Numerical Study of the Velocity Decay of Offset Jet in a Narrow and Deep Pool

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Abstract: The present study examines the configuration of an offset jet issuing into a narrow and deep pool. The standard $k-\varepsilon$ model with volume-of-fluid (VOF) method was used to simulate the offset jet for three exit offset ratios (OR = 1, 2 and 3), three expansion ratios (ER = 3, 4 and 4.8), and different jet exits (circular and rectangular). The results clearly show significant effects of the circumference of jet exits ($L_{\text{exit}}$) in the early region of flow development, and a fitted formula is presented to estimate the length of the potential core zone ($L_{\text{PC}}$). Analysis of the flow field for OR = 1 showed that the decay of cross-sectional streamwise maximum mean velocity ($U_m$) in the transition zone could be fitted by power law with the decay rate $n$ decreased from 1.768 to 1.197 as the ER increased, while the decay of $U_m$ for OR = 2 or 3 was observed accurately estimated by linear fit. Analysis of the flow field of circular offset jet showed that $U_m$ for OR = 2 decayed fastest due to the fact that the main flow could be spread evenly in floor-normal direction. For circular jets, the offset ratio and expansion ratio do not affect the spread of streamwise velocity in the early region of flow development. It was also observed that the absence of sudden expansion of offset jet is analogous to that of a plane offset jet, and the flow pattern is different.

Keywords: offset jet; potential core; decay rate; $k-\varepsilon$ model

1. Introduction

Offset jets are common in drainage systems [1], slot fishways [2], and hydraulics engineering [3]. The offset jet is formed when a fluid jet discharges into an ambient medium above the floor and parallel to the axis of the jet exit but which is offset by a certain height. The submerged offset jets in the narrow and deep pool are more complex flow because it can easily be affected by side walls.

The offset jet flow was widely used as energy dissipation downstream of hydraulic structures—for example, the submerged hydraulic jump at an abrupt drop could be considered as an offset jet flow. From an engineering point-of-view, the length of the stilling basin should be as short as possible. The focus of this paper is to find the factors affect the efficiency of energy dissipation of the offset jet flow. Figure 1 shows a sketch of the submerged offset jet in a pool. The jet is mainly divided into three regions according to the relationship with the floor, viz., recirculation region, impingement region, and wall jet region. The Cartesian coordinate system is used with $x$, $y$, and $z$ representing the streamwise, lateral direction, and floor-normal direction, respectively. The exit of the jet is at $x = 0$, and the symmetry plane is at $y = 0$, the pool bottom is at $z = 0$. The symbols $L_x$, $L_y$, $L_z$, $S$, $d$, $h_t$, $U_j$, and $U_m$ represent the length, width, and height of jet pool, offset height, the diameter of jet exit, depth of tailwater, bulk velocity, and cross-sectional streamwise maximum mean velocity, respectively. Likewise, if the jet exit is rectangular, $a_0$, $b_0$ represents the height and width of the rectangle, respectively. The flow field in jet pool can be divided into three zones by the decay of $U_m$: (a) the potential core zone, where $U_m$ was equal to the jet exit velocity, $U_j$; (b) transition zone, where the
decay of $U_m$ was rapidly in this zone; and (c) fully development zone, where the decay of $U_m$ became very slow.

![Figure 1](image_url)

**Figure 1.** the sketch of the submerged offset jet in a chamber. Flow divided by a relationship with bottom floor: (1) recirculation region, (2) impingement region, and (3) wall jet region.

