Optimal Operational Adjustment of a Community-Based Off-Grid Polygeneration Plant using a Fuzzy Mixed Integer Linear Programming Model

Aristotle T. Ubando 1,* , Isidro Antonio V. Marfori III 1, Kathleen B. Aviso 2 and Raymond R. Tan 2

1 Mechanical Engineering Department, De La Salle University, 2401 Taft Avenue, Manila 0922, Philippines; isidro.marfori@dlsu.edu.ph
2 Chemical Engineering Department, De La Salle University, 2401 Taft Avenue, Manila 0922, Philippines; kathleen.aviso@dlsu.edu.ph (K.B.A.); raymond.tan@dlsu.edu.ph (R.R.T.)

* Correspondence: aristotle.ubando@dlsu.edu.ph; Tel.: +632-524-4611

Received: 31 December 2018; Accepted: 7 February 2019; Published: 16 February 2019

Abstract: Community-based off-grid polygeneration plants based on micro-hydropower are a practical solution to provide clean energy and other essential utilities for rural areas with access to suitable rivers. Such plants can deliver co-products such as purified water and ice for refrigeration, which can improve standards of living in such remote locations. Although polygeneration gives advantages with respect to system efficiency, the interdependencies of the integrated process units may come as a potential disadvantage, due to susceptibility to cascading failures when one of the system components is partially or completely inoperable. In the case of a micro-hydropower-based polygeneration plant, a drought may reduce electricity output, which can, in turn, reduce the level of utilities available for use by the community. The study proposes a fuzzy mixed-integer linear programming model for the optimal operational adjustment of an off-grid micro-hydropower-based polygeneration plant seeking to maximize the satisfaction levels of the community utility demands, which are represented as fuzzy constraints. Three case studies are considered to demonstrate the developed model. The use of a diesel generator for back-up power is considered as an option to mitigate inoperability during extreme drought conditions.

Keywords: off-grid polygeneration; micro-hydropower plant; fuzzy optimization; mixed-integer linear programming; dual-turbine; multi-objective

1. Introduction

In developing countries, high priority is given to providing access to clean electricity and other essential utilities in remote communities [1]. Access to such amenities is critical to enhancing the quality of life and achieving the Sustainable Development Goals (SDGs) [2]. The seventh SDG focuses on universal access to affordable and reliable energy [3], but as recent as 2014, more than 1 billion people (i.e., about 15% of world population) still had no access to electricity [4]. The lack of access is especially true for geographically isolated rural communities, for which grid connectivity may not be economically or physically viable.

Efforts in providing power to off-grid communities have been pursued to address the rural electrification issue. From 2008 to 2017, the global off-grid renewable energy capacity has grown by about 300%, providing about 6.5 GW in total [5]. The integration of various renewable energy technologies to locally integrated energy sectors (LIES) have been found to significantly reduce
the resource consumption and carbon footprint associated with energy supply [6]. Despite the dependence to climatic conditions and the inherent variability of renewable energy sources, a hybrid power system was proposed to combine renewable energy technologies with conventional energy sources while minimizing the cost and energy losses [7], and accommodating uncertainties, especially in remote areas [8]. The development of off-grid renewable energy systems largely varies and depend on the locally available resources and requirements of the community. In the past decade, an increase in the demand for solar energy solutions has been observed as solar photovoltaic (PV) technology matures [5]. However, for areas where access to flowing bodies of water is possible, micro-hydropower plants are a practical choice for irrigation and to generate electricity for the community [9]. Micro-hydropower plants are a robust and inexpensive renewable energy option [10]. In the context of hybrid power systems, micro-hydropower plants present a viable renewable energy option, given the right geographic location with good power generation potential [11]. A typical off-grid community will also require other utilities, such as purified water for household use. Aside from access to electricity and clean water, such communities may also require ice to preserve their produce (e.g., fish or vegetables). Polygeneration systems have been designed previously to provide such basic requirements [12]. These systems provide an efficient, integrated means to produce multiple material and energy products, which leads to improved system-wide efficiency and reduced emissions, waste, and natural resource consumption [13]. Polygeneration is generally defined as the co-production of various outputs along with electricity; the co-products can include heat (i.e., steam or hot water), cold energy (e.g., ice or chilled water), purified water, and chemical products [14]. In a polygeneration system, the interdependencies among integrated process units make the whole system vulnerable to cascading failures [10]. An operational disruption of such nature arising from any portion of the system leads to the causal operational disturbance cascading through the entire process network. Such disruption significantly affects the overall performance of the system causing divergence from the operational production state of the system [15]. Process systems engineering (PSE) models can play an important role to minimize production loss while maximizing opportunities to operate at an abnormal state for a brief period of time. The optimization approach may then be utilized to find the optimal operational adjustment of a polygeneration system at a perturbed state. A disruptive event, which can be caused by an external (e.g., natural disaster) or internal (e.g., equipment malfunction) trigger, can be measured via a dimensionless index known as inoperability [16]. The inoperability concept may be applied in representing operational disruption using the inoperability input-output modelling (IIM) framework [17]. In the context of a process network such as the polygeneration system, the inoperability can be defined as the loss of capacity of a system to operate relative to its normal state, and is represented by a dimensionless number ranging from a value of 0 (fully operational) to 1 (fully non-operational). This index has been used extensively in the literature. A linear programming (LP) model has been utilized for the optimal allocation of resources aiming to minimize losses in the event of a disruption [18]. The IIM theory was further developed in detail presenting case studies of disruption such as malevolent attacks [19]. The IIM framework has later been used as a sequential decision support tool for bioenergy systems [20]. It has been extended to deal with energy-related problems such as the optimization of the energy supply chain [21] and the identification of process bottlenecks in energy systems [22].

