Comparison of CFD Simulation to UAS Measurements for Wind Flows in Complex Terrain: Application to the WINSENT Test Site

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Abstract: This investigation presents a modelling strategy for wind-energy studies in complex terrains using computational fluid dynamics (CFD). A model, based on an unsteady Reynolds Averaged Navier-Stokes (URANS) approach with a modified version of the standard k-ε model, is applied. A validation study based on the Leipzig experiment shows the ability of the model to simulate atmospheric boundary layer characteristics such as the Coriolis force and shallow boundary layer. By combining the results of the model and a design of experiments (DoE) method, we could determine the degree to which the slope, the leaf area index, and the forest height of an escarpment have an effect on the horizontal velocity, the flow inclination angle, and the turbulent kinetic energy at critical positions. The DoE study shows that the primary contributor at a turbine-relevant height is the slope of the escarpment. In the second step, the method is extended to the WINSENT test site. The model is compared with measurements from an unmanned aircraft system (UAS). We show the potential of the methodology and the satisfactory results of our model in depicting some interesting flow features. The results indicate that the wakes with high turbulence levels downstream of the escarpment are likely to impact the rotor blade of future wind turbines.

Keywords: wind simulation; complex terrain; unsteady Reynolds averaged Navier-Stokes (URANS); design of experiments (DoE); unmanned aircraft system (UAS)

1. Introduction

Wind power is currently one of the most promising renewable energy sources. The year 2017 was a record year for annual installations in Europe, with 16.8 GW of additional wind power capacity installed. Wind energy remains the second largest form of power generation capacity in Europe, closely approaching gas installations. In the EU, wind energy overtook nuclear energy in 2013, hydro in 2015, and coal in 2016. In 2017, offshore installed wind power capacity represented 15.8 GW against 153 GW for onshore installations [1]. Onshore installations are mainly built on flat terrain, making them easier to operate compared to those mounted on hilly terrain, where forecasts are more uncertain, wear and tear is greater, and maintenance and construction costs are higher. However, wind energy in mountainous regions has been making inroads in recent years and is of increasing interest to the wind-energy community.

WindForS, a wind energy research cluster in Southern Germany, aims to answer the question of how to optimize installations in complex terrains and extend their service life. In the framework of the
project Wind Science and Engineering in Complex Terrain (WINSENT), a field-test site for research and industry, located behind an escarpment in the Swabian Alps, near the town of Geislingen an der Steige is setting up. The project working plan is divided into two stages: the first phase investigates the local wind flow without wind turbines where different measurement equipment is used to characterize the wind flow, such as towers equipped with anemometers, Lidar [2], eddy-covariance stations, and an unmanned aircraft system (UAS) (see [3–5]). The second stage will include two wind turbines with a nominal output of around 750 kW. The turbine-terrain interference will be studied in this second phase.

Characterizing the wind flow in complex terrain is more challenging compared to flat terrain. At these locations, wind flows are more complex, and they are influenced by changes in topography such as hills, escarpments, and roughness, leading to non-linear features such as high levels of turbulence, wind shear, unsteadiness, etc. Analytical models, mainly developed in the 1970s and 1980s such as the well-known Wind Atlas Analysis and Application Program (WAsP), are capable of predicting the mean wind field only in simple geometries and are suitable only for attached flow (see [6–9] and others). Modelling non-linear features of the flow became a feasible option with the help of computational fluid dynamics (CFD) solvers which retain the nonlinearity of the Navier-Stokes equations and simulate momentum, turbulence, and energy [10]. The commonly referenced field experiment of Bolund hill, which consists of a steep hill, has been used for a blind comparison of models with different ranges of fidelity (linearized and CFD models) as reported in [11]. One of the outcomes of this comparison was that the linearized models were not able to predict the mean flow features such as the speed-up, unlike the CFD models (see [12] for a complete review). In [13], the flow field over a large-scale model of the same hill was investigated experimentally and showed that the mean wind, wind shear, and turbulence level are extremely sensitive to the details of the terrain. Making the edge of the hill sharper resulted in a reduction of the estimated annual energy production by at least 50% and an increase in the turbulent level by a factor of five in the worst-case scenario. They concluded “the mean wind, wind shear, and turbulence level are extremely sensitive to the exact details of the terrain”. This shows that special attention should be paid not only to the model but also to the topography representation in complex terrains by using high-resolution topographic data and information on land use, such as the Corine land cover [14].

The use of large eddy simulation (LES) or detached eddy simulation (DES) in complex terrain has increased in recent years. These models are superior to both steady and unsteady Reynolds averaged Navier-Stokes (RANS) as they have the advantage of providing additional information on turbulent structures and non-linear features of wind flow over complex terrain. However, the requirement of high computational resources and the challenge of obtaining proper inflow boundary conditions limits their usefulness for wind engineering studies where a fast solution is required [10]. In addition, for wind-energy applications, the simulation often needs to be computed for different wind directions or stability conditions. Due to these constraints, RANS/URANS models are still appropriate for use as they provide a good balance between computational effort and model accuracy.

A common problem when using CFD models in a complex terrain is how to specify initial and boundary conditions. A standard way to proceed is to impose a standard logarithmic velocity profile at an inlet which is orientated perpendicular to the wind direction. Another approach is to use numerical weather prediction (NWP) models, also called mesoscale models, to provide more realistic boundary conditions for the CFD simulations. Mesoscale models, generally, have a low spatial resolution with a horizontal extent on the order of 2 km and they generally present a bias on the predicted wind speed and turbulent quantities in complex terrains due to unresolved topographic effects. In [15], the WRF mesoscale model for the Horns Rev wind farm was applied with a horizontal resolution of 333 m and showed that the model still underestimates the power deficit due to its coarse resolution. Nevertheless, as demonstrated in [16], much effort has been made to improve the NWP models. Coupling a mesoscale model to a microscale model (CFD), which presents a more detailed representation of the topography seems to be one of the more promising approaches for wind-energy assessment in complex terrain. Several coupling methods of mesoscale and microscale models have been developed in the last decade,
and an overview of these methods can be found in [10,17]. One of the most common coupling methods is the one-way approach where the mesoscale model is coupled to the microscale model through the lateral boundaries at fixed times (time-slice). This approach has been successfully applied in complex terrain by several authors as [18–20] among others.

