Resonance Detection Strategy for Multi-Parallel Inverter-Based Grid-Connected Renewable Power System Using Cascaded SOGI-FLL

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Abstract: The increasing use of multi-parallel grid-connected inverters introduces both high-quality and high-capacity power, while it tends to cause a resonance instability problem. A resonance damper can virtualize a resistor at resonant frequency to suppress the instability effectively, but the resonant frequency should be detected primarily. However, the resonant current or voltage is severely distorted and oscillating, which will lead to the resonant frequency extraction being more difficult. To address it, this paper proposes a resonance detection strategy based on the cascaded second-order generalized integrators (SOGI) and the normalized frequency locked loop (FLL). The cascaded structure ensures the accuracy by completely filtering the fundamental component from the detected voltage or current, and the normalization accelerates the frequency detection. The proposed method can be used as a crucial unit of the resonance damping controller. Finally, the performance of the proposed method is verified by the MATLAB-based simulation and Hardware-in-the-Loop (HIL)-based emulation results.

Keywords: renewable power system; grid-connected; resonance detection; frequency estimation; instability; cascaded SOGI-FLL

1. Introduction

In order to cope with climate change and the energy crisis, the renewable energy generation, especially the photovoltaic and wind power, is developing rapidly [1,2]. In general, the grid-connected inverters, as the interface between the renewable power and the grid, play important roles in injecting high-quality power into the grid [3,4]. A typical multi-parallel grid-connected inverters system is demonstrated in Figure 1. Although the technological advance of multi-parallel grid-connected inverters has promoted the rapid development of distributed generation, it also results in a complex coupling relationship between the grid and inverters [5,6], which tends to bring about the resonance [7–10]. The resonance in a multi-parallel inverters system not only affects the power quality, but also brings about other problems, such as damaging the relay protection devices and threatening the security and stability of the power grid.

A micro-grid system with wind turbines, energy storage, photovoltaic and resonance damper is shown in Figure 2. Instead of reshaping the damping characteristic of inverters [11], the active damper aims to dynamically suppress the resonance through increasing a damping resistance at the resonant frequency [4,12,13]. However, the active damper only operates at the resonant frequency.
Therefore, the frequency at the resonant point must be precisely obtained to achieve appropriate damping adjustment. There are various techniques to estimate the frequency or phase, such as discrete Fourier transformation, Kalman filter, phase locked loop (PLL), Wavelet transformation, etc. Among these techniques, PLL receives wide attention because of its excellent performance and simple structure [14,15]. It behaves well in normal cases, but the excellent dynamical performance is at the expense of disturbance resistance ability. Moreover, it cannot be applied in the case of uncertain frequency. Discrete Fourier transformation and Wavelet transformation are often used to detect resonance frequency [16]. The former divides the whole frequency band evenly, which means the information at the resonant point could be neglected easily. The latter analyzes the input signal according to its frequency bands so that only the resonance frequency range can be obtained, rather than the accurate and complete resonance information. The traditional resonance detection methods are limited because of the time variation and amplitude distortion of the resonance current.

![Figure 1.](image1.png)

**Figure 1.** Fundamental configuration of multi-parallel grid-connected inverters system.

![Figure 2.](image2.png)

**Figure 2.** Schematic diagram of micro-grid system with wind turbines, energy storage, photovoltaic and resonance dampers.

The Second-Order Generalized Integrator-Frequency Locked Loop (SOGI-FLL) has been studied extensively in recent years, and is composed of two parts: traditional SOGI and FLL [17–22]. The former can generate two orthogonal output signals from the input signal and the latter detects the input signal frequency and provides it to the second-order generalized integrator [19]. SOGI-FLL that only extracts the frequency information simplifies the algorithm and reduces the computation time and complexity [21,23,24]. Multiple paralleled SOGI with a common FLL is proposed to estimate the input signal with multiple components correlated to the fundamental frequency [25,26]. However, it is proved in Reference [27] that the performance of this method will be deteriorated when there are subharmonics in the input signal. The cascaded ANF (Adaptive Notch Filter) structure is proposed in Reference [28] to detect several unknown resonant components from an input signal. However, there is commonly only one resonant component when the multi-parallelled inverters system is
unstable, and the structure is too redundant for only one resonant frequency. Besides that, the effect of algorithm improvement is not obvious and FLL is vulnerable to the grid and SOGI because of the lack of normalization.

