A Glucose-Dependent Pharmacokinetic/Pharmacodynamic Model of ACE Inhibition in Kidney Cells

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Abstract: Diabetic kidney disease (DKD) is a major cause of renal failure. Podocytes are terminally differentiated renal epithelial cells that are key targets of damage due to DKD. Podocytes express a glucose-stimulated local renin-angiotensin system (RAS) that produces angiotensin II (ANG II). Local RAS differs from systemic RAS, which has been studied widely. Hyperglycemia increases the production of ANG II by podocyte cells, leading to podocyte injury. Angiotensin-converting enzyme (ACE) is involved in the production of ANG II, and ACE inhibitors are drugs used to suppress elevated ANG II concentration. As systemic RAS differs from the local RAS in podocytes, ACE inhibitor drugs should act differently in local versus systemic contexts. Experimental and computational studies have considered the pharmacokinetics (PK) and pharmacodynamics (PD) of ACE inhibition of the systemic RAS. Here, a PK/PD model for ACE inhibition is developed for the local RAS in podocytes. The model takes constant or dynamic subject-specific glucose concentration input to predict the ANG II concentration and the corresponding effects of drug doses locally and systemically. The model is developed for normal and impaired renal function in combination with different glucose conditions, thus enabling the study of various pathophysiological conditions. Parameter uncertainty is also analyzed. Such a model can improve the study of the effects of drugs at the cellular level and can aid in development of therapeutic approaches to slow the progression of DKD.

Keywords: PK/PD; podocytes; renin-angiotensin system; benazepril; diabetic kidney disease; diabetic nephropathy

1. Introduction

Hyperglycemia or high blood glucose initiates and aggravates the pathophysiology that can lead to end-stage renal failure in diabetic patients. Diabetic kidney disease (DKD) is one of the common complications of hyperglycemic conditions. In the earlier stages of DKD, the nephrons, which are the basic filtration units of the kidneys, become damaged [1,2]. Blood is filtered in each of thousands of nephrons through a bundle of capillaries known as a glomerulus. Hyperglycemia-induced injury to the glomeruli eventually leads to the loss of renal function. Podocytes are visceral epithelial cells that wrap around the glomerular capillaries and play a vital role in maintaining the structure and function of the glomerular filtration barrier. Because podocytes are terminally differentiated, any damage to them is a critical factor in glomerular injury and diabetic nephropathy. Podocyte injury is a key process in the progression of DKD [3–6].
The renin-angiotensin system (RAS) is a hormone system responsible for maintaining blood pressure and fluid balance. The RAS network of biochemical reactions involves multiple enzymes and hormones and is known to function at systemic (throughout the body) as well as local (tissue or cellular) levels. Angiotensin (ANG) II is one of the hormones in the RAS and is primarily responsible for regulating blood pressure. The RAS is over-stimulated in diabetic conditions, leading to the up-regulation of ANG II in systemic as well as local levels. Angiotensin-converting enzyme (ACE) is responsible for conversion of the precursor ANG I to ANG II. ACE inhibitors are widely used pharmaceuticals for blood pressure regulation that inhibit the production of ANG II and slow the progression of DKD.

The intracellular RAS within podocytes has been shown to function differently than the systemic RAS in certain pathophysiological conditions such as hyperglycemia [7–10]. High glucose conditions trigger the RAS to increase ANG II concentration, especially in the podocytes, leading to irreversible podocyte injury [7,11,12]. The progression of DKD can be slowed by controlling the ANG II concentration to prevent irreversible podocyte loss. While ACE inhibitor drugs used to suppress ANG II are frequently prescribed for use in DKD, their effects on the local RAS in podocytes are not well understood. Also, clinical observations indicate that systemic suppression of ANG II by ACE inhibitor drugs is not always accompanied by ANG II suppression in the kidneys [13].

Mathematical models of the reaction network in the systemic RAS have been published [14–16]. We previously developed a pharmacokinetic/pharmacodynamic (PK/PD) model for an ACE inhibitor benazepril considering normal and impaired renal functions [15]. We refer to this model as ACEInhibPKPD, which is the name of the corresponding GitHub repository for free distribution of the model code [17]. However, this PK/PD model focused on the systemic RAS and is insufficient to predict the effects of ACE inhibitor drugs on ANG II produced by the local RAS. Podocytes express certain RAS enzymes and hormones differently than the systemic RAS with much higher ANG II concentration [8–10]. While several computational models have been proposed for various aspects of renal physiology [18–29], models for the mechanism of hyperglycemia-induced podocyte injury in DKD are only recently appearing in the literature. In a previous publication, we created a podocyte-specific local RAS model that had parameters dependent on the glucose concentration [30]. We refer to this model as glucoseRASpodocytes, which is the name of the corresponding GitHub repository [31]. This glucoseRASpodocytes model lacked the effects of drug dosing. Here, we propose a podocyte-specific PK/PD model to describe how an ACE inhibitor benazepril modulates ANG II concentration in the podocyte local RAS. Benazepril is a commonly used ACE inhibitor to treat hypertension and DKD [32–35]. The objective of this work is to build a physiologically relevant PK/PD model for the local RAS in podocytes to predict ANG II concentration in response to drug dosages and various glucose concentration profiles. The model is detailed in Section 2. In Section 3, we provide results of using subject-specific glucose dynamics data as model input to predict ANG II dynamics. We compare the effects of drug dosages on the ANG II concentration in the local RAS to the systemic RAS in normal and impaired renal function cases and in normal and diabetic glucose conditions. Also, the effects of varying uncertain parameters are explored.

