Detection Method for Soft Internal Short Circuit in Lithium-Ion Battery Pack by Extracting Open Circuit Voltage of Faulted Cell

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Abstract: Early detection of internal short circuit which is main cause of thermal runaway in a lithium-ion battery is necessary to ensure battery safety for users. As a promising fault index, internal short circuit resistance can directly represent degree of the fault because it describes self-discharge phenomenon caused by the internal short circuit clearly. However, when voltages of individual cells in a lithium-ion battery pack are not provided, the effect of internal short circuit in the battery pack is not readily observed in whole terminal voltage of the pack, leading to difficulty in estimating accurate internal short circuit resistance. In this paper, estimating the resistance with the whole terminal voltages and the load currents of the pack, a detection method for the soft internal short circuit in the pack is proposed. Open circuit voltage of a faulted cell in the pack is extracted to reflect the self-discharge phenomenon obviously; this process yields accurate estimates of the resistance. The proposed method is verified with various soft short conditions in both simulations and experiments. The error of estimated resistance does not exceed 31.2% in the experiment, thereby enabling the battery management system to detect the internal short circuit early.

Keywords: lithium-ion battery pack; soft internal short circuit; model-based fault detection; battery safety; internal short circuit resistance

1. Introduction

Lithium-ion batteries are widely used as a power source in electric devices and electric vehicles [1,2], due to their high power density, high energy efficiency and excellent cycle stability [3,4]. The demand for them is expected to rise continuously in the coming years [5,6]. However, safety concerns related to the lithium-ion batteries still remain [7–9] because hazardous incidents such as fire accidents in the Boeing 787-8 aircraft [10] and battery failures in the Samsung Note7 [11] have been frequently reported by media [12]. The main cause of these two events is internal short circuit (ISCr) in the lithium-ion batteries. The IScr can be caused by manufacturing defects [13,14] and various types of abuse such as overcharge [15,16] and overdischarge [17]. Furthermore, when a magnitude of IScr resistance (R_{ISC}) is lower than a particular value [18], a temperature of the battery exceeds a certain point due to the IScr [19–21]. Then, the battery may experience thermal runaway with a fire and can even explode [22–25]. Therefore, the detection of soft IScr, which has a large magnitude of the R_{ISC}, is more necessary than the detection of hard IScr with a small magnitude of the R_{ISC} for user safety to prevent the lithium-ion battery from causing hazardous events such as the thermal runaway.
Recently, for these reasons, methods for detecting the ISCr have been suggested [26,27]. When the ISCr happens in the battery cell, terminal voltage of the cell decreases rapidly and then temperature of the cell increases drastically; these two characteristics can be used as pre-determined thresholds for detecting the ISCr [26]. However, to obtain the threshold values, prior ISCr-test with the batteries were required. Besides the threshold-based method, a detection algorithm based on an equivalent circuit model of the battery has been introduced [27]. Using variation of estimated parameters in both the equivalent circuit model and the energy balance equation, the method for detecting the ISCr was verified with large magnitude of the $R_{ISCr}$, which was larger than 10 $\Omega$ [27]; the 10 $\Omega$ is considered to be the minimum value which must be detected early before occurrence of the thermal runaway [23,27]. However, this algorithm was verified with only one type of current profile and the similar parameter variation may not be obtained depending on various other current profiles due to absence of the $R_{ISCr}$ in the equivalent circuit model.

The $R_{ISCr}$ is regarded as a promising fault index for detecting the ISCr because it can describe self-discharge phenomenon caused by the ISCr in the equivalent circuit model with $R_{ISCr}$ [28,29] and represent heat generated by the ISCr [30]. Therefore, the ISCr detection methods, which directly use the $R_{ISCr}$ as the fault index, have been introduced [29,31–33]. With measurement data of the self-discharge current and the terminal voltage of the battery with ISCr in the particular experiment configuration, the $R_{ISCr}$ can be calculated correctly [29,31]. However, these experimental methods cannot be used as on-board ISCr detection when the restricted experiment system is not configured in actual application environment. Therefore, after analyzing the self-discharge phenomenon caused by the ISCr, the equation for calculating the $R_{ISCr}$ was derived and then the $R_{ISCr}$ (1~20 $\Omega$) was estimated to detect the ISCr [32]. However, the accuracy of the $R_{ISCr}$ estimated from two different load current profiles was low, because the $R_{ISCr}$ in the equivalent circuit model was not used to estimate open circuit voltage (OCV) of the battery with ISCr. To overcome this error, the previously estimated $R_{ISCr}$ in the model was used to update the model iteratively and to estimate the OCV, and then the next estimated $R_{ISCr}$ (5~50 $\Omega$) became accurate enough to detect the ISCr [33].

For a large capacity and a high power, a lithium-ion battery pack, where many battery cells are connected, is used in actual applications such as electric vehicles and energy storage system for the grid [34,35]. Studies for detecting the ISCr in the battery pack have been suggested [36–38]. The ISCr of the battery pack was detected based on the correlation coefficient of terminal voltages of individual cells [36], and the deviations of both state of charge (SOC) and heat generation power were used to detect the ISCr in the pack [37]. However, these two methods were verified with only the hard ISCr having a magnitude of $R_{ISCr}$ (0.36 $\Omega$ for [36] and 0.35~2.4 $\Omega$ for [37], respectively), which is small enough to cause the dangerous incidents such as the thermal runaway in the cell [30]. Especially, temperature data of the individual cells were needed to detect the hard ISCr correctly [37].

Magnitude, differential value and fluctuation of estimated model parameters were acquired to detect the ISCr with a wide range of $R_{ISCr}$ (1~100 $\Omega$) after estimating the parameters in the mean-difference model of the battery pack [38]. These three detection methods for the battery pack have a common constraint: all terminal voltages of the individual cells in the battery pack must be provided.

