

Article

Pore Characteristics and Their Effects on the Material Properties of Foamed Concrete Evaluated Using Micro-CT Images and Numerical Approaches

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Abstract: Foamed concrete contains numerous pores inside the material, and these pores are a significant factor determining the material characteristics. In particular, the pore distribution characteristics of foamed concrete significantly affect its thermal and mechanical properties. Therefore, an appropriate investigation is necessary for a more detailed understanding of foamed concrete. Here, a set of foamed concrete samples with different densities is used in order to investigate the density effects on the pore characteristics, as well as the physical properties of the materials. The pore distribution characteristics of these samples are investigated using an X-ray micro-computed tomography (micro-CT) imaging technique with probabilistic and quantitative methods. Using these methods, the anisotropy, the pore circularity factor and the relative density of cell thickness are examined. The thermal (thermal conductivity) and mechanical (directional modulus and strength) properties of each foamed specimen are computed using numerical simulations and compared with experimental results. From the obtained results, the effects of the pore sizes and shapes on the local and global properties of the foamed concrete are examined for developing advanced foamed concrete with lower thermal conductivity by minimizing the strength reduction.

Keywords: foamed concrete; pore characteristics; micro-CT; probability function; physical property

1. Introduction

Foamed concrete is a material classified as cellular lightweight concrete with entrained air voids. Foamed concrete is a versatile material with high flowability, low cement content and high thermal insulation [1–3]. Since energy efficiency has become an important issue in the civil construction engineering fields, foamed concrete has been widely produced and used as a promising building material due to its low energy consumption and high energy-saving characteristics [4,5].

Foamed concrete is basically a porous material, and it contains numerous pores inside the material. The pore structure inside the material strongly affects the cell (solid) structure, as well as its characteristics and properties [6–8]. Like other types of concrete [9–11], the material properties of foamed concrete are significantly affected by the pore characteristics, and many studies have been reported about the pore characteristics of foamed concrete over the past few years. Kearsley and Wainwright [12] examined the porosity effect on the mechanical property of foamed concrete, and Hilal et al. [13] investigated the size distribution of the entrained pores in foamed concrete. Wei et al. [14,15] characterized and simulated the microstructure of foamed concrete. In particular, Narayanan and Ramamurthy [16], as well as Hilal et al. [17] examined the pore structure inside

foam concrete and demonstrated that porosity is not sufficient to regulate the characteristics of foam concrete, and other pore characteristics, such as pore size, size distribution, shape and cell thickness, should also be considered for more detailed understanding of foam concrete material. In spite of this significance, the investigation of the relationship between the spatial distribution of pores and the physical properties of foamed concrete (i.e., thermal conductivity, elastic modulus and compressive strength) has rarely been performed.

In this study, the correlation between the pore characteristics and material responses of foamed concrete is investigated using both numerical and experimental approaches. Particularly, the effects of local pore characteristics on the physical properties are examined from foamed concrete samples with different densities at the microstructure level. For that purpose, a set of foamed concrete samples with very low densities are produced by using the LithoFoam[®] (Luca Industries International, Berlin, Germany) foam agent. In general, the pores in foamed concrete are secured by using either the pre-foaming or mix foaming methods [2,17]; the foamed concrete specimens used in this study are generated using the pre-foaming method.

Pores in foamed concrete have a role to enhance the insulation effect, while the compressive strength and elastic stiffness decrease as the porosity increases. Thus, an appropriate investigation of the pore structure is required for better understanding the property characteristics of foamed concrete. Here, the pore distributions within foamed concrete samples are described using X-ray micro-computed tomography (micro-CT), which is a nondestructive method. From the micro-CT, a set of 2D images of a sample with pixel sizes in the micrometer range can be produced by X-rays without damaging the specimen [18,19]. To classify the pores and the specimen, the image processing of converting the original CT images into binary images is utilized. Then, a 3D binary image of the sample is obtained by subsequent stacking of the converted cross-sectional images. In particular, a modified watershed 3D algorithm is used here for segmentation and identification of the pores with irregular shapes.

For the characterization of the pore and cell characteristics of the foamed concrete specimens, probabilistic and quantitative methods are used. Probabilistic functions, two-point correlation [20–22] and lineal-path [23,24] are used here for the description of the pore characteristics. These functions can be utilized to describe the clustering level of pores and continuous connectivity using the limited information. In addition, the local pore/cell distributions in the foamed concrete specimen are described to examine the correlation of the local pore characteristics and the behavior of the material [25,26].

The physical properties of foamed concrete specimens are measured experimentally using the Hot Disk instrument compatible with the ISO standard (22007-2) [27]. A finite element (FE) simulation is also conducted to evaluate the numerical properties. Then, the relationship between the material properties (i.e., thermal conductivity and strength) and the pore characteristics (i.e., pore size distribution, pore shape and anisotropy) is investigated. Using the foamed concrete samples with different densities and their obtained material characteristics, the effect of the pore characteristics on the material responses of foam concrete is examined.

2. Preparation of Foamed Concrete Specimens

Foam concrete materials with different densities are prepared to investigate the effect of the pore characteristics on the material properties. Foamed concrete specimens with 100-, 200-, 450- and 600-kg/m³ densities are produced by Luca Industries International with the LithoFoam[®] (Luca Industries International, Berlin, Germany) foam agent, and each specimen is denoted here as LithoPore[®]100, LithoPore[®]200, LithoPore[®]450 and LithoPore[®]600, respectively. Foamed specimens are generated by the pre-foaming method, which uses cement-based mix and preformed foam agent. These components are prepared separately and mingled by blending the produced foam into the cement mix. The foam agent used here consists of synthetic protein with a network former and stabilizer, and a foam concrete with very low density, but relatively high strength compared to other

types of foam concrete can be generated by using this foam agent [28]. General information about the mix design of the specimens given by the manufacturer is shown in Table 1. Here, ordinary Portland cement CEM I 42.5R is used, and the water/cement (binder) ratio is 0.45 for all specimens.

Table 1. Mix design for foam concrete specimens.

Specimen	LithoPore®100	LithoPore®200	LithoPore®450	LithoPore®600
Target (dry) density (kg/m ³)	100	200	450	600
Wet density (kg/m ³)	150–158	305–315	530–545	710–760
Cement content (kg/m ³)	61	170	215	285
Water (kg/m ³)	28	77	125	225
Foam content (kg/m ³)	67.2	64.3	59.2	52.0
Filler (fly ash and calcium carbonate) (kg/m ³)	-	-	95	215
Network former LithoFoam® (kg/m ³)	6	5	5	4
Stabilizer LithoFoam® (kg/m ³)	0.6	0.6	0.6	0.6

Foamed concrete specimens with different densities are presented in Figure 1. Here, all of the measurements of the pore characteristics, properties and their correlations are performed using these samples. Each specimen is cut into about a 30-mm cube for effective measurements of thermal properties. After measurement of the properties, all of the specimens are cut into 10-mm cubes for micro-CT and scanning electron microscope (SEM) imaging for high-resolution micro-CT and SEM images with optimized sample size.