The recent studies on submerged offset jets were carried out by Subhasish Dey [4] to investigate the vertical profiles of time-averaged velocity components, and Reynolds stresses in jet flows for offset ratios OR = 2.8–5.1, submergence ratio SR = 2.4–5.6, expansion ratio ER = 1, and jet Reynolds number $R_0 = 28,475–80,730$, where OR = $S/a_0$ (for circular jet exit $a_0 = d$), SR = $h_i/S$, ER = $L_y/b_0$, and $R_0 = (U_0a_0)/\nu$, $\nu$ is the coefficient of kinematic viscosity of water. They concluded important characteristic length of submerged offset jets, such as the length of the recirculation region and impingement region, are expressed as a function of the $R_0$, OR, and SR. In another attempt, Bhuiyan [5] analyzed the characteristics of submerged turbulent plane offset jets (OR = 0.5–3.6) in channels with rough beds and shallow tailwater depths. The results indicated that for an offset height larger than the jet thickness, the peak velocity, the flow momentum decay faster in the downstream direction in an offset jet than in a turbulent plane wall jet. Durand et al. [6] studied the effect of Reynolds number on 3D offset jets both experimentally and numerically for $R_0 = 34,000$, 53,000 and 86,000. The results indicated the floor-normal location of maximum mean velocity and jet spread to be independent of Reynolds number. The investigated by Nyantekyi-Kwakye [7] on a 3D rectangular offset jet, performed at three offset ratios (OR = 0, 2, and 4) and revealed that large-scale structures dominate the inner layer of the wall jet region. For 3D circular offset jets (with OR ranging from 0–3.5), Agelin-chaab and Tachie [8] using a planar particle image velocimetry (PIV) system conducted the experiments to study the velocity. They observed that OR influenced both the decay of $U_m$ and growth of the shear layer within the developing region. Besides, there have been other experimental studies on 3D offset jets [9–11].

Given the brief overview, it can be concluded that the mechanics of offset jet has been studied extensively. However, the hydraulic properties of submerged offset jets in a narrow and deep pool have not been completely understood, although it was widely used as an efficient energy dissipator in hydraulic engineering located in narrow canyons.

This paper addresses the decay of velocity of offset jets in the narrow and deep pool with various offset ratios, expansion ratios and jet exit shapes, through numerical simulations using a 3D computational fluid dynamics (CFD) model with the $k$-$\varepsilon$ turbulence model coupled with VOF method, which was confirmed perform well in jet flow [10,12–17].
2. Numerical Simulation

2.1. Mathematical Model

An RNG $k$-$\varepsilon$ model has been compared to a standard $k$-$\varepsilon$ model for computing transient jets by Abraham and Maji [18] and concluded that the RNG $k$-$\varepsilon$ model results in predictions of greater mixing in the jets relative to the standard model. The study carried by Nasr and Lai [19] indicated that the standard $k$-$\varepsilon$ turbulence model predicts better than RNG $k$-$\varepsilon$ and Reynolds stress turbulence model.

In this study, the standard $k$-$\varepsilon$ model [20] was used as the turbulence closure

\[ \frac{\partial (\rho k)}{\partial t} + \frac{\partial (\rho u_i k)}{\partial x_i} = \frac{\partial}{\partial x_i} \left[ \left( \mu + \frac{\mu_t}{\sigma_k} \right) \frac{\partial k}{\partial x_i} \right] + G_k - \rho \varepsilon \]  

(1)

\[ \frac{\partial (\rho \varepsilon)}{\partial t} + \frac{\partial (\rho u_i \varepsilon)}{\partial x_i} = \frac{\partial}{\partial x_i} \left[ \left( \mu + \frac{\mu_t}{\sigma_\varepsilon} \right) \frac{\partial \varepsilon}{\partial x_i} \right] + C_{1_\varepsilon} \frac{\varepsilon}{k} G_k - C_{2_\varepsilon} \rho \varepsilon^2 \]  

(2)

where $\rho$ is the density of mixture; $t$ is time; $k$ is turbulent kinetic energy; $\mu$ is the dynamic viscosity of fluid; $u_i$ is component of velocity in the $x_i$ direction; $\varepsilon$ is turbulent energy dissipation rate; $\mu_t$ is dynamic turbulent viscosity; $\sigma_k$, $\sigma_\varepsilon$ is turbulent Prandtl number for $k$ and $\varepsilon$, respectively; $G_k$ is generation of turbulent kinetic energy due to mean velocity gradients; and $\mu_t$ and $G_k$ can be determined as

\[ \mu_t = \rho C_\mu \frac{k^2}{\varepsilon} \]  

(3)

\[ G_k = \mu_t \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \frac{\partial u_i}{\partial x_j} \]  

(4)

The values of the empirical constants in the turbulence model are $C_\mu = 0.09$, $\sigma_k = 1.0$, $\sigma_\varepsilon = 1.3$, $C_{1_\varepsilon} = 1.44$, and $C_{2_\varepsilon} = 1.92$.

