Wave Height Attenuation and Flow Resistance Due to Emergent or Near-Emergent Vegetation

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Abstract: Vegetation plays a pivotal role in fluvial and coastal flows, affecting their structure and turbulence, thus having a strong impact on the processes of transport and diffusion of nutrients and sediments, as well as on ecosystems and habitats. In the present experimental study, the attenuation of regular waves propagating in a channel through flexible vegetation is investigated. Specifically, artificial plants mimicking Spartina maritima are considered. Different plant densities and arrangements are tested, as well as different submergence ratios. Measurements of wave characteristics by six wave gauges, distributed all along the vegetated stretch, allow us to estimate the wave energy dissipation. The flow resistance opposed by vegetation is inferred by considering that drag and dissipation coefficients are strictly related. The submergence ratio and the stem density, rather than the wave characteristics, affect the drag coefficient the most. A comparison with the results obtained in the case when the same vegetation is placed in a uniform flow is also shown. It confirms that the drag coefficient for the canopy is lower than for an isolated cylinder, even if the reduction is not affected by the stem density, underlining that flow unsteadiness might be crucial in the process of dissipation.

Keywords: wave attenuation; energy dissipation; drag coefficient; flexible vegetation; Spartina maritima

1. Introduction

Coastal wetlands and saltmarshes are fundamental for sustaining ecosystems and preserving coasts from erosion and flooding due to storm surge and waves [1–3]. In the last century a widespread reduction in these areas has been observed in countries where short-sighted human activities and an increase of the sea level have strongly affected the morphodynamic equilibrium of intertidal environments [4,5]. Since that vegetation plays a fundamental role in the preservation and restoration of this habitat by controlling the coastal hydrodynamics, an effective strategy to counteract this trend is to promote the development of aphyte plants in wetlands. In particular, vegetation attenuates the action of waves, slows down the flow, and promotes diffusion and deposition processes [6–10]. Accordingly, it (i) enhances particle removal and water quality [11–13]; (ii) positively affects the hydrochory and nautochory of seeds and organic matter [14–17]; (iii) reduces sediment erosion and resuspension, while enhancing sediment deposition [18–20]; and (iv) creates preferred paths for tracers’ dissipation processes [21–23].

This is one of the main reasons for investigations of the interaction between vegetation and flow. Wave attenuation has been widely investigated in controlled laboratory experiments, where vegetation has often been mimicked by rigid dowels or artificial plants [24–29], as well as in field observations, where it has been limited to cross-shore transects. [30–33]. Despite the large amounts of theoretical
and experimental results available in the literature, the interaction of waves with a vegetated canopy still deserves further study. In particular, the drag coefficient, which represents/includes the impact of several phenomena such as sheltering, bed interaction, and non-uniform velocity distribution [34], needs to be assessed.

Wave attenuation resulting from wave–vegetation interaction depends on hydrodynamic conditions such as the incident wave height and period, and water depth, as well as on plant properties such as impact area, density, and flexibility. Many studies focused on different species of plants commonly diffused on saltmarshes and along coastal environments, in order to quantify the plant-specific attenuation of the waves, e.g., *Laminaria hyperborea*, *Spartina alterniflora*, and *Macrocystis pyrifera* [35–37]. Although *Spartina maritima* is a common grass in wetlands and saltmarshes [38,39], only a few experimental studies have considered this type of vegetation [40].

The present work describes and discusses the results of an experimental investigation aimed at studying the flow resistance and wave attenuation capability of *Spartina maritima*. Experiments are carried out in the laboratory under controlled wave conditions; plastic plants mimicking *Spartina maritima* are arranged on the bottom of the wave-flume and experiments consider either emergent or submerged canopy, as well as different plant density. In order to compare and relate resistance characteristics induced by vegetation (e.g., the drag coefficient) under wave and steady flow conditions, additional experiments are performed in steady flow conditions using the same plastic plants, with varying density.

