Optimization of Insulation Thickness of External Walls of Residential Buildings in Hot Summer and Cold Winter Zone of China

Xiaojun Liu 1, Xin Chen 1,* and Mehdi Shahrestani 2

1 Department of Management, Xi’an University of Architecture and Technology, Xi’an 710055, China; xjun_liu@163.com
2 School of the Built Environment, University of Reading, Reading RG6 6DF, UK; m.shahrestani@reading.ac.uk

* Correspondence: azure_0101@163.com

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Abstract: It is important to reduce primary energy consumption and greenhouse gas emissions associated with residential buildings in the hot summer and cold winter (HSCW) zone of China. Changing the insulation thickness of the external walls of residential buildings (ITEWB) is regarded as an effective way to manage such problems within a budget. This paper aims at developing an innovative way to select the optimal insulation thickness of external walls for residential buildings (OTWRB) in the HSCW zone of China, considering economic, energy and greenhouse gas emissions issues associated with the ITEWB. Four different cities and two different operation modes of the air conditioners (continuous and intermittent) are considered in this study. To explain the selection process, typical hypothetical buildings are simulated in Wuhan, Changsha, Hangzhou and Chengdu. Expanded polystyrene is chosen as the material of the insulation layer while split air conditioners are selected as the equipment for space heating and cooling. Integrated Environmental Solutions-Virtual Environment is used for the dynamic operational energy consumption of buildings. Life cycle cost method is adopted to calculate the economic impact of ITEWB on building performance. The Chinese life cycle database is used to quantize the impacts of ITEWB on building performance in the aspect of energy and greenhouse gas emissions based on the life cycle theory. The most appreciated insulation thickness is chosen from the thickness range of 30 mm to 150 mm. We find that for continuous operation mode of air conditioners in Wuhan, the optimal economic insulation thickness is 70 mm, whereas when considering only energy and environmental aspects, the OTWRB is 150 mm. These are all larger than the current insulation thickness which is 30 mm. When the weighting efficiencies of the economy, energy, and greenhouse gas emissions are different, the OTWRB varies from 70 mm to 150 mm for continuous operation mode. The different cities have little influence on the OTWRB while the different operation modes of air conditioners have some influence on the OTWRB.

Keywords: insulation thickness; hot summer and cold winter zone; integrated criteria

1. Introduction

It is imperative to reduce primary energy consumption as well as greenhouse gas emissions related to residential buildings in China since China has made a promise to reduce greenhouse gas emissions as well as primary energy consumption at the Paris Agreement [1]. The building sector is one of the three biggest energy consumers and it is responsible for an enormous amount of greenhouse gas emissions in China [2,3]. Meanwhile, the residential building sector comprises over 40% of the energy consumption in China’s civilian construction sector [4]. Reducing primary energy consumption and limiting the associated greenhouse gas emissions related to residential buildings are the key points of such objectives.
There are five climate zones of China; cold zone, severe cold zone, hot zone, hot summer and cold winter (HSCW) zone, and hot summer and warm winter zone [5]. So far, there have been remarkable results for energy savings and reducing greenhouse gas emissions of the residential building sector in cold and severe cold zones of China. On the other hand, the energy consumption associated with the residential building sector in the HSCW zone has been continuously increasing [6]. According to China’s National Bureau of Statistics [7], there were 21% of the national urban residential population in the HSCW zone. The residential buildings in this area lack central heating systems because of historical reasons [8,9]. The residential buildings rely heavily on mechanical heating and cooling systems to keep indoor thermal comfort, resulting in a lot of operational energy consumption [9,10]. The energy consumption for space heating and cooling systems contributes to 50–60% of residential annual energy consumption [11]. While the thermal efficiency of the envelope of the buildings is relatively poor, implying huge saving potentials in this area [12]. As a result, increasing building envelope efficiency is crucial to reducing primary energy consumption and minimizing greenhouse gas emissions associated with residential buildings in the HSCW zone of China.

Applying an insulation layer on the external wall of a building is a popular method for increasing building envelope efficiency. By reducing heat loss through the wall [6], energy consumption and greenhouse gas emissions associated with the buildings can significantly be reduced economically [13]. Up to this point, applying the insulation layer on the external wall of residential buildings has been promoted by the government recently in the HSCW zone of China.

Insulation thickness is an important parameter to consider when applying thermal insulation, thus, there is considerable research about the optimal insulation thickness of the external walls for residential buildings (OTWRB) [14–18]. Since the climate is one of the most important factors in determining the OTWRB [19–21], it is necessary to cut down the scope of the contest to the HSCW zone of China for the OTWRB recommended in this certain area. However, until recently, a few researchers began to pay attention to the OTWRB in this special part of China. Although these existing studies have made significant efforts for the selection of the most appreciated insulation thickness of an external wall, some shortcomings need to be improved.

One shortcoming is the neglect of the intermittent operation mode of the heating and cooling equipment in the HSCW zone of China. In most research focused on the OTWRB in the HSCW zone of China [22,23], the space heating and cooling equipment is assumed to maintain a comfortable temperature for the whole day over the heating and cooling period. However, according to the results of several investigations [8,12,24,25], there is, in fact, plenty of time when this equipment is not in operation [26]. Moreover, Fang Ruan believed that these two different operation modes of air conditioners (continuous and intermittent) resulted in obvious differences in the operational energy consumption of a building [24]. Based on the conclusion that the heating and cooling demands of buildings affect the OTWRB, it is reasonable to discuss the impact of different operation modes of air conditioners on the OTWRB [19].