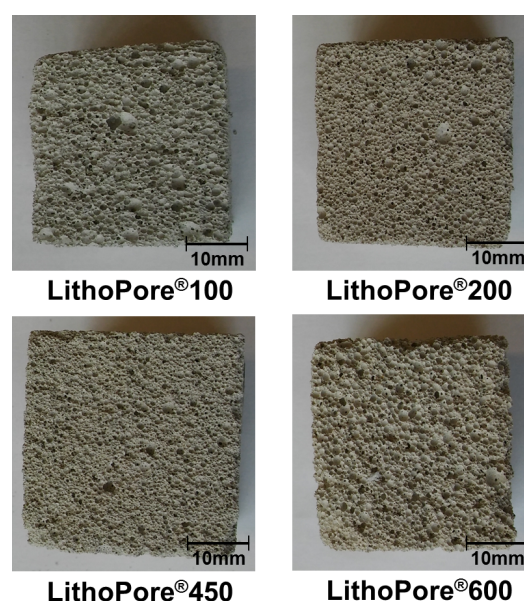


Figure 1. Foamed concrete specimens with different densities.

3. Micro-CT Image and Characterization of the Pore Structure

3.1. SEM and Micro-CT Imaging Method

The morphology of foamed samples can be investigated with different descriptive approaches. For example, secondary electron (SE) images of the foamed concrete specimens in Figure 2, which are performed by SEM, can be used. In these images, numerous spherical pores with different sizes in each specimen can be identified. Moreover, as shown in Figure 3, typical components of cement-based materials, such as C–S–H (calcium silicate hydrates), portlandite (calcium hydroxide) and ettringite, can be identified using the SEM images at acceptable magnification. Focusing on the cement paste, it is clear that the hydration degrees of the specimens are in a relatively early state, and the hardness

will further increase with increasing hydration time. Comparing the amount of C-S-H contents in the lower density samples with those in the higher density samples in Figure 3, the hydration process is more advanced at higher density samples, and the phase composition influences the material strength; this indicates that the thickness of the solid wall, as well as the degree of hydration can affect the strength and thermal property of materials with increasing densities. However, SEM images can only provide the pore characteristics on the surface of the specimen, and the specimens can be easily damaged during the preparation process.

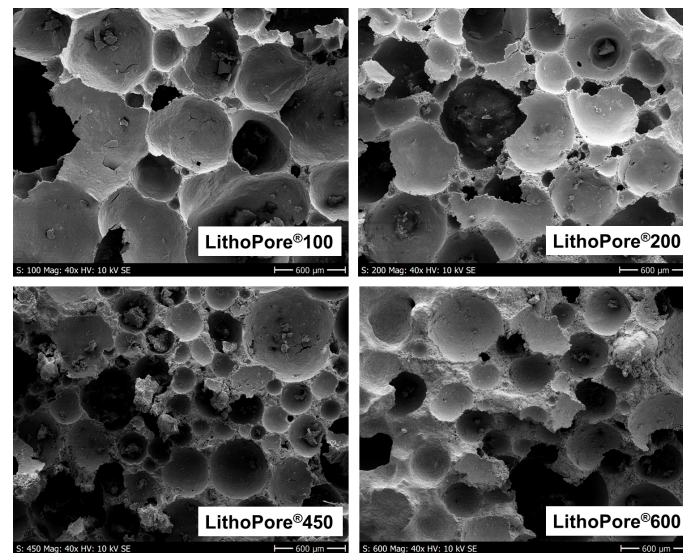


Figure 2. SEM images of the foamed concrete specimens with different densities.

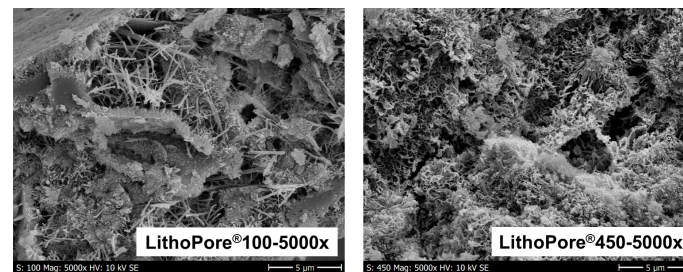


Figure 3. SEM images of LithoPore®100 (density = 100 kg/m³) and LithoPore®450 specimens (density = 450 kg/m³) at 5000× magnification.

In this study, for more detailed examination of the pore characteristics inside the samples, micro-CT images are utilized to examine the pore sizes and distributions of the foamed concrete non-destructively and noninvasively. Figure 4 shows the process of the micro-CT imaging. The first and second figures in Figure 4 are the original eight-bit and region of interest (ROI) of the micro-CT image, respectively. To classify the pores inside the foamed specimen, the cross-sectional binary images are generated by using a proper threshold. Before binarizing the original image, the Bronnikov algorithm [29] is used to improve the micro-CT image contrast. The threshold here is selected based on the Otsu method [30] and experiments. In the original image, a set of pixels that have lower values than the threshold are considered as pores. The binary image is composed of 1000 × 1000 pixels. In the binary image in Figure 4, the white parts represent the voids, and the black parts represent the solid part (cell wall) of the foamed specimen. The 3D binary model of the foamed sample in Figure 4 is obtained by stacking 1000 binarized images.

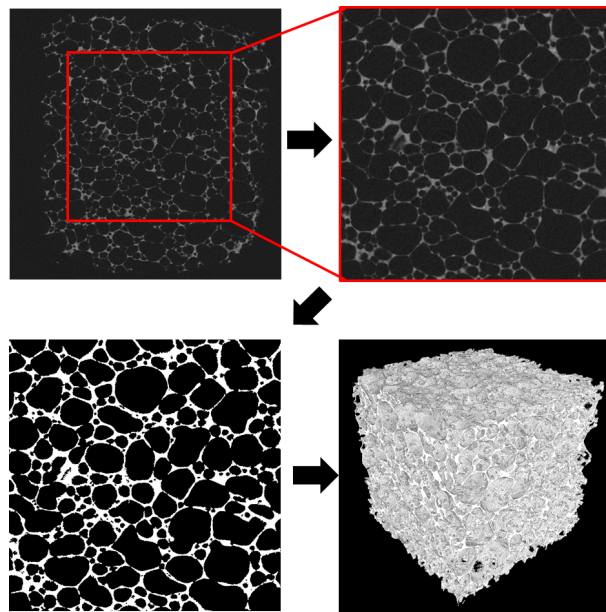


Figure 4. Creation of a 3D binary model using micro-CT images (note: in the binary image, the white represents solid, and the black represents pore).

In addition to the binary imaging, an image segmentation is conducted to enhance the micro-CT image segmentation quality. In Figure 4, some solid parts of the foamed specimen are neglected or faintly described due to the limitation of image resolution. To overcome this phenomenon, a watershed segmentation process is adopted here. The watershed segmentation is an imaging method to visualize a gray level image into its topographic representation [31–33]. In general, the Euclidean or chessboard distance transformation is used for the preprocess of the watershed segmentation; however, these methods have limitations for detecting an object with an irregular shape. Here, the quasi-Euclidean distance transformation is utilized to describe the pores with irregular shapes in the foamed concrete; this algorithm is the method that can measure the total Euclidean distance along a set of horizontal, vertical and diagonal line segments, and even irregular particles can be detected using this method [34]. Figure 5 is the visualization of the watershed segmentation with the quasi-Euclidean distance transformation for the binary image of the foamed specimen. In Figure 5, both circular and irregularly-shaped pores are effectively described, and the neglected solid parts are also reconstructed. The watershed segmentation used here can be also adopted for 3D image data, and more accurate information on the pore shape and size distribution can be obtained using the adjusted image segmentation. In this study, the image toolbox in MATLAB [35] is used for the binarization and segmentation of the micro-CT images.