In this paper, a typical multi-parallel grid-connected inverters system is modeled and analyzed, which will clarify the objective of resonance detection. In order to increase the damping at the resonant point, the resonance detection strategy based on SOGI-FLL is presented. The operating principle of the traditional SOGI-FLL is analyzed in frequency domain and then the improved cascaded and normalized SOGI-FLL structure is proposed to extract the resonant component from the fundamental component. Through the verification of MATLAB (vR2018b, Natick, MA, USA) simulation and HIL (Hardware-in-the-Loop)-based emulation, it can be seen that the proposed SOGI-FLL structure can effectively and quickly detect the resonant frequency in spite of the fact that the resonant frequency is uncertain and the signal to be detected is oscillating.

2. Modeling and Analysis of Multi-Parallel Inverters System

Due to the existence of grid impedance, there is a complex coupling relationship between the inverters in the grid, which is the main cause of the resonance instability [29]. In this section, the typical multi-parallel grid-connected inverters system is modeled and analyzed, which will clarify the objective of resonance detection theoretically. The current loop model of a typical single-inverter grid-connected system is shown in Figure 3a. $G(s)$ represents the controller, $F(s)$ is the disturbance gain of current loop, $P(s)$ is the control objective, and $E'$ represents the PCC (Point of Common Coupling) voltage.

$$I(s) = \frac{I'(s)L(s) - E'(s)Y(s)}{P(s)}$$

(1)

where, $H(s) = Ci(s)e^{-sTd}P(s)$, $L(s) = \frac{H(s)}{1+H(s)} = \frac{Ci(s)e^{-sTd}P(s)}{1+Ci(s)e^{-sTd}P(s)}$, and $Y(s) = \frac{1}{Z(s)} = \frac{D(s)P(s)}{1+Ci(s)e^{-sTd}P(s)}$.

![Figure 3. Current loop model. (a) Block diagram form, (b) admittance form.](image)

The output current can be expressed as an admittance form, as shown in Equation (1). $L(s)$ is the controllable current source gain, and $Y(s)$ is the current loop admittance [30]. According to Equation (1), the Norton equivalent model consisting of controllable current source and current loop admittance can be obtained from the perspective of circuit port equivalence, as shown in Figure 3b. The admittance equivalent model in Figure 3b can be used to analyze the relationship between the PCC voltage and output current, and then obtain the response expression of each part of the whole parallel system. Furthermore, it can be applied to analyze the stability of the multi-parallel inverters system [31,32].

Through using the current loop admittance model of a single inverter, as mentioned above, the equivalent model of the multi-inverters parallel system can be further established, as shown in Figure 4. $Y_p$ represents equivalent admittance of passive devices, $Y_g$ is the grid equivalent admittance,
and $Y_m$ represents the admittance of each current loop ($m = 1, 2, 3, \ldots, n$), and the PCC voltage can be obtained as follows:

$$E'(s) = \frac{E_{Y_g} + \sum_{m=1}^{n} I_m'}{Y_g(s) + Y_p(s) + \sum_{m=1}^{n} Y_m}$$

Figure 4. Equivalent circuit of parallel system.

It can be seen that the PCC voltage can be considered as the response of the total excitation of the parallel system (superposition of all the equivalent current sources) to the total admittance of the parallel system ($Y_{\text{total}}$, the sum of all the admittance, is defined as global admittance in this paper). In addition, when the grid admittance $Y_g$ is large (namely, the grid is approximately ideal), the PCC voltage is basically not affected by the parallel system of each part. On the contrary, when the grid admittance $Y_g$ is relatively small, all parallel inverters will affect the PCC voltage through the global admittance.

