Application of Acoustic Emission to Estimation of Strata Denudation: A Case Study from the Ordos Basin, China

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Abstract: This paper presents a method for reconstructing denudation in sedimentary basins. The principle of this method is to use the Kaiser effect involving the acoustic emission (AE) of rock samples under a uniaxial load test. Based on the proposed method, the denudation thickness since the Late Cretaceous period in the southeastern margin of the Ordos Basin in China was estimated. The results showed that the denudation increased gradually from the northwest (1600 m a.s.l) to the southeast (1800 m a.s.l) of the study area. A comparison of the denudation results with those obtained from other methods illustrated that the AE method was reliable and easy to use. Finally, using computer simulation, we analyzed the influence of strata denudation and ground topography on the current in situ stress. The results suggested that due to the denudation, the horizontal stress played a dominant role in the distribution of the in situ stress of the study area, but the in situ stress could be reduced by the uplifted movement of the ground. The analysis could facilitate future applications of the AE method and improve understanding of the basin stress field.

Keywords: acoustic emission (AE); denudation reconstruction; lateral pressure coefficient; Ordos Basin

1. Introduction

Structural uplift and stratigraphic denudation are common geological phenomena in the evolution of sedimentary basins. The intensity and regional difference of strata denudation reflect the active progress of tectonic and sedimentary environments. Denudation has an important impact on the formation and migration of oil and gas [1–4], which are the most important basic resources for sustainable socio-economic development. Strong denudation even changes the in situ stress. Therefore, reconstruction of this denudation is of great significance for basin evolution research, hydrocarbon evaluation and in situ stress assessment.

The uncertainty of geological conditions and incomplete geological data make it difficult to estimate the denudation of strata. Commonly used methods to reconstruct denudation can be divided into the following types: (1) The geological method, including the stratigraphic contrast method, the sedimentation rate method, and the sedimentation fluctuation process analysis method [5–8]; (2) the geochemical method, including the vitrinite reflectance method, the fluid warp body method, the apatite fission track method, and the cosmogenic nuclides analysis method [9–12]; (3) the geophysical method, including the logging curve method and the seismic stratigraphy method [13].
It is necessary to select the most appropriate method based on the basin evolution history and existing geological data.

For some basins, fundamental limitations have resulted in limited available methods. Taking the Ordos Basin as an example, the seismic stratigraphy method is not applicable because the basin is covered with loess. Moreover, due to the large amount of denudation of the Late Cretaceous and the large variation of sedimentary facies, the geothermal index and the mudstone compaction-trend extrapolation methods are not suitable [10,14]. At present, few methods of reconstructing the basin’s denudation have been reported [15–17]. Therefore, in order to provide the necessary accuracy, new denudation measurement needs to be explored.

In this study, a method based on the Kaiser effect involving acoustic emission (AE) will be proposed, and the mechanism and theory of this method will be discussed. Using this method, the denudation since the Late Cretaceous in the southeastern margin of the Ordos Basin will be computed. Based on the computed results, the influence of denudation and ground topography on the in situ stress of the basin will be analyzed by numerical simulation.

2. Analytical Methods

2.1. Principal of Acoustic Emission to Estimate the Denudation

Many solid materials emit weak acoustic signals under stress [18]. Based on this feature, the AE testing technique is widely used for material damage detection [19–23]. Joseph Kaiser found that if a specimen was once subjected to stress, then it will only have AE activity when the applied load is higher than the largest previous load of stress [24]. This phenomenon is known as the Kaiser effect, which indicates that materials have the ability to accumulate, to retain and, under certain conditions, to reproduce information on the stresses experienced in the past [22,25]. As a geological body, the Kaiser effect of the rock mass reflects its stress environment in the geological history [26–29]. The Kaiser effect takes place in rocks and materials subjected to cyclic loading/unloading. By field directional sampling and an indoor uniaxial loading test, the historical maximum stress in that direction can be retrieved.

As shown in Figure 1a, 0–0′ is the original surface before the uplift and denudation. For a certain depth below ground (generally deeper than 1000 m), it could be assumed that the rock mass is in a hydrostatic stress state [30,31]. The in situ stress at point A is

\[ \sigma_{h0} = \sigma_{v0} = \gamma H \] (1)

where \( \sigma_{h0} \) and \( \sigma_{v0} \) are the horizontal and vertical stresses, respectively, \( H \) is the buried depth of point A before denudation, and \( \gamma \) is the unit depth of gravity of the overlying stratum. In this study, \( \gamma \) is equal to 0.027 MPa/m [30,31].

