Nonlinear Control of a Doubly Fed Generator
Supplied by a Current Source Inverter

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Received: 5 April 2019; Accepted: 6 June 2019; Published: 12 June 2019

Abstract: Nowadays, wind turbines based on a doubly fed induction generator (DFIG) are a commonly used solution in the wind industry. The standard converter topology used in these systems is the voltage source inverter (VSI). The use of reverse-blocking insulated gate bipolar transistor (RB-IGBT) in the current source inverter topology (CSI), which is an alternative topology, opens new possibilities of control methods. This paper presents a novel power control system for a DFIG supplied by a CSI. The authors propose to use multi-scalar DFIG state variables. A nonlinear control method realized by feedback linearization was used to control the active and reactive powers of the generator. In the feedback linearization controls, the nonlinear DFIG model was taken into account. In the control system structure, classical proportional–integral controllers were used. The control variables were the output current vector components of the CSI. Such approach was named the “current control”. The proposed control method is characterized by good dynamic properties which, combined with the inverter properties in the rotor circuit, allow to increase the quality of the energy transferred to the grid by the generator. In the simulation tests, the correctness of the decoupling of the active and reactive power control loops, the dynamics of controlled power changes, and the change of the machine operating range resulting from the increase of the rotational speed of the generator shaft were controlled. The simulation studies also evaluated the impact of changes in the value of the passive elements of the system on the operation of the generator system. Characteristic operating states of the generator system were analyzed using computer simulations.

Keywords: doubly fed induction generator (DFIG); current source inverter (CSI); nonlinear control

1. Introduction

Doubly fed induction generator (DFIG) systems are widely used in wind power plants. The configuration of these systems is based on the use of a voltage source inverter. In a classic configuration of a generator system, the stator of a doubly fed generator is connected to the main grid, while the rotor is supplied by a voltage source inverter (VSI). An alternative but rarely used solution is to use a current source inverter (CSI) to supply the rotor side of the generator. Power electronics constructions with a CSI were popular in the 1980s. In this configuration, circuits with thyristors were used as power switches [1]. Because of their numerous disadvantages, such as a complicated auxiliary supply thyristor system and long switching times, these solutions have been replaced in the market by VSIs with insulated gate bipolar transistors transistors. In the last years, the dynamic development of semiconductor devices has led to the appearance on the market of IGBT transistors with serially connected diodes, which were called reverse-blocking transistors (RB-IGBT) [2,3]. These new semiconductor switches have opened new possibilities for the design and construction of power electronics circuits, CSIs in particular. This fact motivated the authors to look for solutions in the field of DFIG control with CSIs. Another reason for investigating this field is the lack of papers describing...
such solutions in the literature. The literature on the issues of a DFIG powered by a CSI is scarce [4–7]. The fundamental properties of a DFIG supplied by a CSI with regard to operating ranges and power flow were presented in some studies [4,5]. In [4], the author showed a theoretical analysis of the properties of a DFIG system supplied by a controlled current source in the rotor circuit. These results were confirmed in another study [5], in which the cyclo-converter in the rotor power supply system was replaced by a CSI. In both cases, good dynamic properties of this types of system were shown. The authors of [6] proposed the use of a control structure without a rotor speed sensor in the system with the CSI. The proposed solution highlighted some difficulties in using the sensorless control algorithm due to the use of thyristors as switching elements. The possibility to use the multi-scalar nonlinear control of a DFIG was first presented in [7]. However, the described solution used hysteresis current control of the voltage inverter, whose basic disadvantage is the variable frequency of switching power devices.

Most of the available publications concern drive systems with a cage motor supplied by a CSI [8–12]. All authors confirm the high dynamics of the presented CSI systems, emphasizing, however, the hardware difficulties associated with the use of thyristor switches [8,9] and high harmonic content in the output current due to the low-frequency switching of the thyristor [10,11]. A very interesting comparison of the two current inverter structures in the thyristor front-end rectifier and pulse width modulation (PWM) front-end rectifier configuration is shown in [12]. Another area where the application of CSI can be found is permanent magnet synchronous generator control [13,14]. In [13], the authors showed a novel power control system with a CSI inverter based on the field-oriented control (FOC) method. A similar structure of the system is shown in [14]. In both articles, the authors draw attention to the benefits of eliminating the capacitors in the DC link circuit and the general improvement of the reliability of the entire system, with a reduction of losses in the inverter and the high quality of the power transmitted to the network.

