Overview of Low-Temperature Heat Capacity Data for Zn$_2$(C$_8$H$_4$O$_4$)$_2$·C$_6$H$_{12}$N$_2$ and the Salam Hypothesis

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Received: 29 March 2019; Accepted: 9 May 2019; Published: 11 May 2019

Abstract: The review presents the progress in the analysis of low-temperature heat capacity of the metal-organic framework Zn$_2$(C$_8$H$_4$O$_4$)$_2$·C$_6$H$_{12}$N$_2$ (Zn-DMOF). In Zn-DMOF, left-twisted D$_3$(S) and right-twisted D$_3$(R) DABCO molecules (C$_6$H$_{12}$N$_2$) can transform into each other by tunneling to form a racemate. Termination of tunneling leads to a phase transition in the subsystem of twisted molecules. It is suggested that Zn-DMOF may be considered a model system to study the mechanisms of phase transitions belonging to the same type as hypothetical Salam phase transitions.

Keywords: heat capacity; metal-organic framework; triethylenediamine (DABCO) molecules; racemate; Salam hypothesis

1. Introduction

According to the Salam hypothesis, a small parity-violating energy difference (PVED) between amino acid molecules along with the Bose-Einstein (BE) condensation, makes the less stable right enantiomers tunnel into the more stable left enantiomers, by changing their structural forms. This process was described as a second-order phase transition, which is an analog of the Bardeen-Cooper-Schrieffer (BCS) phase transition; therefore, physical properties such as heat capacity and magnetic susceptibility should change during this phase transition according to the BCS laws [1,2]. Even though no such phase transitions have been found in the crystals of known amino acids, the building material of living organisms, the systems demonstrating the BE condensation of chiral molecules are still of interest. A model of BE condensation was developed for a gas of non-interacting chiral molecules to determine the PVED contribution from low-temperature heat capacity data [3]. The present review summarizes low-temperature heat capacity data, which indicate that the BE condensation may work in a subsystem of triethylenediamine (DABCO) molecules (C$_6$H$_{12}$N$_2$) in the metal-organic framework Zn$_2$(C$_8$H$_4$O$_4$)$_2$·C$_6$H$_{12}$N$_2$ (Zn-DMOF) and that the mechanism of Salam phase transitions remains possible. In Zn-DMOF, the enantiomers are represented by left- and right-twisted DABCO molecules, which transform into each other as a result of tunneling.

2. Structure of DABCO Molecule in Zn$_2$(C$_8$H$_4$O$_4$)$_2$·C$_6$H$_{12}$N$_2$

Triethylenediamine (DABCO) appears in the form of two conformational isomers with D$_{3h}$ and D$_3$ point group symmetries, depending on intermolecular interactions. Also, a quasi-D$_{3h}$ form of DABCO is possible due to strong vibrations of the molecule around the C$_3$ axis. The molecules with the D$_3$ symmetry, which can be left-twisted D$_3$(S) or right-twisted D$_3$(R), are considered to be chiral isomers (enantiomers) [4].
Above 223 K, the crystal structure of the metal-organic framework Zn-DMOF is tetragonal, with space group P4/mmm [5]. The horizontal planes are formed by terephthalate anions \([C_8H_4O_4]^{2−}\) (BDC\(^{2−}\)) which are linked to \([Zn_2]\) pairs by carboxylate anions. The vertical edges are formed by DABCO molecules (linkers), the point symmetry of which does not contain a 4-fold rotational symmetry axis (Figure 1). This is the reason why DABCO molecules are orientationally disordered; moreover, D\(_3\)(S) and D\(_3\)(R) forms can transform into each other (by activation or tunneling) [4,6]. Calorimetry, nuclear magnetic resonance, and X-ray structural analysis data provide evidence of the presence of phase transitions in Zn-DMOF at ~14, ~60, and ~130 K [7–12].