In the present paper, the WINSENT test site is studied by means of numerical simulations along with UAS data. We confine the study to a neutral stratification case. Section 2 presents the physical model with its validation, while Section 3 presents the parametric study. The parametric study is conducted with the help of a design of experiment (DoE) method applied to a two-dimensional case. This study intends to assess the sensitivity of our model results for different parameters and predict their effect on some relevant variables for wind turbines. Section 4 gives an overview of the test site and the measurement system, while Section 5 presents the model which uses the one-way coupling approach. The same section compares simulation results against UAS measurements. Section 6 draws a summary and discusses the limitation of the model and possible future improvements.

2. Methods

2.1. Numerical Model

To simulate the atmospheric boundary layer (ABL) flow, the finite volume method (FVM) on the OpenFOAM v2.4.0 (Open Source Field Operation and Manipulation) software, provided by the OpenFOAM Foundation U.K., was used [21]. The OpenFOAM toolbox includes open source C++ libraries released under the general public license (GPL). An unsteady Reynolds Averaged Navier-Stokes approach under the Boussinesq approximation, where density is only influenced by buoyancy forces, was considered [22]. The transport equations for mass, momentum, and potential temperature can be written relative to a hydrostatic state (index \( h \)) in a Cartesian coordinate as:

\[
\frac{\partial (\rho_h)}{\partial t} + \frac{\partial (\rho_h u_j)}{\partial x_j} = 0
\]

\[
\frac{\partial (\rho_h u_i)}{\partial t} + \frac{\partial (\rho_h u_i u_i)}{\partial x_i} = - \frac{\partial p}{\partial x_i} + \frac{\partial}{\partial x_i} \left[ \left( \mu + \mu_t \right) \left( \frac{\partial u_i}{\partial x_i} + \frac{\partial u_i}{\partial x_i} \right) - \frac{2}{3} k \delta_{ij} \right] - \rho_h \left( \frac{\partial - \partial_h}{\partial_h} \right) \nabla \mathbf{F_c} + S_u
\]

\[
\frac{\partial (\rho_h \theta)}{\partial t} + \frac{\partial (\rho_h u_i \theta)}{\partial x_i} = \frac{\partial}{\partial x_i} \left[ \left( \mu + \mu_t \right) \left( \frac{\partial \theta}{\partial x_i} \right) \right]
\]

where \( U_i \) (\( i = 1, 2, 3 \)) are the velocity component in the \( x, y, \) and \( z \) directions, respectively, \( p \) and \( \theta \) are the pressure and potential temperature, \( \mu \) and \( \mu_t \) are the molecular and the turbulent eddy viscosities, \( g \) is the gravitational acceleration, and \( \sigma_h \) is the turbulent Prandtl number. \( \mathbf{F_c} \) is the Coriolis force defined as \( \epsilon_{ijk} f_c U_k \), where \( f_c = 2 \Omega \sin \lambda \) is the Coriolis parameter, a function of the Earth’s angular velocity \( \Omega \) and the latitude \( \lambda \). \( S_u \) is the source term representing a forest canopy and described later by Equation (14). The hydrostatic fluid density \( \rho_h \) is given in a hydrostatic reference state (subscript 0) as a function of the hydrostatic pressure \( p_h \) and the temperature \( T_h \) as:

\[
\rho_h = \frac{p_h}{R_d T_h}
\]

\[
T_h = \sqrt{T_0^2 - \frac{2 A g z}{R_d}}
\]

\[
p_h = p_0 \left( \frac{T_0}{A} + \sqrt{\frac{T_0^2}{A} - \frac{2 A g z}{R_d A}} \right)
\]
with the constant reference pressure \( p_0 \) usually set to 1000 hPa, \( T_0 \) is the reference temperature equal to 288.5 K, \( A = 50 \text{ K} \) and \( R_d = 287.05 \text{ J kg}^{-1} \text{K}^{-1} \) according to [23,24].

We introduce the hydrostatic potential temperature which is, by definition, a function of the temperature and the pressure according to an adiabatic state change as follows:

\[
\theta_h = T_h \left( \frac{p_0}{p_h} \right) \frac{c_p}{R}
\]  

(7)

To close the given set of equations above, the \( k - \varepsilon \) model was used. The standard \( k - \varepsilon \) model, when applied to ABL studies, is known to lead to a turbulent length scale \( l \), that grows approximately linearly with the height and thus, possesses very deep boundary layers. In real ABL flows, the turbulent length scale is limited by the ABL height or the stability [25,26]. To overcome this problem, the mixing length model proposed by [25], which introduces a limiting size of turbulent eddies \( l_{\text{max}} \) in the ABL is used. The two modified transport equations for the turbulent kinetic energy \( k \) and the dissipation \( \varepsilon \) read:

\[
\frac{\partial (\rho_h k)}{\partial t} + \nabla \cdot (\rho_h \mathbf{u} k) = \frac{\partial}{\partial x_j} \left( \mu + \frac{\mu_t}{\sigma_k} \frac{\partial k}{\partial x_j} \right) + P + G + S_k - \rho_h \varepsilon
\]  