2. Methods

In this section, we develop a PK/PD model for the local RAS in podocytes by combining and adapting features from our previous models: glucoseRASpodocytes [30,31] and ACEInhibPKPD [15,17]. First, we describe the PK model for an ACE inhibitor drug in Section 2.1. Next in Section 2.2, we develop the PD model for the reaction network for the local RAS in podocytes and the effects of the drug on the local RAS. Finally, we summarize the numerical methods used to solve the model equations and provide the location of our code repository and software documentation in Section 2.3.
2.1. Pharmacokinetic Model

Pharmacokinetics describes what happens to a drug in the body and is used to study the time course of drug absorption, distribution, metabolism, and excretion processes. We assume that the concentration of the drug that reaches the podocyte cells through filtration of the blood in a glomerulus is the same as the concentration in the systemic blood plasma. Therefore, we use the same PK model [15] for both the local and the systemic RAS. Briefly, a single-compartment model with first-order absorption and first-order elimination rates for ACE inhibitor drugs after oral administration is used. The analytical solution for the concentration of the biologically active diacid form of the drug for repeated doses over time \( t \) with uniform dose size \( d \) at constant time intervals \( \tau \) is \( [15,36] \)

\[
[\text{Drug}]_n(t') = \frac{k_adF}{(k_a - k_e)V} \left( \frac{1 - \exp(-nk_e\tau)}{1 - \exp(-k_e\tau)} \exp(-k_et') - \frac{1 - \exp(-nk_a\tau)}{1 - \exp(-k_a\tau)} \exp(-k_at') \right)
\]

where \([\text{Drug}]_n(t')\) is the drug concentration after the \( n \)th drug dose, \( t' = t - (n - 1)\tau \) is the time after the \( n \)th dose, \( k_a \) is the absorption rate constant, \( k_e \) is the elimination rate constant, and \( V/F \) is the ratio of the volume of distribution to the fraction of the drug absorbed. The parameters for benazepril obtained from patients with normal renal function (NRF) and impaired renal function (IRF) are listed in Table 1.

Table 1. Pharmacokinetic parameter values used for both the systemic and the local renin-angiotensin system (RAS) models for benazepril for renal function cases of normal renal function (NRF) and impaired renal function (IRF).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>NRF</th>
<th>IRF</th>
<th>Units</th>
<th>Sources</th>
</tr>
</thead>
<tbody>
<tr>
<td>( k_a )</td>
<td>1.907</td>
<td>1.645</td>
<td>h(^{-1})</td>
<td>[15,37]</td>
</tr>
<tr>
<td>( k_e )</td>
<td>(1.33 \times 10^{-1})</td>
<td>(3.45 \times 10^{-2})</td>
<td>h(^{-1})</td>
<td>[15,37]</td>
</tr>
<tr>
<td>( V/F )</td>
<td>(7.09 \times 10^4)</td>
<td>(1.07 \times 10^5)</td>
<td>mL</td>
<td>[15,37]</td>
</tr>
</tbody>
</table>

2.2. Pharmacodynamic Model

Pharmacodynamics is the study of the mechanism and the effects of the drug on the body. Here, the PD model depends on the reactions in the RAS, where the drug inhibits the conversion of ANG I to ANG II. The local RAS (Figure 1a) differs from the systemic RAS (Figure 1b) with respect to the reaction network and the parameter values \[7,30\]. Hence, the PD model developed in ACEInhibPKPD \[15,17\] is not used directly, and we have modified it to be relevant to the local RAS in podocytes.

The podocyte local RAS (Figure 1a) as modeled in glucoseRASpodocytes \[30,31\] has more reactions than the systemic RAS (Figure 1b) as modeled in ACEInhibPKPD \[15,17\] including the non-ACE pathway for conversion of ANG I to ANG II, production of ANG-(1-9) and ANG-(1-7) from ANG I, production of ANG III and ANG-(1-7) from ANG II, and binding of ANG II to angiotensin II receptor type 1 (AT1R) and angiotensin II receptor type 2 (AT2R). These reactions are specific to the podocyte local RAS and are not considered in ACEInhibPKPD. The reactions for conversion of ANG I to ANG II by ACE and non-ACE enzymes (Figure 1a) are lumped into a single reaction (Figure 2). An ordinary differential equation (ODE) for change in angiotensinogen (AGT) concentration with respect to time was included in glucoseRASpodocytes although it was absent in ACEInhibPKPD. This AGT equation is used in the present model. AGT is a peptide upstream of ANG II that is consumed at a rate sensitive to glucose concentration in podocytes, and the ANG II concentration indirectly depends on the concentration of AGT. The conversion of ANG I and ANG II into downstream peptides and the binding of ANG II to AT1 and AT2 receptors are included here (Figure 2) as in glucoseRASpodocytes. Glucose dependency was incorporated in the glucoseRASpodocytes model through the rate parameters for some of the reactions. This glucose dependency is preserved here (green arrows in Figure 2). glucoseRASpodocytes included ODEs for the concentrations of ANG-(1-7),
ANG-(1-9), ANG III, AT1R-bound ANG II, and AT2R-bound ANG II. Here, these species are not tracked explicitly as their concentrations do not influence ANG II.