![Figure 1](image_url)

**Figure 1.** The structure of \(Zn_2(C_8H_4O_4)_2\cdotC_6H_{12}N_2\) (Zn-DMOF), space group P4/mnm. Positions of carbon atoms in triethylenediamine (DABCO) molecules are disordered [5]. Hydrogen atoms are omitted for clarity. DABCO and BDC\(^{2−}\) structures are shown in the insets. (Compiled from Figure 1 in [10] and Figure 1 in [1]).

### 3. Mobility of DABCO Molecules in \(Zn_2(C_8H_4O_4)_2\cdotC_6H_{12}N_2\)

In Zn-DMOF, BDC\(^{2−}\) anions and DABCO molecules are involved in activation mobility. According to the nuclear magnetic resonance (NMR) studies of the activation mobility of BDC\(^{2−}\) anions, the \([C_8H_4] \) groups of BDC\(^{2−}\) anions rotate about the C\(_2\) axis through an angle of 180° (flipping) [13–15]. No effect of BDC\(^{2−}\) flipping on the mobility of DABCO in Zn-DMOF was discovered [13,16,17].

According to the detailed analysis of the temperature behavior of the spin-lattice relaxation times of hydrogen nuclei (\(^1H\) NMR \(T_1(T)\)), \(D_3\)(S) and \(D_3\)(R) forms of DABCO can make up a racemic mixture, and their mirror symmetry may be broken during the phase transition at ~60 K [6,11,12]. The time decay of nuclear magnetic moments (M) of hydrogen atoms in DABCO was analyzed to find the distribution of DABCO molecules over different states. Above ~165 K, the time decay of M is a single exponential function characterized by a single value \(T_1\). In this case, DABCO molecules with \(D_3\) and \(D_{3h}\) symmetries reorient similarly, their proton spins constitute a single spin system, the activation barrier is equal to ~4 kJ/mol. Between 165 and 60 K, the time decay of M is a biexponential function containing two values \(T_1\), each corresponding to a certain fraction of nuclear spins in M. The ratio of these fractions is estimated to be \(\psiM/\phiM\). The \(\psiM\) fraction corresponds to \(^1H\) spins of DABCO molecules of the \(D_{3h}\) symmetry, the mobility of which is characterized by a short value \(T_{1\psi}\). The \(\phiM\) fraction corresponds to \(^1H\) spins of the sum of S- and R-forms of DABCO. In this case, these forms are indistinguishable due to tunneling transitions, so the above fraction \(\phiM\) represents the racemic state of DABCO molecules and is characterized by a single value \(T_{1\phi}\) of a larger magnitude. During
the phase transition at 60 K and down to 25 K, the behavior of T_{1L} is interpreted as the termination of tunneling between energy degenerate quantum states of R- and S- forms of DABCO, and their fractions in M remain equal to each other (1/3:1/3). Below 25 K, the decay M is nonexponential and can be conventionally characterized by three values T_{1}. So, the phase transition at ~14 K is associated with the redistribution of DABCO molecules over different energy states characterized by contributions \( \frac{1}{4} \cdot M \), \( \frac{1}{4} \cdot M \), and \( \frac{1}{2} \cdot M \) and the appearance of a chiral polarized state [11].

Note that the racemate state was also reported for 1,4-bis(carboxyethynyl)bicyclo[2.2.2]octane (BABCO) molecules, which are analogs of DABCO. It was shown that the ratio of left- and right-twisted forms of BABCO can be controlled by light [18,19]. The disorder of DABCO and its analogs, which causes phase transitions, is also observed in other systems [20–22].

Thus, the \(^1\)H NMR T_{1}(T) data testify that phase transitions are associated with the mobility of DABCO molecules. The analysis of the function M provides quantitative data on the distribution of DABCO molecules over different states at various temperatures. However, it is still unclear how these states are structurally realized in Zn-DMOF. Low-temperature heat capacity data for Zn-DMOF may be used to clarify this problem.