2. Materials and Methods

2.1. Experimental Setup

To investigate the wave attenuation induced by *Spartina maritima*, experiments are carried out in a wave flume 35.0 m long, 1.0 m wide, and 1.3 m deep; an HR Wallingford paddle generates monochromatic waves. At the opposite end of the flume, a wave absorber damps incident waves (see Figure 1). The wave absorber is made of a sloping (1:3) porous metal plate, covered with a needle-punched geogrid, which ensures, in the present experiments, a reflection coefficient smaller than 10%.

![Figure 1. Scheme of the wave apparatus setup. Distances are in meters.](image)

Fifteen meters downstream of the wave generator, a 16 m long false plane bottom houses the vegetation canopy; the 4 m long reach occupied by vegetation starts 8 m downstream from the upstream edge of the false plane. The artificial plants are inserted in adjacent PVC panels, which are drilled in order to fix the main stem of the plant into holes that are equally spaced 4 cm apart both longitudinally and transversally (see Figure 2a).
The artificial plants chosen for mimicking the real *Spartina maritima* are the same used in other studies aimed at investigating the transport and diffusion of floating seeds in partially emerged saltmarsh vegetation [41,42]. They are plastic plants 15 cm high, with \( n_s = 120 \) stems having a diameter, \( d \), of approximately 2.0 mm. Real *Spartina* is compared to the present artificial plants in Figure 2b.

Six wave gauges measure the free surface oscillation in the flume at 20 Hz sampling rate. Five probes are placed at 0.00 m, 0.66 m, 1.32 m, 2.66 m and 4.00 m from the beginning of the vegetated area, and they recorded the wave attenuation along the canopy, whilst the sixth probe, located 1.5 m upstream of the vegetation field, recorded the approaching wave height, \( H_0 \) (see Figure 1).

Two series of tests are performed. In the first series, waves attenuation is recorded considering four scenarios characterized by different plant configurations with densities \( n_p = 43.75, 84.5, 156.25 \) and 312.5 plant/m\(^2\), arranged as in Figure 3. For each plant configuration, experiments are performed at five water depths, namely \( h = 10, 15, 20, 25, \) and 30 cm. The wave period, \( T \), ranges between 0.7 and 1.4 s and the wave height, \( H_0 \), is selected so that the slope \( H_0/L \) (with \( L \) the wave length) ranges between 0.01 and 0.09. The hydrodynamic conditions are summarized in Table 1.

In the second series of experiments, the configuration having the greatest vegetation density, i.e., \( n_p = 312.5 \) plant/m\(^2\) is investigated in depth. For each of the water depths listed above, nine wave conditions, resulting from the combination of 3 wave periods, \( T = 0.8, 1.0 \) and 1.2 s, and three wave slopes, \( H_0/L = 0.03, 0.05 \) and 0.08, are investigated (for details see Table 1).

### Table 1. Summary of the tests in wave condition.

<table>
<thead>
<tr>
<th>Series 1</th>
<th>( n_p ) (plant/m(^2))</th>
<th>( n ) (stem/m(^2))</th>
<th>( h ) (cm)</th>
<th>( T ) (s)</th>
<th>( H_0/L )</th>
</tr>
</thead>
<tbody>
<tr>
<td>43.75</td>
<td>5250</td>
<td>10 ( \div ) 30</td>
<td>0.7 ( \div ) 1.4</td>
<td>0.01 ( \div ) 0.09</td>
<td></td>
</tr>
<tr>
<td>84.50</td>
<td>10,140</td>
<td>10,140</td>
<td>10 ( \div ) 30</td>
<td>0.7 ( \div ) 1.4</td>
<td>0.01 ( \div ) 0.09</td>
</tr>
<tr>
<td>156.25</td>
<td>18,750</td>
<td>18,750</td>
<td>10 ( \div ) 30</td>
<td>0.7 ( \div ) 1.4</td>
<td>0.01 ( \div ) 0.09</td>
</tr>
<tr>
<td>312.50</td>
<td>37,500</td>
<td>37,500</td>
<td>10 ( \div ) 30</td>
<td>0.7 ( \div ) 1.4</td>
<td>0.01 ( \div ) 0.09</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Series 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>312.50</td>
</tr>
<tr>
<td>37,500</td>
</tr>
<tr>
<td>10 ( \div ) 30</td>
</tr>
</tbody>
</table>
In order to compare and relate resistance characteristics induced by vegetation under wave and in steady flow conditions, additional experiments are performed in uniform flow condition (UF experiment). These tests are carried out in a 6.0 m long, 0.3 m wide, and 0.5 m high tilting flume, in which the same plastic plants are arranged over a 3 m long reach. To ensure uniform flow conditions, a magnetic flowmeter accurately measures the bulk flow rate, and constant water depth is achieved by adjusting the bottom slope and a downstream weir.