Another shortcoming of the existing research is the lack of consideration of the integrated impacts associated with the ITEWB. For the existing research about the OTWRB in the HSCW zone of China, some of them only considered the energy aspect associated with ITEWB [27,28], while the others only considered the economic aspect associated with the ITEWB [29,30]. As previously mentioned, the purpose of applying the insulation layer on the external wall of a building is not only about the economic aspect, there are more considerations about the energy aspect and the environmental aspect of the ITEWB. The possibility of considering all these three objectives associated with the ITEWB is revealed by [31]. Their studies proved that greenhouse gas emissions associated with the ITEWB were reduced at the economic insulation thickness compared to that at the zero thickness. The necessity of considering the integrated impacts in the optimization criteria is proved by [14,32,33]. These findings showed the significant impact of criteria on the OTWRB. As a result, it is worth investigating all of these impacts of the ITEWB and selecting the most appreciated one for buildings located in the HSCW zone.
zone of China. To the author’s best knowledge, there is no paper considering these three factors in the determining process of the OTWRB in the HSCW zone of China.

The innovation of this paper is to develop an innovative method to select the OTWRB considering the integrated impact associated with ITEWB in terms of economic, energy and greenhouse gas emissions issues in the HSCW zone of China. Different weighting efficiencies applied to the economy, energy and greenhouse gas emissions are also considered in this paper. To provide some realistic context, the Chinese cities of Wuhan, Changsha, Hangzhou, and Chengdu are used as hypothetical scenarios where the OTWRB values would be determined. Comparative analysis of the results for these four different cities and two different modes of air conditioners (continuous and intermittent) is conducted to discuss the feasibility of the OTWRB.

2. Materials and Methods

2.1. Hypothetical Building

2.1.1. Physical Information of the Typical Building

The same hypothetical buildings are assumed to be located in Wuhan, Changsha, Hangzhou and Chengdu. As shown in Figure 1, these four cities represent the cities in the middle, western, eastern and southern parts of the HSCW zone of China.

![Figure 1. Four typical cities in the hot summer and cold winter (HSCW) zone of China.](image-url)

The layout and construction information of the building prototype is similar to that of the typical building obtained from the field study carried out by Xueping Li, who surveyed above 40 residential communities built around the 2000s in the HSCW zone of China [34]. Figure 2 shows the floor plan and the elevation drawing of the case study building. The total floor area of this 12-storey hypothetical building is 2701.4 m².
buildings located in the HSCW zone of China. To the author’s best knowledge, there is no paper considering these three factors in the determining process of the OTWRB in the HSCW zone of China. The innovation of this paper is to develop an innovative method to select the OTWRB considering the integrated impact associated with ITEWB in terms of economic, energy and greenhouse gas emissions issues in the HSCW zone of China. Different weighting efficiencies applied to the economy, energy and greenhouse gas emissions are also considered in this paper. To provide some realistic context, the Chinese cities of Wuhan, Changsha, Hangzhou, and Chengdu are used as hypothetical scenarios where the OTWRB values would be determined. Comparative analysis of the results for these four different cities and two different modes of air conditioners (continuous and intermittent) is conducted to discuss the feasibility of the OTWRB.

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Figure 2. Geometry information of the case study building: (a) The floor plan of the case study building; (b) The elevation drawing of the case study building.

The other typological characteristics of the building prototype are in Table 1.

Table 1. Typological characteristics of the building.

<table>
<thead>
<tr>
<th>Resource</th>
<th>Storey</th>
<th>Construction</th>
<th>Plane Form</th>
<th>Floor Area per Household</th>
</tr>
</thead>
<tbody>
<tr>
<td>This paper</td>
<td>12 (multi-story)</td>
<td>reinforced concrete</td>
<td>three bedrooms, one living room and one dining room</td>
<td>around 112 m² (about 100 m²)</td>
</tr>
<tr>
<td>Reference</td>
<td>[35]</td>
<td>[9,36,37]</td>
<td>[9]</td>
<td>[12]</td>
</tr>
</tbody>
</table>

The construction information about the envelope of the building is presented in Table 2. The data is based on the field study carried out by Xueping Li [34].

Table 2. U value of the envelope of the typical building.

<table>
<thead>
<tr>
<th>Resource</th>
<th>U Value of the Building Component (w/m²k)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Ground/Exposed Floor</td>
</tr>
<tr>
<td>this paper</td>
<td>1.79</td>
</tr>
<tr>
<td>[34]</td>
<td>————</td>
</tr>
</tbody>
</table>

As shown in Table 3, the structure of the external wall of the typical building is obtained from the field study carried out by Xueping Li, and it is a very common structure in the HSCW zone of China [34]. EPS (expanded polystyrene) is one of the most widely used insulation materials for external walls in this area [30,38,39]. The thermal conductivity of the EPS is 0.4 w/mk in the case study building.

Table 3. Structure of the external wall of the typical building.

