An Asymmetrical Fuzzy-Logic-Control-Based MPPT Algorithm for Photovoltaic Systems

Chun-Liang Liu 1, Jing-Hsiao Chen 1, Yi-Hua Liu 1,* and Zong-Zhen Yang 2

1 Department of Electrical Engineering, National Taiwan University of Science and Technology, EE-105-1 #No.43, Sec. 4, Keelung Rd., Da’an Dist., Taipei 10600, Taiwan; E-Mails: d10007201@mail.ntust.edu.tw (C.-L.L.); d10107201@mail.ntust.edu.tw (J.-H.C.)
2 Electric Energy Technology Division Power Electronics Department, Industrial Technology Research Institute, Rm#839, Bldg. 51, No. 195, Sec. 4, Chung Hsing Rd., Chutung, Hsinchu 31040, Taiwan; E-Mail: ZZYang@itri.org.tw

* Author to whom correspondence should be addressed; E-Mail: yhliu@mail.ntust.edu.tw; Tel.: +886-2-2733-3141 (ext. 1252); Fax: +886-2-2737-6699.

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Abstract: In this paper, a fuzzy-logic-control (FLC) based maximum power point tracking (MPPT) algorithm for photovoltaic (PV) systems is proposed. The power variation and output voltage variation are chosen as inputs of the proposed FLC, which simplifies the calculation. Compared with the conventional perturb and observe (P&O) method, the proposed FLC-based MPPT can simultaneously improve the dynamic and steady state performance of the PV system. To further improve the performance of the proposed method, an asymmetrical membership function (MF) concept is also proposed. Two design procedures are proposed to determine the universe of discourse (UOD) of the input MF. Comparing with the proposed symmetrical FLC-based MPPT method, the transient time and the MPPT tracking accuracy are further improved by 42.8% and 0.06%, respectively.

Keywords: fuzzy logic control; maximum power point tracking; photovoltaic

1. Introduction

In recent years, the concerns over greenhouse gas emission and the ever rising fuel prices have stimulated urgent demands for alternative energy. Government incentives and the soaring cost of fossil
fuels have significantly promoted the development of renewable energies. Among them, solar energy is one of the most important green energy resources due to its environmental sustainability and inexhaustibility [1–3]. Since the I–V characteristic curve of photovoltaic (PV) cells varies nonlinearly with the insolation and temperature, it is crucial to operate PV system to a specific point to extract maximum solar energy. This technology is normally named as maximum power point tracking (MPPT). Many MPPT methods have been developed and implemented in previous studies, including perturb and observe (P&O), incremental conductance (IncCon), fractional open-circuit voltage, fractional short-circuit current, line approximation, ripple correlation control (RCC) and fuzzy logic control (FLC) approaches. These techniques have high tracking accuracy under steady weather conditions, but still exhibit some trade-offs between tracking speed and tracking accuracy when insolation changes [4,5]. Taking the P&O method for instance, it determines the perturbation directions of the control value (i.e., PV voltage, PV current or duty cycle) of the system according to the measured power in prior state and current state. With larger perturbation steps, it will take less time for the PV system to track the maximum power point (MPP) from one steady state to another. However, the power loss caused by perturbation in the steady state will also increase. On the other hand, a smaller perturbation step can improve the power loss caused by perturbation in the steady state but will slow down the tracking speed. Therefore, how to determine the perturbation step becomes an important issue [6]. To deal with this problem, variable-step size MPPT methods are proposed in many literatures [7–13]. The basic operating principle of these kinds of methods is that when operating point is far from the MPP, larger perturbation step will be used to improve tracking speed. On the other hand, when operating point is close to the MPP, smaller perturbation step will be used to improve steady-state efficiency. However, since PV system is a nonlinear system, how to determine the scaling factor of the perturbation step becomes significant when realizing these variable-step size MPPT algorithms. On the other hand, FLC has advantages that its parameters can be determined without precise and complicate mathematical model and it is capable of operating under highly nonlinear system. As a result, the FLC-based MPPT algorithm attracts many research interests. Recently, numerous MPPT techniques based on FLC have been proposed in the literatures [14–34]. In comparison with conventional P&O algorithm, FLC-based MPPT provides superior tracking performance. However, the design consideration and realization complexity for different kinds of FLC-based MPPT techniques vary greatly.