Regardless of how the rotor of the DFIG is supplied, the active and reactive powers transferred to the grid can be controlled by various methods. The classic approach to active and reactive power control of a DFIG is the FOC [15,16], which can be applied with some variations. Another approach is the direct power control (DPC) [17,18] based on the direct torque control (DTC) method from induction motor control systems. In [19], a different kind of power control systems based on a nonlinear control method was shown. This paper proposes a novel power control system for DFIGs where the rotor is supplied by a CSI. For control system synthesis, a less popular variation of the input–output nonlinear control method based on multi-scalar Z-type variables was used. The performance and utility of the proposed solution were verified in several simulations.

2. Doubly Fed Generator System

A typical VSI supply system with a DFIG is shown in Figure 1a. In this configuration, the rotor of the generator is supplied by voltage rectangular pulses generated by the inverter according to a PWM algorithm. The shapes of the rotor current depend on the adopted PWM method and the parameters of the circuit. The choice and correct application of the PWM method does not guarantee the attainment of rotor currents without any distortions. The cable connection between the buck-to-buck converter and the generator must be shielded to limit electromagnetic interference. The length of the cable is also limited by wave effects.

The supply of the generator rotor by a CSI reduces or completely eliminates the described problems. A standard topology of current source converter (CSC) supply of a DFIG with PWM front-end rectifiers is shown in Figure 1b. The principle of operation of this solution is to maintain a constant direct current value in the DC link circuit of the converter using the grid side of the converter. The rotor side of the converter functions as an electronic commutator to generate a current impulse in accordance with the PWM current algorithm. For a correct operation of the system, a capacitor bank connected to the rotor circuit is used as a filter. The generator system with a CSC consists of a few basic components or
devices: two power stages of the CSI with RB-IGBT or different kinds of power electronic switches, two passive filters with capacitors, and a DC link circuit with main inductance \( L_d \).

DFIG systems with a CSI are characterized by a few positive features in relation to the systems with a VSI. The cable length between the converter and the generator does not have a large effect on the operation of the whole supply system. The occurrence of a short circuit on the generator rotor is not dangerous because it is a natural operating state of the inverter. In the design of the CSI, it is not necessary to use low-inductance connections between converter switches modules to limit overvoltage on the transistors during fast switching. These properties simplify the design of the converter considerably. The main drawbacks of CSI systems include the sensitivity to a sudden current interruption in the load circuit, resulting in the induction of a high voltage and system damage. The inductor in the DC link circuit, which is an energy storage element, especially in high-power systems, is expensive, and its dimensions can be considerable.

3. Generator Model

3.1. Vector Model of the Machine

The dynamics of the DFIG in a vector form set of equations are represented in any reference frame rotating at \( \omega_a \) as [19]:

\[
\frac{d\Psi_{sx}}{d\tau} = -\frac{R_S}{L_S}\Psi_{sx} + R_S \frac{L_m}{L_S} i_{sx} + \omega_a \Psi_{sy} + u_{sx} \\
\frac{d\Psi_{sy}}{d\tau} = -\frac{R_S}{L_S}\Psi_{sy} + R_S \frac{L_m}{L_S} i_{sy} - \omega_a \Psi_{sx} + u_{sy}
\]
\[ \frac{di_x}{dt} = -\frac{L_2 R_r + L_m R_s}{L_S w_o} i_x + \frac{R_S L_m}{L_S w_o} \Psi_{sx} + (\omega_d - \omega_r) i_y - \frac{L_m}{w_o} \omega_r \Psi_{sy} + \frac{L_s}{w_o} u_{ry} - \frac{L_m}{w_o} u_{sx} \]  
\[ \frac{di_y}{dt} = -\frac{L_2 R_r + L_m R_s}{L_S w_o} i_y + \frac{R_S L_m}{L_S w_o} \Psi_{sy} + (\omega_d - \omega_r) i_x - \frac{L_m}{w_o} \omega_r \Psi_{sx} + \frac{L_s}{w_o} u_{rx} - \frac{L_m}{w_o} u_{sy} \]  
\[ \frac{d \omega_r}{dt} = \frac{L_m}{J_L} (\Psi_{sx} i_y - \Psi_{sy} i_x) - \frac{1}{J} T_{dr} \]  