<table>
<thead>
<tr>
<th>Layer (Outside to Inside)</th>
<th>Thickness (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cement mortar</td>
<td>20</td>
</tr>
<tr>
<td>Expanded polystyrene</td>
<td>30</td>
</tr>
<tr>
<td>Reinforced concrete</td>
<td>200</td>
</tr>
<tr>
<td>Cement mortar</td>
<td>20</td>
</tr>
</tbody>
</table>

The thickness of the insulation layer of the external wall of the buildings is 30 mm for EPS for the present situation [40]. In this paper, optional values of insulation thickness of the external wall are 30 mm, 50 mm, 70 mm, 90 mm, 110 mm, 130 mm, and 150 mm.
According to the field studies carried out by [34,40–42], split air conditioners fed by electricity are a popular choice to keep indoor comfort in such an area of China, as there is no central heating system in this area because of historical reasons. The details of the thermal system of the case study building are presented in Table 4. Two operation modes of air conditioners are presented in Table 5.

### Table 4. Thermal system setting of the hypothetical building.

<table>
<thead>
<tr>
<th>Factor</th>
<th>Assumption</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Equipment heat gain</td>
<td>4.3 W/m²</td>
<td>[43]</td>
</tr>
<tr>
<td>Heating space</td>
<td>Living room and bedroom</td>
<td>[44]</td>
</tr>
<tr>
<td>Cooling space</td>
<td>Living room and bedroom</td>
<td>[44]</td>
</tr>
<tr>
<td>Heating period</td>
<td>From 1st December to 28th February of the following year</td>
<td>[45]</td>
</tr>
<tr>
<td>Cooling period</td>
<td>From 15th June to 15th September</td>
<td>[34]</td>
</tr>
<tr>
<td>Heating setpoint temperature</td>
<td>18 °C</td>
<td>[43,45]</td>
</tr>
<tr>
<td>Heating trigger temperature</td>
<td>16 °C</td>
<td>[46]</td>
</tr>
<tr>
<td>Cooling setpoint temperature</td>
<td>26 °C</td>
<td>[43,45]</td>
</tr>
<tr>
<td>Cooling trigger temperature</td>
<td>29 °C</td>
<td>[47]</td>
</tr>
<tr>
<td>Infiltration rate (ach)</td>
<td>1.0/h</td>
<td>[43,48]</td>
</tr>
<tr>
<td>Coefficient of performance (COP) of Heating system</td>
<td>1.9</td>
<td>[30,43,49]</td>
</tr>
<tr>
<td>Coefficient of performance (COP) of Cooling system</td>
<td>2.3</td>
<td>[30,43,49]</td>
</tr>
</tbody>
</table>

### Table 5. Two operation modes of air conditioners of the hypothetical building.

<table>
<thead>
<tr>
<th>Scenario</th>
<th>Space</th>
<th>Daily Operation Time</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Continuous</td>
<td>Bedroom</td>
<td>0:00–24:00</td>
<td>[44]</td>
</tr>
<tr>
<td></td>
<td>Living room</td>
<td>0:00–24:00</td>
<td></td>
</tr>
<tr>
<td>Intermittent</td>
<td>Bedroom</td>
<td>0:00–8:00</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Living room</td>
<td>17:00–22:00</td>
<td>[50]</td>
</tr>
</tbody>
</table>

2.1.2. Meteorological Information of the Typical Building

As shown in Table 6, the meteorological data adopted in this paper is from The Solar and Wind Energy Resource Assessment (SWERA) project. This database has the typical hourly meteorological data, and it is known for accurate solar information. Since solar radiation is significant for the building’s operational energy, particularly for the cooling load, this database is adopted in this paper [51].

<table>
<thead>
<tr>
<th>Location</th>
<th>Dry-Bulb Temperature (°C)</th>
<th>Wind Speed (m/s)</th>
<th>Global Radiation (W/m²)</th>
<th>External RH (%)</th>
<th>HDD</th>
<th>CDD</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wuhan</td>
<td>15.89</td>
<td>2.32</td>
<td>163.14</td>
<td>76.55</td>
<td>1122.62</td>
<td>224.12</td>
</tr>
<tr>
<td>Changsha</td>
<td>16.31</td>
<td>2.36</td>
<td>151.28</td>
<td>80.91</td>
<td>1020.10</td>
<td>220.78</td>
</tr>
<tr>
<td>Hangzhou</td>
<td>15.51</td>
<td>2.50</td>
<td>152.97</td>
<td>77.72</td>
<td>1094.81</td>
<td>169.78</td>
</tr>
<tr>
<td>Chengdu</td>
<td>15.76</td>
<td>1.08</td>
<td>146.03</td>
<td>81.04</td>
<td>949.50</td>
<td>14.40</td>
</tr>
</tbody>
</table>

HDD: heating degree days for the base temperature of 18 °C during the heating period. CDD: cooling degree days for the base temperature of 26 °C during the cooling period.

### Table 6. Meteorological information of the hypothetical building.

2.2. Calculation of Operational Energy Consumption of the Hypothetical Building

Generally, there are two different methods to compute energy consumption for space heating and cooling. One method is the equation-based method and another method is the simulation-based method. In the reference, they found out that the equation-based method might not lead to a desired accurate result of the energy demand for space heating and cooling [52–54]. For a more accurate heat
transfer calculation, the dynamic meteorological data and the dynamic indoor temperature should be considered. However, because of the calculation constraints, this approach makes use of assumptions to simplify the equations in calculating heat transfer.

To overcome this kind of simplification of inputs in the equation-based method, some authors adopted the simulation-based method [53]. Thanks to the great computing power of computers, it can make good use of these amounts of inputs and it can automatically calculate the operational energy consumption of buildings with high accuracy.