If many battery cells are connected in series in the battery pack, many channels with high accuracy and high sample rate for measuring all the individual cell voltages increase the cost of battery management system (BMS). In addition, a data storage unit, needed to save and monitor the measurement data, can lead to increasing the cost of BMS [39]. Furthermore, depending on the applications of the battery pack and the BMS with various topologies, the individual cell voltages may not be provided with high precision and high sample rate and may not be saved due to the cost of the BMS [40,41]. When the data of individual cell voltages are not provided from the BMS, the ISCr detection methods for the pack [36–38] have trouble in deriving the properties of the faulted battery from the battery pack, resulting in problem of detecting the ISCr of the cell in the pack. Therefore, an algorithm for detecting the soft ISCr with load currents and whole terminal voltages of the battery pack is necessary definitely. Moreover, considering data computation, using the whole
terminal voltage for diagnosing the ISCr in the battery pack is more efficient than using all individual cell voltages.

This paper proposes a method for detecting the soft ISCr in the lithium-ion battery pack, where normal batteries and a battery with ISCr are connected in series, with the load currents and the whole terminal voltages of the pack. To reflect the effect of ISCr in the battery pack clearly, the OCV of the faulted cell is extracted from the pack with ISCr. The proposed algorithm estimates the SOC of the battery pack with the extended Kalman filter (EKF) to increase accuracy of the pack SOC. Then, the SOC of the normal cell is obtained with the Coulomb counting method and a stable initial value, which is determined from the estimated SOC of the pack. Using the SOC estimates of the pack and the normal cell, the OCV of the battery cell with ISCr in the pack can be obtained; this shows the self-discharge phenomenon caused by the ISCr obviously. As a result, the $R_{ISCr}$ can be estimated accurately, and the soft ISCr in the battery pack can be detected. To verify the proposed method, various soft ISCr cases were configured for simulation and experiment, and two load current profiles: dynamic stress test (DST) and urban dynamometer driving schedules (UDDS) were used.

The remainder of this paper is organized as follows: the proposed algorithm is carried out in Section 2; the configurations of simulation and experiment are introduced in Section 3; the results of the proposed algorithm and the discussions are presented in Section 4; the conclusions of this study and the outline of future work are summarized in Section 5.

### 2. Method Description

#### 2.1. Overall Scheme for ISCr Detection Algorithm

To detect the soft ISCr in the battery pack, the proposed method estimates the $R_{ISCr}$ of the faulted cell using the whole terminal voltages and the load currents of the pack. As a fault index, the estimated $R_{ISCr}$ can directly inform the user of degree of the ISCr in the pack. If the soft ISCr having a large magnitude of the $R_{ISCr}$ is detected, the BMS can give enough time to cope with the ISCr fault. The overall scheme of the proposed algorithm is depicted in Figure 1, which comprises of four estimation steps: estimating pack SOC ($SOC_p$); normal cell SOC ($SOC_n$); faulted cell SOC ($SOC_f$) and $R_{ISCr}$.

![Figure 1. The scheme of the proposed algorithm.](image)

When the ISCr occurs in a single battery cell, abnormal properties such as the decrease in terminal voltage and the increase in battery temperature are easily observed [42,43]. Hence, measured terminal voltage, current and temperature of the battery cell can be used to detect the ISCr. However, when an
ISCr occurs in the battery pack, which only provides the load currents and the whole terminal voltages of the battery pack, the decrease in the whole terminal voltage caused by the ISCr in the battery pack is not observed conspicuously. Thus, additional decrease in the OCV, induced by the self-discharge current in the faulted cell, should be extracted to ensure the high accuracy of \( R_{ISCr} \) estimates. First of all, using the equivalent circuit model of the battery pack with ISCr and the EKF algorithm, the SOC\(_p\) is estimated. As a second step, the SOC\(_n\) can be calculated by the Coulomb counting method with an initial value of the SOC\(_n\) which is obtained with the estimated SOC\(_p\). Then, using the estimated SOCs of both the battery pack and the normal cells, the OCV of the faulted cell OCV\(_f\) and the SOC\(_f\) are obtained at the third and fourth estimation steps. Once the difference between the initial and present SOC\(_f\) estimates is more than a certain value, which is determined as 0.1 (10% of the total capacity of the cell) and discussed in Section 4.6, the \( R_{ISCr} \) of the faulted cell in the battery pack can be estimated and used to detect the soft ISCr in the pack as the fault index.

2.2. Equivalent Circuit Model of Battery Pack with ISCr

In Figure 2, the battery pack consists of several normal battery cells and one faulted battery cell, and the whole terminal voltage \( V_{tp} \) and the load current \( I_L \) are described, where \( m \) is the number of cells connected in series in the pack. The normal cell is represented by a simple equivalent circuit model [29] composed of the OCV (\( V_{OC} \)) and an internal resistance \( R \). The sum of \( V_{OCs} \) and \( Rs \) of normal cells described in Equations (1) and (2) is used to express the model of normal cells with discretization step in Equation (3), and the sum of the terminal voltages of the normal cells \( V_{t,n} \) can be induced by Ohm’s law in Equation (3) [44].

\[
V_{OC,n}(k) = \sum_{j=1}^{m-1} V_{OC,j}(k),
\]

\[
R_n = \sum_{j=1}^{m-1} R_j,
\]

\[
V_{t,n}(k) = V_{OC,n}(k) + R_n I_L(k).
\]

![Figure 2.](image)

The cell with ISCr is represented by the simple model with the \( R_{ISCr} \), which is connected with the model of the normal cell in parallel [29,38]. The subscript \( f \) is used particularly in parameters associated with the faulted cell. The \( I_L \) is divided into two currents which are the self-discharge current \( I_{1L} \) flowing through the \( R_{ISCr} \) and residual current \( I_{2L} \) (Equation (4)), and \( V_{t,f} \) is the terminal voltage of the faulted cell. The faulted cell model is described in Equations (5) and (6) [33,38]. To represent the model of the battery pack with ISCr, the \( V_{t,p} \) is obtained by adding the \( V_{t,n} \) and the \( V_{t,f} \), as shown in Equation (7).

