Article

Three-Dimensional Urban Expansion Analysis of Valley-Type Cities: A Case Study of Chengguan District, Lanzhou, China

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Received: 20 July 2019; Accepted: 11 October 2019; Published: 14 October 2019

Abstract: The development of cities in the vertical dimension is important in valley-type cities where physical growth is limited by terrain. However, little research has focused on three-dimensional urban expansion of valley-type cities. Lanzhou is a typical valley-type city in China and Chengguan District is the core area of Lanzhou City. This research is aimed at understanding the development of valley-type cities through the analysis of the three-dimensional urban expansion of Lanzhou Chengguan District and providing a reference for urban planning. We extracted five periods of architectural contours and height information between 1975 to 2018 with the support of multi-source remote sensing and network data. We used overlay analysis and mathematical statistical methods to analyze urban horizontal expansion and used the building density, floor area ratio, vertical expansion speed, fluctuation degree, and skyline to analyze urban vertical expansion. We found that the mode of horizontal expansion of Chengguan District shifted from adjacency to enclave through mountain area reclamation. The area with the fastest vertical expansion speed first appeared in the horizontal expansion completed area, and then in both the rapid horizontal expansion area and in the horizontal expansion completed area. Before 2007, the speed of horizontal expansion increased and reached its peak while the vertical expansion speed was relatively stable. After that, the former decreased, and the vertical expansion increased rapidly and dominated the urban development. The vertical expansion of the valley-type city gradually dominates urban development. Urban planning should consider the three-dimensional expansion, especially in the vertical dimension.

Keywords: valley-type city; three-dimensional urban expansion; vertical urban expansion; Lanzhou Chengguan District

1. Introduction

Cities are where humans have the strongest effect on the natural environment [1]. Early urban sprawl tended to encroach on suburban in horizontal direction [2], under the pressure of rapid population growth, with many negative effects on society and the environment [3,4], such as biodiversity loss [5], air pollution [6], and urban heat islands [7,8]. Rapidly growing cities are gradually improving land use efficiency with increasing building height in vertically to control urban outward sprawl [9]. It is more common in Asian countries with high population density to build many middle- and high-rise buildings [10]. Not only for metropolis with developed economies, vertically expansion is also important for relatively large cities of space-restricted, such as valley-type cities, as it
is difficult to expand outward constantly. As an essential aspect of urban compactness, economy, population growth, and residential lifestyle [11]. However, vertical expansion also contributes to “urban diseases” [12,13], such as overcrowding, traffic congestion, pollution, and ventilation obstacle. Therefore, an in-depth understanding of the process of urban time-space expansion and change in three-dimension (both in horizontal and vertical direction) is fundamental for rational planning and efficient use of urban space to sustainable development [14].

Traditional urban expansion research pays more attention to horizontal expansion and ignores vertical expansion [15–17]. With the support of remote sensing, urban three-dimensional information extraction technology have been developed, and some methods or parameters have been applied to study the three-dimensional (3D) expansion in recent years. For example, Zambon et al. [18] acquired official statistics building data in each Greek municipality and proposed the “Vertical-to-Horizontal Growth” ratio to discriminate intense vertical expansion and understand metropolitan transformations comprehensively. Zhang [19] used the monoplotting technique to extract building information and applied a series of indices to analyze architectural landscape in block of Qingdao. Zhang et al. [20,21] employed the SS-coMCRF model to obtain data from medium resolution Landsat image and adopted Gaussian kernel density, overlay analysis to find the different expansion pattern in East Asian megacities and relationships between major socioeconomic factors and urban 3D expansion in Guangzhou. Qin et al. [22] proposed the analysis of the 3D fractal dimension and found that the 3D space utilization of Yangzhou city became more efficient and intensive. There are also studies used radar [23,24] or laser data [25] to extract urban 3D information or presented new methods (e.g., volume [26] extent of urban expansion [27]) to elaborate the anisotropy and spatial heterogeneity of expansion as well as the spatial–temporal characteristics of urban 3D growth. However, the data previous studies used such as active or passive remote sensing data was often limited by expansive prices, difficult access methods, short time spans, and high processing technology. Medium resolution Landsat images are more suitable for studies of large metropolis. Therefore, it is necessary to utilize multi-source data in order to obtain long time series of high-precision urban three-dimensional data. Aerial photographs, historical topographic maps, and high-resolution images developed in recent years and network data or records have made it possible. For example, Zheng et al. [28] used GeoEye images and network data including building height and built year to obtain building footprints and their heights of the residential neighborhoods in Beijing from 1949 to 2009 for residential landscape change analysis. Besides, the analytical methods previous studies employed can only analyze the 3D expansion of entire city or block in terms of amount, but not spatially. Grid analysis can realize the spatialization of quantitative indicators; it also can provide more information than single building height. Such as Qin et al. [22] expressed the 3D morphology expansion with grid analysis and identified areas with the highest expansion intensity.

