Abstract: A multi-level open-end winding converter topology for multiple-motor drives is presented featuring a main multi-level inverter processing the power delivered to the motors and an active filter based on an auxiliary two-level inverter. The main inverter operates at the fundamental frequency in order to achieve low switching power losses, while the active filter is Pulse Width Modulation (PWM) operated to suitably shape the motor currents. The proposed configuration features less phase current distortion than conventional multi-level inverters operating at the fundamental frequency, while achieving a higher efficiency compared to PWM multi-level inverters. Experimental results confirm the effectiveness of such a configuration on both multiple motors-single converter and multiple motor-multiple converter drives.

Keywords: multilevel converter; multi-motor drive; harmonic mitigation; active filter; open end winding motor; high efficiency drive; high reliability applications

1. Introduction

A Multiple Motor Drive (MMD) is composed of some electric motors sharing the load torque [1–5]. Such a configuration costs less than a set of single motor drives, as some resources are shared between the units. Further, compared to a single drive, it is easily expandable by adding new units, moreover, the intrinsic redundancy may be used to mitigate the effects of some kinds of converter and motor faults. MMD are common in paper and textile industry and ironworks, as well as in several industry applications demanding synchronization between two or more axes, high levels of reliability and/or easy expandability. MMD systems can be grouped into two classes, namely: Multiple Motors Fed by a Single Multi-level Converter (MMSC) and Multiple Motors Fed by Multiple Multi-level Converters (MMMC). A single inverter on MMSC delivers power to all the machines, thus leading to only an approximatively proportional load sharing. On MMC the common DC bus supplies a set of inverters, each one powering a single motor. In this case, the torque produced by each motor can be independently controlled, while retaining a common power entry and braking system.

Induction Motor (IM) based MMMCs are frequently used on rail mounted, or rubber tired, gantry cranes, equipping hoist, trolley and leg drives [6–8]. On leg drives MMMCs provide the ground to cope with different wheel diameter, unequal wheels’ adhesion and slipping of transmission devices. MMDs also often equip electric locomotives, powering the axles through spur gearings [9–12]. Dual-Voltage Source Inverter (VSI)/Dual-IM and Mono-VSI/Dual-IM configurations are used with induction motors. The first, being of the MMC type, comprises two induction motors supplied through two power converters. Such a configuration features a higher level of robustness toward inverter faults. Moreover, critical operations caused by pantograph detachment, loss of wheel adherence and
stick-slip perturbation may be faced thanks to a fully independent control of the torque delivered by single machines. In recent years, MMC has also become a viable alternative to single drives on powertrains of electrical and hybrid vehicles, featuring higher flexibility, reliability and transmission efficiency, while helping to increase the available inner space [13,14].

A straightforward way to control the speed of a MMMC is based on the common speed reference technique, providing a common speed reference signal to the speed controller of each unit. A torque follower control approach is however preferable, due to concerns regarding the control precision and system flexibility. According to such a technique, as shown in Figure 1, a single speed command is provided to a master unit, which in turn sends the torque references to the other drives [6]. Torque and flux regulation on single units is generally based on the traditional Indirect Field Oriented Control (IFOC) technique or Direct Torque Control strategy.

**Figure 1.** Common speed reference control of a Multiple Motors fed by Multiple Converters (MMMC) system.

In recent years, Multi-Level Inverters (MLIs) have been introduced on multi-motor drives, in order to generate almost sinusoidal output voltages using low frequency switching power devices, thus achieving high efficiency and electromagnetic compatibility. In addition, power devices are tasked with withstanding a fraction of the total DC input voltage, resulting in a remarkable reduction of dv/dt stresses and switches voltage ratings. However, in order to achieve a comparable phase current Total Harmonic Distortion (THD), MLI topologies working at low switching frequency could require many more power devices than conventional Pulse Width Modulation (PWM) operated bridge inverters. Cost concerns lead to limitation of the number of power devices, resulting in torque ripple and additional losses. These can be addressed by selective harmonic elimination or PWM techniques, as well as, by the addition of line reactors and tuned harmonic filters. Active power filters may also be exploited as they are able to provide a more flexible and effective attenuation of current harmonics [15–24].

An Open-end Winding (OW), multi-level, configuration for MMD applications is proposed in this paper; it features null neutral point fluctuations, low phase current ripple and improved DC bus voltage utilization [25–29]. A distinctive characteristic of the proposed configuration is the asymmetry, because that the two inverters are not of the same type and only one of the two provides power to the motors. In fact, a main multi-level inverter processes the power delivered to the motors, while an active filter, based on an auxiliary two-level inverter (TLI), shapes the phase current. Moreover, the main inverter operates at the fundamental frequency in order to achieve low switching power losses, while the active filter is PWM operated. Finally, the DC bus voltage of the two-level inverter is remarkably lower than that of the main inverter [30–36]. The proposed MMD OW configuration features a higher global efficiency and lower current THD than an equivalent PWM operated multi-level inverter for multi-motor drives [37], exploiting a specific control strategy combining low switching frequency
modulation on the MLI and high frequency PWM on the TLI. Finally, it can be used either on either multiple motors-single converter or multiple motor-multiple converter drives.