Four different plant arrangements are investigated, with \( n_p \) equal to 78.125, 156.25, 312.5, and 625 plant/m\(^2\), respectively (see Figure 4). The bulk flow velocity is approximately 6.7 cm/s in all experiments, whereas, for each plant density, three water depths are considered, i.e., \( h = 5 \text{cm}, 10 \text{cm}, \text{and} 15 \text{cm} \) (Table 2). This means that the UF experiment investigate the behavior of flexible emergent vegetation \( (l_s \geq h) \).

![Figure 4](image-url)

**Figure 4.** Plants distribution for the uniform flow tests: (a) plants density \( n_p = 78.125 \text{ plant/m}^2 \); (b) plants density \( n_p = 156.25 \text{ plant/m}^2 \); (c) plants density \( n_p = 312.5 \text{ plant/m}^2 \); and (d) plants density \( n_p = 625 \text{ plant/m}^2 \).

<table>
<thead>
<tr>
<th>Uniform Flow Test</th>
<th>( n_p ) (plant/m(^2))</th>
<th>( n ) (stem/m(^2))</th>
<th>( h ) (cm)</th>
<th>( T ) (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>78.125</td>
<td>9375</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>156.25</td>
<td>18,750</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>312.50</td>
<td>37,500</td>
<td></td>
<td>5; 10: 15</td>
<td>-6.7</td>
</tr>
<tr>
<td>625.00</td>
<td>75,000</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

### 2.2. The Theoretical Model

The energy of waves propagating through and over vegetation is dissipated due to the action of waves on vegetation [24,26,27]. The general form of the energy conservation equation is

\[
\frac{\partial E}{\partial x} c_g = -\epsilon_v
\]

where \( E \) is the wave energy, \( c_g \) is the wave group velocity and \( \epsilon_v \) is the time-averaged rate of energy dissipation per unit length induced by vegetation.

On assuming \( c_g \) to be constant and recalling that \( E = \rho g H^2 / 8 \), with \( \rho \) the water density, \( g \) the gravity, and \( H \) the wave height, the above equation can be rewritten as

\[
\frac{\partial H^2}{\partial x} = \frac{-8 \epsilon_v}{\rho g c_g}
\]
The dissipation rate $\varepsilon_v$ is commonly estimated assuming the linear wave theory \[6,26,29\]. Mendez and Losada \[26\] obtained the following expression for $\varepsilon_v$:

$$
\varepsilon_v = \frac{2}{3\pi} \rho C_D d n \left( \frac{k g H_0^3}{2\sigma} \right)^3 \frac{3 \sinh^3(k l_s^*) + 3 \sinh(k l_s^*)}{3k \cosh^3(k h)} H^3
$$

where $C_D$ is the drag coefficient of the single stem, $l_s^*$ is the submerged stem height that is equal to $l_s$ in submerged condition (i.e., $l_s/h \leq 1$), and to $h$ in emergent conditions (i.e., $l_s/h > 1$), and $n = n_p n_s$ is the average stems density, i.e., number of stems per unit area, $k = 2\pi/L$ is the wave number, and $\sigma = 2\pi/T$ is the angular frequency.

