Creative Sculpture from Patchwise Modules

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Abstract: The sculptor adapts the geometry of spline surfaces commonly used in 3D modeling programs in order to translate some of the topological nature of these virtual surfaces into his sculpture. He realizes the patchwise geometry of such surfaces by gluing square modules of neoprene rubber edge to edge to define the surface which he then torques and bends into sculptures. While limited by the nature of actual materials, the finished sculptures successfully incorporate the expressive tension and flow of forms sought by the sculptor. He presents images of finished works and provides an analysis of the emotive values of a select sculpture.

Keywords: spline surfaces; patchwise; module; sculpture

1. Introduction

The depiction of topological surfaces in the rigid materials of traditional sculpture was an early pursuit of modern abstract art [1,2] and today still remains a fixture in many examples of mathematical sculpture (Figure 1). Topological concepts have also been a trigger for advanced explorations by less mathematical sculptors.

Figure 1. Alexander Crum Brown (1838–1922), half-twist surface. Science Museum Group Collection
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During the 1970s, Post-Minimalist sculptures such as those by Eva Hesse [3] and Robert Morris [4] broke the stark reins of Minimalism in part by turning to soft industrial materials such as latex...
and felt in lieu of metal and rigid plastics. Best known were the soft sculptures of common objects by Claes Oldenberg (Figure 2) [5].

![Figure 2.](image.png)

Figure 2. Claes Oldenburg, Stedelijk Museum, Collectie/Nationaal Archief: Fotocollectie Anefo, Verhoeff, Bert, 1970.

2. Previous Work

There are many sculptors who create topologically interesting sculptures by developing their own methods. Some of us, such as Heleman Ferguson [6,7], George Hart [8–12], Nat Friedman [13–16] Charles Perry [17–19], James Mallos [20–24], Henry Segerman [25,26], Rinus Roelofs [27–32], David Reimann [33,34], and myself [35–43] share our methods by publishing papers in conferences, journals, and magazines.

However, there are also many sculptors who intuitively create new topologically interesting forms and do not publish and explain how they created these forms. Some of these artists' works have been studied by mathematicians. We can find publications on the mathematical aspects of sculptures of Bruce White [44], Robert Morris [45], Robert Longhurst [46,47], Anish Kapoor [48–50], Larry Frazer [51], Charles Ginnever, [52], Bathsheba Grossman [53–55] Tony Smith [4,56], Richard Serra [4,57], Keizo Ushio [58], Brent Collins [59–61] , Carlos Sequin [62–64] Ilhan Koman [65,66], and Eva Hild [67–71].

One of the common methods to construct complicated topological sculptures is to use modular elements. For two-manifold surfaces, the modular construction corresponds to the cellular decomposition of the original surface [72,73]. This decomposition can be used to classify these modular sculptures as physical data structures [12,74], and these physical mesh data structures can be considered instances of thickened graphs embedded on orientable two-manifold surfaces [75].

Many mathematical toys, such as Flexeez, space chips, and ITSPhUN, are also designed to construct such physical data structures [76,77]. Reimann’s sculptures from flexible rectangular modules [33] and George Hart’s modular Krigami sculptures [6] are also examples of such structures. Akleman demonstrated that any two-manifold surface can be constructed by cylindrical quadrilateral modules [76]. In this paper, I present another method for constructing sculptures from rubber sheet modules that can be considered spline patches.
3. Materials and Methods

Topology has sometimes been called “rubber sheet geometry” in contrast to the fixed constraints of Euclidean geometry. No matter how stretched and flexed is a rubber sheet, however, it hardly approaches the ideal properties of a topological sheet. Nonetheless, rubber sheets can demonstrate some of the behavior of a surface as its points and edges loosen and the surface garners greater degrees of freedom. This paper explores the application of neoprene sheeting to fabricate sculptures that display topological effects, albeit in a highly constrained mode.

To this end, the project took its cue from the methods employed by spline surface modeling programs to generate and modify three-dimensional surfaces. The sculptor selected the surface building geometry of patchwise construction featured in the program Rhino 3D (Version 5, Robert McNeel and Associates, Seattle, WA, USA). Specifically, Rhino is known as a non-uniform rational basis spline (NURBS) modeler.

Building sculptures from modules of rubber sheeting is akin to the patchwise computer modeling of 3D surfaces. The transformation of rubber sheets actually conforms more closely to the properties of spline geometry, which describes the bending of material under force, than to pure topology.