For this study, the volume-of-fluid (VOF) method was used as the two-phase flow model to track the water surface in the domain. The VOF method is widely used to determine the position of the interface of two or more immiscible flows [21,22]. Air and water were the primary and secondary phases, respectively. In the calculation, all fluids share the turbulence model. For air-water two-phase flow, $\alpha_a$ and $\alpha_w$ are the volume fraction of air and water, respectively. For each control cell,

\[ \alpha_w + \alpha_a = 1 \]  

(5)

If the cell contains only air, the value of $\alpha_w = 0$; if the cell is full of water, the value of $\alpha_w = 1$; and if the interface cuts the cell, then $0 < \alpha_w < 1$. The volume fraction of water, $\alpha_w$, is calculated from [23]

\[ \frac{\partial \alpha_w}{\partial t} + V \cdot \nabla \alpha_w = 0 \]  

(6)

where the $V$ is the fluid velocity. The fluid properties, such as density $\rho$ and molecular viscosity $\mu$, are adjusted according to the volume fraction. It should be noted that other numerical methods can also be used to study the detailed flow properties in complex contexts [24–29], the choice of numerical methods depends on the research focus.

2.2. Simulation Setup

ANSYS ICEM 16.0 (ANSYS®, Canonsburg, PA, USA) was utilized to develop the numerical models for 13 types of offset jet. Hexahedral grids were used throughout the computational domain. The grid meshing is shown in Figure 2. A Cartesian coordinate system is used so that the origin is at the center of the intersection of the offset wall and floor. The computational domain consists of the pipe and jet pool. The jet is discharged from offset wall offset by a height $S$ above the floor.
The total pipe length is 1 m, and the type of pipe can be divided into the circular pipe and rectangular pipe. The length, $L_x$, and height, $L_y$, of the pool are 8 m and 0.8 m, respectively. For the circular pipe, the offset ratio (OR) varied from 1 to 3, the expansion ratio (ER) varied from 3 to 4.8 as the width of the jet pool increased from 0.3 m to 0.48 m. For the rectangular pipe, the aspect ratio (AR) of the exit varied from 0.33 to 11.46. Moreover, the area of exit remains constant for all shape of exits. The parameters of all cases are given in Table 1, and the jet exits and the offset wall are shown in Figure 3.
2.3. Initial Conditions and Boundary Conditions

All the variables except at boundaries (such as $u_i$, $P$, $k$, and $\varepsilon$) are initialized at zero. The computed data are stored at every alternate time step for post-processing. All computations are conducted on an Inter core i7 3.60 GHz Windows machine.

The boundary conditions were set as follows.

- **Inflow boundary**: the inlet was treated as an inlet velocity boundary with the velocity was set as 5 m/s.
- **Outflow boundary**: pressure outlet boundary was selected at the outlet, the depth of tailwater was fixed at 0.55 m with the help of user-defined function (UDF).
- **Free surface**: pressure inlet was employed, and its value was the standard atmospheric pressure, the operating pressure and density were selected as 101,325 Pa and 1.225 kg/m$^3$, respectively.
- **Wall boundary**: for the parameters investigated in this study, the data near the wall was ineffective. No slip boundary condition is considered for velocity. To avoid the fine mesh required to resolve the viscous sub-layer near the boundary, so standard wall function method has been used.

2.4. Numerical Discretizations

ANSYS Fluent 16.0 (ANSYS®, Canonsburg, PA, USA) was utilized to perform the simulation. The governing equations are discretized using the implicit Finite Volume Method (FVM). The SIMPLE algorithm, using a relationship between velocity and pressure corrections to enforce mass conservation and to obtain the pressure field, was applied to couple the velocity and pressure. The least-squares cell-based method was used to calculate the gradient. PRESTO! was used to discretize the pressure and Geo-Reconstruct was used for the volume fraction. The second-order upwind scheme was used for the momentum and the first-order upwind for the turbulent kinetic energy and the dissipation rate with ANSYS Fluent’s default under relaxation values for all parameters. The time step was $\Delta t = 0.0001$–$0.001$ s and the iteration number was always less than 2.