In the present experiments all the parameters of Equation (3) are assumed to be constant, hence Equation (2) has the following analytical solution:

$$
H = \frac{H_0}{1 + \frac{K_v}{2} x}
$$

where $H_0$ is the incident wave height at $x = 0$, corresponding to the upstream cross section of the vegetated reach, and $K_v$ is the dissipation coefficient due to the vegetation

$$
K_v = \frac{8}{9\pi} \rho C_D d n \left( \frac{k g H_0^3}{2\sigma} \right)^3 \frac{3 \sinh^3(k l_s^*) + 3 \sinh(k l_s^*)}{3k \cosh^3(k h)} H_0
$$

Alternatively, Kobayashi et al. \[6\] proposed to linearize the energy equation by approximating $H^3 \approx H^2 H_0$ in Equation (3). With this assumption, the wave height decreases exponentially, as follows:

$$
H = H_0 e^{-\frac{K_v}{2} x}
$$

Both hyperbolic and exponential models, expressed by Equations (4) and (6) respectively, are commonly adopted in the literature to describe the wave attenuation in the presence of vegetation. Nevertheless, the results of the present investigations clearly show that the linearized solution fits the experimental results better.

The drag coefficient, $C_D$, is the only unknown of the problem, hence it can be inferred from experimental data. Specifically, in the present experiments, $K_v$ is estimated by minimizing the difference between observed and expected wave attenuation according to Equation (6), then, $C_D$ is estimated from Equation (5).

In the literature, the drag coefficient $C_D$ is expressed as a function of either the Reynolds number, $Re$, or the Keulegan–Carpenter number, $KC$. The stem Reynolds number is

$$
Re = \frac{u_c d}{\nu}
$$

where $\nu$ is the water kinematic viscosity and $u_c$ is the horizontal velocity amplitude averaged over the stem height, which can be approximated by the velocity at the top of the canopy, when $kl_s^*$ is relatively small, i.e.,

$$
u_c = \frac{k g H_0 \cosh(k l_s^*)}{2\sigma \cosh(k h)}
$$

$u_c$ is representative of the velocity magnitude acting on the stem, notwithstanding it is approximately the actual velocity at the top of the canopy, since the vertical velocity profile with submerged vegetation can differ quite a bit from the profile predicted by the linear wave theory \[43\].

The Keulegan–Carpenter number, also called the period number, is:

$$
KC = \frac{u_c T}{d}
$$
Most experimental studies express the drag coefficient as a power law of either $Re$ or $KC$:

$$C_D = \alpha_{Re} \cdot Re^{-\beta_{Re}}, \quad C_D = \alpha_{KC} \cdot KC^{-\beta_{KC}}$$  \hspace{1cm} (10)

where $\alpha_i$ and $\beta_i$ are calibration coefficients.

In the case of vegetated uniform flow, the literature provides many bulk expressions to estimate the drag coefficient, which are based on experimental, theoretical, and computational investigations [25,44–46].

Among the many available models, the simple model created by Nepf [25] for the case of a dense array of emergent rigid cylinders provides reasonable and effective results [46,47]. Therefore, this approach is used in the present study for the estimation of $C_D$ in the uniform flow experiments. The force balance in the flow direction is

$$\frac{\tau_b}{\rho} + \frac{1}{2}C_D \rho d^2 \frac{l_s}{d} U^2 = gh \frac{\partial h}{\partial x}$$  \hspace{1cm} (11)

where $\tau_b$ is the bed shear stress and $U$ is the flow velocity averaged over the stem height. In the present case, the stem density is very high and drag resistance turns out to be much greater than bed shear stress; accordingly, $\tau_b$ is neglected in Equation (11). In addition, only the emergent vegetation condition is investigated, so that $U$ is the bulk flow velocity. The choice to perform the UF experiment with only emergent vegetation is essentially due to the large variability of flow velocity in the vertical direction when the vegetation is submerged [48,49]. This aspect is not taken into due account by the $C_D$ formulation in Equation (11).