\[
I_L(k) = I_{1L}(k) + I_{2L}(k),
\]

\[
V_{t,f}(k) = V_{OC,f}(k) + R_f I_{2L}(k),
\]

\[
V_{t,p}(k) = V_{t,n}(k) + V_{t,f}(k).
\]
with the Coulomb counting method \[44\] in Equation (9), where After assuming that \(R\) is the parameter of the normal battery model \[48\]. Using the RLS algorithm, the \(E_{\text{OC}}\) algorithm is used to identify the sum of \(R_n\) and \(R_f\) in Equation (8). The recursive least squares (RLS) algorithm is used to identify the parameter of the normal battery model \[48\]. Using the RLS algorithm, the \(R_p\) is obtained from the \(V_{t,p}\) and the \(I_t\) of the normal battery pack. Then, the estimated \(R_p\) is used to configure the state space model of battery pack with ISCr in the EKF algorithm. When the \(I_t\) is positive during battery pack charging and negative during discharging, in recursive discrete-time form, the \(SOC_p\) is calculated with the Coulomb counting method \[44\] in Equation (9), where \(\eta\) is the charging and discharging efficiency, \(\Delta t\) is the sample period and \(C_n\) is the nominal capacity of the normal battery pack. In this study, the charging and discharging efficiency is defined as 1.

\[
V_{t,p}(k) = V_{\text{OC},p}(k) + R_p I_t(k),
\]

\[
SOC_p(k+1) = SOC_p(k) + \frac{\eta \Delta t}{C_n} I_t(k).
\]

To estimate the \(SOC_p\) using the EKF algorithm, the corresponding equations are listed in Table 1, where \(x_k\) is the \(SOC_p\), \(y_k\) is the \(V_{t,p}\), \(u_k\) is the \(I_t\), \(k\) is the sample index, and \(w_k\) and \(v_k\) are the zero mean Gaussian noise with covariance of \(Q\) and \(T\).

<table>
<thead>
<tr>
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<tr>
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2.3. Estimation of Pack SOC Using EKF

The EKF algorithm is a common method to estimate accurate SOC because the estimates are not affected by measurement noise dominantly due to properties of the battery system reflected in the state space model \[45–47\]. In this paper, the EKF algorithm is used to estimate the \(SOC_p\) correctly. After assuming that \(R_{\text{ISCr}} \gg R_f\) in the model of battery pack with ISCr (Equation (7)), the simplified \(V_{t,p}\) can be expressed with battery pack OCV (\(V_{\text{OC},p}\)) and whole internal resistance \(R_p\) which is the sum of \(R_n\) and \(R_f\) in Equation (8). The recursive least squares (RLS) algorithm is used to identify the parameter of the normal battery model \[48\]. Using the RLS algorithm, the \(R_p\) is obtained from the \(V_{t,p}\) and the \(I_t\) of the normal battery pack. Then, the estimated \(R_p\) is used to configure the state space model of battery pack with ISCr in the EKF algorithm. When the \(I_t\) is positive during battery pack charging and negative during discharging, in recursive discrete-time form, the \(SOC_p\) is calculated with the Coulomb counting method \[44\] in Equation (9), where \(\eta\) is the charging and discharging efficiency, \(\Delta t\) is the sample period and \(C_n\) is the nominal capacity of the normal battery pack. In this study, the charging and discharging efficiency is defined as 1.

\[
SOC_p(k+1) = SOC_p(k) + \frac{\eta \Delta t}{C_n} I_t(k).
\]

To estimate the \(SOC_p\) using the EKF algorithm, the corresponding equations are listed in Table 1, where \(x_k\) is the \(SOC_p\), \(y_k\) is the \(V_{t,p}\), \(u_k\) is the \(I_t\), \(k\) is the sample index, and \(w_k\) and \(v_k\) are the zero mean Gaussian noise with covariance of \(Q\) and \(T\).

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2.4. Estimation of Normal Cell SOC

After starting to estimate the \(SOC_p\), the imprecise \(SOC_p\) can be obtained for several seconds because of the incorrectly assumed initial value of the \(SOC_p\). Thus, the estimated \(SOC_p\) obtained from the stable point \(p_{st}\), where \(P_k\) is lower than a certain small value, is used to estimate the \(SOC_n\),
and the $p_{st}$ is the sample index. By assuming that the $SOC_p(p_{st})$ equals to the $SOC_n(p_{st})$ at the stable point, the next $SOC_n$ can be calculated with the $I_L$ and the Coulomb counting method described in Equation (9).

### 2.5. Estimation of OCV and SOC for Faulted Cell

The relationship between OCV and SOC of the normal battery pack (Figure 3) obtained from the prior test [49] is essential for conducting the proposed algorithm. The fully charged battery pack is rested for 3600 s to obtain the OCV, which is equal to the terminal voltage, at 100% SOC. Then the battery pack is discharged with 0.5C (1 A) for 720 s to set 90% SOC, where the C (C-rate) is defined as the charge and discharge current of the battery, and then rested for 3600 s to get the OCV at 90% SOC. By repeating the process, the relationship between OCV and SOC can be obtained. Using the relationship, the $OCV_p$ and the $OCV_n$ can be acquired and are expressed in Equations (10) and (11), where $h$ is the function representing the relationship. By subtracting $OCV_n$’s from the $OCV_p$, the $OCV_f$ is calculated. In sequence, the $SOC_f$ is obtained from the inverse function $h^{-1}$ of $h$ (Equation (12)).

\[
\hat{V}_{OC,p} = h(\hat{SOC}_p), \quad (10)
\]

\[
\hat{V}_{OC,n} = h(\hat{SOC}_n), \quad (11)
\]

\[
\hat{SOC}_f = h^{-1}(\hat{V}_{OC,f}). \quad (12)
\]

![Figure 3. Relationship between open circuit voltage (OCV) and state of charge (SOC) of the normal battery pack.](image)

In the process of using the $h^{-1}$ to obtain the $SOC_f$, the accuracy of $SOC_f$ is dependent on the slope from the relationship between OCV and SOC; i.e., in the range from 100% SOC to 50% SOC with the steep slope from the relationship a small $SOC_f$ error is caused by error of the $V_{OC,f}$, while a large $SOC_f$ error can be induced by the same error of the $V_{OC,f}$ in the range from 50% SOC to 10% SOC with the gradual slope. To avoid this problem, the data of $V_{t,p}$ and $I_L$ were used to conduct the proposed algorithm until the estimated $SOC_f \leq 0.55$.