where \( R_s \) and \( R_r \) are the resistances of stator and rotor windings, \( L_s, L_r \) are the inductances of stator and rotor windings, \( L_m \) is a mutual inductance between the generator windings. The symbols \( J \) and \( T_{dr} \) indicate the moment of inertia and the drive torque of the machine, respectively.

### 3.2. Multiscalar Z-Type Model of the Machine

The dynamics of the DFIG can be written in a different mathematical form. It is necessary to adopt new nonlinear variables to derive the system of equations. The nonlinear variables, named Z-type multi-scalar, are defined differently as follow [19]:

\[ z_{11} = \omega_r \]  
\[ z_{12} = \Psi_{sx} i_y - \Psi_{sy} i_x \]  
\[ z_{21} = \frac{\Psi_S}{\omega} \]  
\[ z_{22} = \Psi_{sx} i_x + \Psi_{sy} i_y \]

Determining the derivatives of such adopted variables, taking into account Equations (1)–(5) of the mathematical model, leads to a new system of equations:

\[ \frac{dz_{11}}{dt} = \frac{L_m}{J_L} z_{12} - \frac{1}{J} m_0 \]  
\[ \frac{dz_{12}}{dt} = -\frac{1}{T_v} z_{12} + z_{11} z_{22} + \frac{L_m}{\omega_o} z_{11} z_{21} + \frac{L_s}{\omega_o} u_{r2} - \frac{L_m}{\omega_o} u_{sf1} + u_{s11} \]  
\[ \frac{dz_{21}}{dt} = -2 \frac{R_S}{L_S} z_{21} + 2 \frac{R_S L_m}{L_S} z_{22} + 2 u_{sf2} \]  
\[ \frac{dz_{22}}{dt} = -\frac{1}{T_v} z_{22} + \frac{R_S L_m}{L_S w_o} z_{21} + \frac{R_S L_m}{L_S} z_{12}^2 + \frac{z_{22}^2}{z_{21}} - z_{11} z_{12} + \frac{L_s}{\omega_o} u_{r2} - \frac{L_m}{\omega_o} u_{sf2} + u_{s22} \]

where

\[ u_{r1} = u_{ry} \Psi_{sx} - u_{rx} \Psi_{sy} u_{r2} = u_{rx} \Psi_{sx} + u_{ry} \Psi_{sy} \]  
\[ u_{s11} = u_{sy} i_x - u_{sx} i_y u_{s22} = u_{sx} i_x + u_{sy} i_y \]  
\[ u_{sf1} = u_{sy} \Psi_{sx} - u_{sx} \Psi_{sy} u_{sf2} = u_{sx} \Psi_{sx} + u_{sy} \Psi_{sy} \]

Such a transformation of the system in Equations (10)–(13) leads to a reduction in the order of the DFIG model. By writing the model equations in this form, the Z-type multi-scalar variables are independent from the selected coordinate system and only depend on the length of selected vectors and the angle between them.

The application of the feedback in the form

\[ u_{s11} = m_1 - z_{11} z_{22} - \frac{L_m}{w_o} z_{11} z_{21} - \frac{L_m}{L_S w_o} z_{21} + \frac{L_s}{w_o} u_{r1} + \frac{L_m}{w_o} u_{sf1} \]  
\[ u_{s22} = m_2 - \frac{R_S L_m}{L_S w_o} z_{21} - \frac{L_S}{L_S} z_{12}^2 + \frac{z_{22}^2}{z_{21}} + z_{11} z_{12} - \frac{L_s}{w_o} u_{r2} + \frac{L_m}{w_o} u_{sf2} \]
results in two decoupled second-order linear systems. Two subsystems can be distinguished in this system. The first mechanical subsystem is

\[
\frac{dz_{11}}{dt} = \frac{L_m}{J_L} z_{12} - \frac{1}{J} T_{dr}
\]