4. Low-Temperature Heat Capacity in Zn\(_2\)(C\(_8\)H\(_4\)O\(_4\))\(_2\)C\(_6\)H\(_{12}\)N\(_2\)

All phase transitions in Zn-DMOF (at ~14, ~60, and ~130 K) are second-order phase transitions [10]. Table 1 shows the maximum values of the anomalous parts of heat capacity \( \Delta C_p = C_p - C_p^1 \), where \( C_p \) is the heat capacity of the substance and \( C_p^1 \) is the regular part of heat capacity “in the absence of phase transitions”. The entropy of the phase transitions is shown in Table 2.

<table>
<thead>
<tr>
<th>P (P \cdot 10^5 Pa)</th>
<th>~14 K</th>
<th>~60 K</th>
<th>~130 K</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.51</td>
<td>6.0 ± 0.4</td>
<td>8.0 ± 0.2</td>
<td>23.0 ± 0.3</td>
</tr>
<tr>
<td>1.52</td>
<td>5.0 ± 0.4</td>
<td>11.0 ± 0.2</td>
<td>23.0 ± 0.3</td>
</tr>
</tbody>
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<table>
<thead>
<tr>
<th>T_{c} (K)</th>
<th>~14</th>
<th>~60</th>
<th>~130</th>
</tr>
</thead>
<tbody>
<tr>
<td>P</td>
<td>ΔS/R</td>
<td>ΔS/R</td>
<td>ΔS/R</td>
</tr>
<tr>
<td>0.51</td>
<td>0.42 ± 0.05</td>
<td>0.14 ± 0.02</td>
<td>0.30 ± 0.04</td>
</tr>
<tr>
<td>1.52</td>
<td>0.28 ± 0.04</td>
<td>0.23 ± 0.02</td>
<td>0.30 ± 0.04</td>
</tr>
</tbody>
</table>

The obtained data indicate that the absorbed atoms of \(^4\)He affect the states of D\(_3\)(S) and D\(_3\)(R) forms of DABCO (phase transitions ~14 and ~60 K) and do not affect the ordering and disordering of BDC\(_{2}^-\) anions during the phase transition at 130 K. This result can be explained by the fact that the structure of DABCO is flexible [23,24] as compared to that of BDC\(_{2}^-\) anions and can therefore be deformed in the presence of adjoining \(^4\)He atoms, whereas the structure of BDC\(_{2}^-\) anions remains unchanged.

The temperature dependence of heat capacity of Zn-DMOF is almost linear between the phase transitions at ~14, ~60, and ~130 K and above 130 K [8,10,11] to indicate the presence of a one-dimensional elastic continuum [8,12]. Figure 2 shows the comparison of experimental [8] and tabulated (Tarasov model) [25,26] heat capacity values using the fitting parameters obtained in [11].
was interpreted as an order-disorder phase transition associated with a change in the relative spatial vibrations in the chain. The repeated vibrating unit along the lattice vibrational modes become three-dimensional [8,25].

The temperature dependence of the volumetric heat capacity \( C_v \) is expressed in terms of two relationships, \( \frac{C_v}{3Nk} \) and \( T/T_m \), where \( N \) is the number of repeated vibrating units, \( T_m = \frac{h\nu_m}{k} \), \( h \) is the Planck constant, \( k \) is the Boltzmann constant, and \( \nu_m \) is the maximum frequency of stretching vibrations in the chain. The repeated vibrating unit along the \( c \) axis in Zn-DMOF consists of two Zn atoms and one DABCO molecule (\( \{\text{Zn}_2\text{DABCO}\} \)) [5].