2. Open Winding Multiple Motors Fed by a Single Multi-Level Converter—MMSC

Although the proposed approach can be applied to a system composed of an arbitrary number of machines, a system comprising only two identical induction motors, sharing the total load torque, is considered for simplicity. The proposed MMSC structure is shown in Figure 2; the stator windings of the two OW induction motors IM1 and IM2, are parallel connected to a MLI and a TLI, but only the first actually delivers active power to both motors, the second being operated as an active filter. This makes the proposed configuration different from most common OW motor drives, where the power supplied to the motors is evenly shared between the two inverters. The TLI, which supplies a null average power to the motors, can be supplied through a floating capacitor, avoiding the need for an additional power source and also making the two DC voltage sources $V_{DC}'$ and $V_{DC}''$ independent. The motors are assumed to be speed controlled through an IFOC technique, but the load sharing between the motors cannot be managed. The output phase voltage of an MLI may take $n$ different levels. The magnitude of each level is generally defined as the voltage across the mid-point of the DC bus and the output phase terminal. The number of possible voltage levels is generally odd, including a zero level and $n-1$ non-zero levels and each level is identified by the value of the coefficient $l'=0,1,2,\ldots,n-1$. The $i$-phase MLI output voltage $V_{MLI,stepi}$ is thus given by:

$$V_{MLI,stepi} = \frac{2l' - n + 1}{2(n-1)} V_{DC}'$$  \hspace{1cm} (1)

**Figure 2.** Proposed Open-end Winding (OW) Multi-level inverter (MLI) + Two Level Inverter (TLI) Multiple Motors Fed by a Single Multi-level Converter (MMSC) configuration.

In the same way, the $i$-phase TLI output voltage $V_{TLIi}$ is given by:

$$V_{TLIi} = \frac{(2l'' - 1)}{2} V_{DC}''$$  \hspace{1cm} (2)

where $l'' = 0,1$ is the $i$-phase TLI actual output voltage level.

The voltage $V_{mi}$ across a generic ‘$i$’ motor phase winding, is finally given by:

$$V_{mi} = V_{MLI,stepi} - V_{TLIi} - Vn'n''$$  \hspace{1cm} (3)
where $V_{n'n''}$ is the voltage across the mid points $n'$ and $n''$ of the two DC buses, which is given by:

$$V_{n'n''} = \frac{1}{3}(V_{MLI_a} + V_{MLI_b} + V_{MLI_c}) + \frac{1}{3}(V_{TLI_a} + V_{TLI_b} + V_{TLI_c})$$

(4)

The phase voltage $V_{mi}$ takes the zero level and further $4(n + 1)$ non-zero levels when $V_{DC''} = V_{DC'}/[2(n - 1)]$, while, some additional non-zero levels become available if $V_{DC''} < V_{DC'}/[2(n - 1)]$ [31].

The voltage levels which the proposed asymmetrical hybrid multilevel inverter configuration may take are more numerous than those of conventional Neutral Point Clamped (NPC) or Flying Capacitor (FC) MLI topologies with the same amount of power switches. In other words, the same phase voltage THD can be achieved with the proposed MMSC configuration using fewer power devices. Moreover, the proposed configuration features a switching frequency which is that of the TLI, although the main inverter switches at the fundamental frequency [37]. This leads to use power devices optimized for low switching frequency operation (i.e., featuring a low on-state voltage drop) in the MLI, and power devices suitable for high switching frequency in the TLI.

A suitable motor phase voltage modulation strategy was formulated taking into account the specific features of the proposed topology, according to the scheme in Figure 3.

The TLI is tasked with compensating low frequency phase voltage harmonics generated by the MLI, which is step driven to reduce the switching power losses. Unwanted low frequency voltage harmonics can be suppressed by setting the voltage reference $V_{*MLI}$ of the TLI to:

$$V_{*TLI} = V_{*MLI,stepi} - V_{*MLI}$$

(5)

where: $V_{*MLI,stepi}$ is the fundamental harmonic of the ith motor phase reference voltage $V_{*MLI,stepi}$. Both quantities are depicted in Figure 4 for the case of a seven-level $V_{MLI,stepi}$ waveform.
The voltage ratio $K_V = \frac{V_{DC''}}{V_{DC'}}$ is a key parameter, because it impacts on the number of inverter voltage levels, on the THD of phase voltages and currents, on the maximum motor phase voltage amplitude and finally, on the ratings of TLI power devices.

The phase voltage $V_{mi}$ is the difference between $V_{MLIi}$ and $V_{TLIi}$, hence, its space vector diagram can be obtained by combination of the voltage space vector diagrams of the MLI and TLI. The simplest MMSC structure which can be obtained with the proposed approach consists of a Three-Level inverter (3LI) and a TLI (3LI+TLI).