The calibration approach used by Mendez and Losada [26] has been chosen for processing the data to obtain $C_D$. Based on the calibration approach, the experimental value of $C_D$ is estimated from the reduced wave height, which reflects the dissipation of wave energy, using Equations (5) and (6).

3. Results and Discussion

Figure 5 shows an example of wave attenuation when the vegetation density is $n_p = 312.5$ plant/m$^2$, and the wave period and slope are $T = 1$ s and $H_0/L = 0.08$. The attenuation depends on the ratio between vegetation height and water depth, $l_s/h$. Since most energy dissipation occurs in the lower part of the water column obstructed by the stems, the capability of damping turns out to be inversely related to the degree of plant submersion. The overall reduction of $H$ over the 4 m of Spartina for $l_s/h = 1.5$, i.e., for partially emergent condition, is nearly 90% whereas, for $l_s/h = 0.5$, i.e., for submerged conditions, the reduction is smaller than 50%.

![Figure 5. Wave height $H$ along the vegetated reach when density is $n_p = 312.5$ plant/m$^2$ and the relative vegetation height is in the range $0.5 \leq l_s/h \leq 1.5$. Wave period and slope are $T = 1$ s and $H_0/L = 0.08$. Circles denote the experimental data, dashed line are the modeled wave attenuation either with (a) the exponential model given by Equation (6); or (b) the hyperbolic model given by Equation (4).]
Figure 5a,b show the experimental data fitted by the exponential law (6) and by the hyperbolic law (4), respectively. The root mean square error due to the hyperbolic law, $RMSE_h$, is 3.2 mm, while a smaller $RMSE_e = 1.7$ mm is estimated for the exponential law. The comparison between predicted and measured wave height clearly shows that the exponential law better fits the data. For this reason, the exponential model of wave height attenuation is used in the following discussion.

Also, the stem density, $n$, controls wave attenuation, as indicated by Equation (5). Figure 6 shows the estimated coefficient $K_v$ as a function of $n$. Here, $K_v$ values are the average of all the runs having the same stem density and relative vegetation height, $l_s/h$. Interestingly, Figure 6 shows that $K_v$ increases less than linearly with $n$, in spite of what was indicated by Equation (5); this important point is discussed later in the text.

![Figure 6. Coefficient of dissipation, $K_v$, as a function of stem density, $n$. Average $K_v$ are computed for $l_s/h = 1.5$ (blue circles), $l_s/h = 1.0$ (red circles), $l_s/h = 0.75$ (green circles), and $l_s/h = 0.5$ (orange circles). Bars show the range of variability of $K_v$ in the present experiments.](image)

The estimated values for $K_v$ are used, with Equation (5), to estimate the stem drag coefficient, $C_D$. The latter is shown in Figure 7 as a function of the Reynolds number, $Re$, and the Keulegan–Carpenter number, $KC$. The stem drag coefficient reduces with $Re$ as well as with $KC$ increasing, and can be fitted to the following empirical formulas:

$$C_D = 35.6 \cdot Re^{-0.78} \quad (12)$$

$$C_D = 6.5 \cdot KC^{-0.64} \quad (13)$$

A sensitivity analysis is carried out considering the error due to the measure of the water depth, $h$. Such variation has been estimated at $\pm 0.1$ cm and slightly affects the $C_D$s, whose maximum variation is about $\pm 2\%$ in the tests performed with the minimum water depth (i.e., $h = 10$ cm).

The coefficients of determination for Equations (12) and (13) are $R^2 = 0.68$ and 0.59, respectively; hence the regression of computed $C_D$ provides a better correlation with $Re$ compared to $KC$. However, given the observed scatter of data, the above relationships cannot be used to safely estimate the drag coefficient.

