforward fuzzy-logic-based association method based on the chi 2 metric. Shao et al. [12]
used fuzzy k-nearest neighbors and fuzzy C-means clustering to achieve track segment association.
Hong et al. [13] presented a track segment association algorithm by calculating the fuzzy membership
matrix and clustering methodology. All of these methods compare the distances of track segments
point by point without considering the relevance of the track segments’ features, which can cause
invalid track association when a vessel is in a complex situation, such as in a dense channel or strong
clutter interference region.

These track segment association (TSA) algorithms are feasible in theory, however, the backward
prediction error of the present track is often large due to the noise of the system and measurement,
which results in poor accuracy of association. Even worse, the performance of TSA algorithms drops
suddenly due to track crossing and bifurcation when affected by surrounding large vessels or strong
clutters. In order to solve the track breakage problem effectively and track targets steadily and
continuously, we consider combining the conventional tracking algorithm with the machine learning
method, which can achieve track segment association through studying the training dataset. The back
propagation (BP) network has a strong nonlinear mapping ability, although it easily becomes trapped
in local minimums during its training, which limits the stability and accuracy of classification [14,15].
Although the support vector machine (SVM) is able to avoid a local optimal solution, it has some
shortcomings, such as training slowly and having a low efficiency [16,17]. The extreme learning
machine (ELM) is a single hidden layer neural network with low computational complexity and good
general performance [18]. Compared with the traditional neural network, ELM can randomly initialize
the input weight and offset without adjusting during the training process, which make it simple and
fast with the guarantee of accuracy [19]. Moreover, the ELM is more suited to handle small sample
classification problems than deep learning [20,21].

We propose a long-term continuous tracking method based on an interacting multiple model
extended Kalman filter (IMMEKF) combined with an extreme learning machine (ELM). When using the
IMMEKF tracking method alone, we can determine only the intermittent track segments. Long-term
continuous tracking is achieved when the ELM is combined with this method. In order to sufficiently
reflect the track segment features, we associate the tracks on the basis of features extracted from track
segments rather than comparing the distances of track segments point by point. Moreover, we present
a new scheme to solve the problem of track segment association using an ELM network. The method
decides whether the present track segment is associated with the former tracks through the ELM
network, whose feature vectors in the training set are extracted from the track segments obtained by
the IMMEKF. Hence, the long-term continuous tracking of multiple targets can be achieved via the
cooperation between the IMMEKF and the ELM. Both the simulation and the field experiment results
show that the proposed method has better tracking performance than conventional algorithms.

This paper is organized as follows. In Section 2, we briefly introduce the stereoscopic HFSWR
station and the system model of the vessel target. In Section 3, we propose the long-term continuous
tracking method with stereoscopic HFSWR based on IMMEKF combined with ELM. Furthermore,
the simulation and the field data experiment results are presented to show the effectiveness of the
proposed method in Section 4. In Section 5, the results are discussed, and areas for future potential
research are considered. Finally, conclusions are drawn in Section 6.
2. System Model

In this paper, we examine the vessel target tracking for stereoscopic HFSWR [22], which is shown in Figure 1. We consider the T-R/R mode, with one transmitting station and two receiving radar stations working independently along the coast. For this mode, the target position is determined through geometric relation without measuring the target angle. The motion characteristics of the target, such as the radial range \(d\) and the radial velocity \(v\), can be obtained. The distance between the two receiving radar stations is set as \(2a\).

\[
\begin{align*}
X(k) &= [x(k), v_x(k), y(k), v_y(k)]^T \\
\end{align*}
\]

where \(x(k)\) and \(y(k)\) describe the position of the vessel, and \(v_x(k)\) and \(v_y(k)\) represent the vessel velocity along the \(x\) and \(y\) direction, respectively. For the constant velocity (CV), constant acceleration (CA), and constant turn (CT) model [23], the state equation can easily be obtained:

\[
X(k + 1) = A(k)X(k) + B(k)W(k)
\]