### 2.6. Calculation of $R_{ISCr}$

Using the self-discharge phenomenon [32,33], the $R_{ISCr}$ can be estimated with the estimated $SOC_f$. To formulate Equation (16) for calculating the $R_{ISCr}$, the Coulomb counting method is used with respect to the $SOC_f$. $I_L - I_{1L}$ is used in Equation (13), because the faulted cell is discharged from the $I_{2L}$ instead of the $I_L$.

\[
SOC_f(k) = SOC_f(0) + \frac{\Delta t}{Cn} \sum_{n=1}^{k} [I_L(n) - I_{1L}(n)] \quad (13)
\]
To delete the unknown terms, $SOC_f(0)$ and $I_{1L}$, the $k - 1$th equation in Equation (13) is subtracted from the $k$th equation in Equation (13), and then the $I_{1L}$ is replaced with $\frac{V_{i,f}}{R_{ISCr}}$. In Equation (14), $\frac{V_{i,p}}{m}$ is used instead of the $V_{i,f}$ because the $V_{i,f}$ is not provided measurement data from the battery pack with ISCr.

$$SOC_f(k) - SOC_f(k - 1) = \frac{\Delta t}{C_n} I_{n+1}(k) - \frac{\Delta t}{m R_{ISCr}} \sum_{n=p_{st}+1}^{k} V_{i,p}(n)$$  \hspace{1cm} (14)

The estimated $R_{ISCr}$ from Equation (14) using a short interval between $k$ and $k - 1$ is vulnerable to errors of the estimated $SOC_f$ because the slight variation of the estimated $SOC_f$ in a short interval cannot reflect dominant self-discharge phenomenon from the ISCr. Therefore, the interval must be extended by adding the $k - 1, k - 2, k - 3, \cdots, p_{st} + 1$th equations in Equation (14) to the $k$th equations in Equation (14) ($p_{st} + 1 < k$); i.e., the $R_{ISCr}$ is estimated once the difference between the initial estimated SOC ($SOC_f(p_{st})$) and present estimated SOC ($SOC_f(k)$) is more than 0.1, which is 10% of the total capacity of the cell.

$$SOC_f(k) - SOC_f(p_{st}) = \frac{\Delta t}{C_n} \sum_{n=p_{st}+1}^{k} I_{n}(n) - \frac{\Delta t}{m R_{ISCr}} \sum_{n=p_{st}+1}^{k} V_{i,p}(n)$$  \hspace{1cm} (15)

The self-discharge phenomenon from the ISCr can be explained with the last term of Equation (15). For the normal battery cell with $R_{ISCr} \approx \infty$, the last term can be approximated to zero. However, when the ISCr occurs in the cell, the non-zero last term represents an additional decline in the SOC of the faulted cell due to the self-discharge current. Consequently, the estimated $R_{ISCr}$ ($\hat{R}_{ISCr}$) can be obtained with Equation (16) after Equation (15) is rearranged.

$$\hat{R}_{ISCr} = \frac{\frac{\Delta t}{C_n} \sum_{n=p_{st}+1}^{k} V_{i,p}(n)}{[SOC_f(p_{st}) - SOC_f(k)] + \frac{\Delta t}{C_n} \sum_{n=p_{st}+1}^{k} I_{n}(n)}$$  \hspace{1cm} (16)

2.7. Parallel Processing of Proposed Algorithm

Once the $SOC_f(p_{st})$ is obtained, the $SOC_f(p_{st})$ is used in Equation (16) to calculate the $R_{ISCr}$ continuously. If error exists in the $SOC_f(p_{st})$, the error can affect the accuracy of $R_{ISCr}$. Therefore, it is necessary to estimate $R_{ISCr}$s from the various $p_{st}$ positions and apply these estimated $R_{ISCr}$s to the ISCr fault index. Based on the estimates of $SOC_f(p_{st})$, if the difference between $SOC_f(p_{st})$ and $SOC_f(k)$ is more than or equal to 0.01, 0.02, 0.03, \cdots, the proposed methods are carried out sequentially and implemented in parallel with previously executed method to diversify the stable point of estimated SOC of the faulted cell. In this paper, four proposed methods were executed additionally in parallel.

3. Simulation and Experiment

3.1. Simulation Configuration

The simulation model of the battery pack with ISCr was configured with MATLAB/Simulink (MATLAB R2017b, MathWorks, Natick, MA, USA) [50]. In both simulation and experiment configuration, the battery pack was composed of four normal battery cells and a faulted battery cell with ISCr. A first-order RC model [51], where the RC represents a parallel resistor-capacitor sub-circuit, was utilized to describe the normal cell in the battery pack. The parameters for the first-order RC model were estimated with the RLS algorithm [48] and the experimental data of terminal voltage and load current, measured when the normal cell was discharged by load current profiles. The normal cell was same with the cell in the battery pack of the experimental environment. In this study, two load current profiles such as the DST and the UDDS were used to verify the proposed method in simulation and experiment. Prior characteristic tests for obtaining the capacity and the relationship between OCV and SOC of the normal cell were conducted, and these two data were also used for the simulation configuration. The simulation model of the ISCr-faulted cell was represented by connecting
the $R_{\text{ISC}r}$ with the normal model in parallel. In this study, various resistance values such as 50 $\Omega$, 30 $\Omega$, 20 $\Omega$, 10 $\Omega$ and 5 $\Omega$ were used to represent diverse ISCr fault conditions.