This work focuses on presenting a novel application of the inoperability concept on the operational adjustment of a community-based off-grid micro-hydropower-based polygeneration plant. Micro-hydropower plants generate up to 100 kW of electricity [23], which is enough for a small community with 20 to 30 households. Methods for the design [24], feasibility assessment [25], and identification of near-optimal solutions [26] for such facilities have been conducted previously. However, few studies have been conducted for micro-hydropower-based polygeneration systems for remote communities. An off-grid polygeneration system has been designed by Ray et al. [27] for an off-grid community in India using an LP model incorporating economic and reliability analysis. A generic decision support software was developed by Khalilpour and Vassallo [28] for the optimal
design of a polygeneration system for off-grid distributed generation and storage system. However, neither of these studies incorporated micro-hydropower plants as a technology option. Recent studies on the optimal design of a micro-hydropower based polygeneration plant have been conducted using fuzzy optimization models. Such formulations are characterized by non-sharp boundaries of feasible regions, such that constraints can be partially satisfied as defined by their membership functions [29]. A fuzzy LP (FLP) model was developed by Ubando et al. [30] for the optimal design of an off-grid polygeneration plant using a superstructure that includes a micro-hydropower plant, a biomass-based Stirling engine, an ice plant, a diesel engine, and a sewage treatment facility. The work was later extended to a fuzzy mixed-integer linear programming (FMILP) model by Ubando et al. [12] considering vapor compression and absorption chillers as refrigeration options. However, these models were developed for system planning and design, and lack the capability to be used for optimal operational adjustment under abnormal conditions. An off-grid micro-hydropower-based polygeneration system is susceptible to drought which can reduce water flowrate available for the turbines; also, mechanical problems with system components may take longer to repair due to the time delays in bringing spare parts to the site. Kasivisvanathan et al. [15] developed a mixed-integer linear programming (MILP) model which provided the solution for the optimal operational adjustment of a gas-fired polygeneration plant for commercial use. In this study, the objective function is to maximize the operating profit (or minimize economic losses) of the system while employing the inoperability in each process in cases when the system experiences a disruption. A P-graph approach to the same problem was later developed by Tan et al. [31]. In the case of a polygeneration plant for a remote community, it is necessary to consider the demand for each product separately, depending on the needs of the inhabitants. This aspect is addressed in this work using fuzzy optimization using the approach developed by Zimmerman [29]. This approach is known as a “symmetric” fuzzy optimization model, where both constraints and (multiple) objectives are represented by fuzzy membership functions. FLP has been previously used for the optimal design of systems such as combined heat and power plants [32], trigeneration plants [33], and integrated biorefineries [34]. It was extended later to fuzzy MILP (FMILP) for the optimal planning of bioenergy parks [35], multifunctional bioenergy systems [36], and biofuel supply chain networks [37]. However, these models again focused on system design rather than abnormal operations.

This study develops an FMILP model for the optimal operational adjustment of a micro-hydropower-based polygeneration system for off-grid communities. It is assumed that the likely disruption is in the form of drought with varying intensity, which can be introduced into the model as an inoperability parameter. Three case studies are used to demonstrate the efficacy of the developed model under different drought scenarios. The case studies consider different turbine configurations and the option of having a diesel generator back-up. The rest of the paper is organized as follows. The formal problem statement is given, followed by the model formulation. Three case studies then follow. Lastly, conclusions and future prospects are discussed.

