Regional Vicarious Calibration of the SWIR-Based Atmospheric Correction Approach for MODIS-Aqua Measurements of Highly Turbid Inland Water

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Abstract: Water color remote sensing requires accurate atmospheric correction but this remains a significant challenge in highly turbid waters. In this respect, the shortwave infrared (SWIR) band-based atmospheric correction approach has proven advantageous when applied to the moderate resolution imaging spectroradiometer (MODIS) onboard the Aqua satellite. However, even so, uncertainties affect its accuracy. We performed a regional vicarious calibration of the MODIS-Aqua SWIR (1240, 2130)-based atmospheric correction using in situ water surface reflectance data measured during different seasons in Lake Taihu, a highly turbid lake. We then verified the accuracy of the (1240, 2130)-based atmospheric correction approach using these results; good results were obtained for the remote sensing reflectance retrievals at the 555, 645, and 859 nm, with average relative errors of 15%, 14%, and 22%, respectively, and no significant bias. Comparisons with the (1240, 2130)-based iterative approach and (1640, 2130)-based approach showed that the vicarious calibrated (1240, 2130)-based approach has the best accuracy and robustness. Thus, it is applicable to the highly turbid Lake Taihu. It may also be applicable to other highly turbid inland waters with similar optical and aerosol optical properties above water, but such applications will require further validation.

Keywords: vicarious calibration; atmospheric correction; MODIS-Aqua; Lake Taihu; SWIR

1. Introduction

Water color satellite sensors receive top-of-atmosphere (TOA) radiance, which includes water-leaving and atmospheric path radiance. Water-leaving radiance, which can be used to assess water parameters, must be derived from satellite-received TOA radiance [1]. This process is known as atmospheric correction, which is the basis for water color remote sensing. Gordon and Wang [1] proposed an atmospheric correction approach (abbreviated as GW94) based on the “black near-infrared (NIR) water-leaving radiance” assumption. This approach uses two NIR bands to assess aerosol radiance and then interpolates the aerosol radiance to visible (VIS) bands. Previous studies have applied this approach to the sea-viewing wide field-of-view sensor (SeaWiFS) and the moderate-resolution imaging spectroradiometer (MODIS), which have all yielded good results in open ocean waters [2]. For turbid coastal and inland waters, however, the near-infrared water-leaving radiance is apparently greater than zero and, therefore, the “black NIR” assumption is no longer valid. Therefore, the GW94 approach fails to perform accurate atmospheric correction in turbid water. Using the “black NIR”-based approach, studies have developed a number of improved methods for turbid waters, which include
two main categories. The first attempts to develop models to assess the water-leaving radiance in NIR bands mainly using an iterative approach [3–7]. The second approach uses atmospheric information derived from adjacent clear water and interpolates the corrections to the turbid water [8]. These improved approaches usually work well in moderately turbid waters but are not necessarily valid for highly turbid waters since certain waters saturate the NIR bands, rendering these “black NIR”-based approaches completely unusable.

Wang and Shi [9–11] proposed a “black shortwave infrared (SWIR)”-based approach, which assumes that the water-leaving radiance in the SWIR bands is zero and uses two SWIR bands to replace the two NIR bands present in the original GW94 approach. Due to the strong absorption at the SWIR wavelengths from pure water [12], the water-leaving radiance in the SWIR wavelength for even highly turbid water tends to be zero. Therefore, the SWIR-based atmospheric correction approach can be used for highly turbid waters. Previous studies have already verified this approach with its application to MODIS-Aqua data in several areas with highly turbid water, including the East China Sea and eastern coast of the U.S.A. [9,10,13,14]. These studies used two SWIR bands at 1240 and 2130 nm because 14 out of the 20 detectors for the original 500 m resolution 1640 nm band on the MODIS-Aqua are inoperable. However, in certain highly turbid waters, such as areas in Lake Taihu, we cannot neglect the water-leaving radiance at the 1240 nm band and the original (1240, 2130) SWIR-based atmospheric correction approach will overestimate aerosol scattering and underestimate the water-leaving radiance in the visible and NIR bands. To solve this problem, Wang et al. [15] proposed an iterative approach and used the relatively clear water pixels at the center of Lake Taihu to retrieve an aerosol model from the original (1240, 2130) SWIR band-based atmospheric correction and interpolated the aerosol model to the entire lake. With the interpolated aerosol model and the 2130 nm band determined aerosol scattering, they then performed atmospheric correction for the entire lake. Zhang et al. [16] suggested that the center of Lake Taihu is not always relatively clear and, therefore, revised the iterative approach by selecting the 200 pixels with the clearest water in the entire lake, as opposed to only the middle area of the lake. However, there are still several uncertainties in the (1240, 2130)-based iterative method. Lake Taihu is a large lake, with an area of over 2300 km$^2$, surrounded by large metropolitan areas, such as Suzhou, Wuxi, Changzhou, and Huzhou. Therefore, aerosol models applicable above the entire lake may significantly change in certain circumstances. Otherwise, locating relatively clear water in Lake Taihu is not always easy, which leads to the failure of the (1240, 2130)-based iterative method. To avoid these uncertainties, Wang et al. [17] replaced the 1240 nm band with the 1640 nm band and applied the (1640, 2130)-based atmospheric correction approach because the water-leaving radiance at 1640 nm is more likely to be near zero due to higher water absorption at longer wavelengths. However, since 70% of the detectors for the original 500 m resolution 1640 nm band on the MODIS-Aqua are inoperable, the (1640, 2130)-based method cannot be applied operationally.