(8)

\[
\frac{\partial (\rho_h \varepsilon)}{\partial t} + \nabla \cdot (\rho_h \mathbf{u} \varepsilon) = \frac{\partial}{\partial x_j} \left( \mu + \frac{\mu_t}{\sigma_\varepsilon} \frac{\partial \varepsilon}{\partial x_j} \right) + C_{\varepsilon 1}^* (P + G) + S_\varepsilon - C_{\varepsilon 2} \varepsilon^2
\]  

(9)

where \( P \) represents the production rate of turbulent kinetic energy due to shear and \( G \) represents the production/destruction of turbulence by buoyancy forces defined as:

\[
P = \tau_{ij} \left( \frac{\partial u_i}{\partial x_j} \right) = \mu \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \delta_{ij} - \frac{2}{3} \rho_h \frac{\partial u_k}{\partial x_k} \delta_{ij}
\]  

(10)

\[
G = - \frac{1}{T^3} \frac{\mu_t}{\sigma_t} \frac{\partial \theta}{\partial x_i}
\]  

(11)

\( S_k \) and \( S_\varepsilon \) are source terms relative to the forest canopy and described later in Equations (15) and (16). \( \sigma_k, \sigma_\varepsilon, C_{\varepsilon 1}, C_{\varepsilon 2} \) are model coefficients listed in Table 1. These constants were adapted to atmospheric conditions, as proposed by [26]. \( C_{\varepsilon 1}^* \) introduces the maximum mixing length \( l_{\text{max}} \) in the following:

\[
C_{\varepsilon 1}^* = C_{\varepsilon 1} + (C_{\varepsilon 2} - C_{\varepsilon 1}) \frac{l}{l_{\text{max}}}
\]  

(12)

where the mixing length \( l \) is equal to the dissipation length defined as \( l_\varepsilon = \left( \frac{C_\varepsilon^3 k^3}{\sigma_\varepsilon} \right) / \varepsilon \). Several mixing-length models in the literature enable estimation of the limiting turbulent size of turbulent eddies in the ABL \( l_{\text{max}} \), see [27] for a review. For neutral flows, this length is computed using the Blackadar equation [28] as:

\[
l_{\text{max}} = 0.00027 \frac{U_g}{2 \Omega \sin \lambda}
\]  

(13)

where \( U_g \) is the geostrophic wind velocity.

Table 1. Constants used in \( k - \varepsilon \) turbulence models.

<table>
<thead>
<tr>
<th>Turbulence Model Constants</th>
<th>( C_\mu )</th>
<th>( C_{\varepsilon 1} )</th>
<th>( C_{\varepsilon 2} )</th>
<th>( \sigma_\varepsilon )</th>
<th>( \sigma_k )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Standard [29]</td>
<td>0.09</td>
<td>1.44</td>
<td>1.92</td>
<td>1.00</td>
<td>1.3</td>
</tr>
<tr>
<td>Adapted [26]</td>
<td>0.256</td>
<td>1.13</td>
<td>1.90</td>
<td>0.74</td>
<td>1.3</td>
</tr>
</tbody>
</table>
In order to account for the effects of vegetation on the wind flow, terms in the transport equation of momentum Equation (2), turbulent kinetic energy Equation (8), and turbulence dissipation rate Equation (9) were added:

\[
S_u = -\rho h C_d LAD(z) |U| u_i
\]

\[
S_k = -\rho h C_d LAD(z) \left( \beta_p |U|^3 - \beta_d |U| k \right)
\]

\[
S_\varepsilon = -\rho h C_d LAD(z) \frac{\varepsilon}{k} \left[ (C_{d4} \beta_p |U|^3 - C_{d5} \beta_d |U| k) \right]
\]

where $|U|$ is the velocity magnitude and $C_d$ the leaf drag coefficient. The values of this drag coefficient vary between 0.1 and 0.3 for most of the vegetation [30]. A value of 0.2 will be considered for the rest of the study. $\beta_p$, $\beta_d$, $C_{d4}$, and $C_{d5}$ are model constants proposed by [30] and reported in Table 2. Vegetation is discretized into finite volumes where the total amount of leaves per given volume is defined by the leaf area density ($LAD$) and the sum of each layer’s $LAD$ value over the total canopy height $H$ is called the leaf area index ($LAI$). A typical profile of the $LAD$ for a deciduous forest can be seen in Figure 1. The relationship between the $LAI$ and $LAD$ can be expressed as follows:

\[
LAI = \int_0^H LAD(z) \, dz
\]

![Figure 1. Typical distribution of LAD for a deciduous forest. LAI of 2 and 5 are used in the simulations in this study.](image)

<table>
<thead>
<tr>
<th>Closure Constants</th>
<th>$\beta_p$</th>
<th>$\beta_d$</th>
<th>$C_{d4}$</th>
<th>$C_{d5}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value</td>
<td>1</td>
<td>5.1</td>
<td>0.9</td>
<td>0.9</td>
</tr>
</tbody>
</table>

Table 2. Constants used for the canopy model.

The URANS equations were solved using a PIMPLE pressure-velocity coupling algorithm. The PIMPLE solver is considered as it offers the possibility to visualize the transient effects, which will be part of our future investigation. The gradient terms and Laplacian terms were discretized using a 2nd order linear interpolation, while a 2nd order upwind interpolation was applied for divergence terms. The convergence criteria for residuals were ensured to be less than $10^{-6}$.