The computational results are considered to be converged when the residual becomes smaller than 0.001 for all equations. Here, the residual is defined as the square root of the summation of the squares of the difference between right and lefts sides of the discretized equations for a single control volume [30]. The results analyzed and presented in this study were taken from the simulation when quasi-steady state was reached.

2.5. Grids Sensitivity and Model Validation

Grid independence was examined to ensure the reliability of the numerical simulation results. The Case C-O3-E5 was chosen to test mesh sensitivity. Three sets of grids had 1,065,575 (grid 1), 438,221...
(grid 2) and 181,036 (grid 3) cells, respectively. The grid convergence index (GCI) is widely used to estimate discretization uncertainty [31]. The GCI is given by

$$GCI = \frac{1.25|\varphi_3 - \varphi_2|/\varphi_3}{(h_2/h_3)^p - 1}$$

(7)

$$P = \frac{1}{\ln(h_2/h_3)} \left| \ln\left(1 - \frac{\varphi_1 - \varphi_3}{\varphi_2 - \varphi_3}\right) \right| + \ln\left|\frac{(h_2/h_3)^p - \sgn[(\varphi_2 - \varphi_3)/(\varphi_2 - \varphi_3)]}{(h_1/h_2)^p - \sgn[(\varphi_1 - \varphi_3)/(\varphi_2 - \varphi_3)]}\right|$$

(8)

where $\varphi_i$ is the solution on the $i$th grid and $h_i$ is the average grid size on the $i$th grid and $h_1 > h_2 > h_3$.

Figure 4 presents an axial velocity profile along the jet exit axis. In this figure, 80% out of 40 points exhibited oscillatory convergence. The maximum uncertainties in velocity were approximately 12.6%, which corresponds to a maximum uncertainty in velocity of about ±0.25 m/s. Considering the simulation accuracy and the computation efficiency, the final grid number in this study was taken as 438,221.

![Figure 4.](image-url)  
**Figure 4.** (a) Velocity profiles on jet exit axis with three grid sizes; (b) Results from grid 2, with discretization error bars computed using GCI.

To examine simulation accuracy, the physical model experiment of Case C-O3-E5 was performed at the State Key Laboratory of Hydraulics and Mountain River Engineering, Sichuan University, Chengdu. The experimental model is shown in Figure 5. It can be seen from Figure 6 that the calculated results of the height of water surface and velocity distribution were fairly consistent with that of laboratory tests. The results are indicating that the numerical simulation produced reliable and acceptable results.

![Figure 5.](image-url)  
**Figure 5.** Experiment model.
3. Results and Analysis

3.1. Velocity Attenuation

The attenuation of the jet flow in the narrow and deep pool was characterized using the decay of the cross-sectional maximum streamwise mean velocity \( U_m \). Previous studies indicated that \( U_m \) is constant within the potential core region, followed by a rapid decay with streamwise distance in transition zone \([32,33]\). The entrained ambient fluid gets momentum since the jet enters the pool, the section of jet flow continues to expand, and the velocity is decreasing as the results of the mixing of jet and ambient fluid. Figure 7a shows the distribution of \( U_m \) normalized by the jet exit velocity, \( U_j \). Normalized values of \( U_m \) were observed decayed sharply within the region \( x/d > L_{PC} \) and the trend of decay of \( U_m \) varies greatly in the transition zone for different circular offset jet. It can be seen from Figure 7b that the length of the potential core zone \( (L_{PC}) \) varied from 5.0 to 5.5 with changes in ER, and a higher ER indicated a higher \( L_{PC} \).