Except for the uncertainties mentioned above, there are a number of other uncertainties associated with the atmospheric correction of water color remote sensing images. To improve the accuracy of atmospheric correction, previous studies have widely adopted vicarious calibration as an operational method [18–25]. Vicarious calibration uses the in situ-measured water-leaving radiance coincident with the water color remote sensing images to compute the vicarious calibration coefficients, i.e., the gains, to obtain the original TOA radiance of the water color remote sensing images. Vicarious calibration can cancel out the error sources and uncertainties in the atmospheric correction process, thus improving atmospheric correction accuracy. For open ocean waters, studies have performed reliable vicarious calibrations based on the in situ water-leaving radiance measured by the marine optical buoy (MOBY) [20,26]. The vicarious calibration coefficients for MODIS-Aqua have been previously applied to the operational processing of MODIS-Aqua data. However, these calibration coefficients are applicable to clear open ocean waters when using the NIR-based atmospheric correction approach but may not be suitable for highly turbid waters when using the SWIR-based atmospheric correction approach. Therefore, to improve the accuracy of the SWIR-based atmospheric correction approach in highly turbid waters, we recommend the vicarious calibration of the SWIR-based atmospheric correction approach.
for highly turbid waters. In this study, we performed regional vicarious calibration of MODIS-Aqua data over highly turbid waters using the SWIR-based atmospheric correction approach. We used in situ water surface reflectance data measured in the highly turbid Lake Taihu during different seasons to perform the vicarious calibration of the (1240, 2130)-based atmospheric correction approach. We then verified the accuracy of the (1240, 2130)-based atmospheric correction approach with the vicarious calibrated results.

2. Study Area and Data Description

2.1. Study Area Description

Lake Taihu in eastern China was selected as the study area (Figure 1). It is the third largest freshwater lake in China and has an area of over 2300 km² [27]. Lake Taihu is a highly turbid lake, with an average concentration of total suspended matter that is greater than 50 mg L⁻¹ and a maximum concentration of total suspended matter that is greater than 300 mg L⁻¹ [28]. Taihu Lake is located in the core area of the middle and lower reaches of the Yangtze River, and is the source of drinking for surrounding cities such as Wuxi and Suzhou. In recent years, the water properties of Lake Taihu have attracted significant attention for remote sensing data studies [16,17,28–37].

From 2005 to 2014, we performed 12 cruise surveys of Lake Taihu, during which we measured the in situ water surface reflectance at 377 water sampling stations, whose locations are shown in Figure 1. Table 1 lists relevant information, such as the dates and sampling stations, for each cruise survey.

![Figure 1](image-url)  
*Figure 1.* Maps of the location of Lake Taihu, China, and the 377 in situ water sampling stations used during the 12 cruise surveys performed between 2005 and 2014.

<table>
<thead>
<tr>
<th>Cruise Dates</th>
<th>Number of Stations</th>
</tr>
</thead>
<tbody>
<tr>
<td>Oct. 10, 2005</td>
<td>13</td>
</tr>
<tr>
<td>Jan. 7–9, 2006</td>
<td>47</td>
</tr>
<tr>
<td>Jul. 29 to Aug. 1, 2006</td>
<td>39</td>
</tr>
<tr>
<td>Oct. 12–15, 2006</td>
<td>37</td>
</tr>
<tr>
<td>Jan. 7–9, 2007</td>
<td>50</td>
</tr>
<tr>
<td>Apr. 25–27, 2007</td>
<td>40</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Cruise Dates</th>
<th>Number of Stations</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mar. 14–15, 2009</td>
<td>29</td>
</tr>
<tr>
<td>Apr. 17–27, 2009</td>
<td>51</td>
</tr>
<tr>
<td>Oct. 17–18, 2012</td>
<td>9</td>
</tr>
<tr>
<td>May 11–13, 2013</td>
<td>40</td>
</tr>
<tr>
<td>Jul. 21–22, 2014</td>
<td>8</td>
</tr>
<tr>
<td>Oct. 26, 2014</td>
<td>14</td>
</tr>
</tbody>
</table>

Table 1. The dates and sampling stations for each cruise survey performed on Lake Taihu.
2.2. Water Surface Reflectance Measurements

During the 12 cruise surveys, we measured the in situ water surface reflectance spectra at each sampling station with an ASD portable field spectrometer FieldSpec® Pro VNIR (wavelength range from 350–1,000 nm) and FieldSpec® Pro FR (wavelength range from 350–2,500 nm) using the above water method [38]. At each station, we measured the standard panel (L_{sw}(\lambda)), water (L_{w}(\lambda)), and skylight (L_{sky}(\lambda)) on the open deck. With these measurements, we calculated the remote sensing reflectance (R_{rs}(\lambda)) with the following equation:

\[
R_{rs}(\lambda) = \frac{L_{w}(\lambda)}{E_{d}(\lambda)} = \frac{L_{sw}(\lambda) - r_{sky}L_{sky}(\lambda)}{\pi L_{d}(\lambda) / \rho_{p}(\lambda)}
\]  

where \( \lambda \) is wavelength, \( E_{d}(\lambda) \) is the downward irradiance above the water surface, \( L_{w}(\lambda) \) is the water-leaving radiance, \( \rho_{p}(\lambda) \) is the reflectance of the standard panel calibrated in the laboratory, and \( r_{sky} \) is the skylight reflectance at the air–water interface, which can be determined from the look-up table [39]. Wind speeds at each sampling station were measured simultaneously with reflectance measurements and were used to determine \( r_{sky} \) values.

Figure 2 shows the calculated \( R_{rs} \) spectra for the 12 cruise surveys. Previous studies have already applied several of these \( R_{rs} \) data to study the water properties of Lake Taihu [24,29,40–42].

![Figure 2](image-url)
2.3. MODIS-Aqua Description

MODIS, an onboard Aqua satellite, was launched on 4 May, 2002. Of the 36 bands equipped on MODIS, 16 can be used to study water properties, including nine 1 km spatial resolution ocean color bands (i.e., 412, 443, 488, 531, 547, 667, 678, 748, and 869 nm), five 500 m land bands (i.e., 469, 555, 1240, 1640, and 2130 nm), and two 250 m bands (645 and 859 nm). For highly turbid waters, out of the nine ocean color bands, six bands (547, 667, 678, 748, and 869 nm) often become saturated and should not be used. The three SWIR bands (i.e., 1240, 1640, and 2130 nm) can be used for atmospheric corrections. Finally, the eight other visible and NIR bands (i.e., 412, 443, 469, 488, 531, 555, 645, and 859 nm) can be used to study the water properties of highly turbid waters. Out of these eight bands, the four land bands (i.e., 469, 555, 645, and 859 nm) have both higher spatial resolution and radiometric dynamic range and are, therefore, more beneficial when studying the water properties of highly turbid coastal and inland waters, because highly turbid waters produce higher reflectance signals than clear waters. In this study, we analyzed the atmospheric correction result accuracy of these eight bands (i.e., 412, 443, 469, 488, 531, 555, 645, and 859 nm), with a primary focus on the four land bands (i.e., 469, 555, 645, and 859 nm).