**Figure 1.** Reaction network for (a) the podocyte local renin-angiotensin system (RAS) as modeled in glucoseRASpodocytes [30,31] and (b) the systemic RAS as modeled in ACEInhibPKPD [15,17]. Peptides are shown in gray ovals, enzymes are denoted over the reaction arrows, enzymes that are influenced by inhibitory reactions are shown in black ovals, and the angiotensin-converting enzyme (ACE) inhibitor is labeled in the white box. Angiotensin II (ANG II) is highlighted in a red oval as the key peptide of interest. Solid lines denote reactions, open arrow tips indicate degradation reactions, dashed lines denote binding of ANG II to receptors, and red dotted lines with flat ends instead of arrows indicate inhibitory reactions.

**Figure 2.** Glucose-dependent biochemical reaction network for the podocyte local RAS pharmacodynamic model. Peptides are shown in gray ovals, enzymes are denoted over the reaction arrows, enzymes that are influenced by inhibitory reactions are shown in black ovals, and the ACE inhibitor is labeled in the white box. ANG II is highlighted in a red oval as the key peptide of interest. Solid lines denote reactions, open arrow tips indicate degradation reactions, dashed lines denote binding of ANG II to receptors, and red dotted lines with flat ends instead of arrows indicate inhibitory reactions. Thick green lines highlight the processes with glucose-dependent rate parameters.

glucoseRASpodocytes focused on the local RAS, but it did not include the impacts of any drugs on the local RAS. Additionally, the negative feedback of ANG II concentration on the production of renin, which is the enzyme involved in the conversion of AGT to ANG I, was included in ACEInhibPKPD (Figure 1b) but was lacking in glucoseRASpodocytes (Figure 1a). In the present model, we adapt the model from glucoseRASpodocytes for the local RAS by incorporating the effects of an ACE inhibitor drug and the negative feedback of ANG II on renin from ACEInhibPKPD [15]. The resultant glucose-dependent biochemical reaction network for the podocyte local RAS PD model for ACE inhibition is illustrated in Figure 2.
The PD model consists of the constant volume mass balances for four chemical species: AGT, renin, ANG I, and ANG II. Concentrations are denoted by species names inside of square brackets. The glucose-dependent rate parameters are denoted by \( c \)'s, and the glucose-independent rate parameters are denoted by \( k \)'s.

The mass balance for AGT is [30]

\[
\frac{d[AGT]}{dt} = k_{AGT} - c_{\text{Renin}}[AGT] - \frac{\ln 2}{h_{AGT}}[AGT]
\]  

(2)

where \( k_{AGT} \) is the constant production rate of AGT, \( c_{\text{Renin}} \) is the glucose-dependent rate parameter for renin-catalyzed conversion of AGT to ANG I, and \( h_{AGT} \) is the half-life for the degradation of AGT.

The mass balance for renin is [15]

\[
\frac{d[\text{Renin}]}{dt} = s_{\text{Renin}} + k_{f}(\text{ANG II}_0 - [\text{ANG II}]) \left( 1 - \frac{\text{ANG II}_0 - [\text{ANG II}]}{f} \right) - \frac{\ln 2}{h_{\text{Renin}}}[\text{Renin}]
\]  

(3)

where \( s_{\text{Renin}} \) is the constant source of renin in the absence of feedback, the second term is the influence of ANG II negative feedback on renin production, \( \text{ANG II}_0 \) is the initial concentration of ANG II, \( k_{f} \) and \( f \) are parameters for the feedback, and \( h_{\text{Renin}} \) is the half-life for the degradation of renin. The renin source term is computed at steady state by [15]

\[
s_{\text{Renin}} = \frac{\ln 2}{h_{\text{Renin}}}[\text{Renin}]_0
\]  

(4)

where \([\text{Renin}]_0 \) is the initial concentration of renin.

The mass balance for ANG I is [15,30]

\[
\frac{d[\text{ANG I}]}{dt} = c_{\text{Renin}}[\text{AGT}] + k_{\text{Renin}}([\text{Renin}] - [\text{Renin}]_0) - c_{\text{ACE}}[\text{ANG I}](1 - I) - (k_{\text{NEP}} + k_{\text{ACE2}})[\text{ANG I}] - \frac{\ln 2}{h_{\text{ANG I}}}[\text{ANG I}]
\]  

(5)

where the first term represents the glucose-dependent renin-catalyzed contribution to the production of ANG I from AGT, the second term represents the change to ANG I synthesis from AGT due to the feedback of ANG II on renin with rate constant \( k_{\text{Renin}} \), the third term is the ACE-catalyzed conversion of ANG I to ANG II that is subject to inhibition \( I \) by the drug and has a glucose-dependent rate parameter \( c_{\text{ACE}} \), the fourth term is the consumption of ANG I to form ANG-(1-7) and ANG-(1-9) with the glucose-independent rate parameters \( k_{\text{NEP}} \) and \( k_{\text{ACE2}} \), respectively, and \( h_{\text{ANG I}} \) is the half-life for the degradation of ANG I. The first and second terms in (5) both consider the production of ANG I from AGT catalyzed by renin. The first term is from glucoseRASpodocytes and includes glucose dependence in the absence of the ANG II-renin feedback mechanism. The second term is from ACEInhibPKPD to incorporate the effects of the feedback mechanism on changing the production rate.