Figure 5 shows a typical resonance phenomenon. The passive admittance ($Y_g + Y_p$) and the active admittance (the sum of the current loop admittance of all inverters, $\sum Y_m$) create a complex coupling relationship at the frequency of 550 Hz, which results in the resonance instability in the grid.

Figure 5. Bode diagram of passive admittance, current loop admittance and global admittance: resonance phenomena.
3. The Proposed Cascaded Second-Order Generalized Integrator-Frequency Locked Loop (SOGI-FLL)-Based Resonance Detection Method

3.1. Frequency Self-Adaptive SOGI-FLL

The frequency adaptability of SOGI-FLL makes the problems of frequency uncertainty and amplitude divergence of resonance signal solvable. The structure of SOGI-FLL is shown in Figure 6, where the resonance frequency is represented as $\omega'$ that distinguishes it from the input frequency $\omega$. $v'$ and $qv'$ are the two orthogonal output signals of the self-adaptive filter.

![Figure 6. The structure of Second-Order Generalized Integrator-Frequency Locked Loop (SOGI-FLL).](image-url)

The transfer functions of SOGI-FLL can be written from Figure 6 as:

\[
\begin{align*}
(a) & : D(s) = \frac{v'}{v_{in}}(s) = \frac{k\omega'}{s^2 + k\omega' s + \omega'^2} \\
(b) & : Q(s) = \frac{qv'}{v_{in}}(s) = \frac{k\omega'^2}{s^2 + k\omega' s + \omega'^2} \\
(c) & : E(s) = \frac{\varepsilon_v}{v_{in}}(s) = \frac{\varepsilon_v}{s^2 + k\omega' s + \omega'^2} 
\end{align*}
\]

Equations (3a) and (3b) indicate that the detection system in Figure 6 provides band-pass filtering and low-pass filtering characteristic to $v'$ and $qv'$, respectively. Besides that, it is obvious that the bandwidth of the band-pass filter is independent of the center frequency $\omega'$ and only depends on the gain $k$. The static gain of the low-pass filter also depends on the gain $k$. It can be concluded from Equations (3a) and (3b) that the output $qv'$ is always 90° lagged from the output $v'$ [18].

Considering the output $qv'$ and input signal error $\varepsilon_v$, they are in-phase when the input frequency is less than the resonance frequency of SOGI ($\omega < \omega'$) and in opposition when $\omega > \omega'$, as shown in Figure 7. Frequency error signal $\varepsilon_f$ can be effectively adjusted by input error signal $\varepsilon_v$ and output signal $qv'$, $\varepsilon_f > 0$ when $\omega < \omega'$ and $\varepsilon_f < 0$ when $\omega > \omega'$. Consequently, FLL can gradually regulate the deviation of $\omega$ and $\omega'$ by the integrator with the negative gain $-\gamma$ according to the change of $\varepsilon_f$ until $\omega = \omega'$ [20,21].

![Figure 7. Bode diagram of $\varepsilon_v$ and $qv'$ of SOGI-FLL.](image-url)
3.2. Mathematical Description of SOGI-FLL

The state-space equations of SOGI-FLL can be derived from the system shown in Figure 6 and are given in Equations (4)–(6), where \((x_1(t) \ x_2(t))^T\) in Equation (4) is the state vector of the second order generalized integrator, and \(y\) in Equation (5) is the output vector. The behavior of the frequency locked loop is illustrated by Equation (6).

\[
\dot{x} = \begin{bmatrix} \dot{x}_1(t) \\ \dot{x}_2(t) \end{bmatrix} = \begin{bmatrix} -k \omega' & -\omega^2 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix} + \begin{bmatrix} k \omega' \\ 0 \end{bmatrix} v_{in}(t) \tag{4}
\]

\[
y = \begin{bmatrix} v'(t) \\ \omega_o v'(t) \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & \omega' \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix} \tag{5}
\]

\[
\dot{\omega} = -\gamma x_2 \omega' (v_{in} - x_1) \tag{6}
\]

Under the condition of stable operation, there is \(\omega = \omega'\) and \(\omega' = 0\) \([33]\), Equation (4) can be deduced to:

\[
\bar{x}_1 = -\omega^2 x_2 \tag{7}
\]

where, the variables in steady state are denoted with a bar over them.

