Correlation between Dielectric Loss and Partial Discharge of Oil-Pressboard Insulation

Yan Li 1, Min Li 2 and Jun Xie 1,*

1 School of Electrical and Electronic Engineering, North China Electric Power University, Baoding 071003, China; yan.li@ncepu.edu.cn
2 State Grid Baoding Electric Power Company Limited, Baoding 071000, China; 317571076@qq.com
* Correspondence: junxie@ncepu.edu.cn

Abstract: Dielectric loss tanδ and partial discharge (PD) are important indicators for status assessment of oil-pressboard insulation. The correlation characteristics between these two parameters has significance for understanding the material’s degradation and helps to eliminate the information asymmetry for diagnostics. In this paper, the symmetric experimental platform is set up to measure the dielectric loss tanδ and PD for oil-pressboard insulation following the designed procedure consisted of raised and rested voltages. Three sets of samples with different water content were tested. The variation mechanism of tanδ with voltage is explained by proposed equivalent circuit, which introduced an asymmetric component representing defect part. PDs are found to be symmetric in the sinusoidal voltage cycles and their statistical parameters are calculated. Besides, the correlation between dielectric loss difference from raised voltage to rested voltage and PD is researched. Strong correlation is observed between dielectric loss and PD, which offers degradation insight for oil-pressboard insulation and helps to eliminate information asymmetry for material status diagnostics.

Keywords: correlation; dielectric loss; oil-pressboard insulation; partial discharge

1. Introduction

Oil-pressboard insulation material is widely used in transformers, bushings, capacitors, etc. [1–3]. Dielectric loss tanδ and partial discharge (PD) are the two parameters that are used to assess the insulation status [4–6]. As early as 1976, Takahashi E. et al. analyzed the PD characteristics for oil-paper under DC and AC voltages [7]. Later on, researchers studied the PD features under surge voltage [8,9]. Besides the recorded time-resolved data, statistical parameters are used for PD analysis [10,11]. Regarding dielectric loss, besides its own diagnostic function for insulation materials, Ruan J. et al. developed the inversion algorithm to obtain the oil-immersed paper resistivity from dielectric loss for insulation status assessment [12]. Frequency domain spectroscopy measurement is further developed based on dielectric loss to diagnose oil-pressboard [13].

The water content in the oil-pressboard may influence its insulation status, leading to different dielectric loss and/or PD behavior [14–16]. Przybylek P. et al. investigated the influence of cellulose insulation ageing and moistening on dielectric losses [17]. Cui Y. et al. proposed a distributed parameter model to reveal the correlation between moisture distribution and the dielectric response parameters of cellulose insulation [18]. Liao R. et al. performed quantitative diagnosis of moisture content in oil-paper insulation based on frequency domain spectroscopy [19].

The relation between PD and water ingress is also researched. Rowland S.M. et al. measured the PD development for wet oil-paper [20]. Ramya M. et al. found that water in pressboard papers makes the partial discharge inception voltage (PDIV) low and the PD occurred frequently, quickly leading to breakdown [21]. Župan T. et al. designed a capsule
that can be used in the assessment of water content influence on the condition of the oil-paper insulation [22]. Jiang J. et al. reported that there is a sharp reduction of PDIV or a sudden increase of PD intensity due to moisture in oil-paper insulation [23].

Although great effort has been devoted into oil-pressboard characteristics, to characterize its degradation based on single parameter, e.g., dielectric loss or PD, may create information asymmetry and lead to an incorrect result. Understanding their correlation offers insight into material’s degradation mechanism and new tools for diagnostics, which helps to eliminate the information asymmetry in material assessment. This paper focuses on the correlation between dielectric loss tanδ and PD for oil-pressboard material, which was seldom researched by previous scholars. Parameters with strong correlation are identified in this paper, and the dielectric loss dependency upon PD is explained. The scientific goal is to explore the comprehensive degradation characteristics of oil-paper insulation and understand its mechanism, which is helpful for insulation/equipment condition diagnostics. In this paper, the oil-pressboard samples with different water content were prepared in this paper. The dielectric loss and PD for oil-pressboard insulation are measured simultaneously and their correlation is discussed.

This paper is organized, as follows. Section 2 describes the test setup. Section 3 gives the result of dielectric loss tanδ and PD separately for three samples with different water content. Section 4 discussed the correlation between these two parameters. Sections 5 provides conclusions.