The phase voltage of each inverter leg of the 3LI can assume three statuses namely: P, O and N. $P$ denotes that the inverter phase voltage $V_{MLIi} = V_{DC'}$, while $O$ indicates that $V_{MLIi} = 0$, and $N$ that $V_{MLIi} = -V_{DC'}$. The 3LI topology is basically composed of two cells, each one supplied at $V_{DC'}/2$, hence each leg may take three switching states, resulting in $3^3 = 27$ possible inverter switching state combinations. Each space vector can be categorized into zero voltage, small voltage, medium voltage and large voltage on the basis of its magnitude. These are tabulated in Table 1. The TLI instead features $2^3 = 8$ inverter states, leading to 7 voltage vectors. As shown in Figure 5, the 3LI+TLI voltage space vector diagram is obtained by composition of the voltage space vector diagrams of the TLI and the 3LI. The number of available voltage vectors and voltage levels depends on $K_V$, as listed in Table 2, affecting both the THD$_V$ and the peak amplitude $V_{mpk}$ of the phase voltage $V_{mi}$. In particular, $V_{mpk}$ increases with $K_V$, while a minimum THD$_V$ is achieved for $V_{DC''} = V_{DC'}/[(n - 1)]$, [24], thus, the considered 3LI+TLI system gets the minimum THD$_V$ for $V_{DC''} = V_{DC'}/2$. However, $V_{mpk}$ maximization must be also taken into consideration, thus, a useful figure of merit in determining the optimal value of $K_V$ is $K_p = V_{mpk}/(V_{DC'} \times \text{THD}_V)$, which, according to Table 3, is maximized when $V_{DC''} = V_{DC'}/2$. When $V_{DC''}$ is reduced below $V_{DC'}/2$, $K_p$ and $V_{mpk}$ decrease, while the number of voltage levels and voltage vectors increases, as well as THD$_V$. However, the voltage rating of TLI power devices is lowered. For $K_V = 1/8$, the 3LI+TLI is equivalent to conventional six-level NPC or FC inverter structures, which however require six more power devices. By setting $V_{DC''}$ over $V_{DC'}/2$, a higher $V_{mpk}$ is obtained, while the number of voltage levels and voltage vectors is lowered, worsening THD$_V$ and $K_p$. Moreover, when $V_{DC''} = V_{DC'}$, the voltage rating of the TLI switches becomes equal to that of MLI devices.

**Table 1.** Switching states and voltage vector of Three Level Inverter (3LI).

<table>
<thead>
<tr>
<th>Vector</th>
<th>Magnitude</th>
<th>Switching State</th>
</tr>
</thead>
<tbody>
<tr>
<td>Zero vector</td>
<td>0</td>
<td>PPP, OOO, NNN</td>
</tr>
<tr>
<td>Small vector</td>
<td>$1/3 V_{DC'}$</td>
<td>POO, PPO, OPO, OPP, POP, OOP, OON, NON, NOO, ONO, NNO</td>
</tr>
<tr>
<td>Medium vector</td>
<td>$\sqrt{3}/3 V_{DC'}$</td>
<td>PON, OPN, NPO, NOP, ONP, PNO</td>
</tr>
<tr>
<td>Large vector</td>
<td>$2/3 V_{DC'}$</td>
<td>PNN, PPN, NPN, NPP, NN, NNP, PNN</td>
</tr>
</tbody>
</table>

**Table 2.** Power converter specifications vs. $K_V$ for Three Level Inverter + Two Level Inverter (3LI+TLI).

<table>
<thead>
<tr>
<th>$K_V$</th>
<th>Number of Inverter States</th>
<th>Number of Voltage Vectors</th>
<th>Number of Voltage Levels</th>
</tr>
</thead>
<tbody>
<tr>
<td>1/8</td>
<td>216</td>
<td>152</td>
<td>8</td>
</tr>
<tr>
<td>1/4</td>
<td>216</td>
<td>91</td>
<td>6</td>
</tr>
<tr>
<td>1/2</td>
<td>216</td>
<td>37</td>
<td>4</td>
</tr>
<tr>
<td>1</td>
<td>216</td>
<td>61</td>
<td>5</td>
</tr>
</tbody>
</table>
Figure 5. Phase voltage space phasor diagram (a) \( V_{DC''}/V_{DC'} = 1/8 \); (b) \( V_{DC''}/V_{DC'} = 1/4 \); (c) \( V_{DC''}/V_{DC'} = 1/2 \); (d) \( V_{DC''}/V_{DC'} = 1 \).

Table 3. \( V_{mpk} \) and THD\(_{V} \) vs. \( K_V \) (3LI+TLI).