2.2. $k$-$\varepsilon$ Model Validation

The numerical model was verified using the solution of the Leipzig wind profile. This profile was measured from a set of 28 double-theodolite balloons between 9:15 and 16:15 on the 20 October 1931 as reported in [31]. The ABL was considered as horizontally-homogeneous with a geostrophic...
wind speed $U_g = 17.5 \text{ m s}^{-1}$ and a Coriolis parameter $f = 1.13 \times 10^{-4} \text{ s}^{-1}$ corresponding to a latitude of 45 degrees N. Simulations were carried out using two $k-\varepsilon$ models with the constants adapted to atmospheric conditions, as listed in Table 1, except for $C_{\varepsilon 1}$, $C_{\varepsilon 2}$, which were considered as constant in the first model and as a function of the size of turbulent eddies in the second model (Equation (12)), called respectively $k-\varepsilon$ unlimited and $k-\varepsilon$ limited. A maximum mixing length $l_{\text{max}}$ of 36 m was used in the $k-\varepsilon$ limited, as reported by [25,26]. A computational domain of $1 \text{ km} \times 1 \text{ km} \times 3 \text{ km}$ in the $x$, $y$, and $z$ directions, spatially resolved with $50 \times 50 \times 200$ cells was defined. A geostrophic wind velocity $U_g = (17.7, 0, 0) \text{ m s}^{-1}$ at the top of the domain and at a constant roughness length of $z_0 = 0.3 \text{ m}$ was prescribed on the ground. The boundaries at the domain sides were defined as cyclic.

The results of the two models, together with the experimental data, are shown in Figure 2. Figure 2a,b shows vertical profiles of the wind component $v$ perpendicular to the geostrophic wind and the component $u$, parallel to the geostrophic wind $U_g$. The measured vertical profile of the velocity shows a low-level jet and shear on the wind direction. The Coriolis term in the model lead to a turning in the boundary layer which is depicted by the velocity component $v$. While the limited model simulated the profile reasonably well, the unlimited model showed a flat profile. Figure 2c shows a surface wind turned by 24.3° to the geostrophic wind for the limited model. This is close to the measured value of 26°. The unlimited version predicts a smaller cross-isobar angle of 12.0° due to the flat $v$-profile.

![Figure 2](image-url)

**Figure 2.** Vertical profile of the wind velocity component $u$ (a), wind velocity component $v$ (b), tuning of wind (c), mixing length (d), eddy viscosity (e) and turbulent kinetic energy (f).

The limited variant leads to turbulent kinetic energy and viscosity decreasing over the depth of the boundary layer while the standard variant shows a more or less linear increase causing a very
deep boundary layer (Figure 2d–f). Overall, this validation study shows that the limiting effect is significant. For the Leipzig test case, the limited $k – \varepsilon$ model yields results that have a better agreement with the observed profiles. Due to overestimation of the eddy viscosity with increasing height, the effects captured by the unlimited $k – \varepsilon$ model were underestimated.

3. Design of Experiments (DoE) Study

After verifying the capability of the model to reproduce the flow features in the ABL, the next step was to identify primary contributors to the wind flow at the WINSENT test site. One of the main features of the test site is an escarpment covered by heterogeneous vegetation. The two planned test wind turbines, with a hub height of 75 m and a rotor diameter of 50 m will be installed approximately 200 m downstream of the forested escarpment and will be directly influenced by the canopy. Finding the impact of the forest height and density (which varies seasonally as the foliage grows and develops) on the wind flow can be assessed using a DoE approach. Combining CFD simulations with a DoE can be used to accurately rank the importance of the design parameters in a study [32] and can significantly reduce, for a real test site, the amount of simulated case and computational time. In our study, the influence of three parameters (namely the slope of the escarpment $\alpha$, the LAI, and the forest height $H$) on the horizontal velocity, the flow inclination angle, and the turbulent kinetic energy at different locations, corresponding to the future position of the turbines was investigated. Table 3 lists the three parameters and their assigned values.

<table>
<thead>
<tr>
<th>Variable Level</th>
<th>Slope $\alpha$ (°)</th>
<th>Height H (m)</th>
<th>LAI</th>
</tr>
</thead>
<tbody>
<tr>
<td>$-1$</td>
<td>15</td>
<td>20</td>
<td>2</td>
</tr>
<tr>
<td>$+1$</td>
<td>30</td>
<td>25</td>
<td>5</td>
</tr>
</tbody>
</table>

In order to apply the DoE, a simplified test case was defined as shown in Figure 3. The test case represents a simplification of the test site in two dimensions. We consider a 150 m high escarpment and the slope $\alpha$ to be of 15° or 30°, corresponding to a West and West-North-West wind direction. The escarpment is covered by a forest (green block in Figure 3).

![Figure 3](image-url)  
Figure 3. 2D geometry for the DoE study and the location of lines $L_0, L_1, L_2$ and $L_3$, situated 0 m, 100 m, 200 m, and 1000 m downstream of the forested escarpment (green block), respectively.

In the real case, the separation between the forest and the ground is not as sharp, but rather shows a smooth transition. Several studies in the literature on the flow over an escarpment, including wind
tunnel, full-scale and simulations exist [33–35]. However, none of these studies presents results for a vegetated escarpment.

At the inflow, an empirical power law is used to describe the vertical wind profile as in [22]:

\[ u(z) = u(z_r) \left( \frac{z}{z_r} \right)^a \tag{18} \]

where \( \mu(z) \) is the average streamwise velocity at height \( z \). \( \mu(z_r) = 6 \text{ m s}^{-1} \) is the reference wind speed at the reference height \( z_r = 80 \text{ m} \) and \( a \) is the power law exponent. This exponent depends on the surface roughness and the thermal stability parameter \( \alpha \). A value of 0.14 is taken as we assume the neutral case in this DoE study. It is worth mentioning that such a wind profile is an idealized one and is rarely found in a hilly complex terrain. However, our DoE study aims to assess the impact of modelling assumptions for a vegetated escarpment on certain parameters of interest and is not conducted in order to obtain the exact profiles at our specific test site with complex terrains.