We used coincident in situ remote sensing reflectance data to calibrate and verify the atmospheric correction results of the MODIS-Aqua data, which include 18 scenes of images referred to as: A20060080540, A20060090445, A20062100440, A20062110520, A20062120425, A20070070430, A20070080510, A20070090555, A20071160535, A20090730540, A20091070530, A20091120545, A20091160520, A20122910440, A20122920525, A20131320535, A20142020430, and A20142990510.

3. Methods

3.1. Regional Vicarious Calibration Method

The water–air radiometric transfer function [20] is given by the following equation:

\[ L_4(\lambda) = (t_{dv}(\lambda)L_w(\lambda) + L_\alpha(\lambda) + t_\lambda(\lambda) + tL_\beta(\lambda) + T L_g(\lambda))h_{gs}(\lambda)h_{gv}(\lambda)f_p(\lambda) \]  

(2)

where \( L_4(\lambda) \), \( L_\alpha(\lambda) \), \( L_\beta(\lambda) \), and \( T L_g(\lambda) \) are the TOA radiance, aerosol scattering radiance, which includes Rayleigh–aerosol interactions, Rayleigh scattering radiance (air molecule scattering), surface whitecap radiance, and sunglint, respectively; \( t_{dv}(\lambda) \) is the water surface to satellite diffuse transmittance; \( t_{gv}(\lambda) \) and \( t_{gs}(\lambda) \) are the gaseous absorption from the water surface to the sensor and Sun to water surface, respectively; and \( f_p(\lambda) \) is the correction coefficient for the band sensor response to the observed radiance polarization.

Vicarious calibration is based on this water–air radiometric transfer function, which uses the coincidently in situ-measured \( R_w(\lambda) \) to model \( L_4(\lambda) \), followed by regression analysis with the corresponding MODIS-received \( L_4(\lambda) \). Before input into Equation (2), the in situ-measured \( R_w(\lambda) \) should be transformed to \( L_w(\lambda) \) as follows [43]:

\[ L_w(\lambda) = nL_w(\lambda)(f_s\cos(\theta_s)t_{ds}(\lambda)f_s(\lambda)) = (R_w(\lambda)^*F_0(\lambda))(f_s\cos(\theta_s)t_{ds}(\lambda)f_s(\lambda)) \]  

(3)

where \( nL_w(\lambda) \) is the normalized water-leaving radiance, \( F_0 \) is the TOA solar irradiance at the average Earth–Sun distance, \( f_s \) is the adjustment parameter for changes in the Earth–Sun distance, \( \theta_s \) is the solar zenith angle, \( t_{ds}(\lambda) \) is the Sun to water surface diffuse transmittance, and \( f_s(\lambda) \) is the water surface bidirectional reflectance correction parameter.

The parameters in Equations (2) and (3) can be computed using the SeaWiFS data analysis system (SeaDAS 7.2) based on the SWIR (1240, 2130 nm) atmospheric correction approach. We computed \( L_w(\lambda) \) by inputting the coincidently in situ-measured \( R_w(\lambda) \) into Equation (3) and then calculated \( L_4(\lambda) \) by inputting the computed \( L_w(\lambda) \) into Equation (2). We further use the computed \( L_4(\lambda) \) and its corresponding MODIS-received \( L_4(\lambda) \) to perform regression analysis, as shown in Equation (4). We then
obtained the vicarious calibration coefficients for each band. We note that this regression equation only contains gain (λ) but no offset (λ) because this is a more stable technique [20].

\[ L_{\text{Computed}}(\lambda) = \text{gain}(\lambda) \times L_{\text{MODIS}}(\lambda) \]  

(4)

The in situ \( R_{\text{rs}}(\lambda) \) spectra data should be convolved into \( R_{\text{rs}}(\lambda_i) \) with the relative spectral response function for each MODIS-Aqua VIS-NIR band before substitution into Equation (3):

\[ R_{\text{rs}}(\lambda_i) = \frac{\int_{\lambda_{\text{min}}}^{\lambda_{\text{max}}} R_{\text{rs}}(\lambda) f_i(\lambda) d\lambda}{\int_{\lambda_{\text{min}}}^{\lambda_{\text{max}}} f_i(\lambda) d\lambda} \]  

(5)

where \( f_i(\lambda) \) is the relative spectral response function for each MODIS-Aqua band and \( \lambda_{\text{min}} \) and \( \lambda_{\text{max}} \) are the wavelength range of the spectral response function for each band.

We note that the coincident in situ \( R_{\text{rs}}(\lambda) \) or \( nL_{\text{sw}}(\lambda) \) spectra are key parameters in the vicarious calibration process. Vicarious calibration of the NIR-based atmospheric correction approach often uses the in situ \( nL_{\text{sw}}(\lambda) \) spectra measured by the marine optical buoy (MOBY) in clear oceanic waters off Hawaii [20]. Vicarious calibration of the SWIR-based atmospheric correction approach can also use MOBY data, which is beneficial for the NIR-SWIR combined atmospheric correction algorithm [23]. However, MOBY data will also yield larger uncertainties due to the low signal-to-noise ratio that characterizes the SWIR bands over clear oceanic waters. Although we are attempting to improve the SWIR-based atmospheric correction accuracy over highly turbid inland waters, such as Lake Taihu, we do not need to consider the combination with the NIR-based atmospheric correction algorithm. Therefore, to reduce uncertainty caused by the low signal-to-noise ratio, we instead used in situ \( R_{\text{rs}}(\lambda) \) data from the highly turbid Lake Taihu for the vicarious calibration of the SWIR-based atmospheric correction approach. The vicarious calibration results can also counteract local aerosol effects and yield improved accuracy at Lake Taihu, as well as similar adjacent lakes that are highly turbid.