2. Problem Statement

The statement of the problem is formally defined similar to that proposed by Kasivisvanathan et al. [15] and stated as follows:

- An off-grid polygeneration system is assumed to have \( M \) number of products and \( N \) number of installed process units.
- The process units are characterized by fixed input-output stream proportions described by either the yield, efficiency, or the coefficient of performance, depending on the appropriate factor for each unit.
- Each process unit is defined by a minimum part-load operating level below which unstable or uneconomical operation occurs. The input-output ratios of streams for each unit remain fixed for the entire feasible operating range bound by a lower limit (minimum part-load operating level) and an upper limit (the rated capacity with a safety factor). The operational flexibility of the
off-grid polygeneration system is defined by this operational range. The off-grid polygeneration system is further assumed to operate at a new steady state mode where the inoperability transpires.

- For each product stream, a fuzzy membership function is defined to describe the limits on net output, as dictated by basic requirements of the community inhabitants and are assumed to be constant. The fuzzy membership functions are assumed to be linear, and can thus be defined by specifying upper and lower limits. The upper limits signify normal requirements, while the lower limits signify the bare minimum requirements.

- The problem is to determine the optimal adjustment of operating capacities and allocation of streams for each process unit given an inoperability on the availability of water (drought scenario).

3. Fuzzy Mixed Integer Linear Programming Model

The basic MILP model for optimizing abnormal operations was developed in a previous work, and is given in the Appendix A [15]. The weakness of such a formulation is that it places extreme preference for product streams of higher economic value, often at the expense of the other lower-value products. While applicable to many commercial or industrial applications, in the case of remote rural communities, the actual value of basic needs might not be fully reflected in their prices. Instead, a given community may have a set of subsistence-level requirements for essential supplies, all of which need to be balanced based on what are deemed as tolerable shortages. These limits can in turn be modelled as fuzzy membership functions. Thus, the basic MILP model is modified into a fuzzy model to allow for such balanced rationing of capacity during a crisis [38]. The fuzzy MILP model is composed of the objective function and the constraints. The objective function of the model is shown in Equation (1):

$$\text{maximize } \lambda$$

where $\lambda$ is the degree of satisfaction which is represented in every membership function in the model. The $\lambda$-value maximizes the lowest degree of satisfaction achieved among all identified fuzzy objectives. The degrees of satisfaction range from 0 to 1, with 1 signifying complete satisfaction, 0 indicating undesirable result, and values between 0 to 1 illustrating partial satisfaction of the objective. In Figure 1, the degree of satisfaction allows the translation of a variable-value shown in the abscissa into values ranging from 0 to 1 in the ordinate following a linear relation known as the linear membership function.

![Figure 1. The fuzzy linear membership function for (a) maximization, and (b) minimization.](image)

The optimal operational adjustment of the off-grid polygeneration system is subject to the following constraints. The technology matrix is introduced to define the optimal product output of the polygeneration system together with the process scaling vector as shown in Equation (2):

$$\text{s.t. } \textbf{A} \times \textbf{x} = \textbf{y}$$

where $\textbf{A}$ is the technology matrix consisting of elements $a_{ij}$ where $i$ represents the product stream and $j$ represents the technology considered. The technology matrix $\textbf{A}$ is defined by a steady-state operational
material and energy balance which are assumed to be scale invariant. In cases where the material or energy stream is identified as a raw material to a process, the value in matrix $A$ would be represented by a negative value. Similarly, the positive values in matrix $A$ represent the product or by-product streams generated from a process. The process scaling vector $x$ with all elements equal to 1, indicates that all processes $j$ in the system are operating in their optimal capacity. As the drought scenario sets in, the optimal operation adjustment in the off-grid polygeneration will be reflected in the change in values of $x$. The product output $y$ of the off-grid polygeneration system represents the optimal production level of each product stream $i$. The product demand limits utilize membership functions which maximize the product output levels of the polygeneration system given a threshold demand range described in Equation (3). The application of the linear membership function for maximization was introduced by Zimmermann [39] using a fuzzy set framework:

$$y_i \geq y_i^l + \lambda(y_i^u - y_i^l) \quad \forall i$$

(3)

$$y_i \leq y_i^l + \lambda(y_i^u - y_i^l) \quad \forall i = fuel$$

(4)

where $y_i^l$ is the lower threshold limit of each material or energy stream $i$, and $y_i^u$ is the upper threshold limit of each material or energy stream $i$. Equation (3) represents the fuzzy linear membership function for maximizing a product stream. In Equation (3), any value less than $y_i^l$ is considered undesirable while any value greater than $y_i^u$ is highly desirable for a product stream $y_i$. The values between $y_i^l$ and $y_i^u$ are considered as partially acceptable where degrees of satisfaction are described by a linear function with a slope of $\lambda$. Equation (4) represents the fuzzy linear membership function for minimizing a product stream which in this case is the fuel. For minimizing the fuel stream in Equation (4), $y_i^l$ is the highly desired value, $y_i^u$ is the undesirable value, and the values in between are treated as partially acceptable values. The diagram for the fuzzy linear membership function for maximization used in Equation (3) and for minimization used in Equation (4) are shown in Figure 1. The introduction of the drought scenario is described by Equation (5):