Some studies identified some patterns of the expansion process, for example, Frolking et al. [10] found that 100 cities around the world have expanded outwards and upwards, especially in East Asia, and Indian cities were more inclined to expand outwards. In contrast, built-up growth in Surabaya, Indonesia led to vertical rather than horizontal development [26]. Zhang et al. [21] found that three megacities in Central Asia were continuing to grow vertically, although they were at different urban development stages. They also found that cities usually tended to grow vertically in the already developed areas after ending their horizontal expansion. Similarly, findings in Shanghai and in Greece [18,27] shows that, cities often alternate their expansion process between phases of horizontal growth and vertical growth. Other studies found that residential neighborhoods of Beijing form a “low-high” pattern from the urban central areas to the urban edges [28], and the districts architectural landscape differentiation in Qingdao is more consistent with their diverse development history, function, and planning [19]. Other studies simulated the process of urban expansion in Surrey, Canada, and Wuhan, China. Koziatek et al. [2] observed that in Surrey high-rise buildings will be more common near transportation networks, urban centers, and higher population densities, while He et al. [29] noted that in Wuhan the highest buildings will occur near the lake and undeveloped
land. Existing 3D urban expansion studies intend to focus on megacities with high economic. Little information exists on valley-type cities restricted by space. Are there any special urban expansion patterns of these cities with limited spatial patterns? Are these cities entering a period of vertical expansion earlier than plain cities? Answers to these questions are important for understanding the development of these cities.

Therefore, to fill these gaps, the Chengguan District, a most important and most historical region of typical valley-type city Lanzhou in northwestern China, was chosen as the study area. Multi-source data such as aerial photographs, topographic maps, high-resolution images, and network data from year 1975 to 2018 were used to obtain long time spans, high-precision built-up area boundary, building footprints, and heights information. Grid analysis was applied to realize the spatialization of quantitative indicators (e.g., floor area ratio [19], vertical expansion speed [27], and fluctuation degree [30]). The overarching aim of this study is to analyze the urban 3D spatiotemporal expansion process features to provide a case for understanding the process of expansion of valley-type cities.

2. Study Area

Lanzhou is located in the geometric center of China’s land area. As an important node in the northwestern region of China’s “Silk Road Economic Belt”, it has been an important transportation hub connecting the eastern part of China to the northwest region since ancient times. The terrain of Lanzhou City is special. The Yellow River flows out from the many canyons in the upper reaches, and the water flow slows down in the valley. The city is built in a dumbbell-shaped river valley formed by thousands of years of alluvial sedimentation. Lanzhou was an important military fortress in ancient China and is a major town for industrial development in modern China. Chengguan District was named after its location in the ancient city of Lanzhou since the Sui Dynasty. The ancient city was originally built in the dumbbell-shaped river valley eastern basin, that is, the south bank of the Yellow River in the southwest of present Chengguan District, and it has been used as a government center for the state, province or county for more than a thousand years. During the Ming dynasty, the ancient Lanzhou city in the Chengguan District expanded outwards and added an outer city wall, gradually forming an urban pattern of the “inner and outer city”, which laid the scope of the core area of Lanzhou. When Lanzhou City was established in 1941, it was based on the ancient Lanzhou City of the Ming and Qing Dynasties. Therefore, Chengguan District has always been the core area and essence of Lanzhou City. The highest altitude of the two mountains in the north and south of Chengguan District of Lanzhou City reached 2138 m, which is more than 600 m higher than the lowest valley elevation. The Yellow River flows through the city from west to east and streams through Chengguan District for 18 km. In 2017, the total built-up area of Chengguan District was 73.92 km², the GDP was 94.89 billion yuan, and the population was 1,136,100, accounting for nearly 20%, 40%, and 40% of Lanzhou City, respectively, and the population density reached 17,804 people/km². Chengguan District has 26 blocks, including the Linxia Road block and Zhangye Road block (Figure 1), with a total of 155 communities.
3. Materials and Methods

3.1. Data Sources and Extraction of the City Three-Dimensional Information

In order to analyze the horizontal expansion of the city, the built-up area boundaries were extracted from the multi-source data. Depending on the availability, data came from year 1975, 1987, 1998, 2000, 2007, and 2018. Aerial data were used for 1975 (scale 1:40,000) and 1987 (scale 1:3800); topographic map data (scale 1:10,000) were used for 1998; Digital Orthophoto Map (DOM) data (resolution: 1 m) were used as supporting data for 2000; and DOM data (resolution: 0.2 m) and Gaofen-2 satellite image data (resolution: 1 m) were used in 2007 and 2018, respectively. Due to the large number of aerial images and their high overlap, to reduce the computational workload we carried out thinning, splicing, and image registration processing of the first two periods of aerial data with ArcGIS10.5 and ENVI5.3. The overlap accuracy of the processed aerial images was 30%–40%, which met the needs of later aerial images correction. We also preprocessed the satellite image data with FLAASH atmospheric correction and radiation calibration provided by ENVI5.3. After establishing a boundary extraction criterion of urban built-up area based on the multi-source remote sensing data, we applied a visual interpretation method to digitize the built-up area boundaries in each period. Specifically, areas with buildings, well-established municipal infrastructure, and spatially contiguous areas were considered built-up areas, including development areas or new urban areas with important urban functions in the suburbs of the city, but excluding rural settlements surrounded by cultivated land.