3.2. Atmospheric Correction Based on Vicarious Calibration Results

After we obtained the vicarious calibration coefficients for the eight MODIS-AQUA VIS-NIR bands, we substituted them into the SeaDAS 7.2 to perform the SWIR-based atmospheric corrections. In the SeaDAS 7.2 l2gen module, we input the vicarious calibration coefficients for the eight VIS-NIR bands into the “gain” parameters. We note that the “gain” parameters should include 16 numbers for all 16 bands that can be used for water optical property studies, whereas we used the default numbers provided in the SeaDAS 7.2 as the “gain” parameters for the other 8 bands. Table 2 lists the “gain” settings, as well as other parameters for the SeaDAS 7.2.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Meaning</th>
<th>Setting</th>
</tr>
</thead>
<tbody>
<tr>
<td>gain</td>
<td>Vicarious calibration coefficients</td>
<td>[gain(412), gain(443), gain(469), gain(488), gain(531), gain(555), gain(645), gain(859)]</td>
</tr>
<tr>
<td>aer_opt</td>
<td>aerosol calculation mode</td>
<td>−1: Multi-scattering with 2-band model selection</td>
</tr>
<tr>
<td>aer_wave_short</td>
<td>Lower wavelength used for aerosol model selection</td>
<td>1240</td>
</tr>
<tr>
<td>aer_wave_long</td>
<td>Upper wavelength used for aerosol model selection and aerosol concentration</td>
<td>2130</td>
</tr>
</tbody>
</table>
### Table 2. Cont.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Meaning</th>
<th>Setting</th>
</tr>
</thead>
<tbody>
<tr>
<td>cloud_wave</td>
<td>Wavelength used to identify clouds</td>
<td>2130</td>
</tr>
<tr>
<td>cloud_thresh</td>
<td>Threshold used to identify clouds</td>
<td>0.0175</td>
</tr>
<tr>
<td>brdf_opt</td>
<td>Option for running bidirectional reflectance correction (BRDF) factor</td>
<td>0</td>
</tr>
<tr>
<td>resolution</td>
<td>Spatial resolution of outputs</td>
<td>250</td>
</tr>
</tbody>
</table>

#### 3.3. Accuracy Assessment of the Atmospheric Correction Results

We incorporated the vicarious calibration results into the (1240, 2130)-based atmospheric correction, which we refer to as the (1240, 2130)-Cal method. To assess the accuracy of the (1240, 2130)-Cal method, we compared it with the two other methods mentioned previously, i.e., the (1640, 2130)-based method, which we refer to as the (1640, 2130) method, and the (1240, 2130)-based iterative method, which we refer to as the (1240, 2130)-Ite method.

We used the matchups of the in situ $R_{rs}(\lambda)$ measurements coincident with the MODIS-Aqua image pixels to assess the atmospheric correction results with these three methods. There are several requirements used to select the matchups of the in situ $R_{rs}(\lambda)$ measurements coincident with the MODIS-Aqua image pixels. First, the time difference between the in situ $R_{rs}(\lambda)$ measuring time and MODIS-Aqua image acquisition time should not exceed 3 hours. Second, the water should be stable within the time difference, that is, there should be no rain, and the wind speed should not exceed 5 m/s. Third, the MODIS-Aqua image pixels that surround the in-situ sampling sites should be cloudless and absent of high sunglint. Last, in the 3×3 window pixels of the retrieved $R_{rs}(\lambda)$ image that surrounds the sampling station coordinate, the number of valid positive pixels should exceed 5 and the coefficient of variation for the valid positive pixels should be smaller than 40%.

To assess the accuracy of the (1640, 2130) and (1240, 2130)-Ite methods, we used all matchups. To assess the accuracy of the (1240, 2130)-Cal method, we divided the coincident matchups into both calibration matchup data, which were used in the vicarious calibration, and validation matchup data.

The accuracy parameters used in the accuracy assessment include the correlation coefficient (r), average relative error (ARE), root-mean-square deviation (RMSE), and relative root-mean-square deviation (rRMSE). The definitions of the ARE, RMSE, and rRMSE are as follows:

\[
ARE = \frac{\sum_{1}^{N} |R_{rs}^{m} - R_{rs}^{i}|}{N} \tag{6}
\]

\[
RMSE = \sqrt{\frac{\sum_{1}^{N} (R_{rs}^{m} - R_{rs}^{i})^{2}}{N}} \tag{7}
\]

\[
rRMSE = \sqrt{\frac{\sum_{1}^{N} \left( \frac{R_{rs}^{m} - R_{rs}^{i}}{R_{rs}^{m}} \right)^{2}}{N}} \tag{8}
\]

where $R_{rs}^{m}$ and $R_{rs}^{i}$ are the in situ-measured and image-derived $R_{rs}$, respectively, and $\lambda$ is omitted.

### 4. Results

#### 4.1. Vicarious Calibration Results

To perform the vicarious calibration of the MODIS-Aqua VIS-NIR bands, we used the coincident in situ $R_{rs}(\lambda)$ measurements with the eight scenes of the MODIS-Aqua images, including A200620090445, A20062110520, A200700080510, A20071160535, A20090730510, A200910070530, A201222920525, and A20142990510. Using the atmospheric parameters computed with the SeaDAS 7.2 and the in situ-measured $R_{rs}(\lambda)$, we calculated the $L_{c}(\lambda)$ in the eight VIS-NIR bands. Figure 3 shows the scatter plots of the computed $L_{c}(\lambda)$ and MODIS-measured $L_{c}(\lambda)$. By performing a regression between
the computed $L_t(\lambda)$ and MODIS-measured $L_t(\lambda)$, we obtained the vicarious calibration results. Table 3 lists the “gain” of the eight VIS-NIR land bands.