<table>
<thead>
<tr>
<th>( K_V )</th>
<th>( V_{mpk} )</th>
<th>THD(_{V} ) (%)/( K_P )</th>
<th>( \omega_r/\omega_n = 0.1 )</th>
<th>THD(_{V} ) (%)/( K_P )</th>
<th>( \omega_r/\omega_n = 0.3 )</th>
<th>THD(_{V} ) (%)/( K_P )</th>
<th>( \omega_r/\omega_n = 0.7 )</th>
<th>THD(_{V} ) (%)/( K_P )</th>
<th>( \omega_r/\omega_n = 1 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>1/8</td>
<td>0.58 ( V_{DC'} )</td>
<td>51/1.14</td>
<td>45/1.29</td>
<td>30/1.93</td>
<td>19/3</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1/4</td>
<td>0.72 ( V_{DC'} )</td>
<td>36/2</td>
<td>29/2.48</td>
<td>15/4.8</td>
<td>4.0/20.5</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1/2</td>
<td>0.87 ( V_{DC'} )</td>
<td>10/8.7</td>
<td>8/10.88</td>
<td>7.1/12.2</td>
<td>3.5/21.7</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>1.15 ( V_{DC'} )</td>
<td>46/2.5</td>
<td>40/2.88</td>
<td>31/3.7</td>
<td>22.6/5.1</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

According to the proposed approach no active power is delivered to the two IM motors from the TLI. In practice, power devices and motors power losses in the TLI would cause a progressive discharge of the floating capacitor of the TLI DC-bus. Being floating, such a capacitor can only be charged by diverting to it a small quantity of the active power delivered by the MLI to the motors [32–44]. As shown in the control scheme of Figure 6, this is achieved by slightly modifying the TLI reference voltages. Specifically, two additional terms \( V_{dCap} \) and \( V_{qCap} \) are introduced to control the mean current...
flowing through the DC bus capacitor. Since the TLI is not tasked with supplying reactive power to the load, \( V_{dCap} \) can be straightforwardly related to \( V_{qCap} \) by:

\[
Q = \frac{3}{2} \left( V_{qCap} i_d - V_{dCap} i_q \right) = 0 \Rightarrow V_{dCap} = \frac{i_d}{i_q} V_{qCap}
\]  
(6)

The active power \( P \) required to hold \( V_{DC}^{\prime\prime} \) constant is obtained by a PI controller processing the error between the reference DC bus voltage \( V_{DC}^{\prime\prime} \) and the actual voltage \( V_{DC} \):

\[
P = \frac{3}{2} \left( V_{qCap} i_q + V_{dCap} i_d \right) = (V_{DC}^{\prime\prime} - V_{DC}^{\prime\prime}) \left( K_{pVDC} + \frac{K_{IVDC}}{s} \right)
\]  
(7)

where \( s \) is the Laplace operator, and \( K_{pVDC} \) and \( K_{IVDC} \) are, respectively, the proportional and integral gain of the PI controller. By introducing Equation (6) into Equation (7), the \( dq \)-axes voltage reference components \( V_{qCap} \) and \( V_{dCap} \) are obtained:

\[
V_{qCap} = \frac{2}{3} \frac{P i_q}{i_q^2 + i_d^2} \quad V_{dCap} = \frac{2}{3} \frac{P i_d}{i_q^2 + i_d^2}
\]  
(8)

### Figure 6. MLI+TLI MMSC control strategy.

The two additional terms are then transformed to the \( abc \) stationary frame and added to the TLI voltage references obtained from Equation (5). Due to the floating capacitor recharging, the phase current typically increases by less than 1.5% of the rated current. The considered 3LI+TLI topology requires a specific control system which is schematized in Figure 6. It consists of two subsystems, acting on the two inverters. The MLI is voltage controlled, thus, the \( q \), \( d \) axes voltage references \( V_{dqMLI}^{\ast} \) are made equal to the motors back EMF components \( \hat{E}_{q}^{\ast} \) and \( \hat{E}_{d}^{\ast} \), which in turn are estimated by

\[
\begin{align*}
\dot{\hat{E}}_q &= L_s \omega_{\lambda r e} i_d^q \\
\dot{\hat{E}}_d &= -L_k \omega_{\lambda r e} i_q^d \\
\omega_{\lambda r e} &= \frac{R_i}{L_i} + \omega_r \\
L_k &= \frac{l_s l_r - l_d^2}{L_r}
\end{align*}
\]  
(9)

where: \( \omega_{\lambda r e} \) is the rotor flux angular frequency, \( \omega_r \) is the rotor speed of the two machines, and \( L_s \), \( L_r \) and \( L_m \) are respectively the stator, rotor and magnetizing inductances.

As shown in Figure 6, the TLI features a feedback current control, in order to improve the shape of the current waveform and the system dynamic response. The outputs \( V_{dqTLI_{r,j}}^{\ast} \) of the TLI current control loop are transformed to the \( abc \) stationary frame and then added to other voltage reference
components, dealing with compensation of low order stator voltage harmonics and $V_{DC''}$ stabilization, this allows us to obtain the voltage references for the PWM modulator, which are given by:

$$V_{TLi}^* = V_{TLIr,j}^* + V_{MLI,step}^* - V_{MLIi}^* + V_{cap,j}$$ (11)

The currents flowing through the two stator windings cannot individually be controlled. However, even load torque sharing is obtained when considering two identical motors with a high-stiffness mechanical coupling. Whenever these conditions are not verified, torque and current unbalance may yield to a system instability. In this case, the TLI current control structure needs to be modified as suggested in references [45–51].