There are a variety of building simulation tools used in the research, such as Energy Plus, Integrate Environmental Solution-Virtual Environment (IES-VE), and Designer’s Simulation Toolkits (DeST). Among these tools, IES-VE is a popular commercial software used worldwide including China [55]. The validation and accuracy of this software have been proven by the BESTEST (Building Energy Simulation Test) standard of the International Energy Agency (IEA), green building rating schemes and amounts of existing studies [56–59]. Moreover, it has extensive capabilities for modeling customize systems and controls, which allows for the simulation of the intermittent operation mode of air conditioners in the case study.

For this study, ApacheSim module and Apache HVAC module of IES-VE are mainly used. Apache HVAC module is a supplement module for detailed settings of the HVAC system of case study building. The Apache HVAC module enables users to adjust the air conditioner settings, including the operation mode. The ApacheSim module helps users to calculate the space heating and cooling energy consumption of the building automatically. In this software, heat conduction and storage, convection heat transfer, heat transfer by air movement, long-wave radiation heat transfer, solar radiation, casual gains, and thermo-physical properties of air can be all considered in the ApacheSim calculation.

As a verification measure, the operational energy calculated for Hangzhou is compared with the results of past studies. As shown in Table 7, the computed value is comparable with the results in previous studies.

Table 7. Comparison of energy consumption as calculated by IES-VE (Integrate Environmental Solution-Virtual Environment) in this paper for Hangzhou with existing research.

<table>
<thead>
<tr>
<th>Paper Resource</th>
<th>U Value of the External Wall (W/m²K)</th>
<th>Heating Energy Consumption (kWh/m²)</th>
<th>Cooling Energy Consumption (kWh/m²)</th>
<th>Annual Energy Consumption (kWh/m²)</th>
</tr>
</thead>
<tbody>
<tr>
<td>This paper</td>
<td>0.75</td>
<td>25.11</td>
<td>12.06</td>
<td>39.40</td>
</tr>
<tr>
<td>[46]</td>
<td>0.72</td>
<td>26</td>
<td>12.5</td>
<td>38.5</td>
</tr>
<tr>
<td>[60]</td>
<td>0.87</td>
<td>—</td>
<td>—</td>
<td>18–38</td>
</tr>
<tr>
<td>[61]</td>
<td>0.84</td>
<td>—</td>
<td>—</td>
<td>43.42</td>
</tr>
</tbody>
</table>

2.3. Integrated Estimation Method to Select the OTWRB


In this paper, the optimal insulation thickness is obtained based on the integrated impacts of the ITEWB on building performance, with regard to the economic, energy and greenhouse gas emissions aspects.

In the literature, the application of life cycle assessment to the OTWRB is becoming more and more popular [16,21,62]. Based on this theory, three indicators in the paper, which are life cycle cost (LCC), life cycle primary energy demand (LPED) and life cycle global warming potential (LGWP), are selected to present the impacts of the ITEWB on these three aspects.

Under this approach, these three indicators associated with the ITEWB are assessed from cradle to grave. In general, the life cycle stages of insulation include production, transportation, operation, maintenance, demolition and waste management. However, considering the minor effects of transportation, maintenance, demolition and waste management on these three factors in some cases and the difficulty to obtain these data [63], in this paper, only the production stage and the operational stage of the insulation layer are considered. In other words, this study is focusing on
analyzing the impacts of the variation of the ITEWB on the insulation material and the operational
energy consumption during the insulation material’s lifespan.

- **Life cycle cost (LCC)**

  Based on the existing research [18,54], the LCC associated with ITEWB is defined as:

  \[
  LCC_{\text{ins}} = LCC_{\text{operation}} + LCC_{\text{material}}
  \]

  \[
  LCC_{\text{material}} = 10^{-3}C_{\text{ins}}A_w\xi_{\text{ins}}
  \]

  \[
  LCC_{\text{operation}} = C_{\text{op}}Q_{\text{op}}P_1
  \]

  \[
  P_1 = \text{PWF}(N_e, i, d) = \begin{cases} 
  \frac{1}{d-i} \left[ 1 - \left( \frac{1+i}{1+d} \right)^{N_e} \right] & i \neq d \\
  \frac{N_e}{1+i} & i = d 
  \end{cases}
  \]

  The abbreviations used in these equations are shown in Table 8.

- **Life cycle primary energy demand (LPED)**

  \[
  LPED_{\text{ins}} = LPED_{\text{material}} + LPED_{\text{operation}}
  \]

  \[
  LPED_{\text{material}} = 10^{-3}PED_{\text{ins}}A_w\xi_{\text{ins}}\rho
  \]

  \[
  LPED_{\text{operation}} = PED_{\text{op}}Q_{\text{op}}N_e
  \]

  The abbreviations used in these equations are presented in Table 9.

- **Life cycle global warming potential (LGWP)**

### Table 8. Abbreviations used in the life cycle cost of the insulation thickness of the external wall of residential buildings (ITEWB).