### 3.2. Experimental Configuration

Figure 4 shows the experimental set-up for the ISCr tests with the battery packs. Two identical battery packs, A and B, were used to acquire the experimental data. The battery packs were tested in a thermal chamber, and the ambient temperature was maintained at 25 ± 1 °C. The important specifications of the cell are shown in Table 2. The prior tests for battery packs were conducted to obtain the capacities and the relationship between OCV and SOC. Based on the nominal capacity in Table 2, for capacity test, the packs were charged with the constant-current constant-voltage (CC-CV) protocol. For all experiments including the prior tests and the ISCr fault tests, when the batteries were charged, the CC-CV protocol was used. Charge-current was 0.5C (1 A) with upper cutoff-voltage 4.2 V in the CC mode, and cutoff-current was 0.05C (0.1 A) in the CV mode. Then, the packs were discharged with 0.5C as CC discharging [52]. The discharged capacities were regarded as true capacities. The measured true capacities of the battery packs, 2.1974 Ah and 2.1949 Ah for pack A and B, respectively, were used for acquiring the correct relationship between OCV and SOC. To check the distribution of capacities of cells in the pack, the capacity test was conducted for individual cells. As a result, the mean and standard deviation are 2.1944 Ah and 0.0062, respectively, for pack A; and 2.1959 Ah and 0.0071, respectively, for pack B.

The experiments of the battery packs were conducted using a battery test device (Regenerative Battery Pack Test System 17020, Chroma, Taoyuan, Taiwan) with the sample period of 0.1 s. The five 10 $\Omega$ resistances, which have ±5% tolerance, were used to make various true $R_{\text{ISC}r}$s. Their measured true values were 49.91 $\Omega$, 29.98 $\Omega$, 20.00 $\Omega$, 10.02 $\Omega$ and 5.00 $\Omega$, and were used to calculate relative errors of the fault index. These resistances were connected with one of the cells in the pack in parallel to represent the ISCr, and a switch was used to initiate the ISCr faults in the packs when the load current profiles were applied to the packs. For the ISCr experiments, the initial SOC of the pack was set to 90% after the pack was charged and rested for 3600 s. Subsequently, the DST current profile was
used to discharge the pack A until its SOC reaches 10% of its total capacity to prevent the pack from being over-discharged, while the UDDS current profile was used for the pack B.

Table 2. Tested battery.

<table>
<thead>
<tr>
<th>Specification Parameters</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>INR 18650-20R</td>
</tr>
<tr>
<td>Type</td>
<td>LiNiCoMnO₂</td>
</tr>
<tr>
<td>Dimension</td>
<td>Ø18.33 × 64.85 mm</td>
</tr>
<tr>
<td>Mass</td>
<td>45.0 g</td>
</tr>
<tr>
<td>Operating temperature</td>
<td>−20~+75 °C</td>
</tr>
<tr>
<td>Nominal voltage</td>
<td>3.6 V</td>
</tr>
<tr>
<td>Charge cut-off voltage</td>
<td>4.2 V</td>
</tr>
<tr>
<td>Discharge cut-off voltage</td>
<td>2.5 V</td>
</tr>
<tr>
<td>Nominal capacity</td>
<td>2.0 Ah</td>
</tr>
</tbody>
</table>

4. Results and Discussions

4.1. Terminal Voltages of Pack

Figure 5 depicts the terminal voltages of battery pack A and B in the experiments depending on the magnitudes of $R_{ISCr}$. The terminal voltages of the packs were measured until the pack SOC reached 10%. As the magnitude of $R_{ISCr}$ is small, the terminal voltages decreased rapidly compared with the voltages of the normal battery pack, leading to rapid termination of experiments for the battery packs with ISCr. The additional decline in terminal voltages caused by the self-discharge phenomenon of the ISCr was not observed clearly. In addition, because the terminal voltages of the packs were affected by waveforms of load current profiles in common, the terminal voltages fluctuated and the slight difference of voltages between the normal pack and the pack with ISCr was not monitored readily. Therefore, it was difficult to detect the soft ISCr directly with only the measurement data of terminal voltages of the packs.

Figure 5. Terminal voltages of battery packs with different $R_{ISCr}$s in experiment with (a) dynamic stress test (DST) current profile, and (b) urban dynamometer driving schedules (UDDS) current profile.

4.2. Estimation Results of SOCs for Pack and Faulted Cell

As illustrated in Figure 6a, the initial values of $SOC_p$ estimates were 0.5 due to the initially assumed value of the $x_0$, and the estimated $SOC_p$s of the battery pack with ISCr decreased faster than that of the normal battery pack. However, the difference between the normal $SOC_p$ and others.
with various ISCr fault cases did not reflect significantly the effect of self-discharge from the ISCr in the battery pack, consequently leading to inaccurate estimates of the $R_{ISCr}$. Thus, deriving the properties of the faulted cell from the pack with ISCr was necessary to observe the effect of ISCr clearly. The estimated $SOC_f$ is described in Figure 6b with the specific $SOC_f$ range from 90% SOC to 55% SOC. There were no estimated values of $SOC_f$ before the $p_{st}$ was reached, because the $SOC_n$ was calculated after the $p_{st}$ was reached. Please note that by extracting the $V_{OC,f}$ with these $V_{OC,n}$ and $V_{OC,p}$ from the pack with ISCr, the effect of the self-discharge phenomenon, which is not dominantly observed in the $SOC_p$ (Figure 6a), becomes enlarged noticeably in the $SOC_f$ (Figure 6b).