$$y_i > (1 - D) y_i^* \quad \forall i \in R$$

(5)

where $D$ is the drought intensity factor with values ranging from 0% to 100%. A drought intensity factor of $D = 0$ represents a no drought scenario signifying full operational flow level of the river water during normal condition, while a drought intensity factor of $D = 1$ implies that there is no river water flowing. The $y_i^*$ is the normal product output vector which represents the state of fully operational flow levels for all products $i$ in the subset of $R$. The subset of $R$ identifies all products which utilize the river water as raw material. The introduction of the binary variable vector is shown in Equations (6)–(8):

$$b_j x_j^l \leq x_j \leq b_j x_j^u \quad \forall j$$

(6)

$$b_j \in \{0,1\} \quad \forall j$$

(7)

$$f^l \leq \sum_j b_j \leq f^u \quad \forall j \in E$$

(8)

The operational capacity limit of each technology $j$ is described by the lower limit operational capacity $x_j^l$ and the upper limit operational capacity $x_j^u$. Equation (7) defines whether a technology $j$ should operate ($b_j = 1$) or not ($b_j = 0$) during the chosen scenario. The topological binary constraint for the simultaneous selection of power generating technologies within a subset of $E$ is shown in Equation (8) where the subset $E$ represents all power generating technologies. The number of allowable operating technologies is limited by the minimum and maximum number defined by $f^l$ and $f^u$, respectively. The introduction of the binary variable vector $b$ in Equations (6)–(8), enables the developed model in becoming a mixed-integer linear programming which provided the selection of
the appropriate technology for the off-grid polygeneration system. Lastly, Equation (9) ensures that the $\lambda$-value falls within the range of 0 to 1:

$$0 \leq \lambda \leq 1$$ (9)

It should be noted that equipment capital cost and stream prices are not included in the model. In the context of operational optimization, all equipment are assumed to have sunk costs, and there is no longer an option to modify them within any given scenario (Kasivisvanathan et al., [15]). Also, as the model deals with crisis conditions for remote rural communities, it is assumed that actual physical requirements for basic needs take precedence over cost considerations during the emergencies envisioned in this work. The model is solved utilizing Lingo 12.0, linked with MS Excel using the object linking and embedding (OLE) function of Lingo. The computer hardware used is powered by an Intel Core i7 processor with 8 GB of random access memory (RAM). Computational time for the examples in this work was negligible.

4. Case Study

Three case studies are presented to demonstrate the model developed. The first case study focuses on a basic off-grid community-based polygeneration system using a single turbine micro-hydropower plant. The second case study uses the same system in Case Study 1, but considers an additional back-up diesel generator. The third case study considers a dual turbine, instead of a single turbine, coupled with a back-up diesel generator.

4.1. Case Study 1

The case study considers a community of approximately 500 people requiring electricity, clean water, and ice. A single-turbine micro-hydropower plant produces 105 kW of electricity. Since this case study excludes the use of the diesel generator set as a back-up power generator, an ultra-filtration (UF) water treatment facility is considered to produce the required potable water for the community inhabitants, while a centralized ice plant provides for the cooling and refrigeration needs. The balanced process matrix of the case study is shown in Table 1. This matrix also shows the allocation of water flow to various uses within the community (including irrigation downstream of the micro-hydropower plant). The water flow allocation to the community shown in the table allows a dedicated water source for the production of clean water and ice. While a dedicated water flow allocation for the micro-hydropower plant is quantified in the table for power generation purposes. As per convention, positive and negative values in the process matrix signify outputs and inputs into any given process respectively.

**Table 1. The balanced process matrix of case study 1.**

<table>
<thead>
<tr>
<th>Product Stream</th>
<th>Units</th>
<th>WTC 1</th>
<th>WTM 2</th>
<th>UFWT 3</th>
<th>Ice Plant</th>
<th>MHP 4</th>
<th>Product/Raw Materials</th>
</tr>
</thead>
<tbody>
<tr>
<td>Clean Water t/day</td>
<td>0</td>
<td>0</td>
<td>20</td>
<td>−5</td>
<td>0</td>
<td>15</td>
<td></td>
</tr>
<tr>
<td>Ice t/day</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>5</td>
<td>0</td>
<td>5</td>
<td></td>
</tr>
<tr>
<td>Electricity kW</td>
<td>0</td>
<td>0</td>
<td>−1</td>
<td>−4</td>
<td>105</td>
<td>100</td>
<td></td>
</tr>
<tr>
<td>Water to community supply t/day</td>
<td>50</td>
<td>0</td>
<td>−50</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>Water to microhydro plant t/day</td>
<td>0</td>
<td>52,500</td>
<td>0</td>
<td>0</td>
<td>−52,500</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>Rejected Water t/day</td>
<td>0</td>
<td>0</td>
<td>30</td>
<td>0</td>
<td>0</td>
<td>30</td>
<td></td>
</tr>
<tr>
<td>River Water t/day</td>
<td>−50</td>
<td>−52,500</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>−52,550</td>
<td></td>
</tr>
<tr>
<td>Diesel t/day</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td></td>
</tr>
</tbody>
</table>