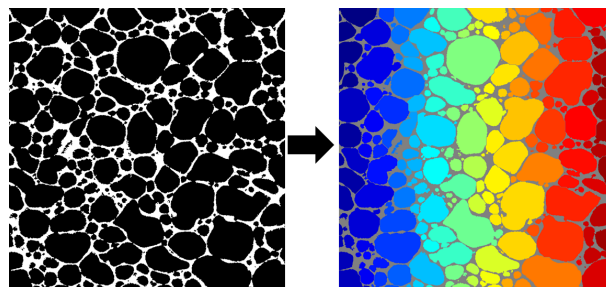


Figure 5. Classification of pores by means of watershed transformation (note: in the right figure, each color denotes a distinct pore).

3.2. Probabilistic and Quantitative Characterization Methods

3.2.1. Low-Order Probability Functions

For the characterization of the pore distribution of the foamed concrete samples, probabilistic methods can be used. Here, two types of probabilistic functions, two-point correlation and lineal-path, are used to characterize the pore distribution within the foamed samples. These probabilistic functions are shown to be effective in describing the spatial distributions of pores [11,20,36]. The two-point correlation function for a pore phase, $P_{pp}(r)$, is the probability that any two randomly-placed points are positioned in the pore region (Figure 6a); this function is utilized to characterize the clustering level of pores [20,22]. The probability of placing both points in the pore region converges to the porosity as the distance between two points approaches zero, and $P_{pp}(r)$ approaches the product of the porosity as r increases as:

$$\lim_{r \rightarrow 0} P_{pp}(r) = f_p, \quad \lim_{r \rightarrow \infty} P_{pp}(r) = [f_p]^2 \quad (1)$$

where f_p is the porosity of the foamed specimen.

The lineal-path function, $L_p(r)$, is also used to describe the pore distribution, and this function can be used as a compensation function of $P_{pp}(r)$ for the different pore characterizations. $L_p(r)$ is the probability of finding a whole random line with length r positioned in the pore region and can provide information about the continuous connectivity of the pores [20,23]:

$$\lim_{r \rightarrow 0} L_p(r) = f_p, \quad \lim_{r \rightarrow \infty} L_p(r) = 0 \quad (2)$$

In the general limits $L_p(r)$, the function converges to zero as the line length increases.

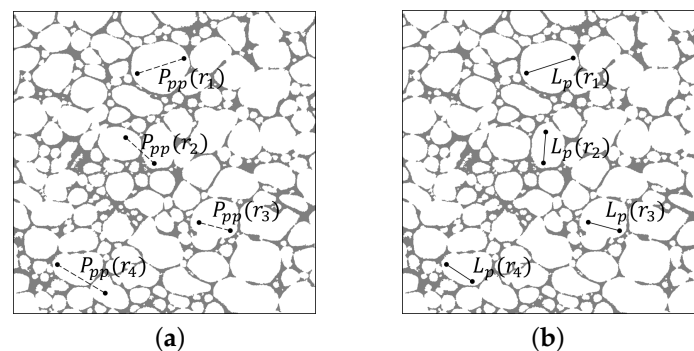


Figure 6. Examples of the probability functions for the foamed specimen: (a) $P_{pp}(r)$, (b) $L_p(r)$ (note: the white regions are pores (p), and the gray regions represent solids; lines are shown as r_i with arbitrary lengths and directions).

3.2.2. Local Volume Ratio and Shape Factor

For the quantitative characterization of the foamed specimen, the concept of the local volume ratio [37] is adopted. In this method, the local volume ratio of a specific component is calculated using a kernel with a specific volume to compute local porosity (or volume). Figure 7 presents a schematic for investigating the local porosity. For example, Kernels 1 and 2 in Figure 7 have different local porosities because each kernel contains different numbers of pore (white) particles depending on its location. The measurement is proceeded by using the kernel along the whole model, and the local porosity distribution is calculated based on the number of pore particles inside the kernel volume at every location in the model. The local volume ratio has a value between zero and one, and then, the local volume ratio distribution for each specimen is described using the contour in 3D space. Like the local porosity, the local volume ratio of the cell (solid) can be obtained here using this method.

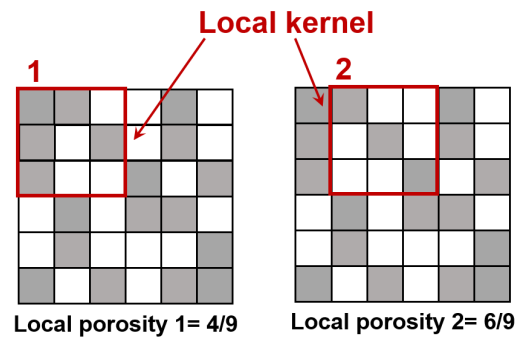


Figure 7. Example of the evaluation of the local porosity distribution (note: in this image, the white represents a pore region, and the local porosity has a value between zero and one).

To describe the shape of each pore in the foamed concrete specimens, the sphericity (or isoperimetric shape factor) is also investigated. The sphericity, S_p , is a parameter to describe the roundness of an object [38] and can be calculated as follows:

$$S_p = 6\sqrt{\pi} \frac{V}{\sqrt{A^3}} \quad (3)$$

where V is volume and A is the surface area of the pore. Here, the sphericity of each pore in the foamed specimens is calculated from the segmented image by counting the voxel numbers of each pore particle, and the surface area is also measured from the boundary configuration of the pore. S_p has a value between zero and one, where the S_p of a sphere is one by definition. Using this index, the shape of pores in the specimen can be identified.

4. Properties Evaluation Using Experiments and Numerical Methods

The heat properties of the real foamed concrete samples are evaluated using an experimental tool. In addition, thermal and mechanical simulations are performed to compute the properties of the 3D models obtained from the micro-CT images. Using the numerical results, the effects of the pore size and distribution on the material properties are effectively examined.

4.1. Experiments for the Evaluation of Material Properties

In this study, the Hot Disk instrument (Hot Disk AB, Göteborg, Sweden) compatible with ISO standard (22007-2) [27] in Figure 8 is used to obtain the thermal properties of the real foamed concrete samples. The material properties, such as specific heat, thermal diffusivity and thermal conductivity, can be effectively obtained using this device. For the measurement, a sensor is positioned between two samples, and this sensor is used for a current supplier, as well as a temperature monitor, as shown in Figure 8. Then, the thermal properties of the sandwich samples are calculated using the information of temperature changes during the measurement. The obtained results are used for the investigation of the thermal properties of the foamed samples with different densities and also utilized for FE analysis as input parameters.

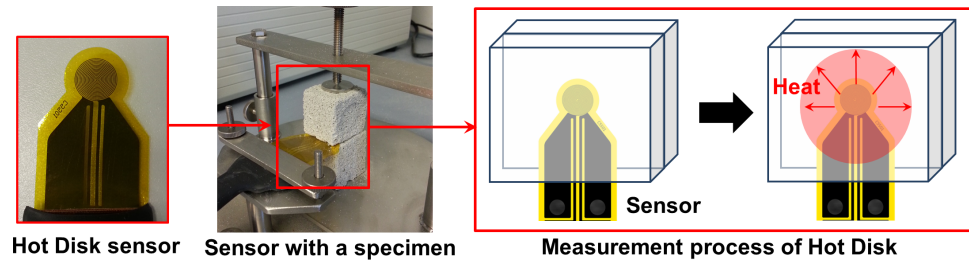


Figure 8. Hot Disk sensor and its operation process for evaluating thermal properties.