2. Test setup and Measurement Procedure

2.1. Test Setup

The test model of oil-pressboard insulation was constructed, as in Figure 1, based on symmetry principle. The voltage electrodes are round plates with 400 mm diameter for high voltage and 500 mm diameter for grounding electrode, as in Figure 1a. The tested square oil-pressboard is from Weidmann and it has side length of 480 mm and 2 mm thickness, as in Figure 1b.

![Figure 1. Schematic show and constructed setup for testing. (a) Schematic of test setup; (b) Picture of test setup.](image)

2.2. Sample Preparation

The samples were prepared as in Figure 2. After cutting and drying, the samples are humidified to have different water content. The samples are weighed hen the humidifying process is finished. With the weight difference, water content is calculated. It is obtained that the water contents for sample B and C are 2.4% and 3.8% separately. While A is the sample without water. More than three samples for each category (A, B, C) were prepared. However, only one test result for each is shown here since they are similar.
Cutting to desired size

Vacuum drying

paper pressboard A

humidifying for 4h

Oiled in vacuum

oil-paper pressboard sample A

Figure 2. Sample preparation with different water content.

2.3. Data Extraction

Figure 3 shows the setup. The rated voltage of testing transformer is 110 kV and its apparent discharge is less than 5 pC. The protection resistor is 10 kΩ. The ratio of voltage divider is 1500:1. A high frequency current probe (HFCT) is used to measure the PD signal. The bandwidth of HFCT is 100 kHz–100 MHz with 1 pC sensitivity. The dielectric loss is characterized by tan δ, which is calculated as (1) by measuring the applied voltage and leakage current, where \( \phi_i \) is the current phase for 50 Hz and \( \phi_u \) is the voltage phase for 50 Hz. The calculation is performed based on FFT spectrum analysis. The Blackman–Harris window and interpolation technique were applied to eliminate the picket fence effect and leakage spectrum’s effect on FFT, as in [24].

\[
\tan \delta = \tan \left[ \frac{\pi}{2} - (\phi_i - \phi_u) \right]
\]

(1)

Figure 3. Setup of partial discharge and tanδ measurement.

The leakage current is measured with microammeter, whose measurement range is from 100 μA to 700 mA and angle error is within ± 0.01°. The partial discharge detector’s sampling frequency is 1 MHz. The test setup fulfills IEC60270. Shielding is considered in the laboratory to guarantee a noise level lower than 5 pC. Dedicated error analysis can be nontrivial [25] and out of the scope of this paper.

Corresponding to Figure 4, the testing procedure is designed, as following:

1. apply 2 kV under which there is no PD. Record voltage and current signal for tanδ calculation;
2. increase voltage with 1 kV step and keep it stable for 1 min;
3. record PD and tanδ data for 5 min. Tanδ data is registered each 30 s, thus 10 data are gathered in 5 min. PD is measured every 6 s with recording length of 20 ms, leading to 50 data;
4. decrease the voltage to 2 kV and keep it for 1 min.;
5. keep the voltage to be 2 kV for 2.5 min while gathering tanδ data. 5 data are recorded with 30 s time step; and,
6. repeat 2–5 until the voltage reaches 0.8 × U₀ (flashover voltage). For sample group A, the stop voltage is 16 kV. For sample group B and C, the stop voltages are 14 kV and 12 kV.

Figure 4. Setup of partial discharge and tanδ measurement.

3. Dielectric Loss and Partial Discharge Statistical Parameters

In order to study the correlation between PD and tanδ, firstly their own statistical parameters are analyzed, as below.