After the formation is lifted and denuded, the current surface becomes 1–1′. For vertical sampling at point A, the stress calculated by AE is recorded as \( \sigma_k \) (Figure 1b). The inclination angles of the formation before and after the denudation are \( \theta \) and \( \theta_0 \), respectively. The deflection angle \( \beta \) of the formation is

\[ \beta = |\theta - \theta_0| \] (2)
Then $\sigma_k$ can be obtained by:

$$\sigma_k = \sigma_v \cos \beta + \sigma_h \sin \beta$$  \hspace{1cm} (3)

According to Equation (1) and Equation (3):

$$H = \frac{\sigma_k}{(\cos \beta + \sin \beta)\gamma}$$  \hspace{1cm} (4)

The denudation thickness of the overlying strata at point A is:

$$\Delta h = H - h = \frac{\sigma_k}{(\cos \beta + \sin \beta)\gamma} - h$$  \hspace{1cm} (5)

where $h$ is the buried depth of point A after denudation, which is equal to the sampling depth.

Studies on the basin evolution in the investigated area indicate that $\beta$ is approximately equal to $0^\circ$ [32]. Therefore, Equation (5) can be simplified as:

$$\Delta h = \frac{\sigma_k}{\gamma} - h$$  \hspace{1cm} (6)

2.2. Influence of Stratum Denudation on In Situ Stress

The uplift and denudation of the formation changes the stress in the rock mass. However, the relative variation amplitudes of $\sigma_v$ and $\sigma_h$ are different, resulting in a change in the lateral pressure coefficient $\lambda$. Assuming the horizontal strain $\epsilon_h$ is equal to zero and the vertical stress $\sigma_v$ is always equal to the weight of the overlying rock mass during the denudation, according to the generalized Hooke's law, the $\epsilon_h$ can be obtained by:

$$\epsilon_h = \frac{1}{E}[\sigma_h - \mu(\sigma_v + \sigma_h)] = 0$$  \hspace{1cm} (7)

where $E$ and $\mu$ are the Young’s modulus and Poisson’s ratio of the rock mass, respectively. Then we have:

$$\sigma_h = \frac{\mu}{1-\mu}\sigma_v$$  \hspace{1cm} (8)

According to Equation (8), the amounts of stress change after denudation are:

$$\Delta \sigma_v = r\Delta h$$  \hspace{1cm} (9)
\[ \Delta \sigma_h = \frac{\mu}{1-\mu} \Delta \sigma_v = \frac{\mu}{1-\mu} r \Delta h \]  

(10)

where \( \Delta \sigma_h \) and \( \Delta \sigma_v \) are the changes in horizontal stress and vertical stress caused by denudation, respectively.

According to Equation (1), Equation (9) and Equation (10), the current \( \sigma_V \) and \( \sigma_h \) are:

\[ \sigma_v = \sigma_{v0} - \Delta \sigma_v = rh \]  

(11)

\[ \sigma_h = \sigma_{h0} - \Delta \sigma_h = rh + r \Delta h \frac{1-2\mu}{1-\mu} \]  

(12)

According to Equation (11) and Equation (12), the current \( \lambda \) is:

\[ \lambda = \frac{\sigma_h}{\sigma_v} = 1 + \frac{\Delta h (1 - 2\mu)}{h (1 - \mu)} \]  

(13)

The study area is dominated by sedimentary rocks like sandstone so the value of \( \mu \) would be set to 0.3, according to the laboratory tests. Then Equation (13) can be simplified as:

\[ \lambda = 1 + 0.57 \frac{\Delta h}{h} \]  

(14)

It can be inferred from Equation (14) that for a certain point underground, the greater the thickness of the upper formation denudation, the higher the current lateral pressure coefficient is.

3. Characteristics of the Study Area

3.1. Geography and Tectonics

The study area is located in the southeast of the Ordos Basin (Figure 2), which is the second largest sedimentary basin in China [33]. It covers an area of 370,000 km\(^2\) with its main body slopes to the northwest [34]. Affected by long-term erosion and cutting of rivers, the study area has formed landscapes with undulations and gullies (Figure 3a). The topography of the study area gradually changed from the loess gullies in the north to the mountains in the south (Figure 3b).