Building height was used to analyze the vertical expansion of the city, and the first step was to obtain these data for year 2018. Data about building footprints and their floors information was obtained from “Baidu Map” data (map.baidu.com) for circa 2018. The built years and floors information was obtained from the real-estate sale website “Anjuke” (www.anjuke.com) [31]. We found that most of the footprints data was correct [28] by comparing them to the 2018 Gaofen-2 satellite images of the study area, but a considerable amount of floors information was missing. The remaining building footprints of the missing or non-updated areas were manually digitized from Gaofen-2 satellite images, and their floors number were found from “Anjuke” website data or counted with windows from satellite images by referring to Baidu Map Street View data. Since residential buildings represented the main building type of Chengguan District, building heights were estimated by multiplying the number of floors by 3 m, according to the typical floor height defined in the residential building code [32].

Besides, heights of newly built shopping malls or office buildings were obtained from their official...
information. On this basis, building footprints and their heights data from the other five periods were obtained. Specifically, buildings that have not changed in each period were distinguished according to satellite images and their built years; the footprints of changed buildings were digitized from satellite images, aerial data, or other source data of each period by visual interpretation, and the number of floors were counted from Google historical maps or image data from each period, un-changed buildings for each period were used as controls, and then building heights were estimated.

Following the Code for Design of Civil Building [33], we classified the buildings into six types, low-rise, multi-story, middle-rise, small high-rise, high-rise, and ultra-high-rise, in which small high-rise and high-rise were decomposed from “High-rise buildings” of 30–100 m. The floors number and height of various types of buildings are shown in Table 1.

### Table 1. Classification of the buildings in terms of building height.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Floor</th>
<th>Height (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Low-rise building</td>
<td>1–3</td>
<td>≤9</td>
</tr>
<tr>
<td>Multi-story building</td>
<td>4–6</td>
<td>9–21</td>
</tr>
<tr>
<td>Middle-rise building</td>
<td>7–9</td>
<td>21–30</td>
</tr>
<tr>
<td>Small high-rise building</td>
<td>10–16</td>
<td>30–50</td>
</tr>
<tr>
<td>High-rise building</td>
<td>17–40</td>
<td>50–100</td>
</tr>
<tr>
<td>Ultra-high-rise building</td>
<td>&gt;40</td>
<td>&gt;100</td>
</tr>
</tbody>
</table>

3.2. Analysis of Urban Expansion

Many different methods or parameters were used to analyze the urban expansion in horizontal and vertical direction through time. First, overlay analysis and mathematical statistical methods (e.g., change rate of the built-up region in each period can be calculated through dividing the area subtracting result of built-up region between two adjacent period by the time difference of these two adjacent years.) were used to analyze the urban horizontal expansion with built-up area boundaries data. Then, building height and footprints information was used to analyze urban vertical expansion. Building density was used to analyze the spatial distribution changes of density of different heights buildings and floor area ratio was used to analyze the intensity of constructed land. The vertical expansion speed index was used to analyze urban vertical expansion speed changes and location of major changes. Skyline analysis and fluctuation degree were used to analyze the change of urban appearance. Floor area ratio, vertical expansion speed, and fluctuation degree were calculated by grid analysis in ArcGIS. First, we used the fishing net tool to create regular grids in the study area (through testing, the grid calculation unit size was determined to be 200 m), and then used the field calculator to count base area and height of building in the grid and the other parameters.

3.2.1. Building Density

Non-parametric kernel density estimation (KDE) is usually used to estimate the probability density function of a sample, and some special aggregation information is found from its distribution. According to the probability theory, Scott [34] defines it as: set \((x_1, x_2, \ldots, x_n)\) to be an independent and continuously distributed sample with the same distribution as the density function \(f\), then the kernel density estimate \(f_h(x)\) is:

\[
\hat{f}_h(x) = \frac{1}{n} \sum_{i=1}^{n} K_h(x - x_i) = \frac{1}{nh} \sum_{i=1}^{n} K\left(\frac{x - x_i}{h}\right). \tag{1}
\]

Note: \(K\) is a non-negative kernel function; \(n\) is the sample size; and \(h\) is the bandwidth; \(x - x_i\) is the distance from the evaluation point \(x\) to \(x_i\).

This paper used the nuclear density analysis tool provided by ArcGIS. The principle was to set the search radius (bandwidth) to produce a smooth circular surface with the sample point as the center.
The density value was estimated by the kernel density function, and the value decreased with the increase of the distance from the center of the circle, and decreased to zero when the distance reached the radius of circle. After multiple tests, we selected 300 m as the search radius.

3.2.2. Floor Area Ratio

The floor area ratio (FAR) \[19\] is an important index for measuring the intensity of constructed land and the comfort of human settlements. The calculation formula is:

\[
\text{FAR} = \frac{\sum_{i=1}^{n} (h_i / C A_i)}{P}.
\]  

Note: \(A_i\) and \(h_i\) are the base area and height of building \(i\), respectively; \(n\) is the number of buildings in the calculation unit; \(C\) is constant (\(C = 3.0\) m); and \(P\) is the area of the calculation unit.

