Proton Radiography by Multiple Coulomb Scattering with Nuclear Emulsion Detectors

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Abstract: The possibility of performing proton radiography by using the proton angular spread due to Coulomb multiple scattering was investigated, for the first time, with an emulsion film detector. Two different phantoms were irradiated with the therapeutic proton beam at the Paul Scherrer Institut (PSI) in Villigen, Switzerland. The first one is a simple polymethylmethacrylate (PMMA) block having two different thicknesses (4 cm and 3 cm), and the second one is a PMMA cube with five aluminum rods embedded along a diagonal. Only one emulsion film was needed to perform the radiography, an important issue as the analysis of this kind of detector is time-consuming. Furthermore, the method showed an enhanced contrast when high atomic-number materials are traversed. This gives an advantage, when compared to proton range radiography.

Keywords: proton radiography; nuclear emulsion; instrumentation for hadron therapy

1. Introduction

Proton radiography is an imaging technique undergoing a growing development, following the widespread use of proton-therapy for cancer treatment. This modality would definitely improve with a clinical use of proton radiography, which provides direct information on the density of the tissues, enhancing the precision of treatment planning. In this framework, different proton radiography systems have been tested [1–3]. Our group investigated the possibility of using emulsion detectors [4] to image different phantoms of the proton therapeutic beam at the Paul Scherrer Institut (PSI) in Villigen, Switzerland. The proton radiography was successfully performed with an Emulsion Cloud Chamber (ECC), a sandwich of emulsion films interleaved with tissue-equivalent plates, that allowed for the assessment of the proton residual range [5]. The same experimental setup also allowed us to evaluate the dose distribution in the halo region of the proton clinical pencil beam [6]. In the present study, we exploit an alternative method to perform the radiography, based on the evaluation of Coulomb multiple scattering of protons while traversing different materials. This approach requires a detector with a high angular resolution, for which emulsion films represent the optimal solution. In fact, one double-layer nuclear emulsion film allows for high precision tracking of charged particles, and the angular distribution can be reconstructed with a resolution of 1 mrad [5]. With this methodology, only a single emulsion film is needed for the proton multiple scattering evaluation, with the clear advantage of a faster data scanning and analysis procedure. Furthermore, the method also features, with respect to the proton range radiography, an increased contrast when different atomic number materials are...
investigated. In this paper, we report on the first results of proton radiography by means of multiple Coulomb scattering with nuclear emulsions. On this basis, the contrast is compared for proton range radiography and proton scattering radiography, with the same phantoms and irradiation conditions.

2. Materials and Methods

For the detector description and irradiation of the phantom, we refer to [5]. Briefly, we imaged the two objects, shown in Figure 1: Phantom 1, a step of polymethylmethacrylate (PMMA) with density 1.20 g·cm⁻³, featuring the two thicknesses of 3 cm and 4 cm; Phantom 2 was a 4.5 cm thick PMMA block containing five rods of aluminum (5 × 5 mm² section) equally spaced along a diagonal.

![Phantom 1 (left) and Phantom 2 (right) used for proton radiography from [5].](image)

The radiography was performed using the Gantry 1 of the PSI, delivering a therapeutic proton beam with kinetic energy of 138 MeV [5,6]. The geometry of the irradiation is shown in Figure 2. In order avoid track overlapping in the emulsion, the particle flux was limited to about 100 protons/mm².

![Scheme of the irradiation of the step (left) and rod (right) phantoms.](image)

The emulsion film used for this work consists of two layers of 44 µm thick sensitive gel, coated on both sides of a 205 µm thick triacetate base (See Figure 3). Ionising particles produce tracks in the two sensitive layers that, once developed through a chemical process, result in a column of silver grains (micro-tracks), visible under an optical microscope. After irradiation and development, the emulsions were scanned at the Laboratory for High Energy Physics (LHEP) in Bern, using an automatic microscope [7] optimised for the reconstruction of highly ionising particles. The signals of protons were clearly visible over a negligible background, thus allowing an efficient track reconstruction.
Figure 3. Schematic view of an emulsion film with two micro-tracks: In yellow, the triacetate base and, in grey, the two sensitive emulsion layers.