4.2. Numerical Simulation for Thermal and Mechanical Analysis

The material properties of the foamed samples are evaluated using the 3D micro-CT images and FE simulations. The ABAQUS package [39] is used for the simulations, and detailed descriptions of the FE formulations for both thermal and mechanical analysis are in [40,41]; only a brief description is presented in this paper.

The modified governing equation for 3D heat flow analysis by considering heat loss is described as follows:

$$\frac{\partial T}{\partial t} = \frac{k}{\rho C} \left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} \right) - \lambda \cdot T^* \quad (4)$$

where T (K) is the temperature, T^* (K) is the surrounding temperature and t (s) is the time. k (W/m/K) is the thermal conductivity; ρ (kg/m³) is the mass density; C (J/g/K) is the specific heat; λ (1/s) is the heat loss coefficient. A weak form of the FE simulation can be obtained by integrating the governing differential equation in Equation (4). The effective heat flux can be calculated by averaging the elemental heat flux, and the effective thermal conductivity is computed from the Fourier law as:

$$k_{(n)} = q_{(n)} L / \Delta T_{(n)} \quad (5)$$

where $\Delta T_{(n)}$, $q_{(n)}$ and L denote the temperature difference along the heat flow direction, the effective heat flux of the sample and the characteristic length, respectively. The directional component is denoted as n .

The mandatory input parameters for the heat transfer analysis, such as the bulk (solid) thermal conductivity and specific heat of the foamed materials, are obtained from the experiments using the Hot Disk machine [27] and the analytical formulation in [2]; the required parameters are given in Table 2. For the boundary conditions, a constant temperature (60 °C) is applied to the top surface in each vertical direction (x , y and z). Heat loss is allowed only in the bottom surface, while other remaining surfaces are assumed to have no heat loss. Here, the heat loss coefficient (λ) and the surrounding temperature of the sample are set as 1.6 (1/s) and 22 °C, respectively. The thermal conductivities for all samples are computed in the x , y and z directions.

Table 2. The input parameters for heat analysis.

Specimens	LithoPore [®] 100	LithoPore [®] 200	LithoPore [®] 450	LithoPore [®] 600
Thermal conductivity (W/m/K)	0.05	0.08	0.14	0.24
Density (kg/m ³)	100	200	450	600
Specific heat (J/g/K)	435	380	250	178

The compressive strengths of the foamed samples are also numerically computed. The ABAQUS package including the concrete damage plasticity (CDP) model is utilized to evaluate the behavior of the foamed samples with different densities and pore distributions. Details of the FE formulations are

presented in [42], and only a brief description is shown in this paper. The governing equation for the stress-strain relation of the CDP model, controlled by a scalar damaged elasticity, is given as follows:

$$\sigma = (1 - d)D_0^{el} : (\epsilon - \epsilon^{pl}) = D_0 : (\epsilon - \epsilon^{pl}) \quad (6)$$

where σ is the stress tensor and d is the scalar stiffness degradation variable, which can take values from zero (undamaged material) to one (fully damaged material). D_0^{el} , D_0 , ϵ and ϵ^{pl} denote the initial elastic modulus, the degraded elastic stiffness, the total strain tensor and the plastic strain tensor, respectively.

Each elemental stress is computed at each element center, and the effective stress is obtained by integrating elemental stresses over the whole volume of the mesh. For the boundary conditions, a displacement is imposed on the top surface in each vertical direction of the Cartesian coordinate system, and a fixed boundary condition is applied to the bottom surface. Other remaining surfaces are set to be traction free. The required parameters, such as elasticity modulus and strength, are selected from the analytical relationship in [2,43,44] and listed in Table 3. The input parameters for the CDP model, such as dilation angle and eccentricity, are selected and adjusted from the data in [42,45]. In these analytical formulations, the required parameters are calculated using the information of the material density and yield strength. The correlation between the pore characteristics and the directional mechanical properties is examined from the results.

Table 3. The input parameters for mechanical simulations.

Specimens	LithoPore [®] 100	LithoPore [®] 200	LithoPore [®] 450	LithoPore [®] 600
Elastic modulus (GPa)	0.6	0.9	2.5	2.9
Poisson's ratio	0.3	0.3	0.2	0.2
Yield strength (MPa)	0.45	0.9	4.2	7.2

5. Results and Discussion

The inner structures of the foamed specimens are visualized using 3D micro-CT images, and the pore characteristics of these specimens are investigated using the probabilistic and quantitative methods. The thermal conductivity, directional modulus and compressive strength are evaluated using experimental and numerical approaches. The obtained results demonstrate the correlation between the pore characteristics and the material properties.

5.1. Micro-CT Image and Characteristics of the Pore Structure

The adjusted 3D micro-CT images of the foamed concrete specimens are shown in Figure 9. Here, the 3D images of the specimens are visualized using the binarization and the watershed segmentation, and the generic solid structure and the pore distribution can be identified; the solid structure of the foam specimen becomes denser as the density of the specimen increases, and the pore shape becomes more spherical with increasing specimen density. From these figures, the effect of the density on the material characteristics can be identified; however, it is difficult to examine the detailed pore characteristics, such as the pore size distribution and shape. Therefore, an appropriate method is desired for characterization of the pore structure.

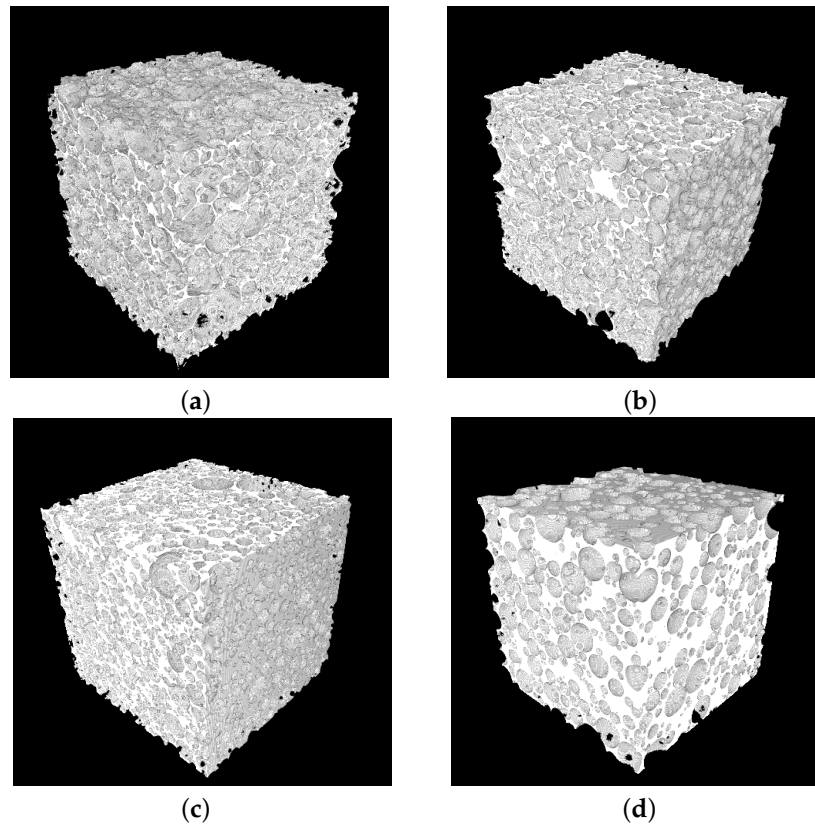


Figure 9. 3D micro-CT images of foamed concrete specimens with different densities: (a) LithoPore®100, (b) LithoPore®200, (c) LithoPore®450, (d) LithoPore®600 (note: in each binarized image, the white region represents solid).