In terms of the input variable selection, most FLC-based MPPT techniques take the error \( e(t) \), usually defined as \( dP_{PV}/dV_{PV} \) or \( dP_{PV}/dI_{PV} \) and the error variation \( \Delta e(t) \) as inputs [14–19]. For these methods, divisions is required therefore increases the computation complexity. Moreover, derivative operation may induce large amounts of errors from merely small amounts of measurement noise. Therefore, additional considerations are required during implementation. In contrast, [20–24] take power variation \( \Delta P_{PV} \) and voltage or current variation \( \Delta V_{PV} \) or \( \Delta I_{PV} \) as inputs, which avoids the precision loss and overflow problem when dealing with fixed-point division, thus simplifies the calculation. The inputs in [25] are \( dP_{PV}/dI_{PV} \) and \( e(t) \) (defined as \( P_{MPP} - P_{PV} \)), while the inputs in [26] are error \( e(t) \) (defined as \( P_{MPP} - P_{PV} \)) and error variation \( \Delta e(t) \). Since the information of MPP should be acquired in prior, these methods are not suitable for practical realization. In [27–34], solar irradiation and cell temperature are used as FLC inputs. However, most of the small PV systems do not equip irradiation and temperature sensors; hence these methods are not suitable for cost-sensitive systems.
Regarding the design of input/output membership functions (MFs), it is known that the input/output MFs design has a great impact on FLCs’ performance. In order to deal with this issue, genetic algorithm (GA), particle swarm optimization (PSO) and Hopfield artificial neural network (ANN) are proposed in the literatures to optimize the FLC MFs [15–17,24]. As for control schemes, typical dual-input fuzzy logic controller is adopted by [14–26]. These controllers employ nine to 49 rules in the rule table, depending on the numbers of linguistic variables in input MFs. However, these methods share similar implementation complexity. Ref. [27–31] uses ANN to assist FLC. ANN technique needs a great amount of training data to acquire reasonable result, thus the solar irradiance and cell temperature are often taken as input variables in such methods, this could limit its application. In order to enhance the FLC efficiency, fuzzy cognitive networks [18,32] and Takagi-Sugeno (T-S) fuzzy technique [33,34] are employed to improve the tracking speed. Comparing with conventional FLC, these methods are difficult to be realized using low-cost microcontrollers due to their complicated computation. Moreover, FLC can be used to adaptively tune the gains of the PID controller utilized in the MPPT controller [35].

The aim of this paper is to design a low cost, high efficiency MPPT algorithm. In this paper, power variation ($\Delta P_{pv}$) and output voltage variation ($\Delta V_{pv}$) are chosen as the inputs of the proposed FLC. The design of the FLC scheme and rule table will be introduced in detail first. To further improve the performance of the proposed MPPT method, an asymmetrical MF concept is proposed. A systematic design procedure verified by grid-search method will be proposed to determine the universe of discourse (UOD) of the input MF. Finally, a low cost digital signal controller (DSC) will be used to realize the proposed method. Experiments are then conducted to validate the correctness and effectiveness of the proposed system. According to the experimental results, the proposed asymmetrical FLC-based MPPT method can simultaneously shorten the tracking time and increase the tracking accuracy comparing with the traditional P&O and symmetrical FLC-based MPPT algorithm.

2. System Configuration

The block diagram of the proposed system is shown in Figure 1. In this study, a low cost DSC dsPIC33FJ16GS502 from Microchip Corp. (Chandler, AZ, USA) is used to implement the developed MPPT algorithm. The utilized DSC provides the required gating signal for the power switch in the power converter and gathers data from the signal conditioning circuits. From Figure 1, the whole system can be divided into three major parts: energy conversion unit, main control unit and data logging system. Detailed descriptions about each unit will be given in the following subsections:

(a) Energy conversion unit: the energy conversion unit is used to supply the power to the load. The topology of the energy conversion unit is illustrated in Figure 2. A simple boost type DC-DC converter is utilized in this paper. By adequately controlling the PWM gating signal, the energy conversion unit can transfer the maximum available PV energy to the load. The design and implementation of this part of circuit is conventional; therefore will not be discussed further here.
The relationship between output voltage and input voltage in boost converter can be expressed as:

\[
\frac{V_o}{V_{in}} = \frac{1}{1 - \delta}
\]  

(1)

where \(\delta\) represents the duty cycle. Assuming the conversion efficiency of the boost converter is 100%, relationship between the output current and the input current can be written as:

\[
\frac{I_o}{I_{in}} = 1 - \delta
\]  

(2)

From Equations (1) and (2), when duty cycle varies, relationship between the input impedance and the output load of the boost converter can be described using Equation (3):

\[
R_{in} = \frac{V_o}{I_o} = (1 - \delta)^2 R_L
\]  

(3)

(b) Main control unit: As shown in Figure 1, the main control unit provides the PWM signal for the boost converter to track the peak power available from PV panel. The utilized DSC gathers and analyzes PV panel data (voltage and current) from the A/D module. After obtaining the required PV panel data, a digital filter is employed to smooth out the acquired signals. The digital filter used in the
proposed system is a 24-order finite impulse response (FIR) filter. The equation describing a FIR filter can be expressed as in Equation (4):

\[ Y[n] = \sum_{i=0}^{23} a_i X[n-i] \]  

(4)

where \( X \) is the filter input; \( Y \) is the filter output and \( a_i \) is the corresponding coefficient of the designed FIR filter.

After the filtered PV voltage and current are obtained, needed gating signals are then determined using the developed MPPT controller. In this paper, three different MPPT schemes will be implemented for performance comparison, detailed description of these MPPT methods will be provided in Section 3.

3. Derivation of the Proposed FLC-Based MPPT Controller

3.1. Derivation of the FLC-Based MPPT Controller

Figure 3 shows the equivalent circuit of the PV cell, the \( I-V \) characteristic of the PV cell can be mathematically described by Equation (5):

\[
I_{PV} = I_{SC} - I_O \left\{ \exp \left[ \frac{q(V + R_s I)}{nkT_K} \right] - 1 \right\} - \frac{V + R_s I}{R_{SH}}
\]  

(5)

where \( n \) is the ideality factor; \( k \) is the Boltzmann’s constant; \( q \) is the electron charge; \( T_K \) is the temperature in Kelvin; \( R_s \) is the equivalent series resistance; \( R_{SH} \) is the equivalent shunt resistance and \( I_{SC}, I_{PV} \) and \( I_O \) are the photogenerated current; panel current and saturation current, respectively.

**Figure 3.** Equivalent circuit of the photovoltaic (PV) cell.

Figure 4a shows the \( I-V \) curves of the utilized Sanyo VBHN220AA01 solar panel under different irradiation levels, these curves are obtained using MATLAB simulation. The circular markers in the graph represent the calculated maximum power points. The corresponding \( P-V \) curve for 1000 W/m\(^2\) irradiation level is given in Figure 4b. Observing Figure 4b, the absolute value of \( dP/dV \) of a PV panel varies smoothly and is recommended in [10] as a suitable parameter for determining the step size of
the IncCon algorithm. Thus, power variation ($\Delta P_{pv}$) and voltage variation ($\Delta V_{pv}$) from solar cell are also used as the inputs of the proposed FLC-based MPPT controller.

**Figure 4.** (a) $I-V$ and (b) $P-V$ curve for the utilized PV panel.

To achieve MPPT, a fuzzy controller is used to determine the required perturbation step size. The proposed fuzzy controller is carried out every 20 ms. The block diagram of the implemented FLC-based MPPT controller is shown in Figure 5.