![Figure 6. Estimated SOCs with different $R_{ISCr}$s in experiment with DST current profile: (a) battery pack and (b) faulted battery cell.](image)

4.3. Estimated $R_{ISCr}$s from Parallel Processing

When the battery pack A was connected with true $R_{ISCr}$ (49.91 Ω) and discharged with the DST current profile, the $R_{ISCr}$s were estimated from different four stable points of estimated SOC of the faulted cell ($SOC_f(p_{st})$) using the parallel processing (Figure 7). Although the four proposed methods were executed additionally in parallel with the firstly implemented method to diversify the $SOC_f(p_{st})$s, the number of $SOC_f(p_{st})$s can be different in accordance with the ISCr fault conditions in the pack; i.e., even though the four proposed algorithms are added sequentially in all ISCr fault cases, new $SOC_f(p_{st})$s may not be extracted because of the condition, where the $SOC_f(p_{st})$ was obtained if the $P_k$ was lower than the certain small value ($1.4 \times 10^{-6}$) in Section 2.4. In the case of the experiment with the true $R_{ISCr}$ (49.91 Ω), the 1st stable point were obtained from the firstly executed method, while the three stable points were extracted from the the four added algorithms. Figure 7 shows the slightly different $\hat{R}_{ISCr}$s for the true $R_{ISCr}$ (49.91 Ω). Although the $\hat{R}_{ISCr,A}$ obtained from the 4th stable point was most accurate among them in this case, the order of accuracy of $\hat{R}_{ISCr}$s from the diverse stable points was changed depending on various ISCr fault cases. Therefore, to reflect all $\hat{R}_{ISCr}$s in an ISCr fault condition, mean value ($\overline{R_{ISCr}}$) of them was used as the fault index in simulation and experiment results.
The large difference between the SOC index, which was calculated with the \( \hat{R}_{ISCr} \), and the 1st stable point, where the \( \hat{R}_{ISCr,1} \) starts to be obtained, were different. Thus, the different start points for estimating the \( R_{ISCr} \)s are aligned to zero in Figure 8, and the time of x-axis represents the total time used to obtain the \( R_{ISCr} \) with the \( \hat{R}_{ISCr} \). Estimation results from two different current profiles were similar, and the values of \( R_{ISCr} \) slightly fluctuated because they were affected by waveforms of the current profiles.

The \( R_{ISCr} \) in Equation (16) is estimated with difference between the SOC\(_f\)(\( p_{st} \)) and the SOC\(_f\)(\( k \)), which reflects the self-discharge phenomenon caused by the ISCr. At the same time, to discharge the pack, the difference between the SOC\(_f\)(\( p_{st} \)) and the SOC\(_f\)(\( k \)) becomes large as the magnitude of \( R_{ISCr} \) is small (Figure 6b). In addition, the large difference can be obtained from long discharge time. The large difference between the SOC\(_f\)(\( p_{st} \)) and the SOC\(_f\)(\( k \)) is insensitive to errors of estimated SOC\(_f\), leading to accurate estimates of the \( R_{ISCr} \). In cases of ISCr 50 Ω, 30 Ω and 20 Ω, compared to cases of ISCr 10 Ω and 5 Ω, large errors of the \( R_{ISCr} \), caused by errors of estimated SOC\(_f\), occur in the early stage for estimating the \( R_{ISCr} \) because of subtle difference between the SOC\(_f\)(\( p_{st} \)) and the SOC\(_f\)(\( k \)) in short discharge time. However, the \( R_{ISCr} \)s in cases of ISCr 50 Ω, 30 Ω and 20 Ω gradually approach true \( R_{ISCr} \)s because the difference between the SOC\(_f\)(\( p_{st} \)) and the SOC\(_f\)(\( k \)) becomes large gradually as the pack is discharged, resulting in the dominant effect of the self-discharge phenomenon compared with that of the estimation errors of SOC\(_f\). It is also the reason that the \( R_{ISCr} \) is used as the fault index, which was calculated with the \( \hat{R}_{ISCr} \)s for the different stable points in the parallel processing considering errors caused by the position of SOC\(_f\)(\( p_{st} \)). Although the large difference was obtained for each cases ISCr 10 Ω and 5 Ω, the \( R_{ISCr} \) still had errors, because using the \( \frac{V_{f}}{m} \) instead of the \( V_{i_f} \) in Equation (16) greatly affected the \( R_{ISCr} \) estimates compared to the cases of ISCr 50 Ω, 30 Ω and 20 Ω; i.e., while the \( \frac{V_{f}}{m} \) was similar with the \( V_{i_f} \) for ISCr 50 Ω, 30 Ω and 20 Ω, the difference between the \( \frac{V_{f}}{m} \) and the \( V_{i_f} \) became large in cases of ISCr 10 Ω and 5 Ω, leading to large errors of the \( R_{ISCr} \).

To evaluate the accuracy of the \( R_{ISCr} \), relative errors of the estimates were calculated with Equation (17). The relative errors of the final values in \( R_{ISCr} \) (final relative error) with the various ISCr fault conditions are shown in Table 3. It should be noted that the final relative errors are less than or equal to 10% except for the ISCr 5 Ω case. Even though the final relative errors of ISCr 5 Ω in the DST and the UDDS were about 26%, the ISCr fault (5 Ω) can be detected with the \( R_{ISCr} \). In addition, although the magnitude of \( R_{ISCr} \) (10 Ω) is regarded as the minimum value which must be detected early [23,27], the \( R_{ISCr} \) (5 Ω) in the cell cannot sufficiently increase the temperature of the battery.

**Figure 7.** Estimated \( R_{ISCr} \)s from different stable points in experiment with true \( R_{ISCr} \) 49.91 Ω and DST current profile.