The lock frequency error in steady state can be derived from Equation (4) as:

\[
\bar{\epsilon}_f = \omega' x_2 (v_{in} - \bar{x}_1) = \frac{x_2^2}{k} (\omega'^2 - \omega^2) \tag{8}
\]

Substitute Equation (8) into Equation (6),

\[
\dot{\omega}' = -\gamma x_2 \omega' (v_{in} - \bar{x}_1) \tag{9}
\]

Considering \(\omega \approx \omega'\) in this case, \(\omega^2 - \omega'^2\) is approximately equal to \(2(\omega' - \omega)\omega'\), Equation (8) gives rise to Equation (10).

\[
\dot{\omega}' = -\frac{\gamma x_2^2}{k} (\omega' - \omega) \omega' \tag{10}
\]

Defining the frequency error as \(\delta = \omega' - \omega\), Lyapunov energy function and its gradient equation are established as follows:

\[
V(\delta) = \delta^2 > 0 \\
\frac{dV(\delta)}{dt} = \frac{1}{2} \delta \dot{\delta} = -\frac{1}{2} (\omega' - \omega)^2 (\omega' + \omega)^2 \frac{x_2^2}{k} < 0 \tag{11}
\]

According to the Lyapunov stability criterion, FLL is progressively stable. Supposing a given input signal \(v_{in} = V \sin(\omega_1 t) + V' e^{\omega_t} \sin(\omega_2 t)\), which can be considered as a signal mixed by a fundamental signal \(v_1 = V \sin(\omega_1 t)\) and a divergent resonant signal \(v_2 = V' e^{\omega_t} \sin(\omega_2 t)\), when the system operates steadily, the transfer functions of input signals error are \(\varepsilon_{v1}(s)\) and \(\varepsilon_{v2}(s)\) caused by \(v_1\) and \(v_2\) respectively, they can be easily obtained by Equation (3c), and the Bode diagram of \(\varepsilon_{v1}(s)\) and \(\varepsilon_{v2}(s)\) is illustrated in Figure 8. The gain is \(-90\) dB at \(\omega < \omega_1\) and \(25\) dB at \(\omega < \omega_2\), which implies the input signal error \(\varepsilon = \varepsilon_{v1} + \varepsilon_{v2}\) can filter the fundamental component completely and keep the resonant component so that it can be used to detect the resonance frequency.
3.3. The Proposed Cascaded and Normalized SOGI-FLL Strategy

Equation (11) reflects the convergence rate of the signal and Equation (10) can be converted to Equation (12).

\[ \dot{\omega}' = -2\frac{\gamma}{k\omega'} V^2 (\omega' - \omega) \] (12)

It should be noted that the relevance of the frequency \( \omega' \) and magnitude \( V \) to the rate of convergence can be eliminated through normalizing the self-adaptive parameter \( \gamma \). Then, the normalization achieved through multiplying the correlation coefficient could make the derivative function of the output frequency to be related only to the adaptive parameter \( \gamma \). The normalized derivative of the output frequency can be expressed as:

\[ \dot{\omega}' = -2\gamma (\omega' - \omega) \] (13)

Figure 9 shows the structure of normalized SOGI-FLL. The cascaded and normalized SOGI-FLL is proposed to separate fundamental component and extract the resonance components, as shown in Figure 10. The structure is divided into two parts. The former part, SOGI (without FLL), sets its extraction frequency as the fundamental frequency. The latter part is the normalized SOGI-FLL that uses the output signal error of the former SOGI to extract resonance component.
Figure 10. The structure diagram of cascaded and normalized SOGI-FLL.