3. Open Winding Multiple Motors Fed by Multiple Multi-Level Converters—MMMC

The proposed OW approach can also be used on MMMC systems. An MMMC system is in general able to control the load sharing between the two motors, because providing an independent control of the stator currents of the two induction motors. However, according to the proposed approach, this would require two independent MLI and two TLI. A simpler structure was thus developed by connecting the two motors to a single MLI on one side and to a five-leg two level inverter (TLI5) on the other side, thus reducing the number of inverter switches and the associated power losses [51,52]. The circuitual scheme and the control block diagram of such a topology (MLI+TLI5) are shown in Figures 7 and 8. Two different PWM strategies can be adopted on five-leg inverters [51–53]. A first one is based on the cancellation of the voltage reference of the inverter phase common to the two motors. In practice, for each set of reference voltages, the reference of the common phase is algebraically subtracted to the voltage references of the other two phases, while the common phase reference becomes equal to the difference between the two c-phase voltage references. A major drawback of this strategy is a reduction in the maximum motor phase voltage by a factor of 1/3 compared to a standard three phase motor drive. In order to overcome this drawback a second PWM strategy can be adopted, which is based on the addition, rather than subtraction, of the common phase voltage reference to the references of the other phases.

Figure 7. MLI+TLI5 OW MMC configuration.
According to such an approach [46], the five-leg TLI voltage references are given by:

\[
\begin{align*}
V_{TL,1a}^* & = V_{T1r,1a}^* + V_{T1r,1c}^* + V_{MLI,step}^* - V_{MLIa}^* \\
V_{TL,1b}^* & = V_{T1r,1b}^* + V_{T1r,1c}^* + V_{MLI,step}^* - V_{MLIb}^* \\
V_{TL,1c}^* & = V_{T1r,1c1}^* + V_{T1r,1c2}^* + V_{MLI,step}^* - V_{MLIc}^* \\
V_{TL,1d}^* & = V_{T1r,1a2}^* + V_{T1r,1c1}^* + V_{MLI,step}^* - V_{MLIa}^* \\
V_{TL,1e}^* & = V_{T1r,1b2}^* + V_{T1r,1c1}^* + V_{MLI,step}^* - V_{MLIb}^*.
\end{align*}
\]

(12)

Since both motors are connected to a single MLI, voltage harmonic compensation is exerted by acting on the TLI a, b, d and e phase voltage references.

The average values of q-d back EMF components \(\bar{E}^q\) and \(\bar{E}^d\) are estimated from Equations (9) and (10), by assuming:

\[
\begin{align*}
\dot{i}_q^* & = \dot{i}_{d1}^* = \dot{i}_{d2}^* \\
\dot{i}_{q1}^* & = K_1 \dot{i}_q^* \\
\dot{i}_{q2}^* & = K_2 \dot{i}_q^*
\end{align*}
\]

(13)

(14)

where:

\[
K_1 = \frac{T_{e2n}}{T_{e1n} + T_{e2n}} \quad K_2 = (1 - K_1)
\]

(15)

By assuming the use of two identical motors, the q-axis current references can be imposed as:

\[
\dot{i}_{q1}^* = \dot{i}_{q2}^* = 0.5 \dot{i}_q^*
\]

(16)

4. Power Losses Assessment

The total power losses of the OW MMSC topology of Figure 2 were evaluated and compared with those of a system consisting of a single 3LI supplying two wye connected induction motors. Two different cases were investigated. In the first case, a conventional drive topology was considered, in which a single multilevel inverter was step operated and feeds two parallel connected induction motors. In the second case the inverter is operated according to a \(f_{swTLI} = 10\) kHz space vector PWM modulation. The obtained results were then compared with those obtained with the 3LI+TLI topology, where the 3LI was driven according to a step modulation with \(f_{swMLI} = \omega \rho / 2\pi\), while a \(f_{swTLI} = 10\) kHz sinusoidal PWM strategy was used on the TLI. The TLI floating DC-bus was built around a 480 \(\mu F\) capacitor, while \(V_{DC}^*\) was set at 580 V and \(V_{DC}^* = V_{DC}^/4\) at 145 V. This leads to the use of Insulated Gate Bipolar Transistor (IGBT) devices on the 3LI and MOSFET on the TLI.
The inverter power losses, consisting of the switching losses $P_{\text{swMLI}}, P_{\text{swTLI}}$ and conduction losses $P_{\text{cMLI}}, P_{\text{cTLI}}$ were calculated as in [31]:

$$
P_{\text{swMLI}} = 0.5 V_{ce} i_{\text{swMLI}} (t_{\text{on1}} + t_{\text{off1}}) \quad P_{\text{cMLI}} = \delta V_{ce} i_{C}
$$

$$
P_{\text{swTLI}} = 0.5 V_{DS} i_{\text{swTLI}} (t_{\text{onM}} + t_{\text{offM}}) \quad P_{\text{cTLI}} = R_{DS(on)} i_{D}^2
$$

(17)

The motor joule losses $P_{\text{joule}}$ and motor iron losses $P_{\text{iron}}$ are given by:

$$
P_{\text{joule}} = R_{s} i_{s}^2 + R_{r} i_{r}^2 \quad P_{\text{iron}} = \frac{E^2}{R_{fe}}
$$

(18)

The induction motors parameters are listed in Table 4, while technical data of the IGBT used in the MLI and the MOSFET used in the TLI are summarized in Tables 5 and 6, respectively. The systems were run at $\omega_f = 100$ rad/s.