Figure 10 illustrates the probability functions for the pore sizes of the foamed specimens in the x , y and z directions. In these functions, r and D represent the distance between two random points and the specimen edge length, respectively. In $P_{pp}(r)$, a large probability for a specific direction indicates that larger pore clusters exist in that direction. For example, in Figure 10a, $P_{pp}(r)$ in the x direction is relatively smaller than those of the y and z directions; it denotes that the pores are less clustered in the x direction, and the pore distribution in this specimen is anisotropic. Another probability function, $L_p(r)$, can be used to describe the continuous connectivity of pores. In Figure 10b, $L_p(r)$ of the LithoPore®100 sample in the z direction is slightly larger than the x and y directions, and it denotes that the maximum pore size in the z direction is larger than other directions; the anisotropy of the pore shape can be examined using $L_p(r)$. From $P_{pp}(r)$ and $L_p(r)$ in Figure 10a,b, it is identified that the LithoPore®100 sample contains anisotropic pores. The pore characteristics of other samples are also examined using the probability functions. The functions of each sample in Figure 10c–h are almost the same in the x , y and z directions, although small differences are found in Figure 10f,h when r/D is larger than 0.15; this means that the pores in the LithoPore®200, 450 and 600 samples are closer to spherical (isotropic) than those of the LithoPore®100 sample. In particular, the relative pore size within the specimen can be described using $L_p(r)$. In Figure 10b, the function values become zero when r/D is about 0.45, while those in Figure 10f,h become zero when r/D is about 0.25. The results confirm that the degree of pore clustering, which represents the pore size, becomes smaller as the density of the specimen increases for the foamed samples used in this study.

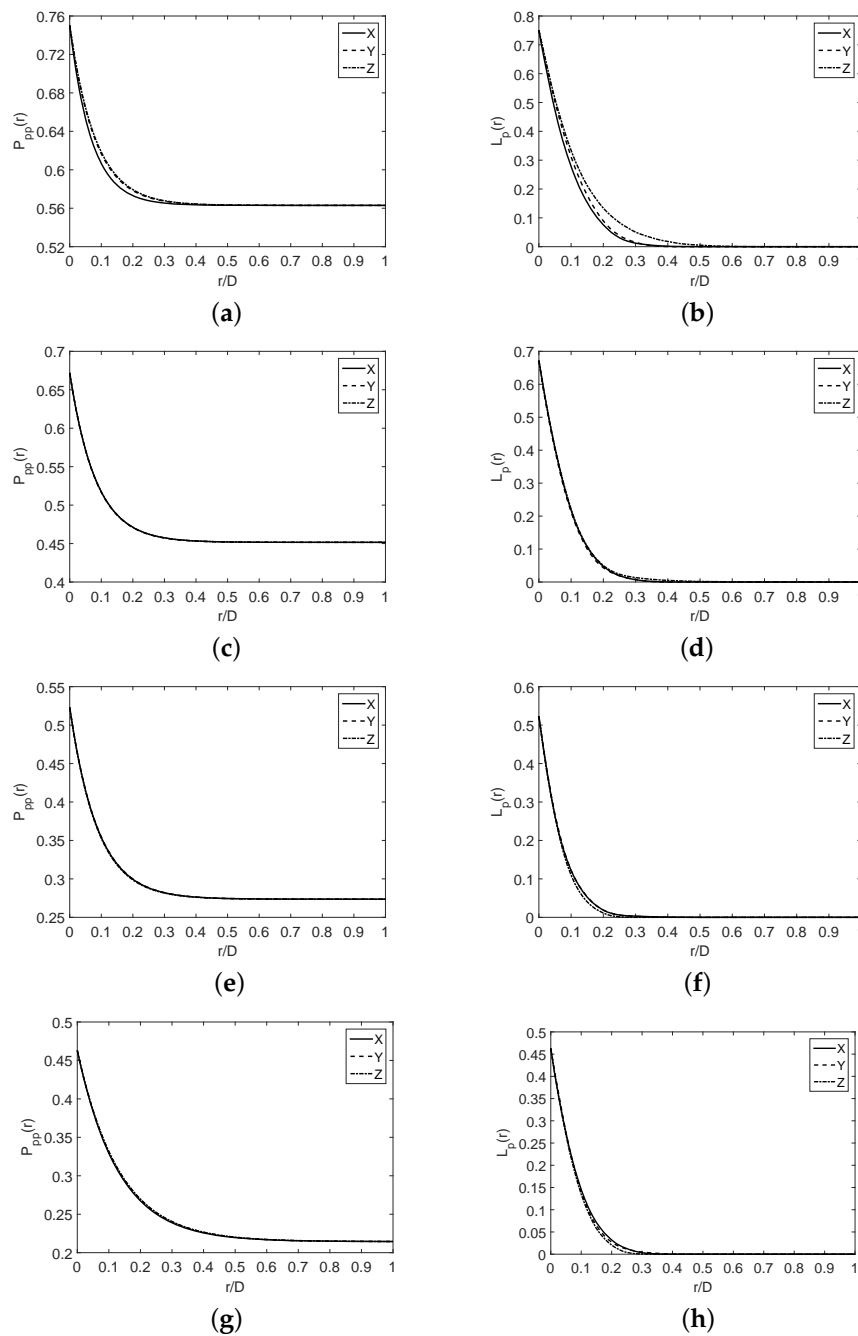


Figure 10. Probability functions for the pore sizes of the foamed specimens: (a) $P_{pp}(r)$ of LithoPore® 100, (b) $L_p(r)$ of LithoPore® 100, (c) $P_{pp}(r)$ of LithoPore® 200, (d) $L_p(r)$ of LithoPore® 200, (e) $P_{pp}(r)$ of LithoPore® 450, (f) $L_p(r)$ of LithoPore® 450, (g) $P_{pp}(r)$ of LithoPore® 600, (h) $L_p(r)$ of LithoPore® 600 (note: in each function, r is the distance between two points, and D is the length of the specimen).

In addition to the probabilistic descriptions of the pore characteristics, the quantitative investigations are also performed. Figure 11 shows the pore size distributions of the foamed specimens, which are calculated using the 3D images. In this figure, it is identified that the foamed specimen with low density (LithoPore® 100) contains more large pores than the other specimens, and the portion of the pores with a radius less than 0.2 mm increases as the specimen density increases; this indicates that the pore size tends to increase as the density of the foamed specimen decreases. The shape factor of the pores is also investigated. Figure 12 presents the sphericity distribution of each specimen. In this figure, the sphericity shows a tendency to increase as the specimen density increases; it denotes that

the pore shape in the specimen becomes more spherical (or isotropic) as the density of the specimen increases. From these results, it is demonstrated that the pore size and shape in the foamed specimen are affected by the density of the solid; the pore size decreases as the density increases, and the generic pore shape becomes more isotropic as the density increases because the dense solid structure plays the role as a frame for holding the spherical pores.