$E_b(s)$ and $D_r(s)$ are the transfer function of the former and latter parts respectively, and the output of cascaded SOGI-FLL can be expressed as:

$$v_r' = D_r(s) \cdot V_{in} \cdot E_b(s)$$

The Bode diagram of (14) is shown in Figure 11. The gain is $-170$ dB at 50 Hz. The fundamental frequency current can be thoroughly filtered by the former part. In addition, the resonant frequency of the current information has been retained, because the gain is 0 dB at the resonance point.

Figure 11. The Bode diagram of the output of cascaded SOGI-FLL.

4. Simulation and HIL-Based Emulation Results

To verify the validity and rationality of the proposed strategy, the MATLAB model and hardware-in-the-loop emulation platform (as shown in Figure 12) are established. The simulation is built to validify the advantage and effectiveness of the cascaded and normalized SOGI-FLL and the HIL-based emulation is built to validify the effectiveness of resonance suppression using the proposed method. It should be noted that the resonance instability is difficult to be emulated on the practical experimental platform due to security risks. Therefore, the HIL platform is adopted in this paper to verify the proposed method. The power hardware circuit (four parallel grid-connected voltage source inverters (VSIs)) is implemented in the RT-Box. A designed controller based on DSP (TMS320F28335) and field programmable gate array (FPGA (EP2C5Q208C8)) is connected to RT-Box and can be tested completely to achieve optimal control performance without the risk of damaging the power hardware. The sampling frequency is 20 kHz, and switching frequency is 10 kHz. The transformation between actual system and virtual system is shown in Figure 13. A similar application can be found in the paper published on IEEE Transactions on Industrial Electronics by Freijedo from EPFL (Swiss federal Institute of Technology in Lausanne) [34].
4.1. MATLAB-Based Simulation Results

Based on Figures 9 and 10, the MATLAB simulation platform can be built. The accuracy and speed of the proposed strategy are difficult to be assessed in the unstable grid-connected system due to the fact that there are several resonant components rather than only one. Thus, the input signal is simulated by a fundamental signal mixed with a divergent resonant signal in this paper. Table 1 shows the parameters of the mixed input signals and SOGI-FLL. Especially, the value of \( k \) needs to be considered comprehensively. The larger the value of \( k \), the faster the dynamic response speed of SOGI. However, the filtering effect of SOGI will get worse when \( k \) increases. Therefore, a compromise is needed. Through the validation and comparison, it can be seen that the dynamic performance is optimal when \( k \) equals 1.414, and it is universal. \( \gamma \) mainly affects the frequency adaptability of FLL. Before normalizing \( \gamma \), it is highly nonlinear and needs to be calculated repeatedly. With the normalization, \( \gamma \) is neither affected by power grid nor by SOGI. As mentioned in Reference [30], the value of \( \gamma \) can be set according to the following expression: 

\[
\gamma = -\frac{5}{t_s}, \quad t_s \text{ is the expected setting time.}
\]

In this paper, \( t_s \) is 0.05 s, so \( \gamma \) is chosen as \(-100\). Using these parameters, a mixed input signal which contains both a fundamental component and a resonant component would be acquired. When the resonant frequency changes, the performance of cascaded SOGI-FLL dynamic extraction of resonant frequency can be verified.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Fundamental current signal</strong> ( i_0 )</td>
<td>Amplitude 100 A&lt;br&gt;Frequency 50 Hz</td>
</tr>
<tr>
<td><strong>Resonant current signal</strong> ( i_1 )</td>
<td>Amplitude 20 A&lt;br&gt;Frequency 320 Hz</td>
</tr>
<tr>
<td><strong>Resonant current signal</strong> ( i_2 )</td>
<td>Amplitude 20 A&lt;br&gt;Frequency 800 Hz</td>
</tr>
<tr>
<td>The gain of SOGI-FLL ( k )</td>
<td>1.414</td>
</tr>
<tr>
<td>The negative gain of FLL ( \gamma )</td>
<td>(-100)</td>
</tr>
</tbody>
</table>
4.1.1. Resonance Extraction Effect Validation