We define the speed-up ratio \( S_u \) as being the mean wind speed at a height \( z \) above the ground divided by the mean wind speed of the undisturbed flow at the same height:

\[ S_u = \frac{u(z)}{u_{\text{undisturbed}}(z)} \tag{19} \]

Similarly, we define \( S_k \) as the speed-up ratio for the turbulent kinetic energy as:

\[ S_k = \frac{k(z)}{k_{\text{undisturbed}}(z)} \tag{20} \]

Speed-up ratio profiles for the wind speed downstream of the escarpment along \( L_0, L_1, L_2 \) and \( L_3 \) are presented in Figure 4. All the possible configurations of variables listed in Table 3 were simulated, and, additionally, the case of an escarpment with no canopy was simulated. The case without forest allows one to distinguish between the effect caused by the slope of the escarpment and the canopy. Figure 4 reveals the influence of the canopy, particularly up to 80 m above ground level (agl.). At \( L_0 \), i.e., at the crest, the speed-up ratio shows a reduction in the velocity due to the drag effect generated by the forest, whereas for the case with no canopy, a strong acceleration of the flow can be seen. This effect is still perceptible 1 km downstream of the escarpment (at position \( L_3 \)). The same observation was made in the work of [33]. There, a wind tunnel investigation of the flow over several escarpment shapes with a slope of 2:1 (26.7°) and 4:1 (14.0°) was performed. It was found that the region of influence of the escarpment persists 10 \( H \) (\( H \) being the escarpment height) downstream of the crest. The largest speed-up ratios were found close to the ground and decreased with increasing height for all cases. The location of the maximum moved upward as the flow proceeded downstream. The inclusion of a forest along the escarpment deflected the position of the maximum speed-up ratio \( S \) to higher altitudes. At \( L_1 \), the position of the maximum of \( S_u \) located between 10 m and 20 m agl. with no canopy model, and between 80 m and 90 m agl. for the cases with a canopy. The maximum values of \( S \) for a slope of 30°, are higher than in the case of 15°. For example, at \( L_1 \), a maximum value of 1.33 and 1.26 was reached with a slope of 30° and 15°, respectively. This effect was reduced 1 km downstream of the crest, where a maximum of 1.27 and 1.24 was reached. For the same forest height (blue vs. red lines), as expected, a higher deceleration of the flow, i.e., lower value of \( S_u \) was observed for an \( \text{LAI} \) of 5 instead of an \( \text{LAI} \) of 2. All the positions, except the crest position, show an acceleration of the flow at the relevant heights for a wind turbine (between 80 m and 100 m agl.).
Figure 4. Speed-up profiles for the horizontal velocity at $L_0$, $L_1$, $L_2$ and $L_3$ position for an angle of 15° (a–d) and 30° (e–h). The red and blue curves are the simulation results with an LAI of 2 and 5, respectively. The solid and dashed lines indicate a forest height of 20 m and 25 m, respectively.

Figure 5 presents the results for the speed-up ratio for the turbulent kinetic energy speed, $S_k$. Speed-up ratio profiles for the turbulent kinetic energy are highly dependent on the canopy height and the LAI. The crest position ($L_0$) shows a maximum turbulent kinetic energy occurring near the top of the canopy and decaying rapidly above the forest. At position $L_3$, the high turbulence levels indicate that the wake generated behind the crest was not dissipated. However, the case without forest seems to be almost recovered and suggests that the changes in the turbulent kinetic energy were only
due to the canopy. In general, the turbulent kinetic energy levels increased with the slope angle of the escarpment, but also with the forest height.

Figure 5. Speed-up profiles of the turbulent kinetic energy at $L_0$, $L_1$, $L_2$, and $L_3$ position for an angle of 15° (a–d) and 30° (e–h). The red and blue curves are the simulation results with a LAI of 2 and 5, respectively. The solid and dashed lines indicate a forest height of 20 m and 25 m, respectively.

The results of the DoE on the 2D escarpment are shown in Figures 6–8. The DoE method was applied at two points, $P_1$ and $P_2$, located at different altitudes (50 m, 75 m, and 100 m agl.) on the lines
The absolute effects of each factor, listed in Table 3, on the horizontal velocity, the inclination angle and the turbulent kinetic energy were evaluated. A similar behaviour for the horizontal velocity (Figure 6) and the flow inclination angle (Figure 7) can be seen: the main variability in the response is dominated by the slope of the escarpment. This becomes even more evident for the flow inclination angle. The effect of the forest height \(H\) or the leaf area index \(LAI\) remains small relative to the slope, except for the lowest positions at 50 m agl., where the forest height parameter can exceed the same absolute value as the angle (Figure 6). Generally, as we go further downstream of the escarpment (\(P_1\) vs. \(P_2\)), the effect for the three parameters becomes smaller. The response for the turbulent kinetic energy \(k\) was different. The forest height, followed by the \(LAI\), was as important as the slope at lower levels. All the effects were then dissipated at 100 m agl.