The observation vector is described as

\[
Z(k) = [d_1(k), v_1(k), d_2(k), v_2(k)]^T
\]

where \(d_1(k)\) and \(d_2(k)\) are the radial range, and \(v_1(k)\) and \(v_2(k)\) are the radial velocity. The measurement model is

\[
Z(k) = H(X(k)) + V(k)
\]

where the observation noise \(V(k)\) is zero mean Gaussian white noise. Based on the geometrical relationship between the state and the measurement, the nonlinear measurement function \(H(X(k))\) can be determined accordingly:

\[
H(X(k)) = \begin{bmatrix}
\frac{x-a}{\sqrt{(x-a)^2+y^2}} & 0 & 0 \\
\frac{y}{\sqrt{v_y}} & \frac{x-a}{\sqrt{(x-a)^2+y^2}} & 0 \\
\frac{(x-a)^2+y^2}{\sqrt{v_y}} & \frac{y}{\sqrt{v_y}} & \frac{x-a}{\sqrt{(x-a)^2+y^2}} \\
\end{bmatrix}
\]

Figure 1. Schematic diagram of the stereoscopic High frequency surface wave radar (HFSWR) system.

At time point \(k\), the state is described as

\[
X(1) = [x(1), v_x(1), y(1), v_y(1)]^T
\]

where \(v_x(1)\) and \(v_y(1)\) are the vessel velocity along the \(x\) and \(y\) direction, respectively. For the constant velocity (CV), constant acceleration (CA), and constant turn (CT) model [23], the state equation can easily be obtained:

\[
X(k + 1) = A(k)X(k) + B(k)W(k)
\]

The observation vector is described as

\[
Z(k) = [d_1(k), v_1(k), d_2(k), v_2(k)]^T
\]

where \(d_1(k)\) and \(d_2(k)\) are the radial range, and \(v_1(k)\) and \(v_2(k)\) are the radial velocity. The measurement model is

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H(X(k)) = \begin{bmatrix}
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\frac{y}{\sqrt{v_y}} & \frac{x-a}{\sqrt{(x-a)^2+y^2}} & 0 \\
\frac{(x-a)^2+y^2}{\sqrt{v_y}} & \frac{y}{\sqrt{v_y}} & \frac{x-a}{\sqrt{(x-a)^2+y^2}} \\
\end{bmatrix}
\]
The process of the target fusion and tracking algorithm based on IMM is shown in Figure 2, and the specific details of the algorithm are presented below.

![Flow graph of interacting multiple model extended Kalman filter (IMMEKF).](image)

**Figure 2.** Flow graph of interacting multiple model extended Kalman filter (IMMEKF).

### 2.1. Interacting Input

\[
\bar{c}_i = \sum_{j=1}^{m} u_j(k)p_{ij} \sum_{j=1}^{m} p_{ij} = 1, \ i, j = 1, \cdots, m
\]

\[
u_{ij}(k) = \frac{u_j(k)p_{ij}}{\bar{c}_i}
\]

\[
\hat{X}_0(k) = \sum_{j=1}^{m} u_{ij}(k)\hat{X}_j(k)
\]

\[
P_0(k) = \sum_{j=1}^{m} u_{ij}(k)\left\{P_j(k) + [\hat{X}_j(k) - \hat{X}_0(k)](\hat{X}_j(k) - \hat{X}_0(k))^T\right\}
\]

where \(\bar{c}_i\) is the normalizing constant, \(u\) is the model probability, \(p\) is the model transition probability, \(m\) is the number of the motion model, \(\hat{X}\) is the state estimation, and \(P\) is the residual covariance matrix variance.

### 2.2. Model Filtering

\[
\hat{X}_1(k+1|k) = H_i(k+1|k)\hat{X}_0(k)
\]

\[
P_j(k+1|k) = A_i(k+1|k)P_0(k)A_i^T(k+1|k) + B_i(k)Q(k)B_i^T(k)
\]

\[
K_i(k+1) = P_i(k+1|k)H_i^T(k+1)\left[H_i(k+1)P_i(k+1|k)H_i^T(k+1) + R_i(k+1)\right]^{-1}
\]
\[ P_t(k+1) = [I - K_t(k+1)H_t(k+1)]P_t(k+1) \]  
\[ \hat{X}_t(k+1) = \hat{X}_t(k+1|k) + K_t(k+1) [Z_t(k+1) - H_t(k+1)\hat{X}_t(k+1|k)] \]

where \( Q(k) \) is the covariance of the process noise and \( R(k) \) is the covariance of the observation noise.