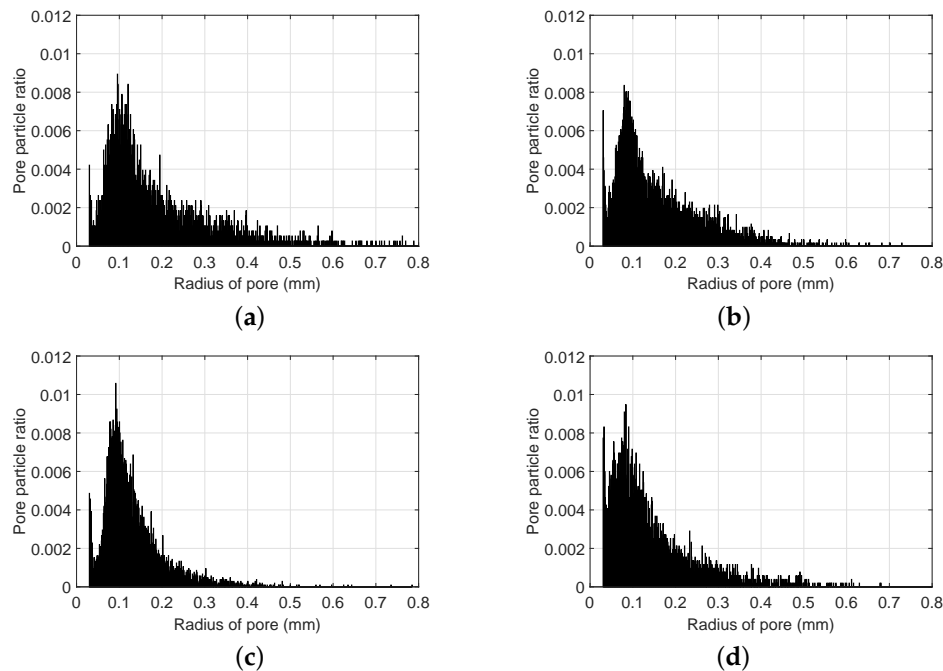


Figure 11. Pore size distribution of the foamed specimens: (a) LithoPore[®]100, (b) LithoPore[®]200, (c) LithoPore[®]450, (d) LithoPore[®]600.

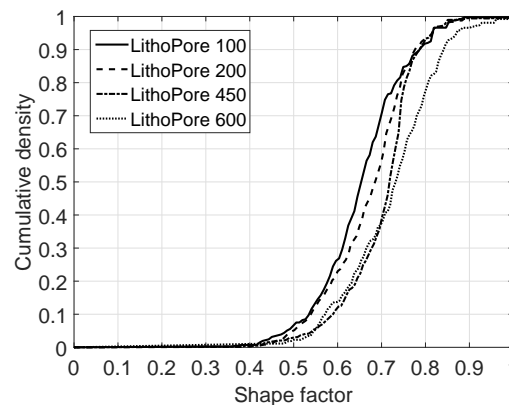


Figure 12. Comparison of the shape factors for the foamed specimens.

5.2. Material Properties of the Foamed Specimens

The properties of the foamed samples are computed using the FE simulations. Here, only a selected volume element (SVE) of each sample in Figure 13 is used for the simulation to improve the computational efficiency. To investigate the thermal properties of the foamed specimen, the thermal conductivities of each specimen are computed. Figure 14 shows the temperature isosurfaces of the heat flows in different directions, and the influence of the pore distributions on the heat transfer can be examined from this temperature contour. In each left, middle and right figure of Figure 14, the isosurfaces in the x , y and z directions are presented, respectively. In these figures,

many fluctuations can be found near the pore regions, particularly the vicinity of the large pores. In addition, the directional heat flow is different in each direction even in the same specimen; this denotes that the spatial distribution of pores in each foamed specimen strongly affects the heat transfer.

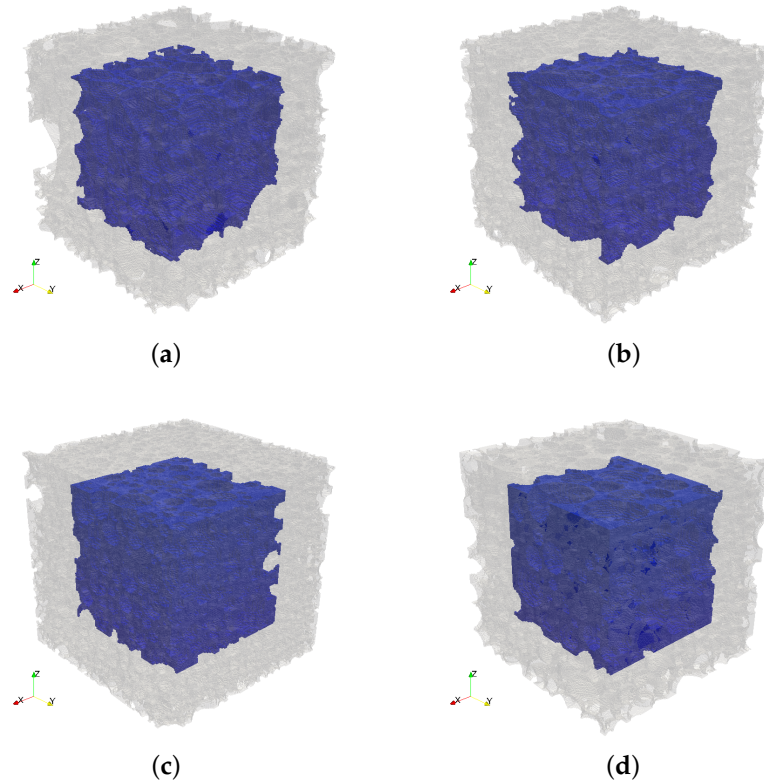


Figure 13. Selected volume element (SVE) of the specimen for numerical analysis: (a) LithoPore® 100, (b) LithoPore® 200, (c) LithoPore® 450, (d) LithoPore® 600 (note: transparent meshes of each figure are the specimens in Figure 9).

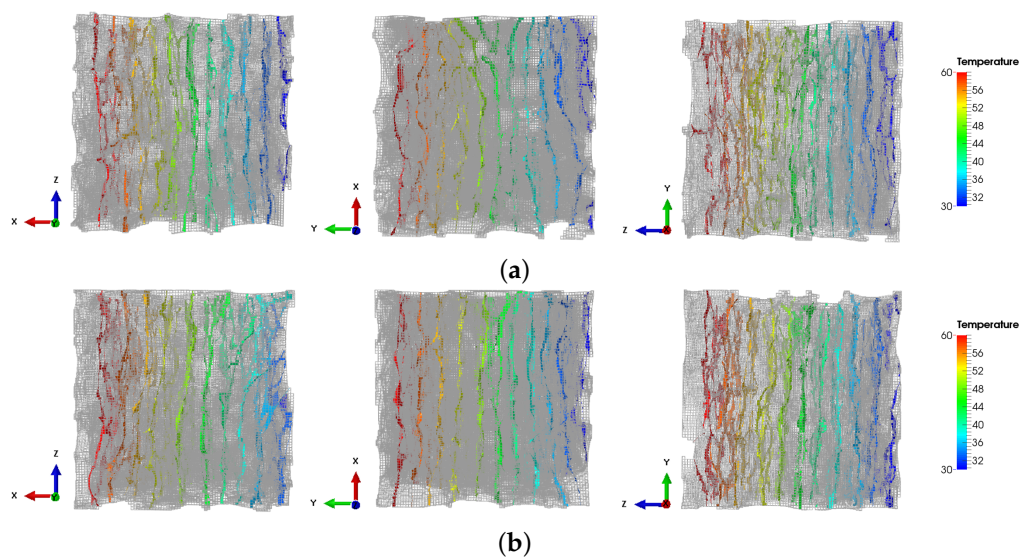


Figure 14. Cont.