The mass balance for ANG II is [15,30]

\[
\frac{d[\text{ANG II}]}{dt} = c_{\text{ACE}}[\text{ANG I}](1 - I) - (c_{\text{AT1}} + k_{\text{AT2}} + k_{\text{APA}} + k_{\text{ACE2}})[\text{ANG II}] - \frac{\ln 2}{h_{\text{ANG II}}}[\text{ANG II}]
\]  

(6)

where the first term is the production of ANG II in the presence of ACE that is subject to inhibition \( I \) by the drug; the second term is the consumption of ANG II as it converts into downstream peptides and binds to AT1 and AT2 receptors; \( c_{\text{AT1}} \) is the glucose-dependent rate parameter for binding of ANG II to AT1 receptor; \( k_{\text{AT2}}, k_{\text{APA}}, \) and \( k_{\text{ACE2}} \) are the glucose-independent rate parameters for binding of ANG II to the AT2 receptor and conversion of ANG II to ANG III and ANG-(1-7), respectively; and \( h_{\text{ANG II}} \) is the half-life for degradation of ANG II.

The observed percent inhibition \( I \) of benazepril is described by a Hill-type function as [37]
where \([\text{Drug}]_{50}\) is the drug concentration that yields 50% inhibition, and \(m\) accounts for the degree of sigmoidicity.

Glucose dependency is included in the parameters designated by \(c_x\), where \(x = \text{Renin}, \text{ACE}, \) and \(\text{AT1}\). In glucoseRAS podocytes [30] these parameters were found to be the most sensitive and were each considered to be a linear function of glucose. The glucose-dependent parameters are calculated using [30]

\[
c_{\text{Renin}} = a_{\text{Renin}}[\text{Glucose}] + b_{\text{Renin}}
\]

(8)

\[
c_{\text{ACE}} = a_{\text{ACE}}[\text{Glucose}] + b_{\text{ACE}}
\]

(9)

\[
c_{\text{AT1}} = a_{\text{AT1}}[\text{Glucose}] + b_{\text{AT1}}
\]

(10)

where \([\text{Glucose}]\) is the concentration of glucose and the coefficients \(a_x\) and \(b_x\) in (8)–(10) are obtained from parameter estimation detailed in [30].

The feedback parameters \(k_f\) and \(f\) were originally estimated for the systemic RAS in ACEInhibPKPD. However, these parameters are formulated in terms of deviation variables in (3). Because the magnitude of \([\text{ANG II}]\) initial values and deviations are drastically different in the local RAS as compared to the systemic RAS, we scale the parameters \(k_f\) and \(f\) for the podocyte local RAS model as

\[
k_f = k_{f, \text{sys}}[\text{ANG II}]_{0, \text{sys NRF}} / [\text{ANG II}]_{0}
\]

(11)

\[
f = f_{\text{sys}}[\text{ANG II}]_{0, \text{sys NRF}} / [\text{ANG II}]_{0}
\]

(12)

where \(k_{f, \text{sys}}\) and \(f_{\text{sys}}\) are the values of the feedback parameters estimated in [15], \([\text{ANG II}]_{0, \text{sys NRF}}\) is the initial ANG II concentration for the systemic RAS NRF case, and \([\text{ANG II}]_{0}\) is the initial ANG II concentration for the local RAS (for both NRF and IRF). In Section 3.2, we explore the impacts of the uncertainty in these parameters.

The PD parameter values and their sources are listed in Table 2. For the systemic RAS model, the PK and PD parameters and the initial conditions are different for the NRF and IRF cases. However, due to insufficient information about the local RAS, only the PK parameters (Table 1) are varied for the cases of NRF and IRF, while the PD parameters and initial concentrations (Table 2) for the local RAS model are kept the same for both NRF and IRF.