**Figure 5.** Block diagram of the implemented FLC-based maximum power point tracking (MPPT) controller.

In this paper, the inputs of the proposed MPPT controller are the power variation ($\Delta P_{pv}$) and the voltage variation ($\Delta V_{pv}$). The MFs of the utilized input and output variables for the proposed controller are illustrated in Figure 6. Figure 6a shows the MFs of the input variables; both $\Delta P_{pv}$ and $\Delta V_{pv}$ MFs are in triangular form. Figure 6b is the MF of the output (duty cycle step size $\Delta D$), which is also in triangular form. In Figure 6, $dP$ stands for power variation, $dV$ represents voltage variation and $dD$ denotes duty cycle variation. For linguistic variables, P represents positive, N represents negative, B,
S, and ZE are defined as big, small and zero, respectively. From Figure 6, each of the input variables $\Delta P_{pv}$ and $\Delta V_{pv}$ is mapped into five different linguistic values. Therefore, the proposed FLC will contain 25 different rules. The complete set of the fuzzy control rules for the proposed system will be explained in Section 3b. The defuzzification method used in this paper is the commonly used center of gravity method as shown in Equation (6):

$$Y_{COG} = \frac{\sum_{i} Y_i(X_i)X_i}{\sum_{i} Y_i(X_i)}$$

where $Y_i$ is the inference result of rule $i$; $X_i$ is the corresponding output of rule $i$; and $Y_{COG}$ is the output.

Figure 6. Membership functions of the input and output variables (a) Membership function of $\Delta P_{pv}$ and $\Delta V_{pv}$; (b) Membership function of $\Delta D$.

3.2. Parameters Design of FLC-Based MPPT Controller

It is known that the FLC performance will be affected by the design of MFs. Generally, the shape of MFs in FLC can be in triangular, trapezoidal, symmetric Gaussian function, generalized Bell curve and sigmoidal function forms. Since a low cost DSC will be used in this paper to realize the proposed FLC-based MPPT controller, triangular MF is adopted to reduce the computation complexity. Next, the UOD of the MFs will be determined by the following procedures:

(1) Designing the UOD of the output MF: In this paper, duty cycle variation is chosen to be the output variable. The advantage of using duty cycle as the control variable is its simplicity. For direct duty control, no close-loop control is needed to achieve voltage control for MPPT realization [10]. FLC-based MPPT algorithm can be regarded as an adaptive P&O method with its perturbation step automatically adjusted by FLC. For P&O method, a larger step can achieve better tracking dynamic but will increase fluctuation on steady state, and vice versa. Therefore, the maximum value of the perturbation step has to be determined first. In the paper, the maximum perturbation step in MPPT, $dD_{\text{max}}$, is set as 5%;

(2) Designing the UOD of input MFs: In this context, voltage variation $\Delta V_{pv}$ and power variation $\Delta P_{pv}$ are chosen to be input variables. The UOD of $\Delta V_{pv}$ and $\Delta P_{pv}$ can be determined by the following procedures:
With a 1% step size, a profile can be plotted by increasing duty cycle from 0% to 100% with x-axis represents duty cycle and y-axis represents voltage variation or power variation, as shown in Figure 7. In Figure 7, the simulation is conducted under the standard test condition (1000 W/m², 25 °C). From Figure 7a, the maximum value of $\Delta V/\Delta D$ will be utilized to determine the UOD of $\Delta V_{pv}$ (denoted as $dV_{max}$). Likewise, the UOD of $\Delta P_{pv}$ (denoted as $dP_{max}$) can be determined in similar ways. In this paper, $dV_{max}$ is 1.5 V and $dP_{max}$ is 8.2 W.

Figure 7. Concept of determining the universe of discourse (UOD) of input MFs (a) Determining the UOD of $\Delta V_{pv}$; (b) Determining the UOD of $\Delta P_{pv}$.

For control rule design, since $\Delta V_{pv}$ and $\Delta P_{pv}$ are taken as the inputs and $\Delta D$ is chosen as the output in this paper; therefore, the control rule should be determined according to the relationships between these variables. From Figure 6, each of the input variables $\Delta V_{pv}$ and $\Delta P_{pv}$ is mapped into five different linguistic values. Therefore, the rule base of the proposed FLC will contain 25 different rules. The basic principle of designing the rules is explained as follows:

As mentioned in Section 2, boost converter is utilized in the paper. As shown in Equation (3), the operating point will move from right to left along the $P-V$ curve when duty cycle increases and vice versa. For the proposed system, a positive $\Delta P/\Delta V$ value indicates that the operating point lies on the left-hand side of MPP. In this case, a negative value of $\Delta D$ is needed to make the operating point moving toward right to reach MPP. On the other hand, a negative $\Delta P/\Delta V$ value represents that the operating point locates on the right-hand side of MPP. Therefore, a positive value of $\Delta D$ is needed. Consequently, the sign of the $\Delta P/\Delta V$ can be used to determine the sign of the output variable $\Delta D$. Next, the magnitude of the output variable $\Delta D$ can be determined using the following design principles. Figure 8 shows a typical $P-V$ curve of a PV panel. Observing Figure 8, when the operating point is far from the MPP (like point A or B in Figure 8), a larger $\Delta D$ is required to rapidly reach the MPP. On the contrary, when the operating point is close to the MPP (like point C or D in Figure 8), a smaller $\Delta D$ can be used to reduce the fluctuation on steady state. Therefore, the value of $|\Delta P/\Delta V|$ can be utilized to determine the magnitude of the output. Based on this concept, a complete set of fuzzy rules for the proposed FLC are summarized in Table 1. In Table 1, darker color represents larger number while lighter color indicates smaller number. Red represents positive value, green represents negative value and white represents zero.
Figure 8. Typical $P-V$ curve of a solar panel.

Table 1. Complete rule base for the proposed FLC.

<table>
<thead>
<tr>
<th>$\Delta P_{pv}$</th>
<th>$\Delta V_{pv}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>NB</td>
<td>NB</td>
</tr>
<tr>
<td>Rule1</td>
<td>Rule6</td>
</tr>
<tr>
<td>NS</td>
<td>NS</td>
</tr>
<tr>
<td>Rule2</td>
<td>Rule7</td>
</tr>
<tr>
<td>ZE</td>
<td>ZE</td>
</tr>
<tr>
<td>Rule3</td>
<td>Rule8</td>
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<tr>
<td>PS</td>
<td>PS</td>
</tr>
<tr>
<td>Rule4</td>
<td>Rule9</td>
</tr>
<tr>
<td>PB</td>
<td>PB</td>
</tr>
<tr>
<td>Rule5</td>
<td>Rule10</td>
</tr>
</tbody>
</table>

4. Derivation of the Proposed Asymmetrical FLC-Based MPPT Controller

4.1. Grid Search Method to Determine the UOD of $\Delta P_{pv}$

In Section 3, the design procedures of the proposed symmetrical FLC have been explained. To further improve the performance of the proposed FLC, the derivation of asymmetrical input MF technique will be explained. Figure 9 shows the $dP/dV$ vs. duty cycle curve, which can be obtained by dividing Figure 7b with Figure 7a. Observing Figure 9, the $dP/dV$ curve of a solar cell has different slopes on two sides. That is, when operating point locates at the left-hand/right-hand side of the MPP, the generated power variation will be larger/smaller under a fixed duty cycle variation. Thus, when designing the UOD of input variable $\Delta P_{pv}$, it is essential to take this phenomenon into consideration. To deal with this issue, a variety of artificial intelligence (AI) methods have been proposed in the literatures to obtain the optimal configuration of the MFs. These AI methods include GA, PSO and Hopfield ANN [15–17,24]. According to the experimental results, these AI approaches can acquire the optimal configuration in most cases. However, the problem of using AI techniques is that the parameters of these algorithms (for example, the population size, rate of crossover and rate of mutation in GA or the inertia factor, social rate and cognitive rate in PSO) are hard to determine. On the other
hand, it can be observed that the UOD of $\Delta P_{pv}$ has relatively larger impact on the proposed FLC-based MPPT controller, which implies that the problem complexity can be reduced if only the $\Delta P_{pv}$ optimization is taken into account. Therefore, grid search technique is employed in this paper to obtain the optimal design of the UOD of $\Delta P_{pv}$ Figure 10 shows the implementation concept of the grid search method used in this paper. First, this study fixed the $dP_{PB}$ value at $POS_{max}/100$ W (referring to Figure 10, $POS_{max} = 2 \times dP_{max}$ in this paper), and the $dP_{NB}$ value was gradually reduced from $NEG_{max}/100$ W to $NEG_{max}$ W ($NEG_{max} = -1 \times POS_{max}$) through a fixed increment of $NEG_{max}/100$, yielding a total of 100 points. Subsequently, the $dP_{PB}$ value was increased to $2 \times POS_{max}/100$ W through a fixed increment of $POS_{max}/100$; with this new value, the previous procedure, in which the $dP_{NB}$ value experienced a 100 point decrease, was repeated. This process was repeated until the $dP_{PB}$ value is equal to $POS_{max}$ W. This test method produced 10,000 ($100 \times 100$) combinations of simulation test points. Then, according to these possible UOD combinations, simulation is conducted under a step change in solar irradiation from 0 to 1000 W/m² for the proposed system. The steady-state tracking time can then be observed in a 3D plot in which the z-axis represents the numbers of tracking steps. Consequently, it can be concluded that the point with the lowest z-axis value indicates the optimal UOD combination. To reduce the complexity for optimization, the shape of the $\Delta P_{pv}$ MF remains as triangle shape and the ratio of large value to small value remains as 2 to 1 (that is, $dP_{NS} = (dP_{NB}/2)$; $dP_{PS} = (dP_{PB}/2)$). Additionally, to take every tracking situation into account, the simulation is carried out using two initial conditions—initial duty cycle value equals to 10% (representing the tracking from right to left along the $P-V$ curve) and 90% (representing the tracking from left to right along the $P-V$ curve). Then, the tracking time required for both cases is summed up as the total tracking time. Figure 11 shows the obtained 3D simulation result under different UOD configurations. The obtained optimal results are $dP_{PB} = 7$ W and $dP_{NB} = -2.5$ W.