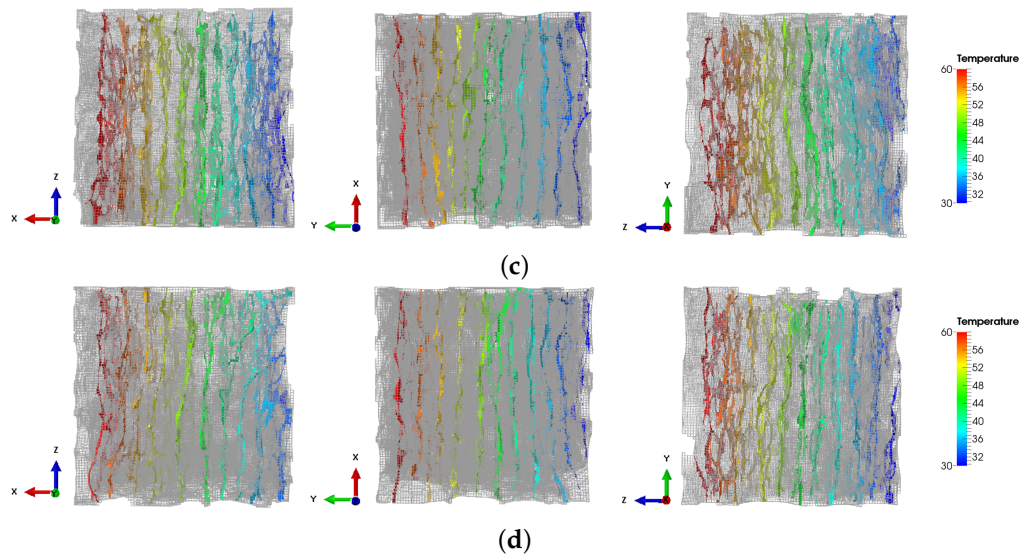


Figure 14. Temperature isosurfaces of the foamed specimens: (a) LithoPore[®]100, (b) LithoPore[®]200, (c) LithoPore[®]450, (d) LithoPore[®]600 (note: in each figure, the left figure is in the x direction heat flow, and the middle and right figures are in the y and z directions, respectively).

For the quantitative comparison of the heat flows of the foamed samples, the thermal conductivities are computed by averaging the local heat flux in each sample, as shown in Figure 15. It is confirmed that the computed thermal conductivity values are in good agreement with the properties given by the manufacturer of the LithoPore[®] specimens, which are denoted as the reference in the figure. In Figure 15, the thermal conductivity increases as the specimen density increases. The relationship of the pore characteristics and the thermal conductivity can be examined by comparing Figures 10 and 15. In the LithoPore[®]100 specimen, it is confirmed from $L_p(r)$ that the pores are more clustered for the z direction than other directions, and the thermal conductivity in that direction is higher than those of the x and y directions. Likewise, other specimens show a similar tendency between the probability function and the thermal conductivity; the thermal conductivity is larger as the specimen contains larger pore clusters along that direction because more solid areas can be secured for the direction so that heat can flow. These results confirm that the thermal conductivity of the foamed specimen is strongly affected by the material density, as well as the pore shapes and distributions.

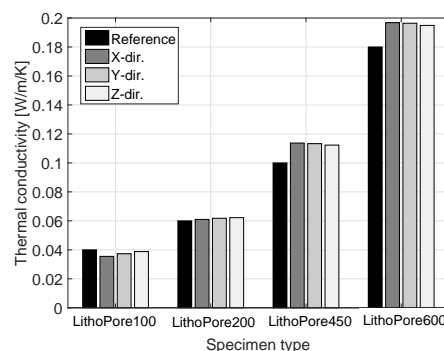


Figure 15. Comparison of the thermal conductivity values of the specimens in the x , y and z directions.

The mechanical responses of the SVEs are also investigated in this study. Figure 16 shows the directional modulus and compressive strength of the foamed samples in different directions. The computed mechanical data are also in reasonable agreement with those given by the manufacturer. Both mechanical properties increase as the density of the specimen increases, likewise the thermal

conductivity. In addition, the directional trends of the properties are almost identical to the probabilistic characteristics. In Figure 16a,b, the properties are larger when the specimen contains larger pores along a specific direction, and this relates to the anisotropic effect of pore shapes on the material properties in [40]; in a porous specimen, the stress concentration mainly occurs at the pore edges, and these local stress concentrations cause early failure of the sample. For a more detailed understanding of the stress concentration of the foamed specimens, the stress distributions of the SVEs are examined. Figure 17 shows the stress contours of the LithoPore[®]100 and LithoPore[®]600 specimens in different directions. In these figures, the stress distributions at the peak strength of the specimens are described. In both specimens, the peak strength values can be found at the edge of the pores in the direction perpendicular to the loading axis. In particular, the stress concentrations occur in the vicinity of the relatively large pores. Figure 18 illustrates the local volume of solids in the specimens. Comparing Figures 17 and 18, it can be examined that the stress concentration generally occurs at the region with low solid density; therefore, it demonstrates that the peak strength of the foamed specimen can be found in the narrow region of the solid part, and the material failure is initiated from these regions of the specimen. These results confirm that the pore shapes and sizes strongly affect the material behavior, and the local density of the solids also contributes the mechanical properties of the foamed material.

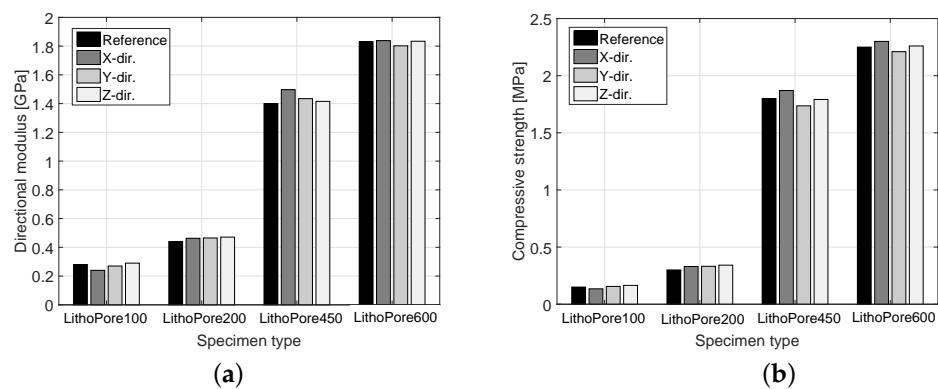


Figure 16. Comparison of the mechanical properties of the specimens in the x , y and z directions: (a) directional modulus, (b) strength.