### 2.3. Updating Model Probability

\[ u_t(k+1) = \frac{\Lambda_t(k+1)\hat{e}_t(k+1)}{\sum_{i=1}^{m} \hat{e}_i(k+1)} \]

\[ \Lambda_t(k+1) = \frac{\exp\left\{ -\frac{1}{2}(v_t(k+1))^T S_t(k+1)^{-1}v_t(k+1) \right\}}{\sqrt{2\pi \det(S_t(k+1))}} \]

where \( v \) is measurement residuals and \( S \) is the residual covariance matrix.

### 2.4. Estimation Fusion

\[ \hat{X}_t(k+1) = \sum_{i=1}^{m} X_t(k+1)u_t(k+1) \]

\[ P(k+1) = \sum_{i=1}^{m} u_t(k+1) \left\{ P_t(k+1) + [X_t(k+1) - \hat{X}(k+1)][\hat{X}(k+1) - \hat{X}(k+1)]^T \right\} \]

### 3. Long-Term Continuous Tracking Method

For conventional tracking methods of HFSWR, the trajectory of vessel targets often breaks in segments due to interferences from other vessels, strong clutters, instant maneuvering, etc. In this section, we present a long-term continuous tracking method on the basis of the ELM network by extracting effective features to associate the track segments of the same vessel.

#### 3.1. ELM Model

As is shown in Figure 3, the extreme learning machine (ELM) is a single hidden layer neural network with low computational complexity and good general performance [24,25]. Compared with the traditional neural network, ELM can randomly initialize the input weight and offset without adjusting during the training process [26], which make it simple and fast with the guarantee of accuracy [27].

![Extreme learning machine (ELM) network model.](image)

**Figure 3.** Extreme learning machine (ELM) network model.
Supposing there are $N$ arbitrary data, the ELM network with $M$ hidden layer nodes can be expressed as follows:

$$\sum_{j=1}^{M} \beta_j g(w_j \cdot x_i + b_j) = y_i (i = 1, 2, \cdots, N)$$  \hspace{1cm} (19)

where $g(x)$ is the activation function, $w_j$ is the input weight, $\beta_j$ is the output weight, and $b_j$ is the bias of the $i$th node.

The aim of neural network learning is minimizing the output error, which can be expressed as follows:

$$E(w, b, \beta) = \sum_{i=1}^{N} \|y_i - t_i\|$$  \hspace{1cm} (20)

$$\min_{w, b, \beta} E(w, b, \beta) = \min_{w, b, \beta} \|H(w_1, \cdots, w_M; b_1, \cdots, b_M; x_1, \cdots, x_N)\beta - T\|$$  \hspace{1cm} (21)

$$H\beta = T$$  \hspace{1cm} (22)

$$\hat{\beta} = H^+ T$$  \hspace{1cm} (23)

where $H$ is the output of the hidden layer, $\beta$ is the output weight, $T$ is the output of mathematical expectation, and $H^+$ is the Moore-Penrose generalized inverse of matrix $H$.

### 3.2. Feature Extraction

In order to sufficiently reflect the track segment features, we associate the tracks based on features extracted from track segments rather than comparing the distances of track segments point by point. To improve the tracking performance in a complex environment, more features should be extracted for track association. In this paper, we selected the average velocity, average curvature, ratio of the arc length to the chord length, and the wavelet coefficient as the feature vectors to train and test the ELM.

#### 3.2.1. Average Velocity ($\bar{v}$)

Velocity as an inherent property varying with vessels can be reflected in the track segments, and thus we select the average velocity of the track segment as an important characteristic variable, which is defined as follows:

$$\bar{v} = \frac{\sum_{i=0}^{n} \sqrt{v_{xi}^2 + v_{yi}^2}}{n}$$  \hspace{1cm} (24)

where $v_{xi}$ is the velocity component of the vessel along the $x$ axis, and $v_{yi}$ is the velocity component of the vessel along the $y$ axis.