3.1. Splines and Patches

The concept behind this investigation borrows from spline geometry’s view of surfaces, which defines a patch as a surface region to varying degrees independent of the rest of the surface, but integrated by principles of continuity with neighboring regions. It uses control points, which the sculptor can drag to different positions thus pulling the surface in a new direction. In addition, the sculptor may increase or decrease the pulling of the surface toward the point by adjusting the weight assigned to each point [78]. The sculptor then controls both the pressure and response actuating a surface and how that response carries over into adjacent patches.

Each surface patch can connect with its neighbors in varying degrees of continuity such that transformations effected by the control point can spread to these neighbors. In the program Rhino, the sculptor can apply surface properties controlling how far this transformation might spread across patches. This property is specified by the degree of the polynomials defining the surface: the higher the degree, the broader the spread. Quadratic equations define a degree 2 surface, whereas cubic equations determine a degree 3 surface. Similarly, quartic and quintic equations are responsible for degree 4 and degree 5 surfaces, respectively.

The spline surface is topologically a rectangular net of \( m \) spline curves in one direction and \( n \) spline curves perpendicular to the first set (Figure 3). The \( n \times m \) intersection points between those two sets of spline curves serve as control points to define the shape of the patch. Each point affects both intersecting curves simultaneously to create two directions of curvature for the patch to follow. The two directions are labelled \( U \) and \( V \).

Spline geometry provides two properties for transforming the rectangular surface into closed surfaces. First, the surface can curve back on itself such that the opposite edges join on what is termed a seam. The surface is then rendered continuous through this seam as with a cylindrical surface. Second, the longitudinal splines terminating on the open edges of the cylinder can converge on a single point to effect a singularity where all of these splines terminate on the same point. A singularity at each end of the cylinder might transform it into an approximate sphere, as seen with the north-south lines on a world globe.
Spline geometry derives its procedural origins from drafting and its mathematical expressions from the Euler–Bernoulli formulation for the bending of beams under lateral force. Spline curves closely mimic the bending pattern of flexed materials, especially such common materials as wood, metals, plastics, and rubber. Traditionally, a spline was a flexible drafting tool for tracing non-circular curves. The tool was usually a thin, straight-grained length of wood that draftsmen in the ship building industry used to interpolate curves between points that had been previously plotted using compass and straightedge methods. Draftsmen employed heavy metal weights, termed ducks, to fix the spline in place and then adjusted—or faired—the spline to flow as smoothly as possible through the given points (Figure 4). These weights provided the lateral forces to bend the spline.

**Figure 4.** Using a spline at Boeing Company in the early 1960s just prior to the development of computer-aided design (CAD) technology. The draftsman positions his “ducks” to pass the spline smoothly through a set of given points [79].

### 3.2. Material Constraints

Most flexing materials do so with only single curvature, disallowing most topological features. However, materials, such as rubber, can also stretch to permit double curvature and consequently conform more closely to a spline surface resulting in zero Gaussian curvature.
The sculptures created under this project comprise square neoprene patches, cut by water jet at a gasket-making facility from a sheet whose thickness is 12 mm, 1/25 the width of the 30 cm squares. This proportion follows from specific requirements of the surfaces forming the sculptures. The first requirement is that the patches join one another edge to edge to create tangent continuity between the patches. The glue is a methacrylate compound (i.e., Super Glue (Super Glue Corporation, Ontario, CA, USA)) commonly employed to glue rubber. The 12 mm thickness allows sufficient glue contact between patch edges, while permitting excellent visual continuity across the seams.

The second requirement is that the surface be stiff enough to retain the form of the sculpture, albeit allowing sufficient flexibility. Again, the 1:25 proportion meets this need. However, this stiffness raises a problem of continuity across vertices. Where three or more patches joined as their edges approach a vertex point, they cannot flex sufficiently to meet at that point and a gap causes an unwanted break in the flow of the surface (Figure 5a). Removing the corners solves this problem, while changing the shape of the patch to resemble a cross (Figure 5b). In this case, the voids were 90° arcs of 10 cm radius. This adaptation of the patch opened the fortunate option of creating circular voids through the surface and into the internal spaces of the sculptures.

![Figure 5](image1.png)  
*Figure 5. (a) Patchwise “cube”. Patches cannot close at the vertices, since this requires a singularity and is only possible given a surface of little or no thickness; (b) Modified patch. The problem disappears along with the corners of the patch.*

4. Results

When compared to the virtual patchwise surfaces, the neoprene representations lacked considerable freedom to transform. The sphere in Figure 3b, for example, is possible because its patches expand at the equator and compress to a point at the poles. The neoprene can do neither. However, it can fold and torque to create physical stresses that can serve to convey a sense of stress within the viewer.

Results are presented here as a gallery of sculptures created under this project. Beginning with sculptures of only two patches, the images go on to illustrate outcomes requiring four and then six patches.