**Table 4. Technical specifications of the Induction Motors.**

<table>
<thead>
<tr>
<th>$P_n$ (HP)</th>
<th>$V_n$ (V)</th>
<th>$\phi p$</th>
<th>$L_s$ (mH)</th>
<th>$L_r$ (H)</th>
<th>$L_m$ (H)</th>
<th>$R_s$ (Ω)</th>
<th>$R_r$ (Ω)</th>
<th>$R_\ell$ (Ω)</th>
<th>$J$ (Kg·m²)</th>
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</thead>
<tbody>
<tr>
<td>3</td>
<td>400</td>
<td>2</td>
<td>0.32</td>
<td>0.32</td>
<td>0.31</td>
<td>2.6</td>
<td>902</td>
<td>2.7</td>
<td>0.016</td>
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</table>

**Table 5. MLI IGBT Data.**

<table>
<thead>
<tr>
<th>$V_{\text{ces}}$ (V)</th>
<th>$I_c$ (A)</th>
<th>$T_1$ (°C)</th>
<th>$V_{\text{ceo}}$ (V)</th>
<th>$t_{\text{on}}$ (ns)</th>
<th>$t_{\text{off}}$ (ns)</th>
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<td>600</td>
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<td>150</td>
<td>0.75</td>
<td>60</td>
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**Table 6. TLI MOSFET Data.**

<table>
<thead>
<tr>
<th>$V_{\text{DSS}}$ (V)</th>
<th>$I_{\text{DSS}}$ (A)</th>
<th>$T_1$ (°C)</th>
<th>$R_{\text{DS(on)}}$ (mΩ)</th>
<th>$t_{\text{on}}$ (ns)</th>
<th>$t_{\text{off}}$ (ns)</th>
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Figure 9 deals with power losses estimation for the three considered cases, taking into account the motor (core and winding) and inverter (switching and conduction) power losses and considering the first ninety harmonics of the stator current and voltage.

**Figure 9.** Motor iron losses $P_{\text{iron}}$, motor joule losses $P_{\text{joule}}$, MLI conduction losses $P_{\text{cMLI}}$, MLI switching losses $P_{\text{swMLI}}$, TLI conduction losses $P_{\text{cTLI}}$ and TLI switching losses $P_{\text{swTLI}}$: (a) 3LI step modulated; (b) 3LI PWM modulated; (c) 3LI+TLI configuration.

When the step modulated 3LI feeds the two wye connected induction motors, as shown in Figure 9a, power losses largely consist of motor joule losses, because the motor currents are affected by low order harmonics components. When the 3LI PWM modulated feeds the two wye connected induction motors, as shown in Figure 9b, motor joule losses are still dominant, but higher switching losses occurs. Finally, the 3LI+TLI configuration is considered. Since the MLI is step modulated and
the phase motor current waveform is made close to a sinusoidal one by the active power filter, motor and MLI inverter losses are considerably reduced, especially at heavier loads.

The 3LI+TLI topology features a higher efficiency at medium and high loads, while at low loads its efficiency is comparable with that of the PWM driven 3LI. Based on computed motor and inverter losses, total efficiency was evaluated in the three considered cases, as shown in Figure 10.

![Figure 10. Total efficiency of the MMSC: (a) 3LI step operated; (b) 3LI PWM operated; (c) 3LI+TLI configuration.](image)

A comparison between the performance of the 3LI+TLI5 topology and that of a conventional system consisting of two PWM operated 3LIs supplying two wye connected induction motors was also accomplished. The results shown in Figure 11, confirming that the 3LI+TLI5 MMMC is more efficient than the conventional one, especially at heavy loads.