1 Water to Community; 2 Water to Microhydro; 3 Ultra-Filtration Water Treatment; 4 Microhydro Plant.

Under normal conditions, the community requires 100 kW of electricity, 15 t/day of purified water, and 5 t/day of ice. These values define the upper limits of the fuzzy membership functions of product requirements. To meet these demands, the polygeneration plant requires a river water flowrate of 52,550 t/day. Under crisis conditions, it is assumed that the community needs a bare
minimum of 50 kW of electricity, 10 t/day of purified water, and 2 t/day of ice. These values define the lower limits of the fuzzy membership functions of the product demands. It is also assumed that the micro-hydropower plant has a minimum part-load operating level equivalent to 45% of its rated capacity. The drought index represents the fractional reduction of river water flowrate relative to normal conditions. The case study is then solved at increasing levels of drought, using increments of 10%. The polygeneration system schematic diagram is shown in Figure 2.

The optimal solutions to Case Study 1 for different drought intensities are shown in Table 2. The table shows the overall degree of satisfaction, $\lambda$, the optimal operating states of the process units, and the optimal net output levels of the products. As the drought level $D$ increases progressively to 0.50 (which represents 50%), the value of $\lambda$, component operating states, and net output all decline. However, the increments of the $\lambda$-value are not evenly distributed due to the effect of the previously specified fuzzy membership functions of product requirements. For drought intensity levels of at least $D = 0.60$ (or 60%), it becomes impossible to find a feasible solution, which means that the bare minimum requirements of the community cannot be met. The optimal operating states of the polygeneration plant during a mild drought ($D = 0.10$) and moderate drought ($D = 0.50$) are shown in Figures 3 and 4, respectively.

### Table 2. The resulting process capacity factor and the optimal production level for case study 1.

<table>
<thead>
<tr>
<th>Drought Level, $D$</th>
<th>Optimal Process Scaling Vector, $x$</th>
<th>Optimal Production Level, $y$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>WTC 1</td>
<td>WTM 2</td>
</tr>
<tr>
<td>0%</td>
<td>1.00</td>
<td>1.00</td>
</tr>
<tr>
<td>10%</td>
<td>0.80</td>
<td>0.92</td>
</tr>
<tr>
<td>20%</td>
<td>0.60</td>
<td>0.84</td>
</tr>
<tr>
<td>30%</td>
<td>0.40</td>
<td>0.76</td>
</tr>
<tr>
<td>40%</td>
<td>0.20</td>
<td>0.68</td>
</tr>
<tr>
<td>50%</td>
<td>0.01</td>
<td>0.60</td>
</tr>
</tbody>
</table>

1 Water to Community; 2 Water to Microhydro; 3 Ultra-Filtration Water Treatment; 4 Microhydro Plant.
the diesel generator is shown in Table 3. This case is a 60 kW capacity. The balanced process matrix of the polygeneration system incorporating the diesel generator is shown in Table 3.

As the drought level intensifies, the capacity of the diesel generator comes in standard capacity size which in this case is a 60 kW capacity. The balanced process matrix of the polygeneration system incorporating the diesel generator is shown in Table 3.

Furthermore, it can be noted that the ice plant is affected most since its disrupted state had an even higher disruption level (e.g., 12% and 60% disruption) than the experienced water reduction of 10%.

However, the increments of the water treatment facility can still operate at 92% of its normal operating capacity. This scenario was aggravated when the water treatment facility was up to 0.50 which resulted in the reduction in operating capacity of the ice plant to 40% and that of the water treatment facility to 60% of normal operating conditions. Furthermore, it can be noted that the ice plant is affected most since its disrupted state had an even higher disruption level (e.g., 12% and 60% disruption) than the experienced water reduction of 10% and 50%.

4.2. Case Study 2

Case study 2, on the other hand, considers the effect of the additional back-up diesel generator to the system in the previous example. This diesel generator can produce supplementary electricity as the drought level intensifies. The capacity of the diesel generator comes in standard capacity size which in this case is a 60 kW capacity. The balanced process matrix of the polygeneration system incorporating the diesel generator is shown in Table 3.
Table 3. The balanced process matrix of case study 2.