**Figure 9.** Concept for determining the UOD of the input variables $\Delta P_{pv}$. 
Figure 10. The implementation concept of the grid search method (different $dP_{NB}$ with $dP_{PB}$ fixed).

Figure 11. The obtained 3D simulation result for different UOD configuration.

4.2. Systematic Approach to Determine the UOD of $\Delta P_{pv}$

Because grid search method is capable of searching every possible region and its generated 3D surface is a smooth surface; therefore, the proposed grid search method can yield optimal results. However, grid search method requires large amount of simulations (20,000 simulations in this case), thus increases the complexity of design. Consequently, a simple design method which can be used to determine the UOD of the MF of $\Delta P_{pv}$ is also proposed in this paper. It can also be observed from Figure 9 that the $dP/dV$ values of fixed duty cycle variation on two sides of the MPP are not identical. After conducting integration for the $dP/dV$ curves on both sides of MPP, the area under the curve on the left (area B) was 2093, the area under the curve on the right (area A) was 278, and the ratio of area B to area A was 7.53. Therefore, if the MF of $\Delta V_{pv}$ remains unchanged, the asymmetrical UOD problem can be adequately addressed by setting the ratio $dP_{PB}$ and $dP_{NB}$ as 7.53 (i.e., $dP_{PB} = 8.2$ and $dP_{NB} = -1.1$). Although this method cannot guarantee to obtain the optimal solution, it can efficiently determine the configuration of the UOD of $\Delta P_{pv}$ with quite satisfactory performance. Experimental results for these two methods will be provided in Section 5 for comparison.
5. Experimental Results