4.1. Two-Patch Surfaces

The results were surprising in how a very few patches could yield surfaces of sculptural interest. For example, only two patches when combined yielded seven sculptures as illustrated in Figure 6. This surface offers six extended edges that fold into one another in several combinations.
4.2. Four-Patch Surfaces

With four patches the sculptures engaged more substantial volumes, as in the sculpture *Chamber* depicted in Figure 7. The biomorphic effects sought by the sculptor began to appear as the sculptures suggested the shapes of organs. The title *Chamber* alludes to the terminology applied to organs that function as containers, as in the chambers of the heart.

![Figure 6](image1.png)

**Figure 6.** (a) Six untitled sculptures derived from the joining of two modules; (b) Close-up of *Goblet*, untitled sculpture from two modules.

![Figure 7](image2.png)

**Figure 7.** (a) Surface of four modules; (b) *Chamber*, four neoprene modules, 30 × 30 cm each.

4.3. Six-Patch Surfaces

The most effective products for this sculptor emerged when surfaces comprised six patches. At that number, the surface patches connected while generating multiple passages that displayed a variety of surface tensions. In addition, the voids created by the corner extractions achieved similar variability.

The pattern taken by the patches formed a cross like the one seen when a cube unfolds. Figure 8 depicts this pattern with two edge flanges joined into a seam. The unfolded cube net provides a total of fourteen edges available for joining to one another. By contrast, a rectangular two by three array of patches would yield only ten edges to be joined, with seven internal seams already formed. In addition, this arrangement allows considerably more suppleness in order to shape sculptures of more engaging complexity.
Figure 8. Six patches arrayed in a cross pattern. This served as the starting surface for sculptures shown in Figures 9–11.

Two of the sculptures formed from the pattern of modules depicted in Figure 8 were Flay (Figure 9) and Chieftain (Figure 10). The title Flay references animal skins mounted for display, while Chieftain recalled for the sculptor the oversized headpieces worn in tribal wars of Pacific Islanders.

Figure 9. Flay, neoprene rubber, 66 cm high × 45 cm wide × 21 cm deep.
5. Discussion: Vented Torso

Lucas Cowan, curator of the exhibit *Invoking the Absence*, chose Vented Torso (Figure 11a,b) for display in the rotunda of the Elks National War Memorial in Chicago. That spring of 2014, Vented Torso found, for a number of reasons, an appropriate home in the famed Beaux Arts sanctuary.

One reason was the strong classical proportions effected by the underlying grid of patches. Additionally, the circular voids generated by the corner extractions of the modules caused a parallel system of proportions to penetrate the sculpture’s surface. The base, for example, is a circle created by joining two patches by their adjacent edges. Just above the base three patches join to enclose two circular voids to flank the base on two sides. The voids expand proportionally as the torso widens through its chest. This third level of holes is formed by two rings of four patches. The last two voids open to the left and right as one arm of each patch flanges outward, suggesting the cropped arms of classic torsos. A skewed connection of two opposite patches at the top of the torso introduces a twist suggesting the classic *contrapposto* pose of ancient Greek figure sculpture.
Figure 11. (a) Vented Torso, neoprene rubber, 74 cm high × 37 cm wide × 33 cm deep; (b) Vented Torso, side view, installed at the Elks Memorial. The sculpture’s proportions are in accord with those of Beaux Arts architecture.

The play between flexibility and stiffness in the neoprene patches yields curvature and torsion, which together suggest a twisting torso. The industrial nature of the material also implies body armor—in fact, many viewers saw it as a symbol of damaged body armor. a fitting theme for the purpose of the memorial. One might conceive the sculpture as an abstraction of the torso in the same sense as armor fitted to the body: it simplifies and smooths over the contours of a soldier’s body. Other sculptures using these neoprene modules followed this same concept by appearing as pieces of armor such as helmets or breastplates.

On another level, and one of particular interest to the sculptor, Vented Torso represents a juncture of the geometric and the organic forms. Traditionally, artists have analyzed sculpture into two categories: either geometric or biomorphic with the division relatively distinct. More contemporary applications of geometry, such as patchwise computer modeling, bridge this divide. This has had a profound influence on the work of sculptors like Anish Kapoor, whose application of NURBS geometry has characterized his recent work, most notably Chicago’s famed “Cloud Gate” (Figure 12).
Figure 12. Anish Kapoor, “Cloud Gate” (with non-uniform rational basis spline (NURBS) overlay), stainless steel, 10 m × 13 m × 20 m, 2006. Photo by Nat Friedman, a possible NURBS analysis by Stephen Luecking [48]. The geometry was created by editing the globe in Figure 3b.

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References:


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