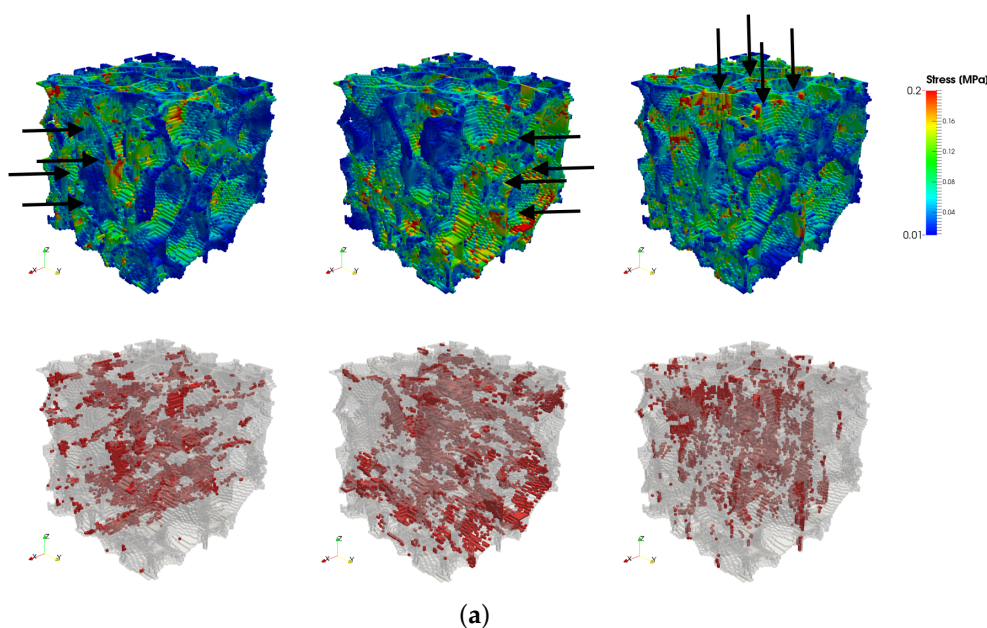


Figure 17. Cont.

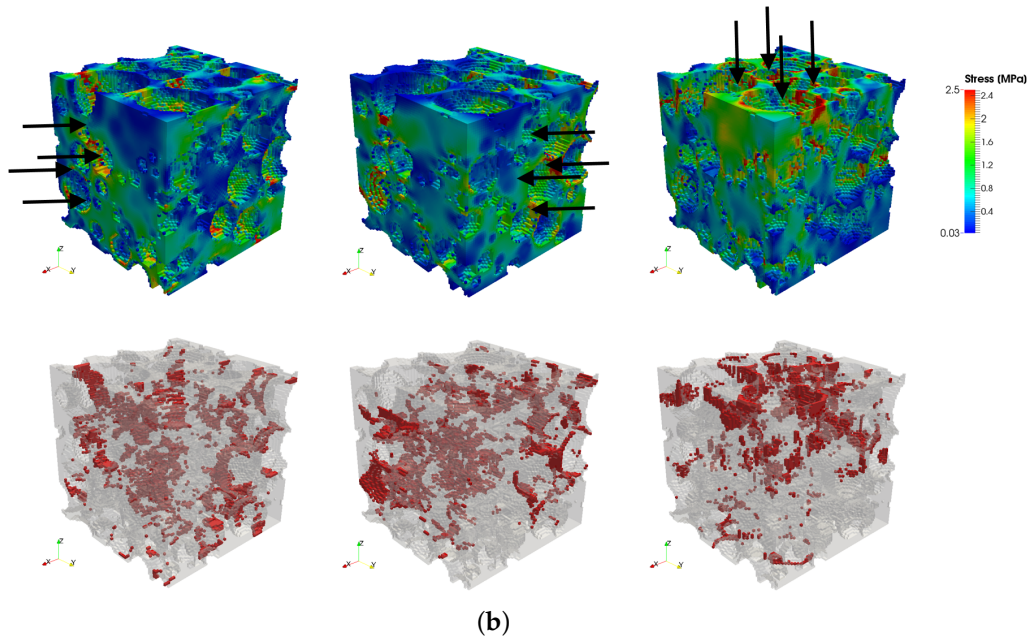


Figure 17. Stress contour of the specimens: (a) LithoPore® 100, (b) LithoPore® 600 (note: the upper figures are von-Mises stress contour, and the lower figures show the elements on the yield strength, which are mapped on to the transparent meshes; in each figure, the left is the case of loading in the x direction, the middle and right figures show loading in the y and z directions, respectively).

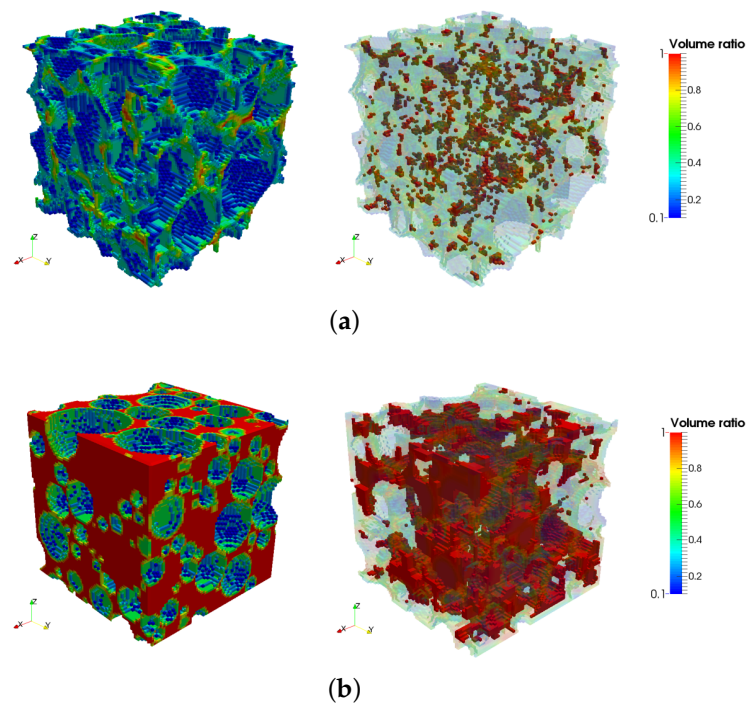


Figure 18. Solid density contour (left) and high dense region of solids (right): (a) LithoPore® 100, (b) LithoPore® 600 (note: in the right figures, the regions with over a 0.9 volume ratio are only mapped on to the meshes to emphasize highly dense regions).

6. Conclusions

The effects of the pore characteristics on the material properties of foamed specimens were evaluated at the microstructural level. For that purpose, foamed concrete specimens with different

densities were utilized in this study. In addition to the X-ray micro-CT imaging with the modified segmentation technique, the probabilistic and quantitative characterization methods were adopted to investigate the characteristics of the foamed specimen without damaging the specimens. Several pore characteristics, such as anisotropy, pore shape factor and local solid density, were examined, and the correlation of the pore distributions and the physical properties was evaluated. The required parameters for the numerical analysis were obtained from the experimental tool and analytical formulations, then the thermal conductivity and mechanical properties (i.e., directional modulus and strength) of the foamed specimen were obtained using the FE simulations. From the results, the effects of the pore sizes, shapes and distributions on the material properties of the foamed concrete materials were examined.

The results of $P_{vv}(r)$ and $L_v(r)$ confirmed that the pore size (or clustering) becomes smaller as the density of the specimen increases for the case of the foamed specimens used in this study. In addition, the pore sizes and shapes in the foamed specimen are affected by the density of the solid as the pore shape becomes more isotropic as the density increases because the dense solid structure holds the spherical pores inside the specimen. The physical properties are strongly affected by the pore characteristics. The pore characteristics affect the directional heat transfer and mechanical properties due to the anisotropic effect. In particular, the pore shapes and sizes, as well as the local density of the solids strongly affect the properties and failure of foamed concrete, and these characteristics should be carefully considered to generate high-performance foamed material. Although more in-depth investigation should be performed on the physical and chemical structure, the systematic tools used here can be effectively utilized to develop advanced foamed concrete as a complementary approach to experiments.

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