There are two main reasons for this low accuracy. Firstly, the exact definition of the plant impact area per unit of height. This length is the cylinder diameter when the vegetation is simulated by rigid dowels. In the case of Spartina maritima, which is a porous barrier to the flow where stems can overlap each other, forming a net-like structure [41,42], it is only approximatively equal to the stem diameter. Secondly, the parameter $C_D$ considers all the effects that contribute to the overall dissipation...
process, so a single contribution cannot be distinguished, e.g., the extended wake zone within the stems’ array [50–52] and stem flexibility [53].

In order to improve the correlation between the measured and predicted $C_D$ values, Mendez and Losada [26] suggest replacing $KC$ in Equation (13) with a modified Keulegan–Carpenter number, i.e., $Q_{KC} = KC / (l_s/h)^{0.76}$, which accounts for the impact of submergence. Anderson and Smith [29] extended the same correction to Equation (12) by replacing $Re$ with $Q_{Re} = Re / (l_s/h)^{1.5}$. Close inspection of Figure 7 shows that both these corrections, applied to the present results, are ineffective.

In the present case, some improvement in the estimation of the drag coefficient is achieved by considering the impact of stem density, $n$. In Figure 8, the estimated drag coefficient, $C_D$, is distinguished for each class of relative stem density, $nd^2$, and, for each density, the experimental data are fitted by Equation (10). The relatively high values of the coefficients of determination ($R^2 > 0.90$) confirm the overall significant improvement. This result proves that the drag experienced by each single stem reduces with increasing dimensionless density $nd^2$, i.e., with increasing $n$ in the present experiments. This causes the coefficient $K_v$ to increase less than linearly, as noted above (see Figure 6).

![Figure 7](image-url)

**Figure 7.** Drag coefficient, $C_D$, versus Reynolds number, $Re$, (panel (a)) and Keulegan–Carpenter number, $KC$, (panel (b)). The solid black line represents the regression of experimental data (circles) according to Equation (10).
Figure 8. Predicted drag coefficient, $C_D$, versus Reynolds number, $Re$, (panel (a)) and Keulegan–Carpenter number, $KC$, (panel (b)) for the four stem densities. The table in the insets gives the coefficients $\alpha$ and $\beta$ to be used in Equation (10).

It is worth noting that the exponent $\beta$ slightly varies with $n d^2$, since it ranges between 0.79 and 0.86 for $C_D = C_D(Re)$ and between 0.71 and 0.81 for $C_D = C_D(KC)$. On the contrary, the coefficient $\alpha$ significantly reduces when $n d^2$ increases (see the coefficient values reported in Figure 8). By forcing $\beta_i$ to be constant, the following empirical formulas are found:

$$C_D = \frac{12.0}{\sqrt{n d^2}} Re^{-0.80}$$

$$C_D = \frac{4.0}{\sqrt{n d^2}} KC^{-0.80}$$

Figure 9 shows the comparison between the measured drag coefficient and that computed by Equation (14) (panel a) and Equation (15) (panel b). The data are well arranged along the line of perfect agreement, demonstrating that the proposed formulas can explain the measured values well.

Figure 9. Predicted versus experimental drag coefficient, $C_D$: given by Equation (14) (panel (a)) and by Equation (15) (panel (b)). Solid black line indicates perfect agreement between the data and the empirical formulas.
A relevant observation is that the stem drag coefficient in the present experiments is much smaller than the drag coefficient for an isolated cylinder under uniform flow conditions (by approximately one order of magnitude). This is not a new result (see, e.g., [54]), but the reasons for these small $C_D$s are not yet well understood. The observed large drag reduction can be ascribed to either wave flow unsteadiness and/or the relatively high stem density, as observed above, so that wakes interaction dramatically affects $C_D$ values [54].

To investigate this circumstance in more depth, we use the results of the experiments performed with uniform flow conditions.