The assessment of the scattering angle can provide useful information on the object to be imaged. The root-mean-square scattering angle projected onto any plane is given by [8]:

\[ \theta = \frac{13.6}{\beta c p} z \sqrt{\frac{x}{X_0}} \left( 1 + 0.038 \ln \left( \frac{x}{X_0} \right) \right), \]  

(1)

with \( z = 1 \) for protons, and where \( c \) is the light velocity, \( \beta \) is the ratio between the particle velocity and \( c \), \( p \) is the particle momentum in MeV/c, \( x \) is the thickness of the traversed material, and \( X_0 \) is the radiation length of the considered material, which can be expressed by means of the approximated formula [8]:

\[ X_0 \approx \frac{716.4 A}{Z(Z+1) \ln \left( \frac{287}{\sqrt{Z}} \right)}, \]  

(2)

where \( Z \) and \( A \) are the atomic number and weight, respectively. Differences due to the type of traversed materials translate into a difference in the root mean square (RMS) of the scattering angles. If \( x \) and \( y \) are the two planar dimensions on the emulsion film, the angles, with respect to the normal direction of the incident beam (\( z \)), can be given as \( \tan \theta_x \) and \( \tan \theta_y \):

\[ \tan \theta_x = \frac{x - x_0}{d}, \]  

(3)

\[ \tan \theta_y = \frac{y - y_0}{d}, \]  

(4)

where \( d \) is the distance between the two layers, and \((x_0, y_0)\) and \((x, y)\) are the proton coordinate in the first and second emulsion layer, respectively. The scattering angle RMS can be assessed from \( \tan \theta_x \) and \( \tan \theta_y \).

Protons crossing the phantoms were simulated by means of the software package SRIM [9], providing the directional cosines of the trajectory of the transmitted ions, starting from a perfectly collimated beam with the initial energy of 138 MeV. The unit vector of the emerging trajectory is then given by:

\[ \vec{v} = (v_x, v_y, v_z) = (\cos \hat{x}, \cos \hat{y}, \cos \hat{z}), \]  

(5)

where \( \hat{x}, \hat{y}, \) and \( \hat{z} \) are the angles between the unit vector and the corresponding axis of the reference frame. \( \tan \theta_x \) and \( \tan \theta_y \) are related to the unit vectors, according to:

\[ \tan \theta_x = \frac{v_x}{v_z} = \frac{\cos \hat{x}}{\cos \hat{z}}, \]  

(6)

\[ \tan \theta_y = \frac{v_y}{v_z} = \frac{\cos \hat{y}}{\cos \hat{z}}, \]  

(7)
where $z$ is the direction of the beam.

3. Results

The RMS values of $\tan \theta_x$ and $\tan \theta_y$ are reported, in Figure 4, as a function of the $y$ coordinate of the phantoms. The step of Phantom 1 (top) and the rods of Phantom 2 (bottom) are clearly visible. The plots in the top row of Figure 4 show that the experimental data were concentrated around two mean scattering angle values, corresponding to the two thicknesses, 4 cm and 3 cm, of Phantom 1. In the bottom row of Figure 4, the scattering profiles of Phantom 2 clearly show the presence of aluminum rods. The scattering angle, due to the rods, was found to be dependent on the rod depth inside the PMMA block. The first peak on the left corresponds to the aluminum rod closest to the incident protons. As expected, the RMS had an increasing trend, going from the first to the fifth rod, according to the inverse relationship between the Coulomb scattering and the velocity of the particle, which was slowed down in PMMA.

![Figure 4](image.png)

Figure 4. Root mean square (RMS) of $\tan \theta_x$ and $\tan \theta_y$ for Phantom 1 (top) and Phantom 2 (bottom). Experimental data are reported in black, while the simulation results are in red. The difference in the average RMS of $\tan \theta$ in $x$ and $y$ is due to the divergence for the pristine beam.