![Figure 3](image_url) A comparison between the moderate resolution imaging spectroradiometer (MODIS)-Aqua measured $L_t(\lambda)$ in Lake Taihu with the computed $L_t(\lambda)$ via the in situ-measured $R_{rs}(\lambda)$ and atmospheric correction parameters calculated with the SeaDAS 7.2. The units for the MODIS-measured and computed $L_t(\lambda)$ are W m$^{-2}$ µm$^{-1}$ sr$^{-1}$.

**Table 3.** The regional vicarious calibration results for the MODIS-Aqua visible and near infrared (NIR) bands using the in situ $R_{rs}(\lambda)$ in the highly turbid Lake Taihu with the (1240, 1640)-based atmospheric correction algorithm. The default gains in SeaDAS 7.2 are also shown in this table.

<table>
<thead>
<tr>
<th>Band (nm)</th>
<th>412</th>
<th>443</th>
<th>469</th>
<th>488</th>
<th>531</th>
<th>555</th>
<th>645</th>
<th>859</th>
</tr>
</thead>
<tbody>
<tr>
<td>gain (This study)</td>
<td>1.0383</td>
<td>1.0651</td>
<td>1.0915</td>
<td>1.0795</td>
<td>1.0930</td>
<td>1.1005</td>
<td>1.1220</td>
<td>1.0800</td>
</tr>
<tr>
<td>gain (SeaDAS 7.2 default)</td>
<td>0.9722</td>
<td>0.9872</td>
<td>1.0139</td>
<td>0.9923</td>
<td>0.9995</td>
<td>1.0014</td>
<td>1.0253</td>
<td>1.0184</td>
</tr>
</tbody>
</table>

4.2. Atmospheric Correction Accuracy Assessment

We compared the atmospheric correction accuracy of the three methods, i.e., the (1640, 2130), (1240, 2130)-Ite, and (1240, 2130)-Cal. First, we computed their atmospheric correction accuracy with matchups for the in situ $R_{rs}(\lambda)$ measurements coincident with the MODIS-Aqua image pixels. Then, we further compared the typical atmospheric correction result images using the three methods.

4.2.1. Comparison of Atmospheric Correction Accuracy

Figure 4 shows the scatter plots for the matchups of the in situ $R_{rs}(\lambda)$ measurements coincident with the atmospheric correction results for the MODIS-Aqua using the three methods, i.e., the (1640, 2130), (1240, 2130)-Ite, and (1240, 2130)-Cal. The points for the (1240, 2130)-Cal results were divided into calibration points, referred to as (1240, 2130)-Cal (Cal), and validation points, referred to as (1240, 2130)-Cal (Val). Table 4 lists the calculated ARE, RMSE, rRMSE, and $r$. The accuracy of the atmospheric correction results for the (1240, 2130)-Cal method was computed using both validation and total matchups.
Figure 4. The scatter plots of the matchups for the in situ $R_{rs}(\lambda)$ measurements coincident with the atmospheric correction results of MODIS-Aqua based on the three methods, i.e., the (1640, 2130), (1240, 2130)-Ite, and (1240, 2130)-Cal. The points for the (1240, 2130)-Cal results were divided into calibration, referred to as (1240, 2130)-Cal (Cal), and validation points, referred to as (1240, 2130)-Cal (Val). Table 4 lists the valid matchup numbers for each band based on each method.

<table>
<thead>
<tr>
<th>Approach</th>
<th>Band (nm)</th>
<th>Valid matchup numbers</th>
<th>$R_{rs}$ range (sr$^{-1}$)</th>
<th>ARE (sr$^{-1}$)</th>
<th>RMSE (sr$^{-1}$)</th>
<th>rRMSE (%)</th>
<th>$r$</th>
</tr>
</thead>
<tbody>
<tr>
<td>(1640, 2130)</td>
<td>469</td>
<td>50</td>
<td>0.004–0.035</td>
<td>52%</td>
<td>0.015</td>
<td>62%</td>
<td>0.15</td>
</tr>
<tr>
<td></td>
<td>555</td>
<td>89</td>
<td>0.005–0.051</td>
<td>28%</td>
<td>0.013</td>
<td>35%</td>
<td>0.58</td>
</tr>
<tr>
<td></td>
<td>645</td>
<td>92</td>
<td>0.002–0.054</td>
<td>24%</td>
<td>0.010</td>
<td>31%</td>
<td>0.75</td>
</tr>
<tr>
<td></td>
<td>859</td>
<td>77</td>
<td>0.002–0.029</td>
<td>26%</td>
<td>0.004</td>
<td>41%</td>
<td>0.81</td>
</tr>
<tr>
<td>(1240, 2130)-Ite</td>
<td>469</td>
<td>95</td>
<td>0.003–0.025</td>
<td>29%</td>
<td>0.009</td>
<td>36%</td>
<td>0.25</td>
</tr>
<tr>
<td></td>
<td>555</td>
<td>112</td>
<td>0.010–0.039</td>
<td>28%</td>
<td>0.014</td>
<td>33%</td>
<td>0.25</td>
</tr>
<tr>
<td></td>
<td>645</td>
<td>112</td>
<td>0.007–0.035</td>
<td>26%</td>
<td>0.012</td>
<td>31%</td>
<td>0.67</td>
</tr>
<tr>
<td></td>
<td>859</td>
<td>109</td>
<td>0.002–0.030</td>
<td>40%</td>
<td>0.006</td>
<td>96%</td>
<td>0.69</td>
</tr>
</tbody>
</table>

Based on Figure 4, we observe that the $R_{rs}(\lambda)$ results from the (1240, 2130)-Cal method are closer to the 1:1 line compared with the results from the (1640, 2130) and (1240, 2130)-Ite methods. For the $R_{rs}(\lambda)$ results from the (1240, 2130)-Cal method, the distribution of the calibration points (referred to as (1240, 2130)-Cal(Cal)) are similar to those of the validation points (referred to as (1240, 2130)-Cal(Val)). For the $R_{rs}(\lambda)$ results at different bands from the (1240, 2130)-Cal method, the $R_{rs}(\lambda)$ values at the 555, 645, and 859 nm bands are closer to the 1:1 line while the $R_{rs}(\lambda)$ results at the 469 nm band show a slight scatter.