Figure 10 shows the drag coefficient estimated with Equation (11), as it varies with the dimensionless density $n_d^2$. The drag coefficient $C_D$ of a smooth isolated cylinder is affected by the wake structure, and depends only on $Re$, according to many empirical expressions [55]. For the case of a cylinder array, the downstream elements experience lower impact velocity due to the velocity reduction in the wake of the upstream cylinders; hence, the drag coefficient also depends on cylinder spacing and arrangement. Consequently, the downstream cylinders experience reduced drag. This sheltering effect occurs when the average spacing of the cylinders in the array is relatively small [44]. Consistently, Nepf [25] observed that the bulk drag coefficient remains approximately constant up to values of dimensionless density $n_d^2 \cong 0.01$ and then decreases with increasing array density for both random and staggered arrangements; for $n_d^2 = 0.1 - 0.5$, the measured drag coefficient scatters in the range $C_D = 0.06 - 0.6$. Consequently the present values of $C_D$ are consistent with Nepf’s findings. In our UF experiment, values of $C_D$ are quite invariant with $n_d^2$. However, independently of the stem submergence, $C_D$ is at a minimum for $n_d^2 = 0.075$; this may be due to a slight canalization of the flow promoted by the in-line arrangement of the plants (see Figure 4b). Also, the submergence ratio seems to slightly affect the $C_D$ values, perhaps because of the shape of the plants adopted in the tests: their stems gather together in a short basal tuft, thus showing a non-constant impact area along the vertical.

Based on the same artificial vegetation, the comparison between the experimental drag coefficients, one estimated in the presence of waves and the other in uniform flow conditions, could be interesting at this stage. In fact, information derived from both cases could be shared.

The inferred drag coefficients in uniform flow are 4–5 times smaller than the corresponding $C_D$s estimated in wave conditions at the same Reynolds number ($C_D \cong 0.4 - 1.2$ by Equation (14) for $n_d^2 = 0.04 - 0.3$ and $Re = 135$). The smaller $C_D$ values in uniform flow, as well as the dependency of $C_D$ values on stem density observed in wave conditions, can be ascribed to the hydrodynamic conditions, and, in particular, to the unsteadiness that prevents the wake zone from fully developing in the canopy.

How to relate the drag coefficients to each other in uniform and wave conditions is still an open question that demands specific investigations, the results of which would be useful for building an in-depth understanding of wave attenuation in wetlands, and hence in the controlling of coastal hydrodynamics.

![Figure 10. Experimental drag coefficient $C_D$ versus dimensionless density $n_d^2$. Dotted black line shows the drag coefficient predicted by Equation (14) for $Re = 135$ in oscillatory flow.](image-url)
4. Conclusions

The present work investigated the resistance to flow of flexible vegetation in waves and in uniform flow conditions. The experiments highlighted the role of stem density in the wave attenuation process; the drag experienced by each single stem is reduced as the density increases, while the overall resistance, and hence wave attenuation, increases when stem density increases. The stem sheltering effect is possibly why the measured drag coefficient, both under wave and uniform flow conditions, is smaller than the $C_D$ of an isolated cylinder. Interestingly, the drag coefficient measured under wave conditions has the same order of magnitude as that measured in uniform flow, for a comparable Reynolds number and stem density, although the latter turns out to be a little smaller. This circumstance suggests that it could be possible to share knowledge on the drag coefficient from one field to the other; however, this issue needs to be further investigated, possibly by mimicking the vegetation with rigid dowels, in order to reduce the number of degrees of freedom, such as the vegetation flexibility and the non-constant impact area along the vertical.

Both Reynolds ($Re$) and Keulegan–Carpenter (KC) numbers are found to suitably collapse the measured drag coefficient; the present experimental conditions were such that $Re$ and KC were substantially related to each other, thus preventing us from understanding which of the two non-dimensional numbers is best suited to describe the variability of the drag coefficient. This point also deserves further, specific investigation.

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Conflicts of Interest: The authors declare no conflict of interest.

References


52. Tanino, Y.; Nepf, H.M. Laboratory investigation of mean drag in a random array of rigid, emergent cylinders. *J. Hydraul. Eng.* **2008**, *134*, 34–41. [CrossRef]

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