(19)

\[
\frac{dz_{12}}{dt} = \frac{1}{T_v} (-z_{12} + m_1),
\]

(20)

and the second electromagnetic subsystem is

\[
\frac{dz_{21}}{dt} = -2 \frac{R_s}{L_s} z_{21} + 2 \frac{R_s L_m}{L_s} z_{22} + 2 u_s f_2
\]

(21)

\[
\frac{dz_{22}}{dt} = \frac{1}{T_v} (-z_{22} + m_2)
\]

(22)

where \(T_v\) is a combination of generator parameters and defines the electromagnetic time constant of a machine, and \(m_1\) and \(m_2\) are the new control signals.

It is possible to create a different form of the mathematical generator model by selecting another variant pair of vectors from a set of machine state variables, for example by combining pairs, such as \((\Psi_r, i_s)\) or \((\Psi_m, i_r)\), etc. The difficulty in each case, if it exists, is to find decoupling equations of the model and mathematical formulas for active and reactive powers expressed with the use of nonlinear variables.

4. Active and Reactive Power Control System

The power control system of a DFIG should provide decoupled control of active and reactive powers. Active \(s_p\) and reactive \(s_q\) powers using Z-type multi-scalar variables (6)–(9) can be expressed in a per-unit (p.u.) system in the form:

\[
s_p = \frac{1}{L_s} u_s f_2 - \frac{L_m}{L_s} \frac{u_s f_1 z_{12}}{z_{21}} + \frac{u_s f_2 z_{22}}{z_{21}}
\]

(23)

\[
s_q = \frac{1}{L_s} u_s f_1 - \frac{L_m}{L_s} \frac{u_s f_1 z_{22}}{z_{21}} - \frac{u_s f_2 z_{12}}{z_{21}}
\]

(24)

It should be noted that Equations (23) and (24) may be simplified due to the fact that in steady-state, the auxiliary variables \(u_s f_1\) and \(u_s f_2\) are approximately equal to 1 and 0 in p.u. In the simplified version of the equations, they take the form:

\[
s_p = \frac{L_m}{L_s} z_{12}
\]

(25)

\[
s_q = \frac{1}{L_s} \frac{L_m}{L_s} z_{22}
\]

(26)

The components of the rotor current in a stationary reference frame can be calculated from the values of the \(u_{s1}\) and \(u_{s2}\) variables by the expression:

\[
i_{rαS} = \frac{u_{s1} u_{sβS} + u_{s2} u_{sαS}}{u_s^2} i_{rβS} = \frac{u_{s2} u_{sβS} - u_{s1} u_{sαS}}{u_s^2}
\]

(27)

In this way, the determined components of the rotor current after transformation (Equation (32)) to a stationary rotor reference frame, using the rotor position angle \(φ_r\), are the reference values for the PWM algorithm.

Figure 2 presents a schematic diagram of the nonlinear control strategy. The control system has four proportional–integral controllers (PI) controllers in two independent power control loops. The inner control loops are responsible for the control of the multi-scalar variables \(z_{12}\) and \(z_{22}\). The outer
loops allow for active and reactive power control and set the reference values for the inner PI controllers. The gains of all PI controllers are shown in Table A2 in Appendix A. This cascade control system approach is used most commonly.

The model of the analyzed supply system with a CSI is shown in Figure 3.

This section presents the model description and simulation results in order to illustrate the behavior of the proposed active and reactive power control system of a DFIG supplied by a CSI. The model of the analyzed supply system with a CSI is shown in Figure 3.