We can further analyze the accuracy reported in Table 4. First, the valid matchup numbers from the (1640, 2130) method are the smallest, which is mainly due to the fact 70% of the detectors are inoperative in the 1640 nm band. Valid matchup numbers for the (1240, 2130)-Ite method are also smaller than those based on the (1240, 2130)-Cal method, which is mainly due to the fact that the (1240, 2130)-Ite method does not work on several images absent of clear water. Therefore, the (1240, 2130)-Cal method yielded the most valid matchup numbers, which indicates that it is a more robust method. Second, for the ARE, RMSE, and rRMSE, the valid matchup numbers from the (1240, 2130)-Cal method are the smallest. Third, for $r$, the valid matchup numbers from the (1240, 2130)-Cal method are the largest. Lastly, the difference between these accuracies for the (1240, 2130)-Cal (Total) and (1240, 2130)-Cal (Val) is...
2130)-Cal (Val) methods are similar. Therefore, these results suggest that the (1240, 2130)-Cal method has the highest accuracy and robustness.

Table 4. The accuracy, based on the matchups, of the in situ $R_{rs} (\lambda)$ measurements coincident with the atmospheric correction results for MODIS-Aqua using the three methods, i.e., the (1640, 2130), (1240, 2130)-Ite, and (1240, 2130)-Cal. For the (1240, 2130)-Cal, accuracies were computed for both the total and validation matchup data, which are reported as (1240, 2130)-Cal (Total) and (1240, 2130)-Cal (Val), respectively. The valid matchup numbers vary for the different bands and with respect to the atmospheric correction method because the valid atmospheric-corrected $R_{rs} (\lambda)$ value must be positive and the coefficients of variation must be smaller than 40% in the 3×3 window that surrounds the coincident in situ $R_{rs} (\lambda)$ measurements.

<table>
<thead>
<tr>
<th>Approach</th>
<th>Band (nm)</th>
<th>Valid matchup numbers</th>
<th>$R_{rs}$ range (sr$^{-1}$)</th>
<th>ARE</th>
<th>RMSE (sr$^{-1}$)</th>
<th>rRMSE</th>
<th>$r$</th>
</tr>
</thead>
<tbody>
<tr>
<td>(1640, 2130)</td>
<td>469</td>
<td>50</td>
<td>0.004–0.035</td>
<td>52%</td>
<td>0.015</td>
<td>62%</td>
<td>0.15</td>
</tr>
<tr>
<td></td>
<td>555</td>
<td>89</td>
<td>0.005–0.051</td>
<td>28%</td>
<td>0.013</td>
<td>35%</td>
<td>0.58</td>
</tr>
<tr>
<td></td>
<td>645</td>
<td>92</td>
<td>0.002–0.054</td>
<td>24%</td>
<td>0.010</td>
<td>31%</td>
<td>0.75</td>
</tr>
<tr>
<td></td>
<td>859</td>
<td>77</td>
<td>0.002–0.029</td>
<td>26%</td>
<td>0.004</td>
<td>41%</td>
<td>0.81</td>
</tr>
<tr>
<td>(1240, 2130)-Ite</td>
<td>469</td>
<td>95</td>
<td>0.003–0.025</td>
<td>29%</td>
<td>0.009</td>
<td>36%</td>
<td>0.25</td>
</tr>
<tr>
<td></td>
<td>555</td>
<td>112</td>
<td>0.010–0.039</td>
<td>28%</td>
<td>0.014</td>
<td>33%</td>
<td>0.25</td>
</tr>
<tr>
<td></td>
<td>645</td>
<td>112</td>
<td>0.007–0.035</td>
<td>26%</td>
<td>0.012</td>
<td>31%</td>
<td>0.67</td>
</tr>
<tr>
<td></td>
<td>859</td>
<td>109</td>
<td>0.002–0.030</td>
<td>40%</td>
<td>0.006</td>
<td>96%</td>
<td>0.69</td>
</tr>
<tr>
<td>(1240, 2130)-Cal (Total)</td>
<td>469</td>
<td>98</td>
<td>0.002–0.033</td>
<td>33%</td>
<td>0.009</td>
<td>40%</td>
<td>0.58</td>
</tr>
<tr>
<td></td>
<td>555</td>
<td>129</td>
<td>0.014–0.048</td>
<td>15%</td>
<td>0.007</td>
<td>20%</td>
<td>0.70</td>
</tr>
<tr>
<td></td>
<td>645</td>
<td>130</td>
<td>0.008–0.050</td>
<td>14%</td>
<td>0.006</td>
<td>19%</td>
<td>0.84</td>
</tr>
<tr>
<td></td>
<td>859</td>
<td>122</td>
<td>0.002–0.028</td>
<td>22%</td>
<td>0.003</td>
<td>29%</td>
<td>0.90</td>
</tr>
<tr>
<td>(1240, 2130)-Cal (Val)</td>
<td>469</td>
<td>25</td>
<td>0.002–0.031</td>
<td>39%</td>
<td>0.010</td>
<td>47%</td>
<td>0.78</td>
</tr>
<tr>
<td></td>
<td>555</td>
<td>51</td>
<td>0.014–0.048</td>
<td>20%</td>
<td>0.008</td>
<td>24%</td>
<td>0.77</td>
</tr>
<tr>
<td></td>
<td>645</td>
<td>52</td>
<td>0.008–0.050</td>
<td>18%</td>
<td>0.007</td>
<td>24%</td>
<td>0.83</td>
</tr>
<tr>
<td></td>
<td>859</td>
<td>46</td>
<td>0.002–0.028</td>
<td>28%</td>
<td>0.003</td>
<td>35%</td>
<td>0.88</td>
</tr>
</tbody>
</table>