**4.4. Estimation Results of \( R_{ISCr} \) in Simulation**

Figure 8a shows the \( \hat{R}_{ISCr} \)s with different ISCr fault conditions when the DST current profile was applied to the pack with ISCr, and Figure 8b depicts the \( \hat{R}_{ISCr} \)s obtained from the UDDS current profile. The \( \hat{R}_{ISCr} \)s in the specific SOC\(_f\) range from 90% SOC to 55% SOC are described in Figure 8. Depending on the various ISCr fault cases, the SOC\(_f\)(\( p_{st} \)) and the 1st stable point, where the \( \hat{R}_{ISCr,1} \) starts to be obtained, were different. Thus, the different start points for estimating the \( R_{ISCr} \)s are aligned to zero in Figure 8, and the time of x-axis represents the total time used to obtain the \( R_{ISCr} \) with the \( \hat{R}_{ISCr} \). Estimation results from two different current profiles were similar, and the values of \( R_{ISCr} \) slightly fluctuated because they were affected by waveforms of the current profiles.
which is too low to cause the thermal runaway [30,37]. The reason that the magnitude of the $R_{ISCr}$ is 5 $\Omega$ and more for verification is to show that the proposed algorithm can be applied to detection of the soft ISCr. If the proposed method detects various soft ISCr faults, we can conclude that there is sufficient time to provide against the thermal runaway in the battery pack.

$$\text{Relative error} = \left| \frac{R_{ISCr} - \overline{R_{ISCr}}}{R_{ISCr}} \right| \times 100\% \quad (17)$$

Figure 8. Estimated $\overline{R_{ISCr}}$s from the various ISCr fault cases in simulations: (a) DST current profile and (b) UDDS current profile and in experiments: (c) DST current profile and (d) UDDS current profile.

Table 3. Final relative errors (%) of $\overline{R_{ISCr}}$ in simulation depending on the ISCr faults.

<table>
<thead>
<tr>
<th>Discharge Condition</th>
<th>True ISCr Resistance</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>5 $\Omega$ 10 $\Omega$ 20 $\Omega$ 30 $\Omega$ 50 $\Omega$</td>
</tr>
<tr>
<td>DST</td>
<td>26.2 9.9 7.9 4.1 2.1</td>
</tr>
<tr>
<td>UDDS</td>
<td>25.4 9.0 4.4 2.9 1.7</td>
</tr>
</tbody>
</table>

4.5. Estimation Results of $R_{ISCr}$ in Experiment

Figure 8c,d show the estimation results of the $\overline{R_{ISCr}}$ in the experiment with the DST and the UDDS current profiles. The tendency of the obtained $\overline{R_{ISCr}}$ in experimental results was similar to that of the simulation due to the reasons explained in Section 4.4. In addition, the simplified model of the battery pack with ISCr, which was induced by assuming $R_{ISCr} \gg R_f$ (Equation (8)), was validated, because all estimated $R_{ISCr}$s were indeed much greater than the $R_f$ in both simulation and experiment.
In particular, the main difference between simulation results and experimental results was that the relative errors in the experiment increased (Table 4) because in all ISCr faults cases, the $R_{ISCr}$s in the experiment were generally under-estimated compared to those of the simulation. Contrary to the configuration of the simulation, the characteristics of individual cells in the experiment, such as capacity, internal resistance, and relationship between OCV and SOC, were not identical. Due to both the model difference and measurement noise, the errors of $SOC_f$ estimates of the experiment increased compared to that of the simulation, leading to large errors of the estimated $SOC_f$ in the experiment. This large errors of $SOC_f$ estimates increased the values of the denominator in Equation (16); this was main cause to incur the under-estimation of $R_{ISCr}$ in the experiment. Meanwhile, in case of ISCr 5 $\Omega$, the final relative errors in the experiments decreased compared to the results of simulation, because the $R_{ISCr}$ for ISCr 5 $\Omega$ with large relative errors in the simulation became close to the true value of $R_{ISCr}$ by the under-estimation in the experiment. Although the relative errors of the experiment increased compared to those of the simulation, the obtained $R_{ISCr}$ was accurate enough to be used as the fault index to detect the soft ISCr before the thermal runaway occurs in the battery pack, and to classify the various ISCr fault conditions.

<table>
<thead>
<tr>
<th>Discharge Condition</th>
<th>True ISCr Resistance</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>5.0 $\Omega$</td>
</tr>
<tr>
<td>DST</td>
<td>3.3</td>
</tr>
<tr>
<td>UDDS</td>
<td>2.2</td>
</tr>
</tbody>
</table>

### 4.6. Other Discussions

For the normal battery pack, the self-discharge current $I_{1L}$ cannot flow through $R_{ISCr}$ and the faulted cell is discharged by the load current $I_L$. Therefore, the $SOC_f$ is represented as Equation (18) with the $I_L$, and the equation for obtaining the $R_{ISCr}$ for the normal battery pack ($\hat{R}_{ISCr,n}$) can simply be expressed with both the measured $V_{t,p}$ and the $\epsilon$ (Equation (19)) which is the difference value between the estimated $SOC_f$ and the true $SOC_f$.

$$SOC_f(k) = SOC_f(p_{st}) + \frac{\Delta t}{C_{n}} \sum_{n=p_{st}+1}^{k} I_L(n)$$  \hspace{1cm} (18)

$$\hat{R}_{ISCr,n} = \frac{\frac{\Delta t}{C_{n}} \sum_{n=p_{st}+1}^{k} V_{t,p}(n)}{\epsilon}$$  \hspace{1cm} (19)

When the $SOC_f$ is estimated with the DST load currents and the whole terminal voltages of the normal battery pack in the specific region, the maximum value and relative error of the $\epsilon$ were 0.0197 and 3.6%, respectively, for the simulation; and were 0.0502 and 8.4%, respectively, for the experiment. Actually, in Section 4.5 as the reason for the under-estimation of $R_{ISCr}$ in the experiment, it was checked that the error of estimated $SOC_f$ for the experiment was larger than it for the simulation. These two maximum errors were used to calculate the $\hat{R}_{ISCr,n}$ for the normal cases in both simulation and experiment. Due to the non-zero value of $\epsilon$, the obtained $\hat{R}_{ISCr,n}$ monotonically increased. In Figure 9, the dotted lines show $\hat{R}_{ISCr,n}$s of the normal battery pack in the specific region and represent reliable maximum values of $R_{ISCr}$s for all ISCr fault cases. If the obtained $R_{ISCr}$ exists in the region above the dotted line, the $R_{ISCr}$ are determined as unreliable estimation values, while the region under the dotted line is defined as the reliable estimation region of the $R_{ISCr}$.
Figure 9. Reliable maximum $\hat{R}_{ISCr,n}$ in simulation and experiment with normal battery pack and DST current profile: (a) simulation and (b) experiment.