The system model is divided into a few parts. The grid side inverter operation was not directly included in the simulation program. This part of the simulation system was replaced by an adjustable voltage source. One of the control strategies of the DFIG supplied by a CSI was based on a forced constant value of the current in the DC link. The current source inverter worked in various modulation indexes (defined as the ratio of the rotor current module to the value of the DC-link current). The reference current $I_{ref}$ was then treated as the input of the PI controller and compared to the measured value of...
the DC-link current. The voltage obtained from the PI controlled output is marked as $e_d$, and its value not only is constant but also depends on the DFIG working points. The dynamics of the current $i_d$ in a direct current link circuit is expressed as:

$$\frac{di_d}{dt} = -\frac{R_d}{L_d} i_d + \frac{1}{L_d} (e_d - u_d)$$

(28)

The value of direct voltage $u_d$ is

$$u_d = \frac{i_{ref} R_u + i_{f} R_u R_f}{L_d}$$

(29)

For a correct operation of the system, an output filter connected directly to the current inverter terminals is required. The voltage on the output filter $C_m$ changes the value according to:

$$\frac{du_c}{dt} = \frac{1}{C_m} (i_f - i_r)$$

(30)

Taking into account the dynamics of voltage $u_c$ changes on the passive filter, the rotor voltage at the terminals of the generator rotor is defined as

$$u_r = R_c (i_f - i_r) + u_c$$

(31)

where all vector quantities are in bold.

It was assumed that the power stage of the rotor side CSI was an ideal lossless energy conversion system. The main purpose of the rotor side CSI was to form a sinusoidal output rotor current. In the simulation program, the space vector pulse width modulation (SV-PWM) method described in [20] was used. In this method, six active vectors and three passive vectors are used. A typical sequence of space vectors is passive–active–active. The passive vector denotes a state where two transistors are switched on in the same branch of power stage in a current inverter. It is a natural operating state of the current inverter and it is not dangerous for the converter. The transition between consecutive sequences of space vectors must take place during an uninterrupted flow of DC current, therefore it is necessary to keep the overlap time short. If this does not occur, the lack of a continuous current leads to high-voltage spikes on the DC-side inductor, which may damage the transistors. In the simulation, an overlap time value equal to zero was assumed. A detailed analysis of the influence of the overlap time effect on the operation of the SV-PWM current source inverter has been presented [21].

The sequence of SV-PWM has a large influence on common-mode voltage reduction and may cause bearing currents, especially in high-power machines, as described in [22]. Another interesting aspect of the construction of CSI, shown in [23], is the use of silicon carbide transistors, which allow to increase the frequency of the PWM modulator to tens of kHz and reduce the size of passive elements in the inverter.

In order to analyze the operation of the proposed power control system simulation, studies were performed. The simulation tests included checking the correctness of the decoupling of the active and reactive power control loops, the dynamics of controlled power changes, and the change of the machine operating range resulting from the increase of the rotational speed of the generator shaft.

The simulation studies also evaluated the impact of changes in the value of the passive elements $L_d$ and $C_m$ of the system on the operation of the generator system.

All simulation results were obtained using a simulation program written in C++ programming language by the research team. Open and free software was used to write the simulation program. The classical Runge–Kutta method with 1 $\mu$s integration step was used to integrate the differential equations of the generator system. The simulation program contained the DFIG model according to Equations (1)–(5), the functional CSI model with the output filter (28)–(31), and all structures of a control system. The discrete nature of the control system and of the power converter was taken into account. A control system impulse period of 150 $\mu$s was assumed. In the simulation, according to the
real machine, the parameters of a 2 kW wound-rotor induction machine were considered. All values obtained on the basis of the simulation studies were expressed in per units.

The parameters of the simulation model and the reference units are shown in Table A1 (Appendix A).

The position and rotor speed of the generator were known.

The following description method of vector reference frame was adopted on all presented simulation results. The model vector components in a stationary rotor reference frame have indexes αR and βR, while the vector components in stationary stator reference frame have indexes αS and βS.

The following scenarios were investigated in the simulations:

1. Changes of the CSI parameters influencing the stator and rotor current and voltages—Figures 4 and 5;
2. Changes of the reference active and reactive powers—Figure 6;
3. DFIG system behavior during changes of the rotor speed from under-synchronous to over-synchronous speed with constant reference active and reactive powers—Figure 7.
4. DFIG system behavior during changes of the active and reactive powers with constant driven torque—Figure 8.

In the above investigations, all the changes of the reference reactive and active powers were limited to the nominal value of stator and rotor current. Typical tests are performed with a DFIG connected to the grid while controlling the active and reactive powers by an inverter on the rotor side.