4.2.2. Comparison of Atmospheric-Corrected Images

We used a scene of a MODIS-Aqua image, acquired on April 26, 2009, named A20091160520, to compare the atmospheric-corrected $R_{rs}$ images based on the (1640, 2130), (1240, 2130)-Ite, and (1240, 2130)-Cal methods. We set the spatial resolution of the atmospheric-corrected $R_{rs}$ result image at 250 m. The $R_{rs}(645)$ and $R_{rs}(859)$ images had finer spatial patterns since their original spatial resolution was 250 m and did not require spatial interpolation. Figure 5 shows a comparison of the atmospheric-corrected $R_{rs}(645)$ and $R_{rs}(859)$ images based on the three different methods. There are five coincident in situ $R_{rs}$ measurements and Figure 5a shows their locations as red dots. We further compared the five matchups of the in situ $R_{rs}$ spectra with the corresponding atmospheric-corrected $R_{rs}$ spectra in Figure 6. Table 5 lists the average ARE of these five matchups.
Figure 5. The atmospheric-corrected \( R_{\text{rs}} \) images of a scene from a MODIS-Aqua image acquired on 26 April 2009, based on the (1640, 2130), (1240, 2130)-Ite, and (1240, 2130)-Cal methods. (a) is the \( L_t(645) \) image, which shows the locations of the five coincident in situ \( R_{\text{rs}} \) measurements as red dots. (b–d) are the atmospheric-corrected \( R_{\text{rs}}(645) \) images based on the (1640, 2130), (1240, 2130)-Ite, and (1240, 2130)-Cal methods, respectively. (e) is the \( L_t(859) \) image. (f–h) are the atmospheric-corrected \( R_{\text{rs}}(859) \) images based on the (1640, 2130), (1240, 2130)-Ite, and (1240, 2130)-Cal methods, respectively. The (1240, 2130)-Cal method retrieved an AOT(555) = 0.33 (Mean) ± 0.10 (Std).

Figure 6. A comparison of the five matchups for the in situ \( R_{\text{rs}} \) spectra with corresponding atmospheric-corrected \( R_{\text{rs}} \) spectra from the MODIS-Aqua image acquired on 26 April 2009, which was processed using the three different methods. The five subfigures show the comparison results on the five in situ locations, the red dots in Figure 5a.
Table 5. The average relative error (ARE) of the five matchups for the in situ $R_s$ spectra with the corresponding atmospheric-corrected $R_s$ spectra from the MODIS-Aqua image acquired on 26 April 2009, processed using the three different methods.

<table>
<thead>
<tr>
<th>Approach</th>
<th>Band(nm)</th>
<th>412</th>
<th>443</th>
<th>469</th>
<th>488</th>
<th>531</th>
<th>555</th>
<th>645</th>
<th>859</th>
<th>Mean</th>
</tr>
</thead>
<tbody>
<tr>
<td>(1640, 2130)</td>
<td></td>
<td>25%</td>
<td>18%</td>
<td>15%</td>
<td>13%</td>
<td>10%</td>
<td>9%</td>
<td>7%</td>
<td>13%</td>
<td>14%</td>
</tr>
<tr>
<td>(1240, 2130)-Ite</td>
<td></td>
<td>24%</td>
<td>22%</td>
<td>23%</td>
<td>21%</td>
<td>13%</td>
<td>19%</td>
<td>16%</td>
<td>17%</td>
<td>19%</td>
</tr>
<tr>
<td>(1240, 2130)-Cal</td>
<td></td>
<td>17%</td>
<td>14%</td>
<td>11%</td>
<td>11%</td>
<td>9%</td>
<td>7%</td>
<td>6%</td>
<td>13%</td>
<td>11%</td>
</tr>
</tbody>
</table>

Based on Figure 5, we observe that there are similar spatial patterns in the retrieved $R_s(645)$ and $R_s(859)$ images from the different atmospheric correction methods. There is significant noise and areas of atmospheric correction failure in the retrieved $R_s(645)$ and $R_s(859)$ images from the (1640, 2130) method, which is mainly due to the inoperable detectors in the 1640 nm band. Most areas of the retrieved $R_s(645)$ and $R_s(859)$ images based on the (1240, 2130)-Ite method were underestimated compared with those retrieved by the (1640, 2130) and (1240, 2130)-Cal methods, which is possibly due to the inappropriate interpolation of aerosol models from clear water. Based on Figure 6, we observe that the $R_s(\lambda)$ spectra retrieved by the (1240, 2130)-Cal method are, overall, the closest to the in situ-measured $R_s(\lambda)$ spectra, though the match-ups of (1) and (3) show a better correspondence with the $R_s(\lambda)$ spectra retrieved by the (1640, 2130) method. This is also observable based on the average ARE listed in Table 5, which is 11% for the (1240, 2130)-Cal method and 14% for the (1640, 2130) method. As for the retrieved $R_s(\lambda)$ spectral shapes, the (1640, 2130) method retrieves even better spectral shapes than the (1240, 2130)-Cal method. Considering all these factors, the results in Figures 5 and 6 and Table 5 indicate that the (1240, 2130)-Cal method produces the best overall $R_s(\lambda)$ results.

5. Discussion

5.1. Effects of the BRDF Correction

The SeaDAS 7.2 default BRDF correction model is the Morel f/Q model, which is an iterative model based on chlorophyll-a [44,45]. This model performs well in clear open ocean waters but has problems when applied to highly turbid coastal and inland waters [27]. We used a scene from a MODIS-Aqua image, acquired on 9 January 2006, named A20060090445, to discuss the BRDF problem.

We used the (1240, 2130)-Cal approach to perform atmospheric correction of this image twice. We did not perform BRDF correction (brdf_opt = 0) the first time, and for the second, we set the BRDF correction as the default value. Figure 7b,c show the atmospheric-corrected $R_s(645)$ results with and without the default BRDF correction, respectively. We further show the BRDF correction factor in Figure 7d, which was computed during the atmospheric correction process with the default BRDF correction.