Figure 2. Tectonic map of the Ordos Basin (modified from Reference [35]).
The Ordos Basin is a Mesozoic landlocked depression basin formed under the influence of the Indo-China movement and is one of the most stable and complete tectonic units in China [36–38]. Studies on basin evolution indicate that the formation has not rotated much in history but currently has a dip angle of 2–3°. Therefore, the formation deflection angle β in the study area should be 0°.

Since the Mesozoic period, the Ordos Basin has experienced four unconformity uplifts and denudation events marked by stratigraphic unconformity interfaces [39,40]. The most intense uplift and denudation event occurred at the end of the Cretaceous period, resulting in the denudation thickness in most parts of the basin, much thicker than that of resedimentary strata [15]. Combined with the sedimentary background of the study area, the stratum denudation thickness estimated by the AE method in this study is equal to that since the end of the Cretaceous.

3.2. Engineering Situation

The samples used in the AE test were collected from an under-construction railway project in the investigated area. The railway runs northwest across the Loess Plateau with an average altitude of 1000 m. Affected by the terrain, some sections had tunnels with an average depth of 100–300 m. In situ stress tests were carried out in three different tunnels by hydraulic fracturing, and the results are shown in Table 1 (data came from [41]). In the depth of the tunnel, the field was dominated by horizontal stress and the direction of principal compressive stress was NEE. ZK1 and ZK2 lay in the mountain area with steep terrain and an average λ of 1.7, whereas ZK3 was in the loess gully area with an average λ of 2.7.

Table 1. Hydraulic fracturing test results (data came from Reference [41]).

<table>
<thead>
<tr>
<th>Site No.</th>
<th>Buried Depth /m</th>
<th>$\sigma_h$ /MPa</th>
<th>$\sigma_b$ /MPa</th>
<th>$\sigma_v$ /MPa</th>
<th>$\lambda=\sigma_h/\sigma_v$</th>
<th>$\kappa H$ $/^\circ$</th>
</tr>
</thead>
<tbody>
<tr>
<td>ZK1</td>
<td>290</td>
<td>12.9–15.8</td>
<td>7.4–9.4</td>
<td>7.8–8.8</td>
<td>1.7–1.9</td>
<td>N79°E</td>
</tr>
<tr>
<td>ZK2</td>
<td>110</td>
<td>4.9–6.5</td>
<td>2.7–4.9</td>
<td>3.2–3.9</td>
<td>1.5–1.9</td>
<td>N75°E</td>
</tr>
<tr>
<td>ZK3</td>
<td>180</td>
<td>13.4–15.9</td>
<td>8.7–9.6</td>
<td>4.9–5.9</td>
<td>2.6–2.8</td>
<td>N74°E</td>
</tr>
</tbody>
</table>

4. Sampling and Test Methods

Nine samples were collected at four different locations in the study area. Among them, samples ZK1, ZK2, and ZK3 were cores from drilled boreholes in the tunnel, and YC4 was obtained from
the surface outcrop. All the samples were sandstone from the Yanchang Formation, Triassic system. They were cut into cylinders with a size of 50 mm × 100 mm (Figure 4), with the long axis of the cylinder vertically downward. In order to reduce the influence of rock sample defects on the judgment of the Kaiser point, rock blocks with homogenous or no obvious cracks were selected.

Figure 4. Photos of some samples, (a) before the test and (b) after the test.

The AE tests were carried out at the Institute of Acoustic, Chinese Academy of Sciences. The experiment instruments mainly included the PCI-2 AE signal acquisition system developed by the Physical Acoustic Corporation, and the electro-hydraulic servo loading system developed by the GCTS Company. Throughout the experiment, the loading system applied a load to the sample, while the PCI-2 recorded the AE signal from the sample during the loading. The experiment is shown in Figure 5.

Figure 5. The uniaxial compression and AE test device. (a) Photo of the device and (b) schematic diagram of the device.

Experiments by Yoshikawa and Mogi revealed no or very little influence of the loading rate on the Kaiser effect in rocks [42], so it was set to a normal rate of 0.02 mm/min in this study. In order to ensure the acquisition of a complete and reliable AE signal, two AE probes were installed at the surface of the sample. In addition, the amplitude threshold of the AE was set to 45 dB to reduce the influence of noise on the Kaiser point determination.