Figure 4 shows characteristic transient waveforms for the simulation model in steady state for different values of the main choke inductance, i.e., \( u_{αR}, u_{βR}, \) rotor voltage vector components, \( i_{αR}, i_{βR}, \) rotor current vector components, \( i_{αS}, i_{βS}, \) stator current vector components, \( I_d, \) current in the DC link circuit, \( e_d, \) controlled voltage source. Changing the main inductance value from 0.05 p.u. to 0.02 p.u. resulted in the appearance of high-frequency oscillations in direct current in the DC link circuit. It caused the deterioration of the working conditions of the PWM algorithm and worsened the operating conditions of the entire power supply system.

![Figure 4. Simulation results: steady-state transients for different values of the main choke inductance: (left) \( L_d = 0.05, C_m = 0.35; \) (right) \( L_d = 0.02, C_m = 0.35. \) (a) Rotor voltage vector components; (b) rotor current vector components; (c) stator current vector components; (d) current in the DC link circuit; (e) voltage in the DC link circuit.](image-url)
In summary, the correct selection of the inductance value of the inductor in the circuit and of the capacitance value of the filtering condenser ensures the correct operation of the system. The current output vector component, $i_{\alpha R}$, rotor current vector component, $i_{\alpha S}$, stator current vector component, $u_d$, voltage in the DC link circuit, $u_{\alpha R}$, rotor voltage vector component. For the sake of clarity, only the component $\alpha$ of the vectors is shown in Figure 5.

The incorrect selection of the capacitance (0.1 p.u.) caused distortions of high harmonics in the rotor and stator currents waveforms. The rotor current was very smooth without any additional high harmonics when the capacitance assumed the proper value of 0.35 p.u.

For the purpose of the simulation studies, the harmonic content (THDi) was assumed in the output current at the level of 1%, and for this value, the parameters of the passive elements ($R_c$, $C_m$, $L_d$) were selected.

The inductance value of the DC choke $L_d$ can be calculated from Equation (32):

$$L_d = \frac{1}{\Delta i_d} \int_{t_1}^{t_2} (e_d - u_d)dt$$

(32)

where $\Delta i_d$ is the allowed current oscillation in the DC-link circuit, and $t_1$, $t_2$ are times resulting from the switching frequency of PWM.

In summary, the correct selection of the inductance value of the inductor in the circuit and of the capacitance value of the filtering condenser ensures the correct operation of the system. The current and the voltage supplying the generator rotor circuit did not contain higher harmonics. This translated into a higher quality of energy transferred to the system.

Figure 5 shows two causes of characteristic transient waveforms for the simulation model in a steady state for different values of $C_m$ passive output filter capacitance, i.e., $i_{\alpha R}$, current inverter output vector component, $i_{c \alpha R}$, current filter vector component, $i_{\alpha \alpha R}$, rotor current vector component, $i_{\alpha S}$, stator current vector component, $u_d$, voltage in the DC link circuit, $u_{\alpha R}$, rotor voltage vector component. For the sake of clarity, only the component $\alpha$ of the vectors is shown in Figure 5.

Figure 6 presents the reaction of the power control system for two reference power changes. In Figure 6, after 100 ms, the reference active power changed from −0.2 to −0.5 p.u. and next, after 600 ms, the reactive power changed from −0.4 to −0.1 p.u. (lagging). While changing the reactive power, the rotor current increased as a result of a build-up of the magnetising current component at the rotor side of the generator. Thus, the stator current decreased. The stator active and reactive power oscillations were smaller than 2% of the reference values and resulted from the natural character of the oscillations were smaller than 2% of the reference values and resulted from the natural character of the rotor side of the generator. Thus, the stator current decreased. The stator active and reactive power

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generator. The decoupling of the active and reactive power control loops was proper. In this scenario, the reference active and reactive powers were changed so to obtain the real DFIG working conditions.