![Figure 6](image_url)

**Figure 6.** Pareto chart of effects for the horizontal velocity at different altitudes on \(L_1\) and \(L_2\).

![Figure 7](image_url)

**Figure 7.** Pareto chart of effects for the flow inclination angle at different altitudes on \(L_1\) and \(L_2\).

Considering a turbine hub-height of 75 m and the top of the rotor blade located at 100 m agl., this parametric study shows that the primary contributor was generally the angle, i.e., for the test site, the wind direction. The forest height \(H\) and \(LAI\) play a significant role only at 50 m agl. This is in accordance with the results from Figure 4, where the main differences for all the configurations were only perceptible in the lower levels. For the simulations of the WINSENT test site, described in Section 4.1, a sensitivity analysis using the same parameter values will be conducted.
The escarpment is covered by a deciduous forest. Downstream, it is essentially flat with an agriculturally used land. Measurements from the German Meteorological Service at Stötten (734 m a.s.l., 48.6657° latitude, 9.8646° longitude), located approximately 2 km upstream of the escarpment, indicate a westward wind direction for most of the year. This wind direction makes the test site interesting in the sense that the predominant wind direction is perpendicular to the escarpment. More details about the WINSENT test site can be found in [36].

4. WINSENT Test Site Overview and Measurement Techniques

4.1. Site Description

The test site is located in the Swabian Alb in Southern Germany. The main feature of the site is an escarpment up to 200 m in height with respect to the valley (Figure 9). The escarpment is characterized by a very steep slope of around 30° from the Northwest and a more gradual slope at around 15° further west. The escarpment is covered by a deciduous forest. Downstream, it is essentially flat with an agriculturally used land. Measurements from the German Meteorological Service at Stötten (734 m a.s.l., 48.6657° latitude, 9.8646° longitude), located approximately 2 km upstream of the escarpment, indicate a westward wind direction for most of the year. This wind direction makes the test site interesting in the sense that the predominant wind direction is perpendicular to the escarpment. More details about the WINSENT test site can be found in [36].

Figure 8. Pareto chart of effects for the turbulent kinetic energy at different altitudes on $L_1$ and $L_2$.

Figure 9. Overview of the test site and the wind rose generated from a cup anemometer at 10 m agl. at the weather station of Stötten for the time frame 2016–2017.
4.2. Description of the Experiment Setup

The field measurements were carried out on the top of the plateau, over and downstream of the escarpment using the multipurpose airborne sensor carrier (MASC) operated by the Environmental Physics group at the University of Tübingen, Germany. The MASC is a UAS which can resolve turbulent fluctuations of wind and temperature with a resolution of about 30 Hz. The wind measurement was performed by measuring the flow speed and flow angles at the aircraft nose with a multi-hole flow probe. Typical absolute errors in wind speed for the sensors mounted on the MASC are of the order of ±0.5 m·s$^{-1}$ (for more information, see [4,5,37,38]). In order to measure the three-dimensional flow field at the test site, a vertical grid of racetracks with legs going back and forth over the test site was performed. The wind speed measurements were then averaged over subsections of 20 m in length along each leg. Each racetrack consisted of two horizontal straight flight legs, one in the flow direction and the second one going against the wind direction. The legs against the wind direction had a higher spatial resolution and thus were used for comparison with the simulation results.

In the present study, we consider the date 27 March 2015. The site was dominated by dry weather, almost neutral ABL, and a northwest wind (290° at the nearby weather station of Stötten during the measuring time). A vertical grid of the racetrack flight pattern with vertical steps of 25 m was performed between 13:00 and 16:00 UTC. The lowest and the highest flight heights were 75 m and 275 m agl., respectively. Two racetracks were flown at each height. In total, three flights with a duration of one hour each were carried out between 13:00 and 16:00. Figure 10 shows a three-dimensional view of the flight path performed by the MASC. The flight path covers the upstream and downstream region of the escarpment.

Figure 10. Flight paths (racetracks) performed on the 27 March 2015. The colors indicate the measured horizontal velocity.

5. Simulation of the WINSENT Test Site

5.1. CFD Settings for the Test Site

The simulations were conducted on two nested domains with varying size and spatial resolution. A parent domain of 20 km × 20 km × 2 km and a nested domain of 5 km × 5 km × 1.5 km, centred on the escarpment, were defined. The terrain data was based on the digital terrain model DTM from
the Baden-Württemberg Authorities for Spatial Information and Rural Development (LGL) with a spatial resolution of 5 m. A horizontal grid resolution of 25 m was provided for the first domain and a finer resolution of approximately 7 m was provided for the small domain (cf. Table 4). A volume mesh, finer near the ground and conforming to the site orography, was constructed for the domains using SnappyHexMesh, the mesh generator of OpenFOAM. Details of meshes can be found in Table 4. Additionally, the digitized landscape model DLM from LGL was utilized to describe the land cover on the Earth’s surface. Three classes of land uses were used for this study: urban, ground, and forest (Figure 11). The urban and the ground classes were assigned values of \( z_0 = 0.50 \) m and \( z_0 = 0.02 \) m for the aerodynamic roughness length. A no-slip boundary condition was used for the velocity. A sensitivity analysis using several \( \text{LAI} \) values and forest height was conducted (cf. Table 5). The source terms, associated with the forest, as described in Equations (14)–(16), were applied to all cells, which were located below the top of the forest canopy.

**Table 4.** Mesh resolutions for the domains.

<table>
<thead>
<tr>
<th>Mesh Properties</th>
<th>Number of Cells</th>
<th>Maximum Cell Size</th>
<th>Horizontal Resolution at the Ground</th>
<th>Vertical Resolution at the Ground</th>
</tr>
</thead>
<tbody>
<tr>
<td>Basis</td>
<td>66.8 million</td>
<td>100 m</td>
<td>25 m</td>
<td>2.6 m</td>
</tr>
<tr>
<td>Nested</td>
<td>25.4 million</td>
<td>50 m</td>
<td>6.75 m</td>
<td>1.2 m</td>
</tr>
</tbody>
</table>

**Figure 11.** Big domain 20 km × 20 km (a). The color indicates the type of classes used in the simulation: red for urban, grey for ground, and green for forest. The black box shows the position of the small domain 5 km × 5 km (b).