From the stable point $p_{st}$, sufficient time to obtain reliable $\hat{R}_{ISCr}$ is necessary. If the $\hat{R}_{ISCr}$ is obtained when the $k$ is very close to the $p_{st}$ in Equation (16), the $\hat{R}_{ISCr}$ can be located in the region above the dotted line, because the values of the dotted line are small in the early stage shown in Figure 9 and the obtained $\hat{R}_{ISCr}$ for ISCr fault cases can be affected by both the estimation errors of $SOC_f$ and measurement noise in the $V_{t,p}$ and the $I_L$. Thus, in the proposed method, the $R_{ISCr}$ was estimated once the difference between the $SOC_f(p_{st})$ and the $SOC_f(k)$ was more than or equal to 0.1; this condition guaranteed that the $\hat{R}_{ISCr}$'s in various ISCr faults of simulation and experiment exist in the reliable estimation region.

When a battery pack is manufactured with used lithium-ion cells, a variation in the characteristics of individual cells in the pack becomes large [41], resulting in large error of $R_{ISCr}$ estimates. However, the battery pack made with used cells can be operated with balanced voltage and SOC due to the proper screening process in configuring the battery pack [53]. Therefore, the proposed method can be applied in both fresh and reused battery pack.

If an ambient temperature in operation environment of the battery varies and the battery model which does not reflect thermal properties of the battery is used to estimate the SOC, errors of estimated SOC become large [54–57], leading to large error of $R_{ISCr}$ estimates. Although in this study the proposed method focused on detecting the soft ISCr at constant temperature, depending on real applications the ambient temperature can be changed [58]. Therefore, detection of ISCr in the battery under varying ambient temperature is a meaningful and interesting subject of research as a future work.

5. Conclusions

In this paper, a method for detecting the ISCr early in the lithium-ion battery pack was introduced. The battery pack with ISCr was represented with the equivalent circuit model with the $R_{ISCr}$ and the EKF algorithm was used to estimate $SOC_p$ accurately. The OCV of the faulted cell was derived from the battery pack with ISCr to reflect the self-discharge phenomenon caused by the ISCr in the battery pack clearly, because the effect of ISCr in the battery pack was not observed in both the $V_{t,p}$ and the $SOC_p$ obviously. Using the Coulomb counting method and the stable initial value of the $SOC_n$, obtained from the estimated $SOC_p$, the $SOC_n$ was calculated. The $OCV_p$ and the $OCV_n$ were acquired from the relationship between OCV and SOC of the normal battery pack, and then the $OCV_f$ was calculated with these two OCV values. Subsequently, the $R_{ISCr}$ ($5\sim50\,\Omega$) of the battery pack with ISCr was estimated accurately using the self-discharge phenomenon in the $SOC_f$. The proposed algorithm was verified for various soft ISCr fault conditions such as diverse magnitudes of true $R_{ISCr}$ and two load current profiles in both the simulation and the experiment. In addition, through estimating the
R_{ISC_r} from the normal battery pack and analyzing it, it was checked that estimated R_{ISC_r}s in the various fault cases were reliable. Using the proposed algorithm, the R_{ISC_r} was estimated with high accuracy, and the soft ISC_r in the battery pack can be detected using the R_{ISC_r} as the fault index. Our future research will focus on increasing the accuracy of the R_{ISC_r} estimates and extending the availability of our proposed algorithm to both the aged battery pack and the battery under varying ambient temperature.

**Author Contributions:** M.S. suggested the main idea of this paper and constructed the proposed detection technique. T.G. contributed the mathematical modeling and thoroughly reviewed the paper. M.P. conducted the experiments and thoroughly reviewed the paper. S.W.K. supervised the work and finally reviewed the paper.

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**Conflicts of Interest:** The authors declare no conflict of interest.

**Nomenclature**

**Symbols**

R_{ISC_r} ISC_r resistance, Ω  
V_t Terminal voltage, V  
I_L Load current, A  
V_{OC} OCV, V  
R Internal resistance, Ω  

I_{1L} Self-discharge current, A  
I_{2L} Residual current, A  
η Charging and discharging efficiency  
Δt Sample period  
C_n Nominal capacity  
h Function of relation between OCV ans SOC  
h^{-1} Inverse function of h  
e Difference error  
x EKF state variable  
y EKF output variable  
u EKF input variable  
w, v EKF process/measurement errors  
Q, T EKF covariances of Gaussian noise  
A EKF state transition matrix  
C EKF observation matrix  
P EKF error covariance matrix  
L EKF Kalman gain  
f EKF state update function  
g EKF output update function  
p_{st} Stable point, sample index
Subscripts

- \( p \) battery pack
- \( f \) faulted cell
- \( n \) normal cell
- \( k \) iteration index
- \( j \) cell index
- \( m \) number of cells in the pack
- \( 1, 2, 3, 4 \) 1st, 2nd, 3rd, 4th stable points

Abbreviations

- ISCr Internal short circuit
- OCV Open circuit voltage
- SOC State of charge
- BMS Battery management system
- EKF Extended Kalman filter
- DST Dynamic stress test
- UDDS Urban dynamometer driving schedule
- CC-CV Constant-current constant-voltage

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