In the same figure, the red points represent the results of the simulation, which takes into account the proton beam spread. Indeed, the RMS angle of the initial beam ($\sigma_{\text{in}}$) and the spread due to scattering inside the target of a given material ($\sigma_{\text{mat}}$) contributed to the RMS of $\tan \theta$ ($\sigma_{\text{tot}}$), such that:

$$
\sigma_{\text{tot}}^2 = \sigma_{\text{in}}^2 + \sigma_{\text{mat}}^2,
$$

(8)

where $\sigma_{\text{mat}}$ was evaluated by means of the simulations based on a perfectly collimated beam, and $\sigma_{\text{in}}$ had to be determined by using the experimental data. It should be noted that $\sigma_{\text{in}}$ was a property of the beam and equally affected all the points. $\sigma_{\text{in}}$ was then calculated by minimising the function:
\[ f(\sigma_{in}) = \sum_{i}^{N} \left( \sigma_{t}^{2}_{\text{tot}} - \sigma_{\text{mat}}^{2}_{i} - \sigma_{\text{in}}^{2} \right)^{2} \delta \sigma_{i}^{2}, \] (9)

where \( \delta \sigma \) is the experimental data uncertainty, and \( N \) the number of experimental points. The obtained \( \sigma_{in} \) values along the \( x \) and \( y \) axes were, then, added in quadrature to the simulated values.

On the basis of the angle RMS values, we can define the contrast as a parameter for the quality of the radiography. In the case of the step phantom, we can assess how well we can distinguish the boundary between the two different thicknesses. For the rod phantom, we have to assess how well we can distinguish between the aluminum rods and the PMMA block where they are inserted. We then define the contrast as:

\[ C = \left| \frac{v_{1} - v_{2}}{(v_{1} + v_{2})/2} \right|. \] (10)

In the case of Phantom 1, \( v_{1} \) and \( v_{2} \) were the RMS angle values corresponding to the two thicknesses. For Phantom 2, the contrast was calculated in correspondence with each rod \( (v_{1}) \), with respect to the PMMA block \( (v_{2}) \). In Table 1, we report the contrast values experimentally obtained and those calculated by means of the simulation for the two phantoms. For comparison, the contrast values for proton range radiography with the same phantoms were calculated on the basis of our previous work [5], and shown in Table 1.

<table>
<thead>
<tr>
<th>RMS of tan ( \theta )</th>
<th>PSR Simulation</th>
<th>PSR Data</th>
<th>PRR Simulation</th>
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</thead>
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<tr>
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<td>0.10</td>
<td>0.12</td>
<td>0.11</td>
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<tr>
<td>Rod 1</td>
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<td>0.06</td>
<td>0.03</td>
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<tr>
<td>Rod 2</td>
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<td>0.20</td>
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<tr>
<td>Rod 3</td>
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<td>0.12</td>
<td>0.06</td>
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</tr>
<tr>
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<td>0.17</td>
<td>0.06</td>
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<td>Rod 5</td>
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<td>0.20</td>
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It is clear that, for Phantom 1, the contrast for the two methods was comparable; while, for Phantom 2, the contrast obtained with the method described in the present paper was about 20%, while with the contrast with proton residual range measurements was only about 5%. Therefore, when there is a substantial difference in the atomic number, the knowledge of mean scattering angle provides complementary information that can be valuable for clinical applications.

4. Conclusions

Proton radiography by multiple Coulomb scattering was performed, for the first time, using one double-layer emulsion film detector. The clinical proton beam of the Gantry 1, in the Centre for Proton Therapy (CPT) of the Paul Scherrer Institut (PSI) in Switzerland, was used.

Two different phantoms were imaged, one featuring a 1 cm step in PMMA and one constituted of five aluminum rods embedded into a PMMA block and located at different distances from the detector. The results obtained with this technique were compared with proton range radiography images of the same phantoms. Proton Coulomb scattering radiography was found to be characterised...
by a much higher contrast for materials of different atomic number—a potential advantage for clinical applications. The two techniques led to a similar contrast, when only PMMA was considered.

Proton radiography with nuclear emulsion films has the advantage of not requiring complex electronic detectors, but has the drawback of being off-line. Furthermore, the chemical development and scanning timing represent a limiting factor for clinical applications. This is mostly the case of the proton range technique, in which a large number of emulsion films are required to assess the path of the protons. On the other hand, the proton scattering technique requires only one film, representing a much faster and simpler solution. The novel imaging methodology described in this paper could be attractive for future developments in proton therapy.

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Conflicts of Interest: The authors declare no conflict of interest.

References
6. Ariga, A.; Braccini, S.; Ereditato, A.; Giacoppo, F.; Nesteruk, K.P.; Pistillo, C.; Scampoli, P. Characterization of the dose distribution in the halo region of a clinical proton pencil beam using emulsion film detectors. JINST 2015, 10, P01007. [CrossRef]