**Table 2.** Pharmacodynamic parameter values for the podocyte local RAS model for benazepril.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Units</th>
<th>Sources</th>
</tr>
</thead>
<tbody>
<tr>
<td>(k_{\text{ACT}})</td>
<td>(2.27 \times 10^6) nmol/L/h</td>
<td>[30]</td>
<td></td>
</tr>
<tr>
<td>(k_{\text{Renin}})</td>
<td>(6.44 \times 10^4) h(^{-1})</td>
<td>[15]</td>
<td></td>
</tr>
<tr>
<td>(k_{\text{NEP}})</td>
<td>0.583 h(^{-1})</td>
<td>[30]</td>
<td></td>
</tr>
<tr>
<td>(k_{\text{ACE2}})</td>
<td>0.382 h(^{-1})</td>
<td>[30]</td>
<td></td>
</tr>
<tr>
<td>(k_{\text{AT2}})</td>
<td>25.1 h(^{-1})</td>
<td>[30]</td>
<td></td>
</tr>
<tr>
<td>(k_{\text{APA}})</td>
<td>43.6 h(^{-1})</td>
<td>[30]</td>
<td></td>
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<tr>
<td>(k_{\text{AGT}})</td>
<td>10.0 h</td>
<td>[14,30]</td>
<td></td>
</tr>
<tr>
<td>(b_{\text{Renin}})</td>
<td>0.250 h</td>
<td>[15]</td>
<td></td>
</tr>
<tr>
<td>(b_{\text{ACE2}})</td>
<td>(1.72 \times 10^{-4}) h</td>
<td>[14,30]</td>
<td></td>
</tr>
<tr>
<td>(b_{\text{AT2}})</td>
<td>(5.00 \times 10^{-3}) h</td>
<td>[14,30]</td>
<td></td>
</tr>
<tr>
<td>([\text{Drug}]_{50})</td>
<td>2.20 ng/mL</td>
<td>[15,37]</td>
<td></td>
</tr>
<tr>
<td>(m)</td>
<td>0.99</td>
<td>-</td>
<td>[15,37]</td>
</tr>
<tr>
<td>(a_{\text{Renin}})</td>
<td>(5.47 \times 10^{-4}) L/mmol/h</td>
<td>[30]</td>
<td></td>
</tr>
<tr>
<td>(b_{\text{Renin}})</td>
<td>(6.16 \times 10^{-11}) h(^{-1})</td>
<td>[30]</td>
<td></td>
</tr>
<tr>
<td>(a_{\text{ACE}})</td>
<td>0.889 L/mmol/h</td>
<td>[30]</td>
<td></td>
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<tr>
<td>(b_{\text{ACE}})</td>
<td>163 h(^{-1})</td>
<td>[30]</td>
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Table 2. Cont.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
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<tbody>
<tr>
<td>$a_{AT1}$</td>
<td>2.55</td>
<td>L/mmol/h</td>
<td>[30]</td>
</tr>
<tr>
<td>$b_{AT1}$</td>
<td>464</td>
<td>h$^{-1}$</td>
<td>[30]</td>
</tr>
<tr>
<td>$k_f$</td>
<td>$6.25 \times 10^{-2}$</td>
<td>h$^{-1}$</td>
<td>[15]</td>
</tr>
<tr>
<td>$f_{sys}$</td>
<td>0.397</td>
<td>nmol/L</td>
<td>[15]</td>
</tr>
<tr>
<td>$[AGT]_0$</td>
<td>$1.70 \times 10^7$</td>
<td>nmol/L</td>
<td>[30]</td>
</tr>
<tr>
<td>$[\text{Renin}]_0$</td>
<td>$2.06 \times 10^{-4}$</td>
<td>nmol/L</td>
<td>[15]</td>
</tr>
<tr>
<td>$[\text{ANG I}]_0$</td>
<td>271</td>
<td>nmol/L</td>
<td>[30]</td>
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<td>$[\text{ANG II}]_0$</td>
<td>21.0</td>
<td>nmol/L</td>
<td>[30]</td>
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<tr>
<td>$[\text{ANG II}]_{0,\text{sys NRF}}$</td>
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<td>nmol/L</td>
<td>[15]</td>
</tr>
<tr>
<td>$[\text{ANG II}]_{0,\text{sys IRF}}$</td>
<td>$2.05 \times 10^{-2}$</td>
<td>nmol/L</td>
<td>[15]</td>
</tr>
</tbody>
</table>

2.3. Numerical Methods and Code Repository

The podocyte-specific, glucose-dependent RAS PD model in Section 2.2 is connected to the PK model described in Section 2.1 to predict the dose-response relationship of benazepril and glucose dynamics on ANG II. The PK/PD model (1)–(12) forms a set of ODEs and algebraic equations that are solved simultaneously using the ode45 ODE solver in MATLAB (Version R2017b, The MathWorks, Natick, MA, USA, 2017). The relative tolerance is set to $10^{-12}$. The time step is restricted to an upper bound of $\tau/500$, where $\tau$ is the dosage interval. To enable code reuse, the MATLAB codes for the mathematical model including parameter values and documentation are available online in an open-source software repository [38].

3. Results and Discussion

The PK/PD model developed in Section 2 was solved to compute $[\text{Drug}]$ and $[\text{ANG II}]$ as functions of time. We considered the following model inputs: drug dose size, number of doses per day, renal function (normal or impaired), and glucose concentration (constant $[\text{Glucose}]$ as well as dynamic $[\text{Glucose}]$ for a representative normal subject or diabetic subject). We studied combinations of these conditions using the model and compared the local RAS model results to the corresponding scenarios using the systemic RAS model to understand the differences between the local and systemic RAS. The simulations were started at the initial conditions corresponding to the case, i.e., $[\text{ANG II}]_0$ for the local RAS for NRF and IRF, $[\text{ANG II}]_{0,\text{sys NRF}}$ for the systemic RAS for NRF, and $[\text{ANG II}]_{0,\text{sys IRF}}$ for the systemic RAS for IRF. We also analyzed the effects of varying uncertain parameters used in the model.

The local RAS PK/PD model was simulated for constant $[\text{Glucose}]$ cases and two cases of dynamic $[\text{Glucose}]$. The constant $[\text{Glucose}]$ cases ranged between the extremes of normal glucose (NG) at 5 mmol/L and high glucose (HG) at 25 mmol/L based on experimental studies [11,39,40]. The dynamic $[\text{Glucose}]$ cases used representative profiles for normal (non-diabetic) and diabetic subjects [41]. The systemic RAS PK/PD model [15] was used for comparison to the local comparison with podocyte local RAS model developed here.