Based on Figure 7, we observe that the $R_s(645)$ image without BRDF correction is smooth along the entire lake and the spatial pattern is similar to that of $L_4(645)$. The $R_s(645)$ image with BRDF correction, however, has several clear jumps mainly located at the center and southwestern areas of the lake. By comparing these images with the BRDF correction factor image, these jumps occur at the edges of the black areas. The value of these black areas is zero, which indicates that the BRDF correction model failed in these areas and did not perform BRDF correction. Therefore, Figure 7 confirms that the SeaDAS 7.2 default BRDF correction is not suitable for highly turbid waters. Unfortunately, there are no other existing operational BRDF correction models for highly turbid waters.

Fortunately, due to the multi-scattering of light in highly turbid waters, the BRDF of highly turbid water is weaker than that of clear ocean water [27]. We can, therefore, temporally ignore the BRDF correction for highly turbid waters, especially when the viewing zenith angle is not large, which will yield reasonable atmospheric-corrected results. For image pixels with large viewing zenith angles,
which can be obtained from the Hisatzen field in l2flags, the atmospheric-corrected results should be used cautiously.

Figure 7. The atmospheric-corrected $R_{rs}(645)$ images of a scene of a MODIS-Aqua image acquired on 9 January 2006, using the (1240, 2130)-Cal method. (a) is the $L_t(645)$ image. (b,c) are the atmospheric-corrected results without BRDF correction and with the default BRDF correction, respectively. (d) is the BRDF correction factor computed during the atmospheric correction process with the default BRDF correction.

5.2. Uncertainty and Applicability Analysis

Except for the BRDF correction, there are several other sources of error in the SWIR-based atmospheric correction method, including the noise in the SWIR bands, the inaccurate aerosol model, and other parameter settings in the SeaDAS 7.2, as well as the non-negligible water-leaving radiance in the 1240 nm band in certain extremely turbid waters. By incorporating the vicarious calibration results into the atmospheric correction process, these errors cancel out to some extent, especially in the macroscopic view. This suggests that the atmospheric-corrected results of a specific image may contain certain errors but that the vicarious calibration significantly cancels out the overall error.

The atmospheric corrections had better accuracy at the 555 (green light), 645 (red light), and 859 nm (NIR) wavelengths than those at the 469 nm (blue light) wavelength, which is possibly due to two reasons. On one hand, blue light is farther from the SWIR bands than the green, red, and NIR bands, such that the aerosol scattering errors are possibly due to derivation over a longer spectral distance because the errors associated with the SWIR bands, aerosol models, and other sources of error may increase during derivation over a long distance. On the other hand, in situ $R_{rs}$ measurements are based on the above-water method and the determination of the skylight reflectance at the air–water interface, $r_{sky}$, which also has associated uncertainty. Since skylight has increased at the blue light wavelength, the error associated with determining $r_{sky}$ causes higher uncertainty in the computed $R_{rs}$ results for blue light. Therefore, the atmospheric-corrected $R_{rs}$ results at 469 nm (blue light) should be used cautiously. While blue light is highly absorbed by high concentrations of suspended particulate matter
and color dissolved organic matter (CDOM) in highly turbid waters, the $R_{rs}$ for blue light is seldom used to retrieve chlorophyll-a and suspended particulate matter in highly turbid waters [28,29,46–48].

The vicarious calibration results are mainly applicable to Lake Taihu as these are based on the coincident in situ-measured $R_{rs}$ data from the lake; however, these may also be applicable to other highly turbid waters with similar optical and aerosol optical properties above water. Even if the calibration results may not be applicable to some waters, the procedure used in this study can be applied to these waters in general, by using the coincident in situ-measured $R_{rs}$ data from these waters to obtain new vicarious calibration coefficients. We expect to validate and extend the present approach to other highly turbid waters in the near future.

6. Conclusions

In this study, we performed regional vicarious calibration of the MODIS-Aqua SWIR (1240, 2130)-based atmospheric correction approach using the in situ water surface reflectance data measured in the highly turbid Lake Taihu during different seasons. We then verified the accuracy of the (1240, 2130)-based atmospheric correction approach with the vicarious calibrated results and compared the results with the other approaches. The main findings of this study are as follows.

First, the vicarious calibration was performed based on the in situ $R_{rs}$ measurements from Lake Taihu coincident with eight scenes of the MODIS-Aqua images. The obtained vicarious calibration coefficient gains for the eight MODIS-Aqua visible and NIR bands at 412, 443, 469, 488, 531, 555, 645, and 859 nm were 1.0383, 1.0651, 1.0915, 1.0795, 1.0930, 1.1005, 1.1220, and 1.0800, respectively.

Second, through the regional vicarious calibration of the VIS-NIR bands, the (1240, 2130)-based atmospheric correction approach yielded good results for the $R_{rs}$ retrievals at the 555, 645, and 859 nm bands for Taihu Lake, with AREs of 15%, 14%, 22% for the 555, 645, and 859 nm bands, respectively, with no significant bias.

Further comparison with the (1240, 2130)-based iterative approach (i.e., the (1240, 2130)-Ite) and the (1640, 2130)-based approach showed that the vicarious calibrated (1240, 2130)-based approach had the best accuracy and robustness.

Finally, our results suggest that the SeaDAS 7.2 default BRDF correction model is not suitable for highly turbid waters since it is weaker than that of clear ocean waters. Therefore, we do not recommend the use of the BRDF correction for the atmospheric correction of highly turbid waters.

These results show that the regional vicarious calibration of the (1240, 2130)-based atmospheric correction approach is applicable to the highly turbid Lake Taihu. This approach may also be applicable to other highly turbid inland waters with similar optical and aerosol optical properties above water but requires further validation.

Author Contributions: Conceptualization, J.L.; formal analysis, Z.L., F.Z., and Q.S.; funding acquisition, B.Z.; methodology, J.L. and F.Z.; validation, Z.Y., Z.L., Y.Y., and Q.S.; writing—original draft, J.L.; writing—review and editing, Z.Y., Y.Y., and B.Z.

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Conflicts of Interest: The authors declare no conflict of interest.

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