3.2.3. Urban Vertical Expansion Speed

The average annual growth of building volume is used to evaluate the vertical expansion speed (VES) of cities in different periods, calculated with Equation (3):

\[
\text{VES} = \frac{(V_{j,t+m} - V_{j,t})}{m}.
\]  

Note: \(V_{j,t+m}\) and \(V_{j,t}\) are the sum of the volumes of the buildings in the \(t + m\) and \(t\) time calculation units, and \(m\) is the given period (years).

3.2.4. Fluctuation Degree

The fluctuation degree (FD) is a regional urban spatial morphological factor, which can characterize the degree of dispersion of building height in the calculation unit [30]. It is often calculated as the ratio of the height standard deviation and the average height of the building in the calculation unit, as follows:

\[
\text{FD} = \frac{\sqrt{\sum_{i=1}^{n} (h_i - \overline{H})^2}}{\overline{H}}.
\]  

Note: \(A_i\) and \(h_i\) are the base area and height of the building \(i\); and \(\overline{H}\) and FD are the number of buildings, the weighted average height and fluctuation degree of buildings in the calculation unit, respectively.

3.2.5. Skyline

The skyline of the city is a representation of the overall image and pattern of the city [35]. In a narrow sense, skyline refers to the contour line formed by the city from a certain angle. In order to observe the change of the city outline from a side view of the city, we used ArcScene to stretch the height of the urban buildings and generate the silhouette of the city buildings in the background from the main axis and vertical axis of the city, which is in the S–N direction and in the W–E direction.

4. Results

4.1. Horizontal Urban Expansion

We overlaid the five periods of built-up area boundary data of the Chengguan District for 1975–2018 (Figure 2), and calculated the area of built-up region and its change rate in each period (Table 2). The results show that the horizontal expansion of Chengguan District was mainly along the original floodplain in the northeast direction, principally by adjacency expansion. Along with the development of the city’s barren mountains, a pattern of enclave expansion gradually appeared.
The speed of horizontal expansion first increased and then decreased. The speed of expansion was the fastest during the period 1998–2007. In 1975, the area of built-up region of Chengguan District was 25.6 km\(^2\), and most of the built-up area was concentrated in the southwest and the north of the Yanchang area across the river from the core area, with fewer built-up areas in the southeast. In 1975–1987, the area of built-up region increased by 5.38 km\(^2\), with a low change rate (0.45 km\(^2\)/a). The main form of urban horizontal expansion was infill expansion, with a small number of adjacency extensions in the north and south. In 1987–1998, the area of built-up region increased by 9.54 km\(^2\), and its change rate increased (0.87 km\(^2\)/a). There were a small number of internal filler expansions in the southeast of the city. The adjacent horizontal expansion was more significant in the northeast direction of the city, the southern part of the Yanyuan block, and the western part of Yannan block. The city began to expand to the urban northwest Yellow River terrace, in the form of enclave expansion, which is a type where the expansion area is spatially separated from the built-up area but functionally connected. In 1998–2007, the area of built-up region increased by 9.45 km\(^2\), and its change rate peaked (1.05 km\(^2\)/a). The main form of urban horizontal growth was adjacent expansion, with the original floodplain in the northeastern as the principal direction. In 2007–2018, the area of built-up region increased by 8.72 km\(^2\), and its change rate decreased rapidly (0.79 km\(^2\)/a). The city expanded intensely to the northern mountain area, where the elevation reached more than 1800 m, in the main form of enclave expansion. This shows that the demand of construction land in Chengguan District was rising gradually, which the plain in the Valley Basin could not meet the demand of urban development, and that urban construction extended far from the core area through enclaves.

![Figure 2](image-url)  
*Figure 2. Expansion of the built-up area of Chengguan District from 1975 to 2018.*

### Table 2. Area and change rate of built area.

<table>
<thead>
<tr>
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</thead>
<tbody>
<tr>
<td>Area (km(^2))</td>
<td>25.6</td>
<td>30.98</td>
<td>40.52</td>
<td>49.97</td>
<td>58.69</td>
</tr>
<tr>
<td>Change rate (km(^2)/a)</td>
<td>0.45</td>
<td>0.87</td>
<td>1.05</td>
<td>0.79</td>
<td></td>
</tr>
</tbody>
</table>

4.2. Vertical Urban Expansion

4.2.1. Changes in Building Height

Through the method described in Section 3.1, we derived the building height model of Chengguan District for the five periods of analysis (Figure 3), and found that for more than 40 years, the
city of Chengguan District had underwent strong vertical growth at the same time as it was expanding horizontally.

In 1975, the buildings of Chengguan District were generally low. Higher buildings (11–21 m) were sporadically distributed around the core area and were more concentrated in the middle of the southern part of the built-up area—East of the Gaolan block, Guangwumen block, and Railway West Village block, west of the military airport.

In 1975–1987, higher buildings (11–21 m) increased in the core area and the Yanchang area, but their distribution was fragmented and sparse. In the middle of the southern built-up area, the buildings of 11–21 m height were centrally distributed and the range expands in the east–west direction, and higher buildings (21–35 m) appeared.

In 1987–1998, a wide range of 21–35 m buildings and a small number of 35–75 m buildings emerged around the core area, forming a gathering centered on the Nanguan Cross. Development during this period added more new 11–21 m buildings in the former military airport area in the southeast of the built-up area, more new 3–11 m buildings in the northeast former Yellow River floodplain, and more new 11–35 m buildings in the northwest mountain platform area.