![Figure 11. Total efficiency of the system: (a) 3LI PWM operated; (b) 3LI+TLI5 configuration.](image)

5. Experimental Tests

The proposed multi-motor drive configurations were experimentally validated using two induction motors, the technical specifications of which are shown in Table 4. The MLI was equipped with an IGBT with parameters shown in Table 5 while the TLI consisted of a MOSFET, detailed in Table 6. Figure 12 shows the test rig. The first prototype featured an MMSC configuration, tailored around a five level NPC main inverter (5LI+TLI). The second prototype was still an MMSC system, but equipped with a three level NPC main inverter (3LI+TLI). The third prototype is instead a MMMC system composed of a five level NPC main inverter and a five-leg, two-level (5LI+TLI5) auxiliary inverter. All the three prototypes are field oriented controlled by a dSPACE board featuring a 100 μs update time. On each drive configuration two induction motors were present with mechanical coupling between them in order to operate them at the same rotational speed. Moreover, the TLI was PWM operated at \( f_{sw,TLI} = 10 \text{ kHz} \), with a 1 μs dead time. The DC bus voltage \( V_{DC} \) of the MLIs was 400 V, while \( V_{DC} \) was set at 50 V when a 5LI was used and at 100 V when a 3LI was used. A controllable mechanical load was realized by exploiting a conventional 3 HP vector controlled induction motor drive, detailed in Table 4.

A steady state test on a conventional step operated 5LI supplying two wye connected induction motors is shown in Figure 13. The test was performed at \( \omega_r = 50 \text{ rad/s} \) and with no load. A remarkable stator current distortion was obtained, due to the low switching frequency. Figure 14 deals with
the same test but using the 5LI+TLI MMSC topology instead of the conventional configuration. The distortion of the motors phase current was remarkably reduced, however; the efficiency was also slightly reduced, being 80% for the 5LI and 76% for the 5LI+TLI system.

![Figure 12. Experimental setup of OW MMSC.](image)

**Figure 12.** Experimental setup of OW MMSC.

![Figure 13. Conventional configuration, both motors are wye-connected and fed by a step operated 5MLI: steady state test at \( \omega_r = 50 \text{ rad/s} \) and with no load. Motor speed \( \omega_r \), a-phase motor \( V_{ma} \), motor currents \( i_{am1} \) and \( i_{am2} \).](image)

**Figure 13.** Conventional configuration, both motors are wye-connected and fed by a step operated 5MLI: steady state test at \( \omega_r = 50 \text{ rad/s} \) and with no load. Motor speed \( \omega_r \), a-phase motor \( V_{ma} \), motor currents \( i_{am1} \) and \( i_{am2} \).

![Figure 14. 5LI+TLI MMSC: steady state test at \( \omega_r = 50 \text{ rad/s} \). Motor speed \( \omega_r \), a-phase motor \( V_{ma} \), motor currents \( i_{am1} \) and \( i_{am2} \).](image)

**Figure 14.** 5LI+TLI MMSC: steady state test at \( \omega_r = 50 \text{ rad/s} \). Motor speed \( \omega_r \), a-phase motor \( V_{ma} \), motor currents \( i_{am1} \) and \( i_{am2} \).
A comparison between the 3LI+TLI and 5LI+TLI MMSC configurations is provided in Figure 15. A steady state test ($\omega_{a1} = \omega_{a2} = 50$ rad/s) performed using the MMC 5LI+TLI system is displayed in Figure 16. The c phase current of the TLI is higher than the currents of the other four phases, as it is given by the combination of the c phase currents of both motors.

![Figure 15](image1.png)

**Figure 15.** (a) MMSC (3LI+TLI); (b) MMSC (5LI+TLI). Steady state test, stator voltage $V_{ma}$, stator current $i_{am1}$, TLI output voltage $V_{TLIa}$ and TLI voltage reference $V^*_{TLIa}$.

![Figure 16](image2.png)

**Figure 16.** 5LI+TLI5 MMC, Steady state test at $\omega_r = 50$ rad/s. (a) Motor speed $\omega_r$, a-phase motor $V_{ma}$, motor currents $i_{am1}$ and $i_{am2}$; (b) motor currents $i_{am1}$ and $i_{am2}$ and common-leg c-phase current $i_c$.

Speed reversals from $\omega_r = -40$ rad/s to $\omega_r = 40$ rad/s accomplished by the 5LI+TLI MMSC and the 5LI+TLI5 MMC prototypes, are shown in Figure 17. The drives feature a good dynamic response.
and an effective floating capacitor voltage control. The torque load was evenly shared between the two motors.

\[ \omega_r, i_q \text{ axes currents components } i_{q1} \text{ and } i_{q2} \text{ and TLI DC Bus voltage } V_{DC}. \]

**Figure 17.** (a) 5LI+TLI5 MMC; (b) 5LI+TLI5 OW MMC: speed reversal with \( i_{dref} = 2 \text{ A} \). Motor speed \( \omega_r \), \( q \)-axes currents components \( i_{q1} \) and \( i_{q2} \) and TLI DC Bus voltage \( V_{DC} \).

In order to assess the capability of the 5LI+TLI5 configuration to individually control the torque produced by the two motors, the previous test was repeated with uneven loading on the two machines. As shown in Figure 18, 70% of the load torque was produced by IM1 and 30% by IM2. Figure 19 shows the phase currents of IM1 and IM2 at the steady state for the MMC. The steady state currents and dynamical torque, as well as, and speed response are quite satisfactory.