3.1. Effects of Doses of Benazepril

Benazepril doses of 2.5 mg and 10 mg for the cases of NRF and IRF were simulated and compared between the local and systemic RAS. Administration of a once daily dose of benazepril was repeated for seven days. Because the systemic RAS model did not have glucose dependency, the local RAS model was kept at constant NG conditions where $[\text{Glucose}] = 5$ mmol/L for fair comparison between the models. The effects of the drug dosages in the local and systemic PK/PD models were compared for $[\text{Drug}]$ (Figure 3) and $[\text{ANG II}]$ (Figure 4).
Figure 3. Simulation results in response to once daily 2.5 mg (yellow) or 10 mg (red) doses of benazepril in the local RAS (dotted curves) and the systemic RAS (solid curves) for [Drug] for (a) normal renal function (NRF) and (b) impaired renal function (IRF).

Figure 4. Simulation results in response to once daily 2.5 mg (yellow) or 10 mg (red) doses of benazepril in the local RAS (dotted curves) and the systemic RAS (solid curves) at constant NG for (a) [ANG II] for NRF, (b) [ANG II] normalized by [ANG II]₀,NRF, (c) [ANG II] for IRF, and (d) [ANG II] normalized by [ANG II]₀,IRF. Please note that the local RAS NRF and IRF cases only differ in the PK parameters used to obtain [Drug]. [ANG II]₀ = [ANG II]₀,NRF = [ANG II]₀,IRF for the local RAS.

As mentioned in Section 2.1, the local and systemic RAS models had the same PK parameters, which only varied between the NRF and IRF cases (Table 1). As expected the [Drug] profiles in the local and systemic RAS overlapped due to the PK parameters (Figure 3).

Although there was no difference between [Drug] profiles for the local and systemic RAS (Figure 3), the resulting effects on [ANG II] were different (Figure 4). For both renal function cases NRF and IRF, [ANG II] was lowered more substantially by the larger dose of benazepril (Figure 4). In all cases, [ANG II] was larger in the local RAS than in the systemic RAS (Figure 4a,c). The normalized [ANG II] decreased more drastically for the local RAS than for the systemic RAS (Figure 4b,d). These results agreed with the clinical observation that the systemic inhibition of ANG II by ACE inhibitors is not always accompanied by elimination of high [ANG II] in kidneys [13]. The differences between NRF (Figure 4a,b) and IRF (Figure 4c,d) [ANG II] responses were due to the enhanced [Drug] accumulation due to smaller \( k_e \) for IRF.
3.2. Effects of Varying the Uncertain Feedback Parameters

Most of the parameters in the local RAS model were either taken from the literature or estimated based on previous experimental observations. The feedback parameters \( k_f \) and \( f \) were uncertain, as discussed in Section 2.2. Without clinical data to verify the scaled values of \( k_f \) and \( f \) for the local RAS, we analyzed the effects on \([\text{ANG II}]\) of varying these parameters in a wide range. The values for \( k_f \) and \( f \) calculated from (11) and (12) were considered as the nominal values and were varied by approximately four orders of magnitude above and below their nominal values (Table 3). Fifty random values were selected for each parameter assuming a uniform distribution within its range. Latin hypercube sampling (LHS) \([42,43]\) was used to generate the combinations of \( k_f \) and \( f \) values. Simulations were performed using the model for these 50 sets of parameters, each set with a random pairing of \( k_f \) and \( f \). The simulation conditions were set to NRF and NG, and a single 5 mg dose of benazepril was administered after 24 h.

Table 3. Values and ranges for varying feedback parameters \( k_f \) and \( f \) to generate random samples to study the effects on \([\text{ANG II}]\).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Nominal Value</th>
<th>Min</th>
<th>Max</th>
<th>Units</th>
<th>Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>( k_f )</td>
<td>(4.91 \times 10^{-5} )</td>
<td>(5 \times 10^{-9} )</td>
<td>(5 \times 10^{-1} )</td>
<td>h(^{-1})</td>
<td>(10^8)</td>
</tr>
<tr>
<td>( f )</td>
<td>(5.04 \times 10^2)</td>
<td>(5 \times 10^{-2})</td>
<td>(5 \times 10^6)</td>
<td>nmol/L</td>
<td>(10^8)</td>
</tr>
</tbody>
</table>

The results (not shown) generated \([\text{ANG II}] < 0\) for some simulations, which is not physically possible. To explore the parameter extrema, different combinations of the minimum and maximum values of \( k_f \) and \( f \) (Table 4) were simulated. The combination of the maximum \( k_f \) and the minimum \( f \) values was the only case that resulted in \([\text{ANG II}] < 0\). Multiple simulations were run keeping \( k_f \) at its maximum value while varying \( f \) (Figure 5a) and keeping \( f \) at its minimum while varying \( k_f \) (Figure 5b) to find a range of values for these parameters that only yield \([\text{ANG II}] \geq 0\). The results indicated that decreasing \( f \) beyond 4 nmol/L while \( k_f \) was at its maximum value resulted in \([\text{ANG II}] < 0\). Additionally, increasing \( k_f \) above \(5 \times 10^{-3}\) h\(^{-1}\) while \( f \) was at its minimum values resulted in \([\text{ANG II}] < 0\). Based on these results, we defined smaller ranges of six orders of magnitude for \( k_f \) (5 \times 10^{-9} to 5 \times 10^{-3} h^{-1}) and \( f \) (5 to 5 \times 10^6 nmol/L) that give \([\text{ANG II}] \geq 0\) for all combinations of \( k_f \) and \( f \) values. The \([\text{ANG II}]\) curves for the 50 simulations varied only slightly, and the mean of the results was hardly distinguishable from the aggregate (Figure 6). \([\text{ANG II}]\) was insensitive to changes in \( k_f \) and \( f \) over a wide range of parameter values. The scaled values for \( k_f \) and \( f \) (Table 3) were well within these ranges, justifying our use of these values in other simulations reported here.