In 1998–2007, the gathering of higher buildings in the core area was expanded, and a large number of high-rise buildings of 35–75 m were added. The area of 21–35 m buildings in the Yanchang area and in the southeast of the built-up area expanded. The newly built buildings in the northeastern part of the built-up area were mainly 11–35 m buildings, and high-rise buildings of 50–90 m also begun to appear.

In 2007–2018, buildings of 35–75 m in core area increased and ultra-high-rise buildings over 100 m in the core area started to be sparsely distributed. Building communities of 35–100 m in other areas were developed rapidly, and became more concentrated along the Yellow River. The newly built buildings in the northeast platform of the built-up area were mainly 90–100 m buildings.

The above analysis shows that the building height of Chengguan District changed dramatically during the study period, showing an upward trend on the whole. In the early days, the urban
construction in the periphery of the core area was high; in 1987–1998, the core areas began to be remodeled and gradually formed the Urban Development Center in the Nanguan Cross; in 2007–2018, the building height increased both in the core built-up area and, even faster, in the mountain terrace area.

Since multi-story and higher buildings have a greater impact on vertical urban expansion, we counted their numbers, areas, and volumes (Figure 4). It can be seen that the height of the buildings playing a leading role in urban expansion was increasing, the proportion of lower buildings was decreasing, and its change rate of area and volume was gradually decreasing. From 1975 to 1987, the newly added buildings were mainly multi-story buildings, with new multi-story and middle-rise buildings accounting for 78% (1483) and 19.5% (371) of newly added buildings, respectively. From 1987 to 1998, the number of newly added mid-rise and high-rise buildings increased, with new multi-story and mid-rise buildings accounting for 49.5% (1446) and 40.3% (1177), respectively. The growth rate in area and volume of mid-rise buildings significantly accelerated. From 1998 to 2007, the newly added buildings were mainly mid-rise buildings. The number of new multi-story buildings was significantly reduced, and the number of small high-rise and high-rise buildings increased. Newly added multi-story, mid-rise, small high-rise, and high-rise buildings accounted for 29.2%, 43.7%, 13.7%, and 12.7%, respectively. The increase rate in area and volume of multi-story and mid-rise buildings significantly slowed down. In 2007–2018, the newly added buildings were mainly high-rise buildings, ultra-high-rise buildings began to appear, and new high-rise and ultra-high-rise buildings accounted for 81.1% and 11.5%, respectively. The rate of increase in the area and volume of high-rise buildings had rapidly increased, while that of multi-story and middle-rise buildings was significantly reduced. In particular, the growth rate of high-rise buildings was much larger than that of small high-rise buildings. This was associated with higher buildings having less floor space, so they were more efficient at meeting the growing needs of the population.

![Figure 4](image-url)

**Figure 4.** (a) Number, (b) area, and (c) volume change for each type of building.

4.2.2. Building Density and Floor Area Rate Change

Due to the small number (176 buildings in 2018) and the small density of ultra high-rise buildings, we calculated the nuclear density of multi-story and above buildings of different periods except for ultra-high-rise buildings, and the results are shown in Figure 5. In 1975, multi-story buildings were located in the west of Jiayuguan Road, in the southern part of the built-up area, and their density in the east of the core area to Jiayuguan block was relatively high. There were relatively few mid-rise buildings, and they were concentrated in the block of Gaolan Road. From 1975 to 1987, the multi-story building expanded to the Yanchangbao area, and its building density increased as a whole. The mid-rise buildings expanded toward the core area, and their density increased slowly. Small high-rise buildings appeared sporadically in the southwestern part of the built-up area. From 1987 to 1998, the multi-story and mid-rise buildings were expanded to the southeast of the built-up area. The density of multi-story buildings increased overall, and the density of mid-rise buildings in the core area and the south of the core area was relatively high. The density of small high-rise and high-rise buildings in the core area increased and their distribution were concentrated. From 1998 to 2007, multi-story and
mid-rise buildings expanded to the northeast of Yantan area. The density of multi-story buildings was generally high, and the density of mid-rise buildings in the Yannan block area increased. Small high-rise and high-rise buildings had a high degree of expansion to the streets of Gaolan block, and their density was highest in the Jiuquan block and Nanguan Cross in the south of the core area. From 2007 to 2018, the scope of multi-story buildings changed little, and its density declined in the Tuanjie Xincun and Zhangye blocks. The range and density of mid-rise and small high-rise buildings had not changed much. Except for Yannan Street and Donggang block, the density of high-rise buildings in most areas of the built-up area had increased significantly, and their density was highest in the northeastern platform of the built-up area.

The change of FAR (Figure 6) shows that from 1975 to 2018, the building FAR increased with the three-dimensional expansion of the city, with the core area having the highest FAR. In 2007–2018, the Wanguo Port, located in Jiayuguan Road in the southeast of the built-up area, was densely built, so its FAR was very high. In addition, the large-scale construction of high-rise buildings had led to the emergence of high-FAR areas in 2018, and only individual grid areas had FAR values greater than 5. In general, in order to ensure the comfort of human settlements, the FAR of high-rise buildings should not exceed 5, and the FAR of multi-story buildings should not exceed 3. In 2018, the FAR of most areas of Chengguan District was between 0–3, and the core area of the city was between 3–5. This shows that the level of human settlement comfort was overall higher in Chengguan District, while it was lower in the core area.