#### 3.2.2. Average Curvature ($\bar{k}$)

Curvature is the rate of change of the angle between the tangent of a point on the curve and the $x$ axis relative to the arc length, which is defined by differentiation to indicate the degree of deviation of the curve from a straight line. The average curvature represents the deviation and regression degree of the course, which reflects the course correction ability varying with vessels under the interference of wind and waves. The average curvature ($\bar{k}$) is defined as follows:

$$\bar{k} = \frac{\sum_{i=0}^{n} \frac{\|l'_i\|^2}{[1 + (l'_i)^2]^{3/2}}}{n}$$  \hspace{1cm} (25)

where $l'_i$ is the first derivative of the arc length, and $l''_i$ is the second derivative of the arc length.
3.2.3. Ratio of the Arc Length to the Chord Length ($R$)

The arc length is the invariant of smooth curved motion, and the chord length has similar invariance. The ratio of the arc length to the chord length can roughly reflect the deviation and regression degree of course varying with vessels under the interference of wind and waves, which is similar to the average curvature. The ratio of the arc length to the chord length is defined as follows:

$$R = \frac{l}{d}$$  (26)

where $d$ is the chord length, and $l$ is the arc length.

3.2.4. Wavelet Coefficient $L$

Wavelet transform is a multi-resolution signal analysis method. It assumes that the measurement sequence is a non-stationary sequence $x(n)$ with polynomial trend. After a wavelet transformation, $x(n)$ can be reconstructed as

$$x(n) = \sum_{k} h(2n - k)x(k) + \sum_{k} g(2n - k)x(k)$$  (27)

where $h$ is the high frequency coefficient reflecting the overall situation of the track and $g$ is the low frequency coefficient reflecting the change of the target movement. In the frequency domain, the trend of the signal is represented by the low frequency part of the signal, which is represented by the low frequency coefficient in a wavelet analysis. The low frequency coefficient of a two-scale wavelet transformation based on the Haar function is taken as a track feature, which can represent the trend of the track segment.

3.3. Procedure of the Tracking Method Based on an IMMEKF Combined with an ELM

The procedure of the target tracking method based on an IMMEKF combined with an ELM is shown in Figure 4. Track segments are obtained by the IMMEKF when tracking the maneuvering target using the stereoscopic HFSWR data, and simultaneously, the ELM decides whether the newly obtained track segment associates with the former segment via feature classification. In this way, the method can achieve long-term continuous tracking of the vessel target.

![Flow graph of the continuous tracking method based on IMMEKF combined with ELM.](image-url)

Figure 4. Flow graph of the continuous tracking method based on IMMEKF combined with ELM.

4. Experiment Results

4.1. Simulation Experiment

We assume that the radar monitoring area is approximately 20 km to 38 km in the x axis and approximately 20 km to 32 km in the y axis, where four vessels maneuvering with multiple models are simulated with MATLAB (MathWorks, Natick, MA, USA). For the conventional tracking method [13], the vessel track breaks into segments, as shown in Figure 5a. Combined with a trained ELM network, the proposed method realizes correct track segment association. As is shown in Figure 5b, different types of track segments are colored according to the classification results obtained by the ELM.
In order to verify the rationality and superiority of the proposed method, we carried out simulations on the basis of different combinations of features and different machine learning methods. To evaluate the association performance, the correct association probability \( R_t \), the error association probability \( R_f \) and the missing association probability \( R_n \) are defined as follows:

\[
R_t = \frac{n_t}{n} \tag{28}
\]
\[
R_f = \frac{n_f}{n} \tag{29}
\]
\[
R_n = \frac{n_n}{n} \tag{30}
\]

where \( n \) represents the total number of track segments in the experiment, \( n_t \) represents the number of correctly associated track segments, \( n_f \) represents the number of incorrectly associated track segments, and \( n_n \) represents the number of missed track segments.