Experimental smoothed values \( C_p \) obtained as functions of temperature in [8] were represented on a log-log plot and fitted by best tabulated values \( C_v/(3Nk) \) for each \( T/T_m \) assuming that \( C_p - C_v \) is small [27] (Figure 3). As a result, it was found that the vibrating chain is formed by \( \sim 38-39 \) \( \{\text{Zn}_2\text{DABCO}\} \) units above 130 K, by \( \sim 30 \) units at 60–130 K, and by \( \sim 12 \) units at 14–60 K (Table 3). Below 14 K, the heat capacity obeys the \( \sim T^3 \) law (Figure 3) to indicate that interchain interactions become stronger and the lattice vibrational modes become three-dimensional [8,25].
The values \( \nu_m \sim 1250 \text{ cm}^{-1} \) and \( \nu_m \sim 765 \text{ cm}^{-1} \) fall into the region of stretching vibrations of DABCO, and \( \nu_m \sim 285 \text{ cm}^{-1} \) fall into the region of Zn-N and Zn-Zn stretchings (Table 3) [28]. Thus, the obtained values \( \nu_m \) correspond to the stretchings in the chains, in accordance with the model [27].

As can be seen, the values obtained from the analysis of \( C_p \) for \([\text{Zn}_2\text{DABCO}]\) units correlate with fractions (M) in different phases of Zn-DMOF, if N and M values above 130 K are taken as a unit (Table 3). The obtained quantitative agreement between NMR data and the analysis of heat capacity suggests the following conclusions. Above 130 K, the chains consisting of \(~39\) \([\text{Zn}_2\text{DABCO}]\) units contain DABCO molecules with D\(_3\)(S), D\(_3\)(R), and D\(_{3h}\) symmetries. At 60-130 K, the longest chains \(~29\) \([\text{Zn}_2\text{DABCO}]\) units contain only D\(_3\) forms in the racemic state. The vibrations of these chains make the largest contribution to the heat capacity, while the vibrations of the chains consisting of D\(_{3h}\) forms make no contribution practically, due to their shorter size. Finally, below \~60 K there are three types of chains \(~12\) \([\text{Zn}_2\text{DABCO}]\) units) of the same length but containing three different DABCO forms (D\(_3\)(S), D\(_3\)(R), and D\(_{3h}\)). The size of the chains below 14 K cannot be estimated, since the heat capacity is no more linear at these temperatures.

5. Heat Capacity Behavior during the Phase Transition at 60 K and the Salam Hypothesis

The PVED values for the DABCO molecule and the \([\text{Zn}_2\text{DABCO}]^{4+}\) cation were obtained in [29]. The difference between the energies of mirror isomers is as small as \(-5\cdot10^{-16} \text{ kJ/mol} \sim 5.2\cdot10^{-18} \text{ eV}\) for DABCO and an order of magnitude higher \(-5\cdot10^{-15} \text{ kJ/mol} = 5.2\cdot10^{-17} \text{ eV}\) for the \([\text{Zn}_2\text{DABCO}]^{4+}\) cation. Therefore, the contribution of PVED increases in the presence of Zn\(^{2+}\) cations and is determined mainly by the contribution of zinc cations. This contribution increases if Zn\(^{2+}\) cations are replaced by heavier cations Cd\(^{2+}\) and Hg\(^{2+}\) [30]. Hence, it can be assumed that the PVED breaking of mirror
symmetry between D3(S) and D3(R) forms of DABCO may be caused by their external environment in the Zn-DMOF structure.

If the symmetry breaking during the phase transition at ~60 K takes place in the chains containing only D3(S) and D3(R) forms of DABCO, then, according to the Salam hypothesis, the behavior of heat capacity must correspond to the behavior of heat capacity during the superconducting phase transition [1,2].

In fact, it was discovered that the temperature behavior of heat capacity of Zn-DMOF is an exponential function below ~60 K (Figure 4) [31]. The behavior of heat capacity in the region of second-order phase transitions was studied using the values of the anomalous part of heat capacity ΔCp3 = Cp3 − CpL3, and the behavior of CpL3 was described using the Tarasov model [25]. Figure 3 shows the obtained ΔCp values.