Figure 5. Nuclear density analysis of different types of buildings at different periods.
4.2.3. Vertical Expansion Speed

Using Formula (3) we calculated the building volume in each unit to map the speed of vertical expansion (Figure 7). We found that from 1987 to 1998, the vertical expansion of the Chengguan District occurred mostly in the urban core area where the horizontal expansion was complete. After 1998, vertical expansion often occurred violently with horizontal expansion, and still appeared in areas where horizontal expansion completed. From 1975 to 1987, the urban vertical expansion speed was low overall, and zero or negative expansion was caused by the presence of demolition and unfinished construction during the development process. From 1987 to 1998, the core area began to be vigorously reformed, the vertical expansion speed was accelerated, and the horizontal expansion occurred in the southeast and northeast, but the vertical expansion speed in the southeast was faster. From 1998 to 2007, the vertical expansion speed in the core area and the Yantan area northeast of built-up area increased significantly, and the vertical expansion speed in Yantan area was faster and wider. From 2007 to 2018, the northeastern platform area and most eastern part of the built-up area experienced dramatic vertical expansion. The vertical expansion was more concentrated in the high-tech district block, the northern Yanbei block and the northeastern platform area.

Figure 6. Building floor area rate change.

Figure 7. Vertical expansion speed change.
We calculated the weighted average height and volume of buildings, and their height and volume change rate (Table 3). The weighted average height of the buildings was obtained by the ratio of the total volume of the buildings to the floor area of the buildings [22]. The results show that from 1975 to 2018, the height and volume of the Chengguan District continued to increase. The weighted average height of buildings increased from 6.12 m to 2.12 m, an increase of 2.47 times, and the maximum height of buildings reached 285 m in 2018. The volume increased from $0.57 \times 10^8$ m$^3$ to $3.26 \times 10^8$ m$^3$, an increase of 4.7 times. The change rate of building height fluctuated but did not change much during 1975–2007, while it quickly rose from 27.61% to 66.8% in 2007–2018. The building volume change rate continued to rise during 1975–2018. It increased the fastest during the period 1998–2007 (increasing by $3.27 \times 10^6$ m$^3$/a from the previous period), and reached $10 \times 10^6$ m$^3$/a in 2007–2018 (increasing by $1.63 \times 10^6$ m$^3$/a from the previous period). Combined with the horizontal expansion change and the area change rate (Figure 2, Table 2), we used the area change rate of the built-up area and the change rate of the building height to characterize the horizontal and vertical expansion speed of the Chengguan area. It can be found that from 1975 to 2007, the horizontal expansion speed increased while the speed of vertical expansion remained relatively stable. From 1998 to 2007, the horizontal expansion speed reached its peak value, and the volume change rate also reached the maximum growth rate, indicating that the horizontal and vertical expansion greatly contributed to the three-dimensional expansion during this period. In 2007–2018, the horizontal expansion speed slowed down and the vertical expansion speed increased, and the volume change rate peaked, indicating that the vertical expansion dominated the urban expansion direction during this period.

<table>
<thead>
<tr>
<th>Year</th>
<th>1975</th>
<th>1987</th>
<th>1998</th>
<th>2007</th>
<th>2018</th>
</tr>
</thead>
<tbody>
<tr>
<td>Weighted average height (m)</td>
<td>6.12</td>
<td>7.87</td>
<td>9.96</td>
<td>12.71</td>
<td>21.20</td>
</tr>
<tr>
<td>Weighted average height change rate %</td>
<td>28.59</td>
<td>26.56</td>
<td>27.61</td>
<td>66.80</td>
<td></td>
</tr>
<tr>
<td>Volume (10$^8$ m$^3$)</td>
<td>0.57</td>
<td>0.84</td>
<td>1.41</td>
<td>2.16</td>
<td>3.26</td>
</tr>
<tr>
<td>Volume change rate (10$^6$ m$^3$/a)</td>
<td>2.28</td>
<td>5.10</td>
<td>8.37</td>
<td>10.00</td>
<td></td>
</tr>
</tbody>
</table>

### 4.2.4. Changes in the Appearance of the City

**Skyline:**

The skyline analysis (Figure 8) shows that the city skyline of Chengguan District had experienced a change from flat to single peak, double peak, and extreme value. The southwestern region developed faster than other regions, followed by the northern middle region. In 1975 and 1987, the height of urban buildings was low and the skyline was flat. The skyline dropped slightly from west to east and from south to north in 1975, and fluctuated slightly in the middle in both directions in 1987. The city skyline showed a peak phenomenon of west high–east low, south high–north low in 1998, indicating that the southwestern part of the city developed more. In 2007, the skyline showed a peak and sub-peak from west to east, a peak and sub-peak from south to north, a slight fluctuation in the east, and the height of the peak in the southwest was greater than that of the previous period. This shows that the middle part of the city was gradually developing but the development degree was not as good as that of the southwest.
5. Discussion

5.1. Factors Affecting the Three-Dimensional Expansion of Chengguan District

It can be seen from the above analysis that the form, main direction and strength of the three-dimensional expansion of Chengguan District were different in different periods. According to
existing research, these differences can be attributed to policy factors, population, economic growth factors, industrial restructuring factors, and natural factors such as topography [36,37].