### 4.1.1. Simulations Based on Different Combinations of Features

Among the four proposed features, \( \bar{v} \) is an inherent property varying with vessels and \( L \) reflects the overall movement trend of the track segment, while both \( \bar{k} \) and \( R \) reflect the degree of deviation and regression of vessels under the interference of wind and waves, respectively. We carried out simulations on the basis of different combinations of features. As is shown in Table 1, \( \bar{k} \) is more effective than \( R \) in characterizing the features of track segments, and the correct association probability reaches the highest when they work together, which illustrates that \( \bar{k} \) and \( R \) can reinforce one another in reflecting the degree of deviation and regression of vessels. Therefore, the proposed method in this paper selects all four of these features to work together for better association performance.

<table>
<thead>
<tr>
<th>( \bar{v},L,\bar{k} )</th>
<th>( \bar{v},L,R )</th>
<th>( \bar{v},L,\bar{k},R )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( R_t )</td>
<td>92.5</td>
<td>89.3</td>
</tr>
<tr>
<td>( R_f )</td>
<td>6.7</td>
<td>9.8</td>
</tr>
<tr>
<td>( R_n )</td>
<td>0.8</td>
<td>0.9</td>
</tr>
</tbody>
</table>

### 4.1.2. Simulations Based on Different Machine Learning Methods

We carried out simulations based on different machine learning methods to show the performance of an ELM. As is shown in Table 2, the ELM has the fastest speed and the highest accuracy compared
with the back propagation (BP) network and the SVM. Moreover, the ELM is more efficient than the BP and the SVM. Hence, we selected the ELM to combine with the IMMEKF in the proposed method in this paper to achieve long-term continuous tracking of multiple targets.

Table 2. Statistical results of track segment association based on different machine learning methods. BP: back propagation; SVM: support vector machine.

<table>
<thead>
<tr>
<th></th>
<th>ELM</th>
<th>BP</th>
<th>SVM</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_t$ (%)</td>
<td>94.7</td>
<td>82.3</td>
<td>89.7</td>
</tr>
<tr>
<td>$R_f$ (%)</td>
<td>4.6</td>
<td>16.8</td>
<td>9.5</td>
</tr>
<tr>
<td>$R_n$ (%)</td>
<td>0.7</td>
<td>0.9</td>
<td>0.8</td>
</tr>
<tr>
<td>Time (ms)</td>
<td>684</td>
<td>5103</td>
<td>1568</td>
</tr>
</tbody>
</table>

4.1.3. Comparison between the Conventional TSA Algorithm and the Proposed Method

The above simulations show that the extracted features of the track segment based on an IMMEKF can adequately reflect the vessel’s attributes and motion characteristics; even better, the ELM can effectively learn the features of different track segments and accurately classify them. Furthermore, we carried out simulations comparing the conventional TSA algorithm and the proposed method. As is shown in Table 3, the proposed method has better performance than the conventional TSA algorithm.

Table 3. Statistical results of track segment association based on simulation (%). TSA: track segment association.

<table>
<thead>
<tr>
<th></th>
<th>Conventional TSA Algorithm</th>
<th>Proposed Method</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_t$</td>
<td>76.5</td>
<td>94.7</td>
</tr>
<tr>
<td>$R_f$</td>
<td>12.1</td>
<td>4.6</td>
</tr>
<tr>
<td>$R_n$</td>
<td>11.4</td>
<td>0.7</td>
</tr>
</tbody>
</table>

4.2. Field Experiment

To compare the performance of the conventional TSA algorithm and the proposed method, we conducted extensive experiments basing the field data collected by a stereoscopic HFSWR system located on the northern shore of Weihai, China, on 21 July 2019. Data from an AIS (automatic identification system) is defined as the ground truth, which includes the number plates of the vessels of each track segment.

We selected the track as an example in Figure 6, where track segments x and y, marked with “*” and “+”, respectively, are the tracks of vessel A, and segment z, marked with “◦”, is the track of vessel B. Although x is close to z, the ELM can determine that the track trend and characteristics between x and y are consistent, which are from the same target. The proposed method associated the track segment correctly in Figure 6c, yet the conventional TSA algorithm associated the track incorrectly in Figure 6b.