5. Results and Discussion

5.1. Thickness of Denudation

In this study, the inflection (change of slope) in the curve, “cumulative AE versus time”, was assumed as the Kaiser point (the intersection of the pink dotted line and the red curve in Figure 6). The dependency of hit rate versus time was used as an auxiliary judgement to make the inflection easier to discriminate. The hit rate means the number of signals received per second, in this study. The stress value corresponding to the Kaiser point was assumed to be the “memorized” stress $\sigma_k$. The cumulative curves and frequency histograms of the AE signals are shown in Figure 6. Some AE activities were detected at stresses below the “memorized” stress $\sigma_k$, which is probably due to the
frictional movement along the existing microcracks or the noise generated by the loading system. When the peak (“memorized”) stress value was attained, the AE activity increased dramatically.

Figure 6. Cont.
The denudation thickness obtained by the vitrinite reflectance was slightly larger due to the older geological age. The denudation computed by AE in this study was 1600–1800 m and 1500–2000 m, respectively [15,16].

Many attempts have been made to reconstruct the denudation in the investigated area (Table 3). The denudation thickness obtained by the vitrinite reflectance since the Middle Jurassic was 1800–2000 m [17]. The denudation thicknesses obtained by the stratigraphic comparison and apatite fission track since the Late Cretaceous were 1600–1800 m and 1500–2000 m, respectively [15,16]. The results of previous studies are similar, and the denudation obtained by vitrinite reflectance was slightly larger due to the older geological age. The denudation computed by AE in this study was 1574–1794 m. In contrast to the methods presented up to now in the basin, the AE method did not rely on logging data or on the assumption that key parameters were required, but directly computed
the denudation thickness through experimentation. It seems that the AE method is easier to use and more applicable.

Table 2. The strata denudation estimated by AE.

<table>
<thead>
<tr>
<th>Sample ID</th>
<th>Kaiser Point/s</th>
<th>Memorized Stress/MPa</th>
<th>H/m</th>
<th>h/m</th>
<th>Δh/m</th>
<th>Average Δh/m</th>
</tr>
</thead>
<tbody>
<tr>
<td>ZK1-1</td>
<td>115</td>
<td>53.3</td>
<td>1977.8</td>
<td>290.0</td>
<td>1687.8</td>
<td>1608.1</td>
</tr>
<tr>
<td>ZK1-2</td>
<td>109</td>
<td>49.1</td>
<td>1818.5</td>
<td>1528.5</td>
<td>1716.9</td>
<td></td>
</tr>
<tr>
<td>ZK2-1</td>
<td>260</td>
<td>50.0</td>
<td>1851.9</td>
<td>135.0</td>
<td>1722.4</td>
<td></td>
</tr>
<tr>
<td>ZK2-2</td>
<td>265</td>
<td>50.6</td>
<td>1874.1</td>
<td>1531.7</td>
<td></td>
<td></td>
</tr>
<tr>
<td>ZK2-3</td>
<td>260</td>
<td>45.0</td>
<td>1666.7</td>
<td>1902.0</td>
<td></td>
<td></td>
</tr>
<tr>
<td>ZK2-4</td>
<td>290</td>
<td>55.0</td>
<td>2037.0</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>ZK3-1</td>
<td>172</td>
<td>53.4</td>
<td>1977.8</td>
<td>200.0</td>
<td>1727.8</td>
<td></td>
</tr>
<tr>
<td>ZK3-2</td>
<td>142</td>
<td>54.3</td>
<td>2011.1</td>
<td>1761.1</td>
<td>1794.4</td>
<td></td>
</tr>
<tr>
<td>YC4-1</td>
<td>60</td>
<td>42.5</td>
<td>1574.1</td>
<td>0.0</td>
<td>1574.1</td>
<td>1574.1</td>
</tr>
</tbody>
</table>

Table 3. Denudation thickness at the southeastern margin of the Ordos Basin measured by different methods.

<table>
<thead>
<tr>
<th>Methods</th>
<th>Geological Ages</th>
<th>Values/m</th>
</tr>
</thead>
<tbody>
<tr>
<td>Vitrinite reflectance [17]</td>
<td>Middle Jurassic</td>
<td>1800–2000</td>
</tr>
<tr>
<td>Stratigraphic comparison [15]</td>
<td>Late Cretaceous</td>
<td>1600–1800</td>
</tr>
<tr>
<td>Apatite fission track [16]</td>
<td>Late Cretaceous</td>
<td>1500–2000</td>
</tr>
<tr>
<td>Acoustic emission (this study)</td>
<td>Late Cretaceous</td>
<td>1574–1794</td>
</tr>
</tbody>
</table>