Table 4. Combinations of minimum and maximum values of \( k_f \) and \( f \) from Table 3 used to study the effects on \([\text{ANG II}]\) after a drug dose.

<table>
<thead>
<tr>
<th>Combination</th>
<th>( k_f )</th>
<th>( f )</th>
<th>([\text{ANG II}])</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>min</td>
<td>min</td>
<td>(\geq 0)</td>
</tr>
<tr>
<td>2</td>
<td>min</td>
<td>max</td>
<td>(\geq 0)</td>
</tr>
<tr>
<td>3</td>
<td>max</td>
<td>max</td>
<td>(\geq 0)</td>
</tr>
<tr>
<td>4</td>
<td>max</td>
<td>min</td>
<td>&lt; 0</td>
</tr>
</tbody>
</table>
Figure 5. Simulation results of [ANG II] response to one 5 mg dose of benazepril at 24 h in the local RAS at constant normal glucose (NG) for NRF for (a) \( k_f \) set at its maximum value of 0.5 h\(^{-1} \) and \( f \) decreased from 5 to 2.5 nmol/L and (b) \( f \) set at its minimum value of 5 × 10\(^{-2} \) nmol/L and \( k_f \) increased from 4 × 10\(^{-3} \) to 6.5 × 10\(^{-3} \) h\(^{-1} \).

Figure 6. Simulation results of [ANG II] response to one 5 mg dose of benazepril at 24 h in the local RAS at constant NG for NRF with 50 random combinations of parameters sampled from the refined ranges of \( k_f \) (5 × 10\(^{-9} \) to 5 × 10\(^{-3} \) h\(^{-1} \)) and \( f \) (5 to 5 × 10\(^{6} \) nmol/L) generated using Latin hypercube sampling (LHS) (colored curves). The mean of [ANG II] from the 50 simulations is shown by the bold black dashed-dotted curve. The inset zooms in around 2 days, which was the time for greatest variations in Figure 5.

3.3. Effects of Varying PK Parameters

The slopes of the curves for [Drug] (Figure 3) primarily depend on the rates of absorption and elimination of the drug. Due to the lack of experimental data in the podocyte cells for the values of the absorption and elimination rate constants (\( k_a \) and \( k_e \)), these values for the local RAS PK model were assumed to be the same as in the systemic RAS (Table 1). However, in a physiological system, a drug must cross various biological barriers and cell membranes to move from systemic circulation into tissues or cells. The ability of the drug to reach targeted tissues or cells depends on multiple factors such as concentration gradients, carrier proteins, protein binding, and other physicochemical interactions. Considering all these factors, it is highly probable that \( k_a \) and \( k_e \) for the local RAS would be different than for the systemic RAS.

We used our model to determine how varying \( k_a \) and \( k_e \) affected the model prediction of [ANG II]. We considered the values of \( k_a \) and \( k_e \) given in Table 1 for NRF as the nominal values and varied each of the parameters uniformly within a range of two orders of magnitude (Table 5). We used LHS to generate 50 random sets of \( k_a \) and \( k_e \) values in their respective ranges. We used the same simulation conditions as in Section 3.2.
Table 5. Values and ranges for varying parameters \( k_a \) and \( k_e \) to generate random samples to study the effects on \([\text{ANG II}]\).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Nominal Value</th>
<th>Min</th>
<th>Max</th>
<th>Units</th>
<th>Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>( k_a )</td>
<td>1.907 \times 10^{-1}</td>
<td>1.907 \times 10^{-1}</td>
<td>1.907 \times 10^{-1}</td>
<td>h^{-1}</td>
<td>(10^2)</td>
</tr>
<tr>
<td>( k_e )</td>
<td>0.133 \times 10^{-1}</td>
<td>0.133 \times 10^{-1}</td>
<td>0.133 \times 10^{-1}</td>
<td>h^{-1}</td>
<td>(10^2)</td>
</tr>
</tbody>
</table>

Varying \( k_a \) and \( k_e \) by small magnitudes had substantial effects on \([\text{ANG II}]\) (Figure 7). The \([\text{ANG II}]\) profiles spread over a wide range of values with different minimum concentrations and slopes depending upon the values of \( k_a \) and \( k_e \). These results indicated that \([\text{ANG II}]\) was highly sensitive to both \( k_a \) and \( k_e \). Further experimental studies focusing on drug pharmacokinetics in the local system need to be conducted to measure \( k_a \) and \( k_e \) in kidney tissues to enhance the accuracy of the model predictions.

![Figure 7](image-url)

**Figure 7.** Simulation results of \([\text{ANG II}]\) response to one 5 mg dose of benazepril at 24 h in the local RAS at constant NG for NRF with 50 random combinations of \( k_a \) and \( k_e \) in the ranges in Table 5 generated using LHS (colored curves). The mean of \([\text{ANG II}]\) from the 50 simulations is shown by the bold black dashed-dotted curve.