**Table 5.** Summary of simulations run to investigate the sensitivity of the model to the \( \text{LAI} \) and forest height \( H \).

<table>
<thead>
<tr>
<th>Run</th>
<th>( \text{LAI} )</th>
<th>Forest Height ( H ) (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Run 1 (no canopy)</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Run 2</td>
<td>2</td>
<td>20</td>
</tr>
<tr>
<td>Run 3</td>
<td>2</td>
<td>25</td>
</tr>
<tr>
<td>Run 4</td>
<td>5</td>
<td>20</td>
</tr>
<tr>
<td>Run 5</td>
<td>5</td>
<td>25</td>
</tr>
</tbody>
</table>

For the nested domain, boundary conditions were extracted from the solution of the parent domain. The parent domain was initialized using input data from the COSMO-DE (Consortium for Small-scale Modeling) weather model of the German Weather Service (DWD, [23]). COSMO-DE has a
horizontal resolution of 2.8 km × 2.8 km and 20 vertical levels in the lower 3000 m of the computational domain. Only hourly data are delivered by the DWD. These data provide the wind components, pressure, air and surface temperature, as well as the turbulent kinetic energy. A time-slice approach was used in order to join the COSMO-DE and the CFD model. In this method, the boundary conditions for the simulation were based on one specific time slice from the COSMO-DE weather model: 27 March 2015, 15:00 UTC.

5.2. Numerical Results

In order to gain a better understanding of the wind flow at Stötten, a global view of the flow pattern at different heights agl. is presented in Figure 12. An additional black line corresponding to the legs performed by the UAS at the same altitude was added. These legs have a length of approximately 1 km. The large differences in the velocity contour plots highlight the complexity of the flow with high gradients of wind speed, especially at lower levels. A high speed-up zone along the escarpment can be seen. This speed-up extends downstream of the escarpment but not uniformly.

Figure 12. Velocity contour plots for leaf area index (LAI = 2) and h = 20 m at 75 m (a), 125 m (b), 175 m (c) and 275 m (d) agl. on the 27 March 2015. The black lines correspond to the UAS flight path.

For the evaluation of the results, the quantities will be plotted along a horizontal line, corresponding to the performed flight path and three vertical lines (Figure 13). Error bars, corresponding to one standard deviation, were inserted for the UAS measurements.
Figure 12. Velocity contour plots for leaf area index (\(L_{\text{A}}I = 2\)) and \(h = 20\) m at 75 m (a), 125 m (b), 175 m (c) and 275 m (d) agl. on the 27 March 2015. The black lines correspond to the UAS flight path.

Figure 13. Position of the horizontal (black line) and vertical (1, 2 and 3) lines for the evaluation related to Figures 14 and 15.

Figure 14 shows the horizontal wind speed and the flow inclination angle at the same altitudes as those presented in Figure 12. The modelled and measured values are in good agreement, although the profile shape of the modelled wind speed at higher levels is slightly over predicted (up to 2 m s\(^{-1}\)) relative to the UAS measurements. The simulation results and measurements show a horizontal profile which is becoming flat with increasing height. This can be explained by the flow becoming more homogeneous with increasing altitude and no longer being influenced by the terrain. At a height of 75 m, the UAS recorded the maximum wind speed at a distance of around 500 m. The simulation predicts a maximum at the same position. This maximum corresponds to the area over the escarpment with a speed-up as shown in the velocity contour plot in Figure 12a,b. This maximum was shifted to the east with increasing altitude, in accordance with the DoE study. At 125 m height, the maximum was located at a distance of 600 m according to the model. The position of this maximum cannot be seen in the measurement data. Figure 14 shows that using a forest height of 25 m lead to a positive velocity bias, except at the lower level of 75 m, where the velocity was reduced. By comparing the results with different LAI values (blue vs. red lines), we see that the foliage density does not have an impact on the horizontal wind speed. At a height of 275 m, the impact of the canopy and the escarpment was strongly reduced: all the canopy variants converge to a similar profile, with the differences getting smaller.

Flow angles, measured by the UAS and predicted by the simulation, indicate a complex flow near the escarpment. Figure 14 shows the flow inclination angles to have a non-constant profile. Such a change in the inclination angle is due to a local phenomenon induced by local features of the terrain. It is noticeable that, for the first two-thirds of the flight path, positive flow angles of up to 10 degrees were reached. This position corresponds to the area located upwind and over the escarpment that is dominated by updrafts. The flow inclination angle becomes smaller with increasing height, indicating that the wind was less deflected by the orography. At a height of 75 m, zero inclination angles appear at a distance of around 800 m for the simulation and 700 m for the measurements. At higher levels, the model no longer predicts large positive values but angles approaching a zero value, indicating a flow that is rather horizontal. In accordance with the simulation results, the UAS also reports zero-angle values at the highest level. Upon observation of the different parametrization of the forest, no significant differences were found. This is in accordance with the 2D DoE study, where the effect on the inclination angle was largely dominated by the slope of the escarpment.
Figure 12. Velocity contour plots for leaf area index ($L_{\text{A}} = 2$) and $h = 20$ m at 75 m (a), 125 m (b), 175 m (c) and 275 m agl. on the 27 March 2015. The black lines correspond to the UAS flight path.

Figure 13. Position of the horizontal (black line) and vertical (1, 2 and 3) lines for the evaluation related to Figures 14 and 15. (a) (e) (b) (f) (c) (g) (d) (h)

Figure 14. Horizontal velocity (a–d) and inclination angle (e–h) at 75 m, 125 m, 175 m, and 275 m agl. on the 27 March 2015. The dots are the UAS measurements and the lines of the simulation results. The colors represent the different values of $L_{\text{A}}$ and height for the forest.