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Explain</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>LCC_{\text{ins}}</td>
<td>Life cycle cost of the ITEWB</td>
<td>yuan</td>
</tr>
<tr>
<td>LCC_{\text{material}}</td>
<td>Life cycle cost of insulation material associated with the ITEWB</td>
<td>yuan</td>
</tr>
<tr>
<td>LCC_{\text{operation}}</td>
<td>Life cycle cost of operational energy associated with the ITEWB</td>
<td>yuan</td>
</tr>
<tr>
<td>C_{\text{ins}}</td>
<td>Cost of insulation material per unit</td>
<td>yuan/m^3</td>
</tr>
<tr>
<td>A_w</td>
<td>Area of external wall</td>
<td>m^2</td>
</tr>
<tr>
<td>\xi_{\text{ins}}</td>
<td>The thickness of the insulation layer</td>
<td>mm</td>
</tr>
<tr>
<td>C_{\text{op}}</td>
<td>Cost of operational energy per unit</td>
<td>yuan/kwh</td>
</tr>
<tr>
<td>Q_{\text{op}}</td>
<td>Annual operational energy consumption</td>
<td>kwh/year</td>
</tr>
<tr>
<td>N_e</td>
<td>Insulation layer lifetime</td>
<td>year</td>
</tr>
<tr>
<td>P_1</td>
<td>Present worth factor (PWF)</td>
<td>–</td>
</tr>
<tr>
<td>i</td>
<td>Interest rate</td>
<td>–</td>
</tr>
<tr>
<td>d</td>
<td>Inflation rate</td>
<td>–</td>
</tr>
</tbody>
</table>

A commonly used Chinese local database, CLCD (Chinese Life Cycle Database) [64], is adopted in this paper to quantify the impacts of the ITEWB on building performance with regard to energy and greenhouse gas emissions aspects.

Based on the existing research [33,53], the LPED related to the ITEWB is defined as:

\[
LPED_{\text{ins}} = LPED_{\text{material}} + LPED_{\text{operation}}
\]

\[
LPED_{\text{material}} = 10^{-3}PED_{\text{ins}}A_w\xi_{\text{ins}}\rho
\]

\[
LPED_{\text{operation}} = PED_{\text{op}}Q_{\text{op}}N_e
\]

The abbreviations used in these equations are presented in Table 9.
Table 9. Abbreviations used in the life cycle primary energy demand of the ITEWB.

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Definition</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \rho )</td>
<td>The density of the insulation material</td>
<td>kg/m³</td>
</tr>
<tr>
<td>( \text{LPED}_{\text{ins}} )</td>
<td>Life cycle primary energy demand of the ITEWB</td>
<td>kgce</td>
</tr>
<tr>
<td>( \text{LPED}_{\text{material}} )</td>
<td>Life cycle primary energy demand of insulation material associated with the ITEWB</td>
<td>kgce</td>
</tr>
<tr>
<td>( \text{LPED}_{\text{operation}} )</td>
<td>Life cycle primary energy demand of operational energy associated with the ITEWB</td>
<td>kgce</td>
</tr>
<tr>
<td>( \text{PED}_{\text{ins}} )</td>
<td>Primary energy demand of insulation material per unit</td>
<td>kgce/kg</td>
</tr>
<tr>
<td>( \text{PED}_{\text{op}} )</td>
<td>Primary energy demand of operational energy per unit</td>
<td>kgce/kwh</td>
</tr>
</tbody>
</table>

Based on [53], LGWP related to the ITEWB is defined as

\[
\text{LGWP}_{\text{ins}} = \text{LGWP}_{\text{material}} + \text{LGWP}_{\text{operation}} \tag{8}
\]

\[
\text{LGWP}_{\text{material}} = 10^{-3} \text{GWP}_{\text{ins}} A_w \xi_{\text{ins}} \rho \tag{9}
\]

\[
\text{LGWP}_{\text{operation}} = \text{GWP}_{\text{op}} Q_{\text{op}} N_e \tag{10}
\]

The abbreviations used in these equations are shown in Table 10.

Table 10. Abbreviations used in the life cycle global warming potential of the ITEWB.

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Definition</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \text{LGWP}_{\text{ins}} )</td>
<td>Life cycle global warming potential of the ITEWB</td>
<td>kgCO₂eq</td>
</tr>
<tr>
<td>( \text{LGWP}_{\text{material}} )</td>
<td>Life cycle global warming potential of insulation material associated with the ITEWB</td>
<td>kgCO₂eq</td>
</tr>
<tr>
<td>( \text{LGWP}_{\text{operation}} )</td>
<td>Life cycle global warming potential of operational energy associated with the ITEWB</td>
<td>kgCO₂eq</td>
</tr>
<tr>
<td>( \text{GWP}_{\text{ins}} )</td>
<td>Global warming potential of insulation material per unit</td>
<td>kgCO₂eq/kg</td>
</tr>
<tr>
<td>( \text{GWP}_{\text{op}} )</td>
<td>Global warming potential of operational energy per unit</td>
<td>kgCO₂eq/kwh</td>
</tr>
</tbody>
</table>

2.3.2. Integrated Estimation Method to Select the OTWRB

To normalize these three indicators, LCC, LPED and LGWP, the min-max method is applied in this paper as shown in Equations (11)–(13). To integrate and consider all these three aspects associated with the ITEWB, a weighting sum method is adopted in Equations (14)–(16).

\[
\text{NLCC}_r = \frac{\text{LCC}_r - \text{LCC}_{r,\text{min}}}{\text{LCC}_{r,\text{max}} - \text{LCC}_{r,\text{min}}} \tag{11}
\]

\[
\text{NLPED}_r = \frac{\text{LPED}_r - \text{LPED}_{r,\text{min}}}{\text{LPED}_{r,\text{max}} - \text{LPED}_{r,\text{min}}} \tag{12}
\]

\[
\text{NLGWP}_r = \frac{\text{LGWP}_r - \text{LGWP}_{r,\text{min}}}{\text{LGWP}_{r,\text{max}} - \text{LGWP}_{r,\text{min}}} \tag{13}
\]

\[
Z_r = w_1 \cdot \text{NLCC}_r + w_2 \cdot \text{NLPED}_r + w_3 \cdot \text{NLGWP}_r \tag{14}
\]

\[
w_1 + w_2 + w_3 = 1 \quad (0 \ll w_1, w_2, w_3 \ll 1) \tag{15}
\]
The abbreviations used in these equations are shown in Table 11. 