**Figure 18.** MMC 5LI+TLI5: speed reversal with. \( i_{dref} = 2 \text{ A} \), \( i_{q1} = 0.7 \text{ } i_q \) and \( i_{q2} = 0.3 \text{ } i_q \). Motor speed \( \omega_r \), \( q \)-axes currents components \( i_{q1} \) and \( i_{q2} \) and TLI DC Bus voltage \( V_{DC} \).
6. Conclusions

The paper has proposed a multi-level converter topology for multiple-motor drives based on a special open-end winding configuration. Applications of such a topology to multiple motors - single converter and multiple motor-multiple converter drives was also discussed. Specifically, two configurations, an MLI+TLI Multi Motor Single Converter system and an MLI+TLI5 Multi Motor Multi Converter system were presented and managed by purposely developed control strategies, combining a low switching frequency modulation on the MLI and high frequency PWM on the TLI. As shown in the paper, in both cases the proposed configurations produced much lower stator current distortion when compared to conventional multi-motor drives equipped with MLI switching at the fundamental frequency. Further, they generated lower power losses when compared to multi motor drives equipped with PWM operated MLI. Although the paper considers only multi motor systems comprising two identical induction machines, the proposed approach can be generalized for systems with an arbitrary amount of motors; it can also be exploited for multi motor systems using synchronous machines, and even for multi motor systems using a mix of machines of different sizes.

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Nomenclature

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tbody>
<tr>
<td>MMD</td>
<td>Multiple Motor Drive</td>
</tr>
<tr>
<td>MMSC</td>
<td>Multiple Motors fed by a Single Converter</td>
</tr>
<tr>
<td>MMC</td>
<td>Multiple Motors fed by Multiple Converters</td>
</tr>
<tr>
<td>IFOC</td>
<td>Indirect Field Oriented Control</td>
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<tr>
<td>TLI</td>
<td>Two-Level Inverter</td>
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<tr>
<td>3LI</td>
<td>Three-Level inverter</td>
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<td>TLI5</td>
<td>Five-leg two level inverter</td>
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<td>3LI+TLI</td>
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<td>3LI+TLI5</td>
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<td>THD</td>
<td>Total Harmonic Distortion</td>
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<tr>
<td>n</td>
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</tr>
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<td>V_MLI_stepi</td>
<td>i-phase MLI output voltage with respect to n'</td>
</tr>
<tr>
<td>V_TLIi</td>
<td>i-phase TLI output voltage with respect to n''</td>
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</table>
V_{mi} \quad i\text{-phase motor voltage}

V_{DC}' \quad \text{MLI DC Bus voltage}

V_{DC}'' \quad \text{TLI DC Bus voltage}

V_{mpk} \quad \text{Peak motor voltage}

i_{abc1} \quad abc \text{ axes IM1 phase currents}

i_{abc2} \quad abc \text{ axes IM2 phase currents}

E_{qd1} \quad qd \text{ axes motor back EMF}

E_{qd2} \quad qd \text{ axes IM1 phase currents}

V_{qdMLI} \quad qd \text{ axes MLI output voltage}

R_s, R_r \quad \text{Stator and rotor resistances}

R_fe \quad \text{Iron resistance}

L_s, L_r \quad \text{Stator and rotor inductances}

L_m \quad \text{Magnetizing inductance}

\omega_{\lambda r} \quad \text{Rotor flux angular frequency}

K_V \quad \text{Voltage ratio } V_{DC''}/V_{DC'}

K_p \quad V_{mpk}/(V_{DC'} + \text{THD}_V)

\omega_r \quad \text{Mechanical Rotor speed}

\omega_{re} \quad \text{Electrical Rotor speed}

\theta_{\lambda r1}, \theta_{\lambda r2} \quad \text{Rotor flux angular positions of IM1 and IM2}

\theta_r \quad \text{Rotor angular positions of IM1 and IM2}

T_{e1n}, T_{e2n} \quad \text{Rated torques of IM1 and IM2}

J \quad \text{Total inertia of motor and load}

pp \quad \text{pole pairs}

V_{ceo} \quad \text{Collector to Emitter Saturation Voltage}

t_{on} \quad \text{Current Turn-On Delay Time}

t_{off} \quad \text{Current Turn-Off Delay Time}

V_{CES} \quad \text{Collector to Emitter Breakdown Voltage}

I_C \quad \text{Collector current}

V_{DSS} \quad \text{Drain-to-Source Breakdown Voltage}

I_{DSS} \quad \text{Drain-to-Source Leakage Current}

R_{DS(on)} \quad \text{Static Drain-to-Source On-Resistance}

P_{iron} \quad \text{Motor iron losses}

P_{joule} \quad \text{Motor joule losses}

P_{CMLI} \quad \text{MLI conduction losses}

P_{swMLI} \quad \text{MLI switching losses}

P_{CTLI} \quad \text{TLI conduction losses}

P_{swTLI} \quad \text{TLI switching losses}

\delta \quad \text{Duty cycle of the 3LI}

f_{swMLI} \quad \text{Switching frequency of the 3LI}

f_{swTLI} \quad \text{Switching frequency of the TLI}

References


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