Figure 6. Simulation results of active $s_{p}$ (red) and reactive $s_{q}$ (black) power step responses in the nonlinear control system. (a) Rotor current vector components; (b) stator current vector components; (c) rotor speed; (d) active and reactive powers; (e) stator flux vector module; (f) multi-scalar variable; (g) multi-scalar variable.
Next, the behaviour of the DFIG system was tested while changing the rotor speed from under to over-synchronous. Figure 7 presents the following waveforms: \(i_{r\alpha R}, i_{r\beta R}\), rotor current vector components and \(i_{s\alpha S}, i_{s\beta S}\), stator current vector components, after the \(\omega_r\) rotor speed has increased from 0.7 p.u. to 1.3 p.u. as a consequence of an increased mean value of the drive torque \(T_{\text{drive}}\).

The regulated values of active \(s_p\) and reactive \(s_q\) powers were maintained at the set values of \(s_p = -0.35\) and \(s_q = -0.4\) (lagging) in the entire range of the rotational speeds tested, despite the oscillating nature of the driving torque. The waveforms presented in Figure 7 confirmed that the control system structure with the proposed multi-scalar transformation and feedback control law, which is based on the DFIG model, was stable.

Figure 8 presents the reaction of the power control system for three changes of the reference active power and one change of the reference reactive power. It was assumed that the drive torque on the generator shaft was constant. This case corresponds to a constant wind speed, which occurs within...
the assumed 5 s time interval. In Figure 8, after 1 s, the reference active power changed from \(-0.2\) to \(-0.5\) p.u. after every 1 s, then after 4 s, the reactive power changed from \(-0.4\) to 0. The power coefficient at the generator output changed in this case from 0.41 to 1. The reactive power necessary to magnetize the generator was generated on the rotor side, therefore, the value of the rotor currents in 5 s was increased. Also, in the shown case, decoupling between active and reactive power control loops occurred, as shown in Figure 8. The power control algorithm worked correctly.

![DFIG system behavior during changes of the active and reactive powers with constant driven torque.](image)

**Figure 8.** DFIG system behavior during changes of the active and reactive powers with constant driven torque. (a) Rotor current vector components; (b) stator current vector components; (c) rotor speed; (d) active and reactive powers; (e) power factor.

6. Conclusions

This study proposes a novel power control system for a DFIG where the rotor is supplied by a CSI. For control system synthesis, a not widely known variation of the input–output nonlinear control method based on multi-scalar Z-type variables was used. The performance and utility of the proposed solution were verified by simulations. All simulation tests confirmed the correctness of the proposed power control system concept. The presented system is characterized by high dynamics of operation.
with independent ability to control the active and reactive powers of the generator. The advantage of the presented solution is represented by the sinusoidal currents in the rotor circuit which translate into high power quality with a reduced harmonics content in the stator currents. The control structure presented in this paper with a multi-scalar transformation confirmed that the DFIG system is stable in the three proposed scenarios. In the case of the CSI structure, it is important to determine the filter capacitor and in the DC-link inductor values. These values influence the control system stability, as shown in the first scenario. The theoretical analysis presented in this paper allows to use the proposed control system structure for practical verifications. This will be presented in future works.

Author Contributions: Conceptualization, K.B.; software, K.B.; validation, K.B.; investigation, K.B.; writing—original draft preparation, K.B.; writing—review and editing, K.B., M.M.; visualization, K.B.; All authors carried out the theoretical analysis and contributed to writing the paper.

Funding: This research received no external funding.

Conflicts of Interest: The authors declare no conflict of interest.

Nomenclature

- \(R_s, R_r\) stator and rotor resistances;
- \(L_s, L_r\) stator and rotor inductances;
- \(L_m\) mutual inductance;
- \(J\) moment of rotor inertia;
- \(T_{dr}\) drive torque;
- \(\omega_r, z_{11}\) pulsation of reference frame;
- \(\omega_a\) mechanical speed;
- \(s_p, s_q\) stator active and reactive powers;
- \(z_{12}, z_{22}, z_{21}\) Z-type multi-scalar variables;
- \(u_{r1}, u_{r2}, u_{si1}, u_{si2}\) Z-type auxiliary multi-scalar variables;
- \(m_1, m_2\) control variables;
- \(i_d\) DC-link current;
- \(e_d, u_d\) DC-link voltages;
- \(R_d, L_{d}\) Resistance and inductance of DC-link choke;
- \(C_m\) output filter capacitance.