On the basis of 60 track segments obtained from field data, we calculated the average correct association probability, average error association probability, and average missing association probability of the two methods. The statistical results are shown in Table 4. Compared with the conventional TSA algorithm, the average correct association probability of the proposed method was increased by 21.7%, and the average error association probability and average missing association probability of the proposed method were reduced by 5.0% and 16.7%, respectively. Hence, the method proposed in this paper can effectively solve the problem of track segment association, which can effectively overcome the track breaking caused by strong sea clutter interference and interference from other vessels near dense channels, and realize the long-term continuous tracking of a specific vessel target with higher accuracy and stronger adaptability.
the track segment correctly in Figure 6c, yet the conventional TSA algorithm associated the track incorrectly in Figure 6b.

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Figure 6. Comparison of track association results: (a) track segments from field data; (b) association results of the conventional TSA algorithm; (c) association results of the proposed method.
Table 4. Statistical results of track segment association based on radar data (%).

<table>
<thead>
<tr>
<th></th>
<th>Conventional TSA Algorithm</th>
<th>Proposed Method</th>
</tr>
</thead>
<tbody>
<tr>
<td>(R_t)</td>
<td>69.5</td>
<td>91.2</td>
</tr>
<tr>
<td>(R_f)</td>
<td>13.1</td>
<td>8.1</td>
</tr>
<tr>
<td>(R_n)</td>
<td>17.4</td>
<td>0.7</td>
</tr>
</tbody>
</table>

5. Discussion

In Section 4.1.1, simulations were carried out on the basis of different combinations of features, which illustrates that the association performance is the best when the four extracted features of the tracks work together; in Section 4.1.2, we gave a comparison among different machine learning methods, which shows that the ELM had the fastest speed and the highest accuracy compared with the BP network and the SVM. Hence, we selected the ELM and all four of those features working together in the proposed method to realize track segment association. In Section 4.2, the proposed method was verified to have a better performance compared with the conventional TSA algorithm on the basis of radar data.

There is no doubt that the method proposed in this paper can effectively improve the track continuity of the target and realize the long-term continuous tracking of a specific vessel target. Moreover, the new method is easy for engineering implementation due to its generality, simple structure, reduced calculations, high learning speed, and high accuracy. In future research, we will consider further mining features of track segments and improving the network structure of the ELM to achieve better association accuracy.

6. Conclusions

We proposed a long-term continuous tracking method for vessel targets with stereoscopic HFSWR based on an IMMEKF combined with an ELM to solve the problem of trajectory breaking in large-scale marine surveillance. The IMMEKF is applied for the vessel target tracking, meanwhile the ELM network is combined to judge whether the present track is associated with the former track segments. For fully embodying the characteristics of track segments, we selected the average velocity, average curvature, ratio of the arc length to the chord length, and the wavelet coefficient as the feature vectors to train and test the ELM. The tracking algorithm IMMEKF and the track segments associating scheme of the ELM work simultaneously and iteratively. Both the simulation and the field experiment results showed that the proposed method has better tracking performance than the conventional algorithms, with an average correct track segment association rate of over 91.2%. Further, field experiment data from stereoscopic onshore HFSWR located in Weihai showed that the ELM-based track association method had higher accuracy, with lower error and missing association probability due to effective features extracted from the track segments. The method can effectively solve the problem of track fracture caused by rapid maneuvering, strong clutter, target occlusion, long sampling intervals, low detection probabilities, and interference from other vessels near channels, providing a new way for long-term continuous tracking of vessel targets in complex environments. Moreover, the new method is efficient and easy to implement due to its simple structure, which allows the real-time tracking of vessel targets for stereoscopic HFSWR.

Author Contributions: Conceptualization: L.Z.; Methodology: D.M. and L.Z.; Software: D.M. and J.N.; Validation: J.N. and D.M.; Investigation: D.M.; Resources: Y.J.; Data Curation: Y.J.; Writing—Original Draft Preparation: L.Z. and D.M.; Project Administration: Y.J.; Writing—Review and Editing: Q.M.J.W. All authors have read and agreed to the published version of the manuscript.

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