Driven by policy factors, urban space development in Chengguan District has progressed in a piecewise pattern. Lanzhou City’s Second Phase of Urban Planning (1978–2000) began with zoning the city from 1985, dividing Chengguan District into the Chengguan central area, the Yanchang area, the Donggang area and the Yantan township, which was planned separately. Chengguan Central area is bordered by the Gaolan Mountain in the south, Huanghe River in the north, Linxia Road block in the west, and Jiayuguan Road block in the east. It was planned to be the political, economic, cultural, and scientific research center of Lanzhou City, and the renovation of its old city has also been clearly planned. The Yanchang area is located across the river from the Chengguan Central area, it was planned as a local industrial area and a living and residential area. The Donggang area starts from Jiayuguan Road block in the west and reaches the Lanzhou Valley exit in the east, north to the tributary of the Yellow River in the south of the city, and south to the north of the Gaolan Mountain, which is an important hub connecting Lanzhou City to Longxi, Guanzhong, and the eastern part of China. It was planned as a comprehensive economic zone for material exchange, warehousing, transit and wholesale to other regions. Yantan township is bordered by the Yellow River in the north and Donggang District in the south. It has a low terrain and was originally a floodplain of the Yellow River. People built dams and reclaimed land, due to its fertile soil, Yantan township became an important base for fruit and vegetables of Lanzhou. The Third Phase of Urban Planning (2000–2010) made group planning for the Chengguan central area, Donggang area, Yantan area, and Yanchang area, respectively. The development of the Lanzhou high-tech industrial development zone in the Yantan Area, which was approved in 1991, became the main reason for guiding the eastward expansion of the Chengguan District during in this period. That is, Yantan township was gradually reducing the planning restrictions on agricultural land. It turned from a melon and fruit vegetable base to a high-tech industrial park where a large number of residential lands have replaced agricultural land. At the same time, planning restrictions on the barren hills have been relaxed, the Jiuzhou economic development zone in the northwest of the Jiuzhou area also promoted the expansion of the city. The Fourth Phase of Urban Planning (2010–2020) strengthened the northern mountain development and strictly controlled the construction of the southern mountain. Therefore, the Lanzhou Country Garden residential area was gradually completed in the Baidaoping area in the northern mountain area. Besides, the industrial structure of Donggang District has undergone a major change, it has turned from industrial areas to integrated logistics parks and residential areas. However, the implementation of urban planning was more about grasping the direction of urban development in functional planning. In the actual implementation process, Lanzhou urban development is more affected by the changes in the economic system after China’s reform and opening-up, the adjustment of state-owned enterprises, economic structure, industrial structure, and housing system reform. The population and the development of various industries far exceeded the expectations of the plan.

Population and economy are the endogenous driving forces for the development of the city. From 1975 to 1987, the population of Chengguan District increased from 431,200 to 586,000, an increase of about 154,000 people; in 1998, it reached 753,000, an increase of about 167,000 people; in 2007, it reached 982,500, an increase of about 229,500 people; in 2007–2018 the vertical expansion accelerated rapidly while the horizontal expansion slowed down. The GDP of Chengguan District increased from 9.19 billion yuan in 1998 to 26.2 billion yuan in 2007, reaching 94.889 billion yuan in 2018, which is 10.3 times that of 1998. In 2009, Yixing Zhou [38] found that economic growth has a logarithmic relationship with urban expansion. In 2018, Some studies [21] discovered that during rapid economic growth, limited space availability, and slow population growth, several megacities in Asia have experienced very slow horizontal growth, but still grew vertically. This is similar to what we found in Chengguan District. In the case of limited horizontal space expansion and continuous population growth, the horizontal
expansion speed of the Chengguan District has slowed down, while the speed of vertical expansion has increased rapidly. This shows that with rapid economic development, its impact on urban horizontal expansion is gradually weakened, while the impact on vertical expansion is still obvious.

Industrial restructuring has affected the vertical expansion of the city. From 1975 to 1987, the interior of the old city was mainly devoted to residential areas, and construction projects mainly dealt with maintenance. Therefore, many multi-buildings were built around the old city, and vertical expansion was limited (Figure 7). After the policy reform, a large number of construction projects of administrative offices, financial commerce, cultural education, science and technology, and residences were carried out in the old city to build the Lanzhou Administrative Economic Center. Therefore, the built-up area becomes gradually dominated by mid and high-rise buildings (Figure 4). Ultra-high-rise buildings, such as the 139 m China–Hungary Friendship Building and the 285 m Hongyun Jinmao Tower, begin to appear. The speed of vertical expansion was very fast, forming a peak of aggregation. Driven by the development of the high-tech industrial development zones, agricultural and agricultural by-product preservation, food processing and transportation, and commercial and trade wholesale markets, the Yantan Area evolves from an agricultural to a comprehensive economic development zone, supporting the development of high-rise office buildings and residential communities, forming the sub-peak of urban development. The Donggang area mainly develops material turnover, wholesale, storage, and transportation due to its advantageous location. While its early buildings are not high, the development of residential quarters has driven it to rapid vertical growth in recent years.