<table>
<thead>
<tr>
<th>Product Stream</th>
<th>Units</th>
<th>WTC 1</th>
<th>WTM 2</th>
<th>UFWT 3</th>
<th>Ice Plant</th>
<th>MHP 4</th>
<th>DGS 5</th>
<th>Product/Raw Materials</th>
</tr>
</thead>
<tbody>
<tr>
<td>Clean Water</td>
<td>t/day</td>
<td>0</td>
<td>0</td>
<td>20</td>
<td>−5</td>
<td>0</td>
<td>0</td>
<td>15</td>
</tr>
<tr>
<td>Ice</td>
<td>t/day</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>5</td>
<td>0</td>
<td>0</td>
<td>5</td>
</tr>
<tr>
<td>Electricity</td>
<td>kW</td>
<td>0</td>
<td>0</td>
<td>−1</td>
<td>−4</td>
<td>105</td>
<td>60</td>
<td>160</td>
</tr>
<tr>
<td>Water to community supply</td>
<td>t/day</td>
<td>50</td>
<td>0</td>
<td>−50</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Water to microhydro plant</td>
<td>t/day</td>
<td>0</td>
<td>52,500</td>
<td>0</td>
<td>−52,500</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Rejected Water</td>
<td>t/day</td>
<td>0</td>
<td>0</td>
<td>30</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>30</td>
</tr>
<tr>
<td>River Water</td>
<td>t/day</td>
<td>−50</td>
<td>−52,500</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>−52,500</td>
</tr>
<tr>
<td>Diesel</td>
<td>t/day</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>−3.6</td>
</tr>
</tbody>
</table>

1 Water to Community; 2 Water to Microhydro; 3 Ultra-Filtration Water Treatment; 4 Microhydro Plant; 5 Diesel Generator Set.

The remote community is assumed to have access to an emergency stock of diesel fuel. This supply, as well as the ease of delivery of additional fuel, is the basis for the fuzzy membership function of the diesel fuel input (in the input-output framework used here, inputs can be treated simply as products with negative net flowrates). In the case study, the diesel generator can operate from 30% to 100% of its rated capacity. With the addition of the diesel back-up generator, a binary variable is added to the model to indicate whether the diesel generator is switched on or off as the drought level intensifies (see Equations (6)–(8)). This feature leads to an FMILP formulation. The system schematic diagram is shown in Figure 5.

Figure 5. The process flowsheet of the polygeneration system of case study 2.

The optimal results of case study 2 at different levels of drought intensity are shown in Table 4. Note that the micro-hydropower plant ceases to operate at a drought level of $D = 0.60$ and beyond. The back-up diesel generator begins to operate at a drought level of $D = 0.20$ (or 20%) and progressively increases output under dryer conditions. The back-up generator is able to protect the community from the impacts of severe drought by extending the operational functionality of the polygeneration system even after the micro-hydropower plant becomes fully inoperable. This switch occurs at a drought level of $D = 0.60$ (or 60%), the electricity of the community is solely produced from the back-up diesel generator set at 90% capacity. This suggests that even at extreme drought conditions where the micro-hydropower plant fails to operate, a smaller capacity diesel generator set of about 54 kW may be considered if it is available in the market. The optimal operating states of the polygeneration plant at $D = 0.40$ and $D = 0.90$ are shown in Figures 6 and 7, respectively.
Table 4. The balanced process matrix of case study 2.