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>NLCCr</td>
<td>Normalized life cycle cost of the ITEWB</td>
</tr>
<tr>
<td>NLPEDr</td>
<td>Normalized life cycle primary energy demand of ITEWB</td>
</tr>
<tr>
<td>NLGWPr</td>
<td>Normalized life cycle global warming potential of ITEWB</td>
</tr>
<tr>
<td>LCCr,min</td>
<td>The minimum life cycle cost of ITEWB</td>
</tr>
<tr>
<td>LCCr,max</td>
<td>The maximum life cycle cost of ITEWB</td>
</tr>
<tr>
<td>LPEDr,min</td>
<td>The minimum life cycle primary energy demand of ITEWB</td>
</tr>
<tr>
<td>LPEDr,max</td>
<td>The maximum life cycle primary energy demand of ITEWB</td>
</tr>
<tr>
<td>LGWPr,min</td>
<td>The minimum life cycle global warming potential of ITEWB</td>
</tr>
<tr>
<td>LGWPr,max</td>
<td>The maximum life cycle global warming potential of ITEWB</td>
</tr>
<tr>
<td>w₁, w₂, w₃</td>
<td>Weighting efficiency assigned to economy, energy and greenhouse gas emissions</td>
</tr>
<tr>
<td>r</td>
<td>Insulation thickness, which is 30, 50, 70, 90, 110, 130, 150 mm in this paper</td>
</tr>
</tbody>
</table>

3. Results and Discussion

3.1. Operational Energy Consumption and the ITEWB

As shown in Figure 3, for the continuous scenario, the heating energy consumption decreases with the increase of the ITEWB, while the impact of the ITEWB on the cooling load is not obvious [65]. The heating and cooling energy consumption of the building is more sensitive to ITEWB when the ITEWB is smaller. These similar trends are also revealed in [66]. Moreover, for Chengdu, with the increase of insulation thickness, the cooling energy consumption is not reduced, instead, it increases slightly [67].

![Figure 3](image-url)  
Figure 3. Heating and cooling energy consumption for scenario continuous for: (a) Wuhan; (b) Changsha; (c) Hangzhou; (d) Chengdu.
With the increase of insulation thickness, the thermal transmittance of the external wall decreases, leading to more difficulties in terms of heat transfer driven by the temperature difference between indoor environment and outdoor environment [66]. This can lead to a reduction in operational energy consumption when the indoor thermal environment is more comfortable. It also can lead to an increase in operational energy consumption when the outdoor thermal environment is more comfortable.

For the HSCW zone of China, in the heating period, the indoor thermal environment is more comfortable compared to the outdoor thermal environment in most of time. In a certain range of insulation thickness, with the thicker insulation layer, the thermal transmittance of the external wall decreases, resulting in less heat loss from the indoor environment. As shown in Figure 4, within a certain range of ITEWB, the impact of the ITEWB on the thermal transmittance of the wall is reduced [68]. As a result, within a certain range of the ITEWB, with the increase of insulation thickness, the heating load of the building decreases and the reduction is smaller and smaller.

![Insulation thickness and thermal transmittance of the external wall](image)

**Figure 4.** Insulation thickness and thermal transmittance of the external wall of the case study building.

In the cooling period, compared to the heating period, there is more time when the outdoor thermal environment is more comfortable. In a certain range of the insulation thickness, with the increase of the ITEWB, for cities in the HSCW zone of China, the impact of the ITEWB on the cooling load is not obvious. Besides that, in some situations, where there is a long period that the outdoor environment is more comfortable compared to the indoor environment, the cooling load is increased with a thicker insulation layer [67].

The annual energy consumption of the building is determined by the sum of heating energy consumption and cooling energy consumption. As shown in Figure 5, for all these four cities in the HSCW, when the ITEWB increases from 30 mm to 150 mm, the annual operational energy consumption of the building decreases.

![Annual operational energy consumption](image)

**Figure 5.** Annual operational energy consumption for scenario continuous.
3.1.1. Impact of Different Cities on the Operational Energy Consumption

As shown in Figure 6, the different cities have different operational energy consumption and the effects of the ITEWB on these cities are different.

![Figure 6. Energy consumption of four cities for scenario continuous for: (a) Heating; (b) Cooling.](image)

This is because the meteorological data of these four cities is different. As shown in Table 6, Wuhan has the largest temperature difference between the indoor environment and outdoor environment based on the HDD and CDD. The annual operational energy consumption of building for Wuhan is the largest.

3.1.2. Impact of Different Operation Modes of Air Conditioners on the Operational Energy Consumption

As shown in Figure 7, the annual energy consumption under intermittent operation mode is less than that under continuous operation mode. Additionally, the annual operational energy consumption of the building is less sensitive to the ITEWB. This is mainly because, under the intermittent operation mode of air conditioners, the operation time of air conditioners is reduced, leading to less heat transfer in the heating and cooling period.