3.1. PD Statistical Parameters

Table 1 lists the derived parameters, provided that \( H_n(q) \) is the phase-resolved data consisted of charge transfer \( q \), and discharge rate \( n \).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Unit</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>( q_t )</td>
<td>pC</td>
<td>total discharge magnitude</td>
</tr>
<tr>
<td>( n_t )</td>
<td>-</td>
<td>total number of discharges</td>
</tr>
<tr>
<td>( q_{avg} )</td>
<td>pC</td>
<td>mean discharge magnitude</td>
</tr>
<tr>
<td>( q_{max} )</td>
<td>pC</td>
<td>maximum discharge magnitude</td>
</tr>
<tr>
<td>( \sigma )</td>
<td>°</td>
<td>mean pulse width of discharge</td>
</tr>
<tr>
<td>( Sk )</td>
<td>-</td>
<td>skewness of ( H_n(q) )</td>
</tr>
<tr>
<td>( Ku )</td>
<td>-</td>
<td>kurtosis of ( H_n(q) )</td>
</tr>
<tr>
<td>( \alpha )</td>
<td>-</td>
<td>Weibull scale parameter of ( H_n(q) )</td>
</tr>
<tr>
<td>( \beta )</td>
<td>-</td>
<td>Weibull shape parameter of ( H_n(q) )</td>
</tr>
</tbody>
</table>

Figure 5a shows the total discharge magnitude \( q_t \). Partial discharge increased with voltage and higher water content leads to more discharge. Mean discharge magnitude and maximum discharge magnitude with voltage are shown in Figure 5b, c with a similar trend.

Figure 6a shows the total number of discharges, which indicates that the voltage increase firstly enhanced the PD number and then hindered it. For the increase part, the
water content did not have significant effect on the result. However, in the PD decrease part, water content lowered the PD occurring. Figure 6b is the mean width of discharge variation with voltage. It can be seen that, with the increase of voltage, the discharge duration firstly increased and then decreased. For the increase part, water content has positive effect on the pulse duration.

Figure 7a,b show the skewness and kurtosis of $H(q)$. These two variables decreased with voltage, while water content also lowered the values. Figure 8 plots the Weibull parameters of $H(q)$. Figure 8a clearly shows that water content affected the scale parameter $\alpha$ above 7 kV. Higher water content referred to bigger $\alpha$. Figure 8b shows the shape parameter $\beta$. For samples with water content, $\beta$ shows a moderate decrease with the voltage. In contrast, this parameter increases a bit with voltage for samples without water.

Figure 5. (a) Relation between total discharge magnitude and voltage; (b) Relation between mean discharge magnitude and voltage; (c) Relation between maximum discharge magnitude and voltage.

Figure 6. (a) Relation between total number of discharges and voltage; (b) Relation between mean pulse width of discharge and voltage.
3.2. Tanδ Statistical Parameters

The average tanδ from step 3 and 5 in Section 2.3 was calculated and is shown in Figure 9. This value increased with voltage and water content. Additionally, there is clear difference for tanδ between Figure 9a,b, which indicates the dielectric loss variation before and after the voltage application.

The difference between these two tanδ is obtained as Equation (2) and it is shown in Figure 10, where tanδ\text{U} is the result in Figure 9a and tanδ\text{2kV} is the result in Figure 9b. It can be seen that the voltage had positive effect on tanδ increase. While under the same voltage, tanδ increase has a positive dependency on water content.

\[ \Delta \tan \delta = \tan \delta^U - \tan \delta^\text{2kV} \] (2)
Figure 10. Dependency of Δtanδ with voltage.

To analyze the tanδ result, an equivalent circuit, as in Figure 11, is proposed. The grey block represents the defect area. The dielectric can be modeled by the double layer structure, as in the left figure of Figure 11, where layer I has defect and its equivalent parameters are R₁, C₁ while layer II has no defect with equivalent parameters R’ and C’. Obviously, these two layers have different equivalent parameters. Layer II without defect has better insulation capability than layer I with defect. Thus, R’ >> R₁, and R’ can be neglected, leading to the circuit in the right part of Figure 11. When voltage U₀ is applied, current can be deduced as:

\[ I = U_0 \frac{\omega^2 C^2 R_1 + \frac{1}{\omega^2 C'}}{1 + \omega^2 (C_1 + C')^2 R_1^2} \]  \hspace{1cm} (3)

here \( \omega = 2\pi f \) and \( f \) is frequency.

Based on Equation (3), tanδ can be expressed as:

\[ \tan \delta = \frac{\frac{1}{\omega R_1 C_1}}{\frac{1}{C_1^2} + \frac{1}{\omega^2 C'_1 R_1^2}} + \frac{\tan \delta_d}{H(1 + \tan \delta_d) + 1} \]  \hspace{1cm} (4)

where \( H = C_1/C' \) and it is defined as defect factor. When the defect is enlarged, \( C_1 \) decreases (layer I gets thicker) and \( C' \) increases, which makes \( H \) smaller. \( \tan \delta_d \) is the dielectric loss for defect part. When \( \tan \delta_d \) is constant, \( \tan \delta \) is reversely related with \( H \). Figure 12 shows the dependency of tanδ with tanδ_d and \( H \), where \( H_1 < H_2 < H_5 \).
Figure 12. Tanδ of insulation characteristic upon defect factor $H$ and tanδ.