3.4. Effects of Glucose Conditions

The local RAS was considered to be functioning at a healthy state for the case of NRF and NG, and the initial condition for this healthy state was taken as the ANG II baseline reference: \([\text{ANG II}]_{\text{baseline}} = [\text{ANG II}]_0\). The local RAS progressed towards an unhealthy state via \([\text{Glucose}]\) increases. The systemic RAS was considered to be functioning at a healthy state for NRF and an unhealthy state for IRF. The healthy baseline reference for ANG II for the systemic RAS was \([\text{ANG II}]_{\text{baseline}} = [\text{ANG II}]_{0,\text{sys NRF}}\). To quantify the deviations from a healthy state in both the local and systemic RAS, \([\text{ANG II}]\) values from simulations without a drug dose were normalized by their respective baseline concentrations. Because the magnitude of \([\text{ANG II}]\) in the local RAS was larger than that in the systemic RAS, this normalization makes the results of the local and systemic RAS models comparable. The local RAS model was run for NRF over seven days without a drug dose for three cases of constant \([\text{Glucose}]\): 5 mmol/L (NG), 10 mmol/L, and 25 mmol/L (HG). These simulations were compared to the systemic RAS for NRF and IRF cases (Figure 8).
Healthy state
Unhealthy state

Figure 8. Simulation results of [ANG II] normalized by the [ANG II]_baseline reference concentrations for the healthy cases for the local RAS ([ANG II]_0) and for the systemic RAS ([ANG II]_0,sys NRF) without a drug dose. The healthy state (yellow) transitions towards the unhealthy state (dark red) for the local RAS (dotted curves) via increasing [Glucose] and for the systemic RAS (solid curves) from normal to impaired renal function.

The results showed that the [ANG II] deflected from the healthy state and increased to new steady states as the [Glucose] conditions or renal functions approached an unhealthy state (Figure 8). For the local RAS, the HG case resulted in a 70% increase in [ANG II] as compared to NG. In the systemic RAS, IRF had 23% higher [ANG II] compared to NRF. The normalized [ANG II] steady state for the local RAS at an intermediate value of [Glucose] at 10 mmol/L was similar to that for the systemic RAS for IRF suggesting that some of the impaired characteristics could be recapitulated by a sustained moderately elevated [Glucose]. Studies have suggested a strong link between hyperglycemia-stimulated ANG II and IRF [4,5,44,45]. Thus, our simulation results agreed with these studies showing that [ANG II] increased for the local and systemic RAS models as the conditions moved towards unhealthy states.

For this study, clinical data for [Glucose] dynamics for normal (non-diabetic) and diabetic human subjects [41] were extracted using Plot Digitizer [46]. The MATLAB functions polyfit and polyval were used to fit curves to the data (Figure 9a). The daily [Glucose] profiles for the normal and diabetic subjects were repeated for five days and used as inputs to the local RAS model. The model was run before and after a single dose of 5 mg benazepril administered at 24 h to examine the effects of the dynamic [Glucose] cases. Before the drug dose (0 ≤ t < 1 day), the [ANG II] variations resulted only from [Glucose] dynamics (Figure 9b). Because the PK parameters were same for both the cases, the [ANG II] immediately dropped to the same value upon dosing at t = 1 day. The [ANG II] rose faster for the diabetic subject than for the normal subject for t ≥ 2 days as the drug was eliminated around t = 2 days, at which point the [Glucose] effects began to dominate.

Figure 9. (a) [Glucose] as a function of time for normal and diabetic subjects with data extracted from [41] and curves fitted with the polyfit function in MATLAB. (b) Simulation results of [ANG II] response to one 5 mg dose of benazepril at 24 h and [Glucose] dynamics in the local RAS.
4. Conclusions

In this work, we presented a mathematical PK/PD model to study and simulate the effects of different dosages of the ACE inhibitor drug benazepril and other conditions on \([\text{ANG II}]\) in the local RAS in podocyte cells in the kidney. The combination of the impact of renal functions on the PK portion of the model and of glucose dependency on the PD portion of the model made this model more physiologically relevant and tailored for the local RAS and inclusive of drug dosing than our previous models [15,30]. The glucose dependency enabled simulation of constant and dynamic \([\text{Glucose}]\) scenarios. The model can be used for patient-specific or population level studies using \([\text{Glucose}]\) dynamics for various cases. Also, the model can be run for user-defined dosing intervals and amounts. The benazepril PK portion of the model was parameterized for normal and impaired renal function. The model can be adapted to study the effects of other ACE inhibitor drugs or combinations of drugs for which the PK parameters have been measured.

Using the model, we compared the effects of drug doses on the local RAS to the systemic RAS. The results agreed with previous clinical studies that found that suppression of the systemic RAS by an ACE inhibitor did not necessarily suppress the intrarenal \([\text{ANG II}]\) to levels below a threshold that could prevent additional DKD damage. These observations raise the question of adequacy of the current therapeutic approaches and suggest that targeting ACE inhibition therapies specifically towards the cellular local RAS could be an effective strategy to further slow the progression of DKD. This presents an open opportunity for more experimental studies to be directed towards ACE inhibition at the local RAS level. Even though some of the parameters used in the model were based on assumptions or their corresponding values in the systemic RAS, we have accounted for the variability of the parameters and studied their effects on \([\text{ANG II}]\). If more experimental data become available, the model can be validated to a greater extent.


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Conflicts of Interest: The authors declare no conflict of interest.

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