![Figure 7. Annual energy consumption for the continuous and intermittent scenarios for Wuhan.](image)

3.2. Result of the OTWRB for Four Cities

The parameters used in the methods described in Section 2.3 are listed in Table 12. These values are obtained from [15,17,23,30,69].
Table 12. Parameters used in the evaluation of the impacts of the ITEWB on building performance.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>i</td>
<td>1%</td>
<td>—</td>
</tr>
<tr>
<td>d</td>
<td>5%</td>
<td>—</td>
</tr>
<tr>
<td>$N_e$</td>
<td>20</td>
<td>year</td>
</tr>
<tr>
<td>$P_1$</td>
<td>13.50</td>
<td>—</td>
</tr>
<tr>
<td>$\rho$</td>
<td>30</td>
<td>kg/m$^3$</td>
</tr>
<tr>
<td>$C_{ins}$</td>
<td>600</td>
<td>yuan/m$^3$</td>
</tr>
<tr>
<td>$C_{op}$</td>
<td>0.52</td>
<td>yuan/kwh</td>
</tr>
<tr>
<td>$PED_{ins}$</td>
<td>3.95</td>
<td>kgce/kg</td>
</tr>
<tr>
<td>$PED_{OP}$</td>
<td>0.46</td>
<td>kgce/kwh</td>
</tr>
<tr>
<td>$GWP_{ins}$</td>
<td>5.64</td>
<td>kgCO$_2$eq/kg</td>
</tr>
<tr>
<td>$GWP_{OP}$</td>
<td>1.01</td>
<td>kgCO$_2$eq/kwh</td>
</tr>
</tbody>
</table>

### 3.2.1. The OTWRB When Considering Only One Criterion

As mentioned in Section 2.3.1, LCC is used for the economic indicator associated with the ITEWB. With the increase of ITEWB, on the one hand, the economic indicator associated with the operational energy decreases as the operational energy demand decreases. On the other hand, the economic indicator associated with insulation material increases linearly with the increase in the insulation material. Figure 8 shows the insulation thickness and the LCC for Wuhan. It shows that when insulation thickness is enlarged from 50 mm to 70 mm, the reduction in the operational energy cost outweighs the increase in the insulation material. However, when the ITEWB extends from 70 mm to 90 mm, the reduction in the energy cost cannot offset the increase in the insulation material. Thus, the lowest LCC is achieved at 70 mm.

![Figure 8. The ITEWB and the life cycle cost (LCC) for Wuhan under a continuous scenario.](image)

The LPED and LGWP are used for the energy and greenhouse gas emissions aspects of the ITEWB, as mentioned in Section 2.3. As shown in Figure 9, the PED of operational energy is a major part of the LPED related to the ITEWB, while the PED of insulation material is only a small part. Changes in insulation thickness determine the operational energy consumption, while the operational energy consumption determines the LPED associated with the ITEWB. The 150 mm ITEWB results in the least operational energy consumption and the least LPED.

The LGWP shows a similar trend as shown in Figure 10. The GWP of operational energy consumption comprises the overwhelming part of the LGWP related to the ITEWB. The 150 mm ITEWB results in the least operational energy and the least LGWP.

![Figure 9. The ITEWB and the life cycle primary energy demand (LPED) for Wuhan under continuous scenario.](image)

![Figure 10. The ITEWB and the life cycle global warming potential (LGWP) for Wuhan under continuous scenario.](image)
value tends to decrease early and then eventually rises. Such relations between the ITEWB and its LCC is also revealed by [15,17,23], the optimal economic ITEWB for these four cities is 70 mm in this case.

- Impact of different cities on the OTWRB when only considering one criterion

As shown in Figure 11, the LCC trend lines for all four cities exhibit similar trends, wherein the value tends to decrease early and then eventually rises. Such relations between the ITEWB and its LCC is also revealed by [15,17,23], the optimal economic ITEWB for these four cities is 70 mm in this case.

Figure 9. The ITEWB and the life cycle primary energy demand (LPED) for Wuhan under continuous scenario.

Figure 10. The ITEWB and the life cycle global warming potential (LGWP) for Wuhan under continuous scenario.

As shown in Figure 11, the LCC trend lines for all four cities exhibit similar trends, wherein the value tends to decrease early and then eventually rises. Such relations between the ITEWB and its LCC is also revealed by [15,17,23], the optimal economic ITEWB for these four cities is 70 mm in this case.

Figure 11. The ITEWB and the LCC for four cities under the continuous scenario.
As shown in Figures 12 and 13, when the ITEWB increases from 30 mm to 150 mm, the LPED and the LGWP decreases. The OTWRB, when only considering energy or greenhouse gas emissions factor is 150 mm for all these four cities.

The impacts of insulation thickness on the LCC, LPED and LGWP are most noticeable for Wuhan, which has the largest operational energy consumption and is less obvious for Chengdu which has the least operational energy consumption. This is because the reduction of energy consumption is more obvious for larger building operational energy consumers when the insulation thickness increases from 30 mm to 150 mm.

- Impact of different operation modes on the OTWRB when only considering one criterion

As shown in Figure 14, for both scenarios, within a certain range of the ITEWB, with the increase of the ITEWB, the life cycle cost associated with the ITEWB decreases to a certain value and then it starts to increase when the ITEWB beyond this value [18,70]. The optimal economic insulation thickness is less for intermittent operation mode than that for the continuous mode. Here are the reasons.