To verify the self-adaptive extraction performance of the proposed cascaded SOGI-FLL-based strategy, the simulation of the fundamental waveform mixing the resonance signal $i_1$ is built. As shown in Figure 14, the current has been mixed by 320 Hz resonance current component. The THD (Total Harmonic Distortion) of the input signal will increase because of the resonance. Through the proposed SOGI-FLL method, the resonance component is extracted, as shown in Figure 15. It is obvious that the resonant component increases from about 100 A to 200 A.

![Figure 14](image1.png)

**Figure 14.** The FFT (fast Fourier transform) analysis of the resonance current. (a) The resonance current; (b) FFT analysis result.

![Figure 15](image2.png)

**Figure 15.** Resonant component extracted by cascaded SOGI-FLL.

The resonance frequency extracted by the proposed cascaded SOGI-FLL is shown in Figure 16, and the frequency of the resonance component is about 320 Hz, and changes to 800 Hz suddenly at 1.5 s. It is obvious that the proposed cascaded SOGI-FLL responds to the frequency change quickly and takes about 0.1 s to track the new resonant frequency.
4.1.2. Comparison of Detection Speed

The comparative result of detection speed is shown in Figure 17. The frequency of the resonance component changes from 320 Hz to 800 Hz suddenly at 1.5 s. The blue curve represents the resonant frequency detected by the unnormalized cascaded SOGI-FLL while the red curve represents the resonant frequency detected by normalized cascaded SOGI-FLL. It is obvious that both methods can quickly respond to the resonance component and track the resonant frequency without the static error. However, the cascaded and normalized SOGI-FLL can respond to the frequency more quickly, this is because the normalized FLL is not affected by the amplitude and frequency of the input signal.

4.2. Hardware-in-the-Loop (HIL)-Based Emulation Results

Figure 18 shows the simulation and HIL-emulation platform, which consists of four traditional grid-connected VSIs. The power hardware circuit is implemented in the RT-Box. To experimentally validate the performance of the resonance detection presented in this paper, a resonance damping controller based on the R-APF (resistive active power filter) method is designed, as shown in Figure 19. The damping resistance $R_{d, \text{ref}}$ is only emulated at the resonance frequency, which can be achieved by adopting the detection strategy proposed in this paper to extract the resonance voltage component from the fundamental voltage component. The effectiveness of resonance suppression will depend largely on the accuracy of the resonance detection.
Figures 18 and 21 respectively, demonstrate the grid-injected current and PCC voltage before and after the resonance damping controller has been taken into operation. The third and fourth subplots in Figures 20 and 21 are the Zoom waveforms of the red box in the first and second subplots. As shown in Figure 20, resonance occurs, and the system becomes instable. The current and voltage waveforms increase dramatically and are extremely distorted. Under the effect of the damping controller, as shown in Figure 19, the resonance is tracked and suppressed quickly, the system resumes stability. The current and voltage waveforms are stable and convergent. The HIL emulation results directly verify that the proposed method can detect the resonance component accurately and can be applied to design a resonance damping controller to suppress the resonance in a multi-parallel inverters system.
5. Conclusions

The resonance generation mechanism in the multi-parallel grid-connected inverters system was analyzed. The SOGI-FLL is frequency-adaptive so that it can be applied to detect the unknown resonant frequency. However, a traditional SOGI-FLL only can extract one frequency and is susceptible to the input signal. In this paper, the cascaded and normalized SOGI-FLL was proposed to separate the fundamental component to detect the resonance disturbances. The MATLAB simulation and HIL-based emulation results show that the improved cascaded SOGI-FLL structure can quickly and effectively detect the resonance disturbances. The proposed method can provide a promising way to detect the resonant frequency for the use of suppressing the resonance in a multi-parallel inverters system, which guarantees the security and stability of the grid.

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References


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