Figure 13 is the tanδ characteristic of sample A. Figure 13a is the measured result and Figure 13b is the ideal tanδ curve for sample A based on Figure 12. When the voltage was lower than 6 kV, PD did not show up severely, both tanδ and $H$ did not vary much, making tanδ increase gently. For the voltage from 7 kV–12 kV, due to PD’s effect, the defect’s dielectric loss tanδ increased. Yet, the defect area did not increase much, which means that $H$ did not change. This can be confirmed by the rather stable curve for sample A in in Figure 9b between 7 kV and 12 kV (after voltage application, dielectric loss did not change). Thus, tanδ increased sharply in this range. For voltage above 12 kV, $H$ decreased, which can be seen in Figure 9(b) for the rise above 12 kV. Additionally, tanδ increased due to continuous PDs. The combined effect changed the curve from $A$ to $B$, then to $C$, as in Figure 13b.

For sample B and C, the tanδ characteristic is analyzed in Figure 14 by taking sample B as an example. There is a tuning point of about 8 kV. This can be explained as tanδ’s increase surpassed the peak, as in Figure 12, due to water effect. If $H$ keeps constant, then the curve decreased (from 8 kV to 10 kV in Figure 14a and point $A$ to $B$ in Figure 14b). With the continuous voltage rise, PD enlarged the defect and lowered the defect factor $H$. Together with the increase of tanδ due to PD’s effect, the curve shown in Figure 14a increased above 10 kV and the curve in Figure 14b changed from $B$ to $D$. 
4. Correlation between PD and Tanδ

The correlation between PD and tanδ is studied by Pearson’s coefficient. For vector $x = (x_1, x_2, \ldots, x_n)$ and $y = (y_1, y_2, \ldots, y_n)$, Pearson’s coefficient is calculated, as below:

$$
r = \frac{\sum_{i=1}^{n} (x_i - \bar{x}) (y_i - \bar{y})}{\sqrt{\sum_{i=1}^{n} (x_i - \bar{x})^2 \sum_{i=1}^{n} (y_i - \bar{y})^2}}
$$

when $r$ is 1, the two vectors are completely positively correlated. When $r$ is −1, the two vectors are completely negatively correlated.

4.1. Correlation between PD and Tanδ Statistical Parameters

Table 2 lists the calculated correlation coefficients. All of the shown absolute values are above 0.7, which indicates strong correlation. The detailed data are listed in Figure 15. As in the Figure, although disturbance is observed, correlation is clear between dielectric loss and PD.

<table>
<thead>
<tr>
<th></th>
<th>$q_t$</th>
<th>$m_t$</th>
<th>$q_{avg}$</th>
<th>$q_{max}$</th>
<th>$\sigma$</th>
<th>$Sk$</th>
<th>$Ku$</th>
<th>$\alpha$</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>0.728</td>
<td>-0.734</td>
<td>0.767</td>
<td>0.712</td>
<td>0.962</td>
<td>-0.734</td>
<td>-0.818</td>
<td>0.718</td>
</tr>
<tr>
<td>B</td>
<td>0.804</td>
<td>-0.709</td>
<td>0.819</td>
<td>0.809</td>
<td>0.871</td>
<td>-0.762</td>
<td>-0.812</td>
<td>0.744</td>
</tr>
<tr>
<td>C</td>
<td>0.837</td>
<td>-0.708</td>
<td>0.808</td>
<td>0.796</td>
<td>0.847</td>
<td>-0.770</td>
<td>-0.837</td>
<td>0.766</td>
</tr>
</tbody>
</table>

(a) tanδ characteristic of sample B; (b) schematic ideal tanδ characteristic for sample B.
Figure 15. (a) Total discharge magnitude with tanδ; (b) Total number of discharges with tanδ; (c) Mean discharges magnitude with tanδ; (d) Maximum discharges magnitude with tanδ; (e) Mean pulse width of discharge with tanδ; (f) Skewness of \( H_n(q) \) with tanδ; (g) Kurtosis of \( H_n(q) \) with tanδ; and, (h) Weibull coefficient of \( H_n(q) \) with tanδ.