<table>
<thead>
<tr>
<th>Drought Level, D</th>
<th>WTC 1</th>
<th>WTM 2</th>
<th>UFWT 3</th>
<th>Ice Plant</th>
<th>MHP 4</th>
<th>DGS 5</th>
<th>Electricity (kW)</th>
<th>Clean Water (t/day)</th>
<th>Ice (t/day)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0%</td>
<td>1.00</td>
<td>1.00</td>
<td>1.00</td>
<td>1.00</td>
<td>1.00</td>
<td>0.00</td>
<td>100.00</td>
<td>15.00</td>
<td>5.00</td>
</tr>
<tr>
<td>10%</td>
<td>0.80</td>
<td>0.92</td>
<td>0.90</td>
<td>0.92</td>
<td>0.88</td>
<td>0.90</td>
<td>90.05</td>
<td>14.01</td>
<td>4.40</td>
</tr>
<tr>
<td>20%</td>
<td>0.68</td>
<td>0.87</td>
<td>0.67</td>
<td>0.87</td>
<td>0.81</td>
<td>0.67</td>
<td>83.88</td>
<td>13.39</td>
<td>4.03</td>
</tr>
<tr>
<td>30%</td>
<td>0.68</td>
<td>0.87</td>
<td>0.67</td>
<td>0.87</td>
<td>0.81</td>
<td>0.67</td>
<td>83.88</td>
<td>13.39</td>
<td>4.03</td>
</tr>
<tr>
<td>40%</td>
<td>0.61</td>
<td>0.85</td>
<td>0.60</td>
<td>0.85</td>
<td>0.77</td>
<td>0.60</td>
<td>80.66</td>
<td>13.07</td>
<td>3.84</td>
</tr>
<tr>
<td>50%</td>
<td>0.52</td>
<td>0.81</td>
<td>0.50</td>
<td>0.81</td>
<td>0.71</td>
<td>0.50</td>
<td>75.82</td>
<td>12.58</td>
<td>3.55</td>
</tr>
<tr>
<td>60%</td>
<td>0.03</td>
<td>0.61</td>
<td>0.00</td>
<td>0.61</td>
<td>0.42</td>
<td>0.00</td>
<td>51.67</td>
<td>10.17</td>
<td>2.10</td>
</tr>
<tr>
<td>70%</td>
<td>0.03</td>
<td>0.61</td>
<td>0.00</td>
<td>0.61</td>
<td>0.42</td>
<td>0.00</td>
<td>51.67</td>
<td>10.17</td>
<td>2.10</td>
</tr>
<tr>
<td>80%</td>
<td>0.03</td>
<td>0.61</td>
<td>0.00</td>
<td>0.61</td>
<td>0.42</td>
<td>0.00</td>
<td>51.67</td>
<td>10.17</td>
<td>2.10</td>
</tr>
<tr>
<td>90%</td>
<td>0.03</td>
<td>0.61</td>
<td>0.00</td>
<td>0.61</td>
<td>0.42</td>
<td>0.00</td>
<td>51.67</td>
<td>10.17</td>
<td>2.10</td>
</tr>
</tbody>
</table>

1 Water to Community; 2 Water to Microhydro; 3 Ultra-Filtration Water Treatment; 4 Microhydro Plant; 5 Diesel Generator Set.

Figure 6. The optimal configuration of the polygeneration system of case study 2 under $D = 0.40$ (or 40%).

Figure 7. The optimal configuration of the polygeneration system of case study 2 under $D = 0.90$ (or 90%).
4.3. Case Study 3

This case study is similar to the previous one, except that a dual-turbine micro-hydropower plant is assumed. This dual-turbine micro-hydro plant consists of two smaller turbines rated at 70 kW and 35 kW, which together gives the system greater operational flexibility. The balanced process matrix for Case Study 3 is shown in Table 5 where the micro-hydropower turbines 1 and 2 are explicitly identified. With the reduction in the size of the turbine, this translates to a system-wide lower part-load operating level for the 70 kW turbine and the 35 kW turbine of the micro-hydropower plant varying drought intensity levels. It can be observed that turbine 2 will shut off at drought intensity levels of \( D = 0.40 \) and 0.50 and will operate again at \( D = 0.70 \) and 0.80.

![Figure 8. The process flowsheet of the polygeneration system of case study 3.](image)

The optimal operational adjustment results for case study 3 using various levels of \( D \) is shown in Table 6. The table shows the dynamic operational capacity of the 2 micro-hydro turbines through varying drought intensity levels. It can be observed that turbine 2 will shut off at drought intensity levels of \( D = 0.40 \) and 0.50 and will operate again at \( D = 0.70 \) and 0.80.
Turbine 1, on the other hand, will continue to operate until it reaches a drought intensity of \( D = 0.60 \) and will shut off at \( D = 0.70 \) and beyond. At elevated drought intensity of \( D = 0.70 \) and 0.80, the smaller turbine provides better operational flexibility allowing appropriate operational adjustments. As a supplementary source of power, the back-up diesel generator begins to operate at a drought intensity of \( D = 0.20 \) and is partially operated until a drought intensity level of \( D = 0.90 \) at 90% part-load capacity. However, the dual-turbine remains operable over a wider range of conditions allowing operational flexibility on drought condition while the diesel generator partially operates from \( D = 0.20 \) to 0.90. The optimal configuration of the polygeneration system for case study 3 is shown in Figures 9 and 10 for \( D = 0.30 \) and \( D = 0.90 \), respectively.

![Figure 9](image_url)
The optimal configuration of the polygeneration system of case study 3 under $D = 0.90$ (or 90%).