To verify the correctness of the proposed FLC-based MPPT controller, a 300 W prototyping circuit is implemented from which experiments are carried out accordingly. The proposed algorithm is validated using an AMETEK Solar Array Simulator TerraSAS DCS80-15 in SAS mode. The parameters of the utilized PV panel are listed in Table 2 and the specification of the utilized power converter is listed in Table 3. As shown in Figure 1, in order to validate the effectiveness of the proposed MPPT controller, experiments will be carried out on the following systems: Two P&O MPPT methods with different perturbation step settings, one proposed symmetrical FLC-based MPPT method and two proposed asymmetrical FLC-based MPPT methods with different settings. All experiments are conducted using the same power circuit to ensure the fairness. Table 4 shows the parameters used in each MPPT algorithm. In this paper, low cost DSC dsPIC33FJ16GS502 from Microchip Corp. is used to realize the aforementioned five kinds of algorithms. Using a 40 MHz oscillator, the required execution times of the P&O MPPT, the symmetrical FLC-based MPPT and the asymmetrical FLC-based MPPT are 1.5 μs, 120 μs and 120 μs, respectively. Figure 12 shows the starting waveform of these five methods for 1000 W/m² solar irradiance and 25 °C PV panel temperature. From Figure 12, the transient times for the fixed step P&O method are 250 ms (for 5% fixed step) and 3.13 s (for 0.5% fixed step), respectively. Additionally, the transient time for the proposed symmetrical FLC-based MPPT controller, the proposed asymmetrical FLC-based MPPT controller (UOD obtained in Section 4.2) and the proposed asymmetrical FLC-based MPPT controller (UOD obtained in Section 4.1) are 1.59 s, 968 ms and 913 ms, respectively. Observing Figure 12, the P&O method with large step exhibits good dynamic performance but larger steady state oscillations; therefore, the MPPT accuracy is rather low. On the other hand, using a small step size can improve the tracking accuracy at the cost of slower dynamic performance. The proposed FLC-based MPPT methods solves this dilemma as evident from Figure 12. It can be seen from Figure 12 that although the transient time of the proposed method is slightly higher than the P&O method using large step size, the oscillation around the MPP for the proposed method is much smaller than that obtained from the P&O method using large step size.

<table>
<thead>
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<th>Parameters</th>
<th>Specification</th>
<th>Parameters</th>
<th>Specification</th>
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<td>Maximum Power (P_{max})</td>
<td>220 W</td>
<td>Short Circuit Current (I_{sc})</td>
<td>5.65 A</td>
</tr>
<tr>
<td>Open Circuit Voltage (V_{oc})</td>
<td>52.3 V</td>
<td>Maximum Power Current (I_{mp})</td>
<td>5.17 A</td>
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<td>Maximum Power Voltage (V_{pm})</td>
<td>42.7 V</td>
<td>Temperature Coefficient (α_v)</td>
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Table 2. Parameters of the utilized PV panel.

<table>
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<td>Rated Output Current (I_o)</td>
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<td>Rated Output Power (P_o)</td>
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<tr>
<td>Switching Frequency (f_s)</td>
<td>50 kHz</td>
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<tr>
<td>Output Voltage Ripple (ΔV_o/V_o)</td>
<td>&lt;1%</td>
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</table>

Table 3. Specification of the utilized boost converter.
Table 4. Parameters of the implemented algorithms.

<table>
<thead>
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<th>No.</th>
<th>Description</th>
<th>Parameters</th>
<th>Note</th>
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<td>P&amp;O (0.5%)</td>
<td>Fixed Duty Cycle 0.5%</td>
<td>denoted as method 1</td>
</tr>
<tr>
<td>2</td>
<td>P&amp;O (5%)</td>
<td>Fixed Duty Cycle 5%</td>
<td>denoted as method 2</td>
</tr>
<tr>
<td>3</td>
<td>Symmetrical FLC</td>
<td>( dP_{PB} = 8.2 \text{W} ) ( dP_{NB} = -8.2 \text{W} ) ( dV_{PB} = 1.5 \text{V} ) ( dV_{NB} = -1.5 \text{V} )</td>
<td>denoted as method 3</td>
</tr>
<tr>
<td>4</td>
<td>Asymmetrical FLC #1</td>
<td>( dP_{PB} = 8.2 \text{W} ) ( dP_{NB} = -1.1 \text{W} ) ( dV_{PB} = 1.5 \text{V} ) ( dV_{NB} = -1.5 \text{V} )</td>
<td>denoted as method 4</td>
</tr>
<tr>
<td>5</td>
<td>Asymmetrical FLC #2</td>
<td>( dP_{PB} = 7.0 \text{W} ) ( dP_{NB} = -2.5 \text{W} ) ( dV_{PB} = 1.5 \text{V} ) ( dV_{NB} = -1.5 \text{V} )</td>
<td>Parameters from Section 4b</td>
</tr>
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</table>