5.2. Effect of Denudation on In Situ Stress

Based on the estimated denudation thickness, the theoretical value of the current lateral pressure coefficient $\lambda$ was calculated, as shown in Table 4. The measured value of the current lateral pressure coefficient $\lambda'$ by the hydraulic fracturing method is also listed in Table 4 for comparison. The value of $\lambda$ is 4.0–8.3 with an average value of 6.1, and the value of $\lambda'$ is 1.2–3.5 with an average value of 2.3. Both the analytical value and measured value indicate that the lateral pressure coefficient increases due to the influence of strata uplift and denudation. However, compared with the measured results, the analytical value is much larger.

Table 4. Theoretical and measured values of the lateral pressure coefficient.

<table>
<thead>
<tr>
<th>Site ID</th>
<th>Depth /m</th>
<th>$\lambda$</th>
<th>$\lambda'$</th>
</tr>
</thead>
<tbody>
<tr>
<td>ZK1</td>
<td>310</td>
<td>4.0</td>
<td>1.7–1.9</td>
</tr>
<tr>
<td>ZK2</td>
<td>135</td>
<td>8.3</td>
<td>1.5–1.9</td>
</tr>
<tr>
<td>ZK3</td>
<td>200</td>
<td>6.1</td>
<td>2.6–2.8</td>
</tr>
</tbody>
</table>

The key assumption of the theoretical derivation is that the current surface is horizontal and somewhat different from the actual terrain. The current surface of the study area is undulating, and ZK1, ZK2 and ZK3 are all located on the topographic abrupt-change zone. For further studies on the impact of topography on in situ stress, a numerical simulation by FLAC$^3$D was adopted to analyze the process of strata denudation.

Five models were built to analyze the influence of ground fluctuation on stress by setting the arc surface at different angles (Figure 8). The numerical models were 3200 m wide. In order to ensure the same denudation thickness above the model center, the heights of different models were varied. The mechanics of the model was homogeneous elastic and the elastic modulus $E = 30$ GPa, Poisson’s ratio $\mu = 0.3$ and the bulk density $\gamma = 27$ kN/m$^3$. The generalized Hooke’s law was adopted as the governing equation to ensure the comparability between numerical simulation and theoretical
calculation. The normal displacement of the lower and surrounding boundary was constrained, and the upper boundary was a free surface. The rock mass was assumed to be in a hydrostatic stress state before the denudation, and the vertical stress and horizontal stress increased linearly with depth. The denudation of the upper strata was simulated by excavation.

Figure 8. The numerical models with different ground arc angles.

The simulation results are shown in Figure 9. When $\phi = 0^\circ$, the values of $\lambda$ at depths of 135 m, 200 m and 310 m are 7.4, 5.6 and 4.0, respectively. The results are very close to the theoretical values (Table 3). When the value of $\phi$ is constant, the value of $\lambda$ decreases as the buried depth increases. The closer to the ground, the greater change in $\lambda$. When the buried depth exceeds 1000 m, the value of $\lambda$ is approximately 1.4. As the value of $\phi$ increases, the amplitude of ground uplift increases and the value of $\lambda$ decreases at the same depth. When the value of $\phi$ increases to 120$^\circ$, the values of $\lambda$ at depths of 135 m, 200 m, and 300 m decrease to 1.9, 1.6, and 1.5, respectively. In this case, the numerical simulation results are close to the measured results, indicating that the topographical terrain is an important cause of the difference in the value of $\lambda$. Therefore, in the measured results, the ground height difference of ZK1 and ZK2 is large, so the value of $\lambda$ is small. Conversely, the ground height difference of ZK3 is small, so the value of $\lambda$ is large.

Figure 9. The lateral pressure coefficients versus depth of five models.
6. Conclusions

A method of computing the denudation thickness in sedimentary basins using the Kaiser effect was proposed. The mechanism and theory of the method was discussed. The method was simple and applicable to basins without large strata deflection.

The method was applied to reconstruct the denudation of the Ordos Basin, and the results were in good agreement with the reported values.

The influence of denudation and ground topography on the current basin's in situ stress field was discussed. From the discussion, the reason for the difference of the measured lateral pressure coefficient in the investigated area was revealed.

In future research, investigation of the evolutionary history of the basin should be conducted for a better understanding of the values computed by the AE method. Furthermore, the combination of the proposed method and other methods is recommended to provide more reliable results.

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References


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