The comparison of the production level of electricity, water, and ice for the three case studies are shown in Figures 11a–c while the diesel fuel consumption for case studies 2 and 3 is shown in Figure 11d. The contribution of the power generating technologies to electricity production for each case study are shown in Figure 12. The back-up diesel generator set enabled an extended production of electricity, water, and ice for the community especially during low to severe drought intensity levels. The dual-turbine micro-hydro assembly with diesel generator set (Case Study 3) provides a more stable production of electricity, water, and ice and is found to be superior compared to the single-turbine micro-hydro plant with diesel generator (Case Study 2) especially for drought intensity levels from $D = 0.60$ to $D = 0.80$. With lower diesel fuel consumption and higher electricity generation, the dual-turbine micro-hydro plant with diesel generator is ideal for areas where drought risk is expected.
were solved to illustrate the model capabilities. This modelling framework is useful for off-grid systems which have been established and have failed to take into consideration system disruptions resulting from the effects of climate change. The model provides decision-makers with a systematic procedure for identifying the optimal operational adjustment to ensure that the community demands for each product output, based on fuzzy constraints. Unlike conventional MILP formulations, the fuzzy bounds provide an optimal solution that gives a more balanced compromise on the reduction of outputs of the facility.

5. Conclusions

A fuzzy MILP model has been developed for the optimal operational adjustment of an off-grid micro-hydropower-based polygeneration system under varying drought intensity scenarios. The polygeneration system produces electricity, purified water, and ice, which are the basic needs of an off-grid community. The model accounts for the integration of the process units to give the optimal solution that gives a more balanced compromise on the reduction of outputs of the facility. A variant of the model also considers the minimization of the fuel consumption of the back-up diesel generator set. Case studies that consider different turbine configurations and diesel back-up options were solved to illustrate the model capabilities. This modelling framework is useful for off-grid electricity systems which have been established and have failed to take into consideration system disruptions resulting from the effects of climate change. The model provides decision-makers with a systematic procedure for identifying the optimal operational adjustment to ensure that the community needs are met.
product demands are satisfied during abnormal conditions. Furthermore, the model can provide insights on the management of external sources of energy.

Future work can apply this model formulation to a broader range of integrated polygeneration systems and consider multi-period models to accommodate variations in product demands. In addition, the potential for the use of alternative methods such as fuzzy P-graph [41] to deal with problems of this class should also be explored together with an examination of the availability and performance of alternative operating conditions.

Author Contributions: All authors contributed to the completion and publication of the study. R.R.T. conceptualized the general idea of the paper. I.A.V.M.III provided key technical information on off-grid microhydro plants. R.R.T., K.B.A., and A.T.U., contributed on the development of the model. K.B.A. thoroughly verified and validated the model. A.T.U. prepared and edited the manuscript, and responsible for drawing the figures. I.A.V.M.III, K.B.A., and R.R.T. revised and reviewed the manuscript.

Funding: This research was funded by Philippine Commission on Higher Education (CHED) PHERNet Project.

Acknowledgments: The research is supported by the Philippine Commission on Higher Education (CHED) PHERNet Sustainability Studies Program and the De La Salle Science Foundation (DLS-SFI) for the publication cost. The pioneering work of the late Godofredo Salazar is acknowledged in establishing the Center for Microhydro Research at De La Salle University.

Conflicts of Interest: The authors declare no conflict of interest.

Appendix A

The basic MILP model for optimizing the polygeneration system during abnormal operations is described by Equations (A1)–(A7) and is similar to the model introduced in [14].

\[
\begin{align*}
\text{max} & = c^T y^* \\
A \cdot x & = y^* \\
b^T x^l & \leq x \leq b^T x^u \\
b & \in \{0, 1\} \\
y^*_{river\_water} & = (1 - D) y_{river\_water} \\
y^* & \geq y^l \\
f^l & \leq b^T e \leq f^u
\end{align*}
\]

The objective function (Equation (A1)) is to maximize the profit of the system, excluding capital cost recovery, where \(c^T\) represents the price vector for the material or energy streams and \(y^*\) is the net output vector during abnormal operations. The model is subject to material and energy balances (Equation (A2)) dependent on the process operational conditions where \(A\) is the balanced process matrix during normal operating conditions and \(x\) is the process scaling vector during abnormal conditions. The scaling vector is bound by the lower \((x^l)\) and upper \((x^u)\) operating capacity limits of each available technology (Equation (A3)) where \(b^T\) is a binary variable (Equation (A4)) indicating whether a technology is operational \((b_i = 1)\) or not \((b_i = 0)\) during abnormal operations. The abnormal conditions occur when there is insufficient river water (Equation (A5)) defined by the drought intensity factor, D. Furthermore, a minimum production level \((y^l)\) for identified product streams must be met (Equation (A6)). There is also a minimum \((f^l)\) and maximum \((f^u)\) number of operational technologies at any given time (Equation (A7)), vector \(e\) represents a column vector with all elements equal to 1.

References