**Figure 12.** Measured starting waveform of five different algorithms. (a) Measured starting waveform for method 1; (b) Measured starting waveform for method 2; (c) Measured starting waveform for method 3; (d) Measured starting waveform for method 4; (e) Measured starting waveform for method 5.
The performances of the tested methods are summarized in Table 5. In Table 5, the tracking accuracy values are obtained using the built-in data logging function of the solar array simulator. The system begins to record the accuracy data when system reaches steady state and the total recorded data contains 125 points (recoding time is 6.25 s with sampling time equals 0.05 s). From Table 5, the tracking accuracies of the proposed methods are better than both of the P&O method. It can be seen that the proposed FLC-based MPPT controller can improve the dynamic and steady state performance of the PV system simultaneously. Moreover, it can also be learned from Table 5 that asymmetrical FLC-based MPPT methods can improve tracking speed over symmetrical FLC-based MPPT method. Although the asymmetrical FLC-based MPPT method obtained in Section 4b does not have optimal tracking speed and accuracy, the design procedure is simple and its performance is still better than that of the symmetrical FLC-based MPPT method. It is worth mentioning that the only difference between asymmetrical FLC-based MPPT method and symmetrical FLC-based MPPT method is the design of the UOD of $\Delta P_{pv}$ MF; therefore, the implementation complexity of these two methods is the same. That is, asymmetrical FLC-based MPPT method can enhance the tracking speed and tracking accuracy over symmetrical FLC-based MPPT without increasing the calculation burden. To further validate the performance improvement of the proposed methods, simulations on the full day energy production are also provided. The obtained data is also provided in Table 5. In these simulations, the irradiance profile used is a built-in “standard sunny day” profile of the utilized solar array simulator (data obtained from the Sandia National Labs, Alameda, CA, USA). From Table 5, asymmetrical FLC-based MPPT methods also have the best full day energy yield.

### Table 5. Summarized performance of methods.

<table>
<thead>
<tr>
<th>Methods</th>
<th>Average steady state output power</th>
<th>MPPT tracking accuracy</th>
<th>Transient time</th>
<th>Full day energy yield</th>
</tr>
</thead>
<tbody>
<tr>
<td>P&amp;O (0.5%)</td>
<td>206.89 W</td>
<td>92.84%</td>
<td>0.25 s</td>
<td>1466.07 Wh</td>
</tr>
<tr>
<td>P&amp;O (5%)</td>
<td>222.45 W</td>
<td>99.82%</td>
<td>3.13 s</td>
<td>1561.15 Wh</td>
</tr>
<tr>
<td>Symmetrical FLC</td>
<td>222.58 W</td>
<td>99.87%</td>
<td>1.28 s</td>
<td>1571.66 Wh</td>
</tr>
<tr>
<td>Asymmetrical FLC #1</td>
<td>222.65 W</td>
<td>99.91%</td>
<td>0.97 s</td>
<td>1573.92 Wh</td>
</tr>
<tr>
<td>Asymmetrical FLC #2</td>
<td>222.69 W</td>
<td>99.93%</td>
<td>0.91 s</td>
<td>1574.56 Wh</td>
</tr>
</tbody>
</table>

1. The full day energy production is 1580.45 Wh for ideal condition.

### 6. Conclusions

In this paper, a FLC-based MPPT method is proposed for the first time. The design and implementation of the proposed method is discussed in detail in this paper. By using the power variation and voltage variation as the inputs, the calculation is simplified. Comparing with the conventional P&O method, the proposed MPPT method can satisfactorily address the tradeoff between the tracking speed and steady state oscillations. To further improve the performance of the proposed MPPT method, an asymmetrical membership function concept is proposed. Two design procedures are presented and experiments are carried out to validate the effectiveness of the proposed method. Comparing with the symmetrical FLC-based MPPT method, the transient time and the MPPT tracking accuracy are further improved by about 42.8% and 0.06%, respectively.
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Author Contributions

Chun-Liang Liu, Jing-Hsiao Chen, Yi-Hua Liu, and Zong-Zhen Yang have contributed in developing the ideas and the experimental design of the work presented in this manuscript. Chun-Liang Liu and Jing-Hsiao Chen have been involved in conducting the experimental work. All the authors are involved in preparing the manuscript. All authors are responsible for the integrity of the work as a whole.

Conflicts of Interest

The authors declare no conflict of interest.

References


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