4.2. Correlation between PD and \( \Delta \tan \delta \)

Because no PD was observed when the voltage was lowered to 2 kV, as in Figure 4, \( \Delta \tan \delta \) can be regarded as the effect the PD during voltage rise.

Tanδ is derived from 50 Hz voltage and current. When there is PD containing 50 Hz component, it will affect the tanδ result. Thus, the 50 Hz component was taken from the PD signal and normalized. The result is compared with tanδ and shown in Figure 16. It can be seen that there is strong correlation between these two variables.
Figure 16. Comparison between tanδ and normalized 50 Hz component from PDs. (a) is for sample A, (b) is for sample B, and (c) is for sample C.

This correlation can be further observed in Figure 17, where a linear relation is shown. To further analyze this phenomenon, PD is simulated based on measured data. Figure 18 shows the typical recorded waveform of PD with reference voltage. The PDs occurred at 0–90° and 180–270°, and they were basically symmetric in the positive and negative cycles. With increase of applied voltage, PD grew, and it covered wider phase range, as in Figure 18b as compared with Figure 18a. For case of ease, the following assumptions are taken for simulated PDs:

1. PDs occur symmetrically with respect to positive and negative cycles;
2. square wave is used to simulate PDs;
3. all PDs have the same amplitude, duration and repetition rate; and,
4. in the positive cycle, the PDs are centered at 45°, while, in the negative cycle, the PDs are centered at 225°.

Figure 17. Relation between Δtanδ and normalized 50 Hz component from PDs.
Figure 18. (a) Measured PD signal with reference voltage; (b) Measured PD signal with higher reference voltage.

Figure 19 shows the simulated PDs. Three simulation tests are performed.

1. PD amplitude A is set to 1. PD duration is set to be 10 μs. The time interval between each PD is 20 μs. The number of PDs is set to be 20, 40, and 60. Their effect to the frequency component is analyzed, as in Figure 20. It shows that, with the increase of PD number, the 50 Hz component is also increased.

2. PD duration is set to be 10 μs. The time interval between each PD is 20 μs. The number of PDs is set to be 20. While PD amplitude A is set to be 1–3. Their effect on the frequency component is analyzed, as in Figure 21. Additionally, the amplitude rise will increase the 50 Hz component.

3. PD amplitude A is set to 2. The time interval between each PD is 20 μs. The number of PDs is set to be 40. While PD duration varies as 10 μs, 20 μs, and 30 μs. Their effect on the frequency component is analyzed, as in Figure 22. Again, the duration enlargement will increase the 50 Hz component.

Figure 19. Simulated PDs with reference voltage.

Figure 20. Total number of discharge effect on PD’s amplitude-frequency result.
5. Conclusions

For oil-pressboard insulation, the discharge magnitude rises with voltage and water content. Dielectric loss $\tan \delta$ increased with voltage. However, there is saturation. For oil-pressboard with water, $\tan \delta$ can even decrease with voltage. An equivalent circuit model is proposed to explain this characteristic, which shows that $\tan \delta$ is dependent on defect area and the dielectric loss of defect part.

Dielectric loss $\tan \delta$ is correlated with PD, specifically with total discharge magnitude, total number of discharges, average discharge magnitude, maximum discharge magnitude, average pulse duration of discharge, Weibull scale parameter, skewness, and kurtosis of phase-resolved data consisting of charge transfer and discharge rate. The dielectric loss difference that is obtained from $\tan \delta$ at raised voltages and rested 2 kV is almost linearly correlated with and contributed by 50 Hz component of PDs.

The strong correlations between dielectric loss and PD, especially between the dielectric loss difference and 50 Hz component of PDs, improves the degradation’s understanding and provides a diagnostic tool for oil-pressboard that helps to eliminate the information asymmetry from single parameter. With the derived data and model, one can observe the correlation between $\tan \delta$ and PD, with which further study of the degradation process of the oil-pressboard insulation material can be performed, and a multi-source information fusion insulation evaluation technique can be developed to improve the power equipment assessment level.

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