Figure 15 presents the vertical profiles of the horizontal velocity and the turbulent kinetic energy at three positions along the flight path. The first position was located a few meters upstream the forest, the second one in the canopy and the last one approximately 300 m downstream of the escarpment (Figure 13). The plots confirm the overprediction of the model relative to the measurements at the upper levels. At position 1, i.e., upwind of the escarpment, the flow seems to already be decelerated. At position 2, the velocity profile shows an inflexion point in the lower height due to the explicit integration of the forest in our model. The effect of the escarpment and forest can be detected even at
position 3; however, the profile becomes more uniform with increasing height. This feature is almost too difficult to observe in the UAS data due to the low resolution in the vertical direction. The strong shear, observed in the horizontal velocity profiles, indicated that there is a large amount of turbulence generated by vertical wind shear. Looking at the profiles of the turbulent kinetic energy, the modelled and observed values of the turbulent kinetic energy decreased with increasing height and attain their maximum values in the region of strong wind shear. The turbulent kinetic energy profiles were highly dependent on the canopy model. Upstream of the escarpment, the maximum simulated value was located at 100 m agl. At position 2, this maximum occurred at approximately 20 m agl., i.e., at the top of the forest, where a large portion of the turbulent kinetic energy was produced, due to high shear and shear-stress. Downstream of the escarpment, this maximum was carried to the upper heights with values between 3.5 and 4.0 m$^2$s$^{-2}$ at a height of 40 m in the model. The UAS measurement also showed an increasing turbulence value of 2.4 m$^2$s$^{-2}$ at a height of 75 m.

Due to a low vertical spatial resolution in the measurements, it is difficult to determine the location and the intensity of this maxima. The simulation results show that the location of this maximum can be critical as it is approaching the bottom of the rotor plane of the future wind turbine. The turbulent kinetic energy profiles obtained at position 3 were the result of a flow which has been decelerated but, in the meantime, production of turbulent kinetic energy near the canopy top was generated.

**Figure 14.** Horizontal velocity (a, b, c and d) and inclination angle (e, f, g and h) at positions 1, 2 and 3 on the 27 March 2015. The dots are the UAS measurements and lines of the simulation results. The colors represent the different values of LAI and canopy height for the forest.

**Figure 15.** Vertical profiles of the horizontal velocity and the turbulent kinetic energy at three positions on the 27 March 2015. The dots are the UAS measurements and lines of the simulation results. The colors represent the different values of LAI and height for the forest.

### 6. Summary and Conclusions

This study aimed to assess whether or not our model can reproduce relevant features of the flow. The results show the potential of the proposed model based on the Boussinesq approximation and
considering the Coriolis effect. The implementation of a limited version of the $k - \varepsilon$ model has been successfully applied to predict the Leipzig experiment profiles. The limited $k - \varepsilon$ model consists of reducing $C_\mu$ to 0.0256 and to make the production of $\varepsilon$ as a function of height. The Coriolis force introduces a velocity component $v$ perpendicular to the direction of the geostrophic wind and causes a turning in the wind. The limiting effect successfully reproduces the Leipzig profile by generating a surface wind turned value close to the experimental one, while the standard $k-\varepsilon$ model obtains about half the limited value.

In the second step, we analyzed the flow on a 2D case of the escarpment. The focus was to understand the impact of the slope of the escarpment, the forest height, and the leaf area density on the horizontal velocity, the flow inclination angle, and the turbulent kinetic energy at turbine-relevant heights. A DoE was applied to the simulation results and showed that the primary contributor is the slope of the escarpment, i.e., for the test site, the wind direction. For the wind speed, it was found that the forest height and LAI plays a minor role in comparison to the slope of the escarpment. However, for the turbulent kinetic energy, we showed that the LAI and canopy height is as important as the escarpment slope.

In the final step, the simulations were performed on the WINSENT test site. The aim of the study was to evaluate the accuracy of a modified version of $k-\varepsilon$ model in complex terrain. A validation against UAS measurements was performed. For the computation, the boundary conditions were derived from the mesoscale COSMO-DE model. Despite the low resolution of the COSMO-DE model, the one-way coupling method works well in complex terrain. The microscale model captures the varying pattern in the test site, such as the deceleration of the wind speed, the upward flow, and the increased turbulent kinetic energy in the lower levels. Generally, a good agreement was found in the lower levels (75 m and 125 m agl.) but discrepancies between the simulated results and the UAS measurements were found at upper levels. While the model shows enhanced absolute turbulent values in the lower altitudes, the measurements could not confirm the location of this maximum due to a low vertical resolution. Measurement campaigns with low flight heights, down to 20 m, are planned and will confirm or disprove the region of high turbulences. A remark on the stability should be mentioned. The assumption of an almost neutral ABL in our study was considered by checking the potential temperature profiles from UAS measurements (between 50 m and 300 m above the ground). This is also true at those levels, but only measurements near the ground could confirm the flow stratification. However, we have to recognize that it was likely a convective ABL and we should acknowledge that limitation in the paper. Additional measurement systems, such as Lidar, an eddy-covariance micro-meteorological station, and a tower equipped with an anemometer are going to be installed permanently on the test site, a few meters on the upwind and downwind side of the escarpment. This will also enable the attainment of values in lower levels and further valuable data for characterizing the flow and its stratification at the WINSENT test site.

The thermal stratification has a large impact on the vertical wind profile and turbulence levels. Therefore, different thermal stratification cases will be conducted in future studies when the complete measurement set up will be running. For a better comparison of UAS measurements and simulation results, the one-way coupling method with only one time step will be replaced by transient outputs from a mesoscale model.

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Conflicts of Interest: The authors declare no conflict of interest.
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