Topographical factors play a limiting role in the horizontal expansion of the Chengguan District. Although the development of Yantan area, Jiuzhoutai area, and Baidaoping area are a manifestation of humans overcoming topographical factors, the north and south mountains bordering the city are still the biggest limiting factors for urban development. In 2007–2018, urban construction development guided Chengguan District to growth vertically. On the other hand, the contradiction between population, economic growth, and terrain constraints was also an important factor leading to the sharp vertical expansion of the city.

5.2. Three-Dimensional Expansion and Existing Problems in Chengguan District

As a typical space-limited river valley city, Lanzhou Chengguan District has a very different development pattern from plain cities. In the horizontal expansion direction, it distinguishes itself from the typical concentric circular growth pattern [39,40], and developed in a piecewise pattern. In the vertical direction, it is different from the classic shape of “high center, low periphery” [21,27], showing a bimodal urban form. We also found that, in recent years, new construction in Chengguan District consisted more often in high-rise buildings taller than 50 m instead of small high-rise buildings of 30–50 m. Similarly to the development in Beijing [28], higher buildings were more efficient at meeting the need of accelerated population growth, and enhanced human comfort by reducing building density, reducing surface temperature, and improving the greening of the environment. However, this phenomenon also reflects the large population density in Chengguan District.

The urban development model of Chengguan District is similar to the alternating form of horizontal expansion and vertical expansion found in Greece [18]. The horizontal expansion proceeded rapidly in the early stages, and then was overcome by an increase in vertical expansion. Due to the limitation of the river valley terrain, the urban areas expanded vertically very fast in 2007–2018. Furthermore, the relationship between the height of the building and the space required in the horizontal direction of the building makes it impossible to increase the height of the building without limitation. Therefore, the horizontal expansion in the mountain reclamation area has occurred in the North Mountain. There are many gentle hillside development pilot zones in the North Mountain that were planned in the fourth edition of Lanzhou urban planning (2010–2020). It is conceivable that Lanzhou City and Chengguan District will experience a large horizontal expansion. However, mountains in the north and south of Lanzhou are mostly loess hilly landforms formed by denudation and accumulation, and are higher than the inner plains of the valley. Although mountain reclamation can alleviate the pressure of
urban population growth, it brings about the consequences of urban soil erosion, increased dust, and ecological deterioration, impeding the sustainable development of the city. Therefore, the expansion of mountain reclamation in Lanzhou City cannot be carried out on a large scale. It is necessary to be cautious and careful in the arrangement of time and space. Vertical expansion still plays an important role in urban development, reasonable vertical expansion can improve land use efficiency and improve people’s quality of life. There are many similar valley-type cities in China facing the same dilemma. Our findings could provide new insights and methods into assessing the extent of urban development and identifying areas with potential vertical expansion, and could also provide an indication of whether the saturation of the urban central development affects the comfort of human habitations.

6. Conclusions

With Chengguan District of Lanzhou as the study area, we analyzed four decades of three-dimensional expansion of the city from 1975–2018. The main conclusions are as follows: (1) Urban horizontal expansion of Chengguan district took place gradually from low-altitude to high-altitude mountain areas, the expansion mode shifted from adjacent-type to enclave-type, the expansion speed increased in 1975–2007, and declined in 2007–2018. (2) Building height was first higher in the surroundings of the core area, lower in core area, and then higher in the core area, and lower outwards. The main types of new buildings changed from multi-story buildings to high-rise buildings with a height greater than 50 m, and from 2007 to 2018, the proportion of new high-rise buildings taller than 50 m reached 81.1%. Building density and floor area ratio was highest in the core area. (3) Vertical expansion initially occurred in the urban core area where the horizontal expansion was complete, later tended to take place simultaneously with horizontal expansion, and still continued where horizontal expansion ended. The vertical expansion speed was relatively stable when the horizontal expansion speed increased rapidly in 1975–2007, and then increased rapidly when horizontal expansion decreased quickly in 2007–2018. (4) The city skyline gradually changed from flat to single peak, double peak and extreme value. The peak showed that the center position of the core area remained unchanged, but its fluctuation degree was relatively low, and the northeast and southeast margins of the built-up area were relatively high. The results of our study could provide a reference for the sustainable development planning and policy formulation of valley-type cities like Lanzhou. However, due to limitations related to data accessibility, the use of manual visual interpretation was characterized by a degree of subjectivity, which might cause errors of interpretation and further improvements are needed in the future.


Funding: The National Natural Science Foundation of China [No. 41530752, 41471163 and 41601064], the Technology Basic Resource Investigation Program of China [No. 2017FY101003] and the Strategic Priority Research Program of Chinese Academy of Sciences, Pan-Third Pole Environment Study for a Green Silk Road (Pan-TPE) [No. XDA2009000001] and the Fundamental Research Funds for the Central Universities [No. 561219050].

Conflicts of Interest: The authors declare no conflict of interest.

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