Appendix A

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Quantity</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>(R_s)</td>
<td>stator resistance</td>
<td>2.833 (\Omega/0.067) p.u.</td>
</tr>
<tr>
<td>(R_r)</td>
<td>rotor resistance</td>
<td>2.867 (\Omega/0.068) p.u.</td>
</tr>
<tr>
<td>(L_m)</td>
<td>magnetizing inductance</td>
<td>0.15 (H/1.123) p.u.</td>
</tr>
<tr>
<td>(L_s, L_r)</td>
<td>stator and rotor inductance</td>
<td>0.164 (H/1.1227) p.u.</td>
</tr>
<tr>
<td>(L_{cr})</td>
<td>leakage inductance</td>
<td>0.014 (H/)</td>
</tr>
<tr>
<td>(P_n)</td>
<td>nominal power</td>
<td>2 kW</td>
</tr>
<tr>
<td>(I_{ns})</td>
<td>nominal stator current</td>
<td>5.5 A</td>
</tr>
<tr>
<td>(I_{nr})</td>
<td>nominal rotor current</td>
<td>3.4 A</td>
</tr>
<tr>
<td>(U_n)</td>
<td>nominal stator voltage</td>
<td>400 V</td>
</tr>
<tr>
<td>(n)</td>
<td>nominal rotor speed</td>
<td>910 rpm</td>
</tr>
<tr>
<td>(f)</td>
<td>nominal frequency</td>
<td>50 Hz</td>
</tr>
<tr>
<td>(r)</td>
<td>turn ratio (N_s/N_r)</td>
<td>1</td>
</tr>
<tr>
<td>(L_d)</td>
<td>choke inductance</td>
<td>6.2 (mH/0.05) p.u.</td>
</tr>
<tr>
<td>(C_m)</td>
<td>filter capacitance</td>
<td>280 (uF/0.35) p.u.</td>
</tr>
<tr>
<td>(U_b = U_n)</td>
<td>reference voltage</td>
<td>400 V</td>
</tr>
<tr>
<td>(I_b = \sqrt{3}I_{ns})</td>
<td>reference current</td>
<td>9.52 A</td>
</tr>
<tr>
<td>(S_b)</td>
<td>reference power</td>
<td>3810 VA</td>
</tr>
</tbody>
</table>
Table A2. Parameters of PI regulators in reference units.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Quantity</th>
<th>Values</th>
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</thead>
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<tr>
<td>kpP</td>
<td>proportional gain for active power controller</td>
<td>1.5</td>
</tr>
<tr>
<td>kiP</td>
<td>integral gain for active power controller</td>
<td>0.15</td>
</tr>
<tr>
<td>kpQ</td>
<td>proportional gain for reactive power controller</td>
<td>1.5</td>
</tr>
<tr>
<td>kiQ</td>
<td>integral gain for reactive power controller</td>
<td>0.15</td>
</tr>
<tr>
<td>kp12</td>
<td>proportional gain for z12 variable controller</td>
<td>2.5</td>
</tr>
<tr>
<td>ki12</td>
<td>integral gain for z12 variable controller</td>
<td>0.5</td>
</tr>
<tr>
<td>kp22</td>
<td>proportional gain for z22 variable controller</td>
<td>2.5</td>
</tr>
<tr>
<td>ki22</td>
<td>integral gain for z22 variable controller</td>
<td>0.5</td>
</tr>
</tbody>
</table>

The transformation from the stator reference frame to the rotor reference frame is defined as follows:

\[
\begin{bmatrix}
    i_{\alpha R} \\
    i_{\beta R}
\end{bmatrix} =
\begin{bmatrix}
    \cos(\varphi_r) & \sin(\varphi_r)
    \\
    -\sin(\varphi_r) & \cos(\varphi_r)
\end{bmatrix}
\begin{bmatrix}
    i_{\alpha S} \\
    i_{\beta S}
\end{bmatrix}
\]

(A1)

References


17. Pura, P.; Iwanski, G. Direct Torque Control of a Doubly-Fed Induction Generator Connected to Unbalanced Grid. Prz. Elektrotech. 2016, 1, 42–46. [CrossRef]