For the continuous operation mode, when the ITEWB increases from 50 to 70 mm, the reduction of operational energy cost result from the reduction of the operational energy consumption can make up for the 20 mm increase in insulation material investment. As a result, the total cost for 70 mm ITEWB is less than that for 50 mm ITEWB. However, for the intermittent operation mode, there is less operational energy consumption and there is less reduction in operational energy consumption. The reduction of operational cost cannot make up to the increase in insulation material investment. As a result, the total cost for 70 mm insulation thickness is more than that for 50 mm insulation.
3.2.2. The OTWRB When Considering Different Weighting Efficiencies

As shown in Figure 15, for these two different operation modes of air conditioners, with the increase of the ITEWB, the LPED and LGWP associated with the ITEWB decrease. For the intermittent scenario, the impact of the ITEWB on the operational energy consumption is less obvious, leading to less obvious variations in the LPED and LGWP compared to the continuous scenario.

Figure 15. Comparison of indicators associated with the ITEWB for two different operational modes of air conditioners of Wuhan: (a) Comparison of LPED; (b) Comparison of LGWP.

3.3.2. The OTWRB When Considering Different Weighting Efficiencies

As shown in Figure 16, the different weighting efficiencies of economy, energy and greenhouse emissions have a certain impact on the OTWRB. When there are fewer weighting efficiencies assigned to the economic criteria, the optimal insulation thickness tends to become larger.

- Impact of different cities on the OTWRB when considering different weighting efficiencies

Figure 16. OTWRB considering different weighting efficiencies of economy, energy and greenhouse emissions for Wuhan under the continuous scenario.
As shown in Figures 17 and 18, the OTWRB for different cities under continuous and intermittent operation modes of air conditioners are roughly the same.

![Figure 17](image_url)  
**Figure 17.** Impact of different cities on the optimal insulation thickness of external walls for residential buildings (OTWRB) when considering different weighting efficiencies of economy, energy, and greenhouse gas emissions under the continuous scenario.

![Figure 18](image_url)  
**Figure 18.** Impact of different cities on the OTWRB when considering different weighting efficiencies of economy, energy, and greenhouse gas emissions under the intermittent scenario.

The OTWRB for Wuhan is the largest while the OTWRB for Chengdu is the smallest for the same weighting system. This is because Wuhan has the largest operational energy consumption while the operational energy consumption for Chengdu is the smallest. As the impact of the increase of ITEWB is more obvious for larger energy consumers, the reduction in operational energy consumption in Wuhan is more than that in Chengdu. As a result, within a certain range of ITEWB, the net benefit by increasing ITEWB in Wuhan is more than that in Chengdu.

- Impact of different operation modes on the OTWRB when considering different weighting efficiencies

In Figure 19, for half of the various weighting systems, the OTWRB for two different operational modes of air conditioners are different. This is because of the certain assumption of the intermittent operation mode in this paper, resulting in differences in operational energy consumption between the continuous operation mode and the intermittent operation mode.
Figure 19. Impact of different operation modes of air conditioners on the OTWRB for Wuhan when considering different weighting efficiency: (a) Weighting 1; (b) Weighting 2.

4. Conclusion and Limitations

4.1. Conclusions

This study proposes a framework to analyze and select the OTWRB in the HSCW zone of China. The criteria for this selection consider the integrated impacts of the ITEWB on building performance quantified by LCC, LPED and LGWP. Hypothetical buildings are simulated with split air conditioners and using EPS as the insulation material in four typical cities of China, which are chosen as Wuhan, Changsha, Hangzhou and Chengdu. Two different operation modes of air conditioners (intermittent and continuous) are considered in this paper. The main findings of this study are as follows:

- For the continuous operation mode of air conditioners in Wuhan, the optimal economic insulation thickness is 70 mm. When considering only the aspects of energy consumption and greenhouse gas emissions, the optimal value is 150 mm. For different weighting efficiencies assigned to the economy, energy and greenhouse gas emissions, the OTWRB is determined to be 70, 90, 110, or 150 mm. For all these weighting systems, the OTWRB is larger than the current insulation thickness, which is 30 mm.
- When the weighting efficiencies assigned to the economy, energy and greenhouse gas emissions change, the OTWRB might also change. In this paper, when the range of insulation thickness is 30 mm to 150 mm, the minimum OTWRB is achieved when the economic factor is the only criterion. On the other hand, the maximum OTWRB is obtained when sufficient weighting efficiencies are assigned to the energy and greenhouse gas emissions factors. When larger weighting efficiencies applied to the energy and greenhouse gas emissions factors, the OTWRB did not become smaller.
- The different operation modes of air conditioners have a certain impact on the OTWRB based on the results of this study.
- The OTWRB is almost the same for these four cities based on the results of this study. The OTWRB is found to be the largest for Wuhan, which consumes the most operational energy, and smallest for Chengdu, which consumes the least operational energy for the same weighting system.

4.2. Limitations

There are still some areas in need of improvement for future research:

- The impact of different kinds of intermittent operation modes of space heating and cooling systems on the OTWRB is not considered in this paper.
- A general formula to optimize ITEWB related to meteorological data is not provided in this paper.
Author Contributions: Conceptualization, methodology, software, validation, formal analysis, investigation, resources, data curation, writing—original draft preparation, X.C.; supervision, X.L. and M.S. For research articles with three authors, all authors have read and agreed to the published version of the manuscript.

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