![Figure 4. Temperature dependence of ΔCp (in gram-atom units) for Zn-DMOF (left) and ΔCp plotted as a function of 1/T below ~60 K (right). ΔCp is shown on the logarithmic scale (according to the data from Figures 2 and 4 in [31]).](image-url)

The region below ~60 K is of particular interest, since it is associated with the termination of tunneling between D3(S) and D3(R) forms of DABCO as the temperature decreases [11,12]. Based on the hypothesis suggested in [1,2], a study was carried out to verify the compliance of heat capacity ΔCp to the exponential dependence ~ exp(−Δ/3 T), where Δ = 1.76 Tc (Δ is the energy gap at 0 K). Figure 4 shows ΔCp as a function of 1/T in the temperature region 15 K < T < 60 K. As can be seen, a good agreement with the exponential law is achieved for the parameter Δ equal to ~56 K (or ~5 × 10−3 eV) [31]. The obtained value Δ turned out to be almost twice as small as expected (~106 K for Tc = 60 K). There is probably some inaccuracy with the parameters determining function CpL, which may cause the error of determining the Δ value. However, the detected exponential behavior of ΔCp below 60 K signifies the presence of a BE condensation. The amplitude of ΔCp during the phase transition at is 60 K = 10 J/mol/K (Table 1), which corresponds to the thermal energy jump (ΔCp−Tc) ≈ 600 J/mol (or 6 × 10−3 eV), which agrees well with Δ. The value of (ΔCp−Tc) is 1015 times bigger than the PVED (~5.2 × 10−18 eV) of one DABCO molecule, but it can be explained by the phenomenon of BE condensation [1,2].

However, neither Cp data nor 1H NMR T1(T) data show any energy difference between D3(S) and D3(R) forms of DABCO below 60 K (according to the Salam hypothesis, the ratio between D3(S) and D3(R) forms of DABCO should change). Apparently, the energy difference between D3(S) and D3(R) forms remains negligible and can be observed only at lower temperatures, when the thermal energy of the crystal approaches zero [6]. Indeed, according to 1H NMR T1(T) data, the decay M as a function of time shows anomalous behavior below 25 K [12], but it is not manifested in the Cp behavior until the phase transition at ~14 K.
6. Conclusions

The Salam hypothesis is considered impossible during the phase transitions in amino acid crystals, since the barriers between L- and D-forms of alanine involve intramolecular bond breaking and are as high as ~200 kJ/mol [32]. In Zn-DMOF, the activation barrier between D$_3$(S) and D$_3$(R) forms of DABCO is estimated to be ~4 kJ/mol [7] and 5 kJ/mol [27] according to NMR data and quantum chemical calculations, respectively. Thus, this barrier is ~40 times smaller than the barrier between L- and D-forms of alanine [30]. The NMR data indicate the presence of tunneling between D$_3$(S) and D$_3$(R) forms of DABCO. The tunneling splitting for the DABCO molecule in the free state is estimated to be ~6 cm$^{-1}$ (~8.6 K) [24], which is comparable to the temperature range of observed phase transitions in Zn-DMOF. The behavior of heat capacity below 60 K corresponds to the heat capacity during the BE condensation. According to the NMR data, still lower temperatures are associated with a redistribution of DABCO with different symmetries over energy states to form a chiral polarized state. In the model system [Zn$_2$DABCO]$^{3+}$, the R-form is most favorable due to the PVED [29,30], but it is currently unclear which symmetry of the chains built of [Zn$_2$DABCO] units corresponds to the most energetically favorable state. The method of resonant X-ray diffraction with circularly polarized X-rays [33] or optical methods seem to be most preferable for use at low and extra-low temperatures.

We believe that metal-organic frameworks or related compounds containing enantiomers in the racemic state (not necessarily amino acid molecules) may be considered as model systems to study Salam phase transitions. Our studies were aimed at revealing the effects of chirality stabilization in isomeric molecules in solids at low temperatures with the goal of exploring the idea of the cold scenario of life origin on the Earth.

Author Contributions: S.K., analysis of heat capacity data, writing and editing of the manuscript, M.R., editing of Χ-rays [33] or optical methods seem to be most preferable for use at low and extra-low temperatures.

Symmetry 2019, 11, 657

Funding: This research received no external funding.

Conflicts of Interest: The authors declare no conflict of interest.

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