As can be observed in Figure 7c–d, the \( L_{PC} \) varies greatly with AR of the rectangular jet exit due to the circumference of exit \( (l_{exit}) \) were changed. When \( l_{exit} \) increased, the \( L_{PC} \) decreased sharply, a fitting formula was used to estimate the relationship of \( L_{PC} \) and \( l_{exit} \) as indicated in Figure 7d, the empirical equation for \( L_{PC} \) was employed as \( L_{PC} = 2100e^{-2(l_{exit}/d)} + 0.5 \).

The decay of the \( U_m \) over distance \( x \) (scaled by \( d \)) for Case R-AR11 is shown in Figure 7c. The most striking feature of Case R-AR11 is that there is no sudden expansion (ER = 1). Thus, the Case R-AR11 is analogous to that of a plane offset jet. The decay of \( U_m \) in the recirculation region is quite sharp, the \( U_m \) drops to a local minimum value due to an increase in pressure resulting from the jet impingement after the reattachment of the jet. The decay of \( U_m \) is rather gradual in the wall jet region. A similar observation was reported by Gu [16] and Dey [4].
The $U_m/U_j$ decay profiles can be grouped based on their characteristics. The power law of the form $U_m/U_j = C(x/d)^{-n}$ is typically used to describe the velocity decay in the transition zone [6,32,34,35], where $C$ and $n$ are a proportionality symbol and decay rate, respectively. The decay rate indicated the extent of entrainment and boundary effects on the jet. Figure 8 shows the variation of $U_m/U_j$ for all cases with the normalized longitudinal coordinate $x/d$ within the transition zone. Rajaratman reported $n = 0.5$ for a plane free jet by considering simplified conservation laws and entrainment hypotheses [36]. The wall jet was observed to be accurately estimated by using the power law. However, the distribution of $U_m/U_j$ for the offset jets are not accurately described by the power law, which should be replaced by a linear fit [32].

For circular offset jet, using the power law fit, the decay rate for the lower offset ratio (OR = 1) circular jet was observed to be accurately estimated with the decay rate $n$ varies from 1.197 to 1.768 as shown in Figure 8a. As can be seen in Figure 8b–c, the distributions of $U_m/U_j$, for the higher offset ratio (OR = 2 or 3) circular jet are not accurately described by the power law. Therefore, a linear fit was used to estimate the decay rates for higher offset ratio jet, the slope $\kappa$ the linear equation was considered as the decay rate. Decay rate $\kappa$ values of 0.110, 0.096 and 0.090 with $R^2$ above 0.94 were obtained for ER = 3, 4 and 4.8, respectively, when OR = 2. Decay rate values of 0.081, 0.048 and 0.049 with $R^2$ above 0.968 were obtained for ER = 3, 4 and 4.8, respectively, when OR = 3. Above analysis and as shown in Figure 8a–c indicated that when the offset ratio is moderate (OR = 2) produces a faster decay than that of higher or lower offset ratio (OR = 1 or 3). The reason is that two circulating vortices were developed below and above jet, respectively. The circulating vortices develop reverse flows against the inflow-jet direction. Negative momentum of the reverse flows reduced the inflow momentum slowing the jet rapidly down.
The decay rates for the various circular jet cases are reported in Table 2. The decay rate value is the largest as the expansion ratio (ER) is 3. There is a stronger jet interaction with the ambient fluid due to the more confined environment.

For rectangular offset jet, the $U_m/U_j$ for $1 \leq \text{AR} \leq 3$ is expressed well by power law form with the decay rate $n$ varies from 1.068 to 1.228 (Table 3), and the $U_m$ decay in transition zone does not show substantial differences (Figure 8d). Therefore, it appears reasonable to assume the effect of the aspect ratio of the rectangular jet on the mainstream attenuation is mainly to influence the length of the potential core zone.
The algorithm for calculating the length of the potential core \( L_{PC} \) and decay profiles in the transition zone could be used to roughly calculate the length of the energy dissipation region \( L_{ED} \). For example, a square offset jet is issued to a pool. The side length of the square is 2.67 m (equivalent diameter is 3 m), the offset height is 3 m, the width of the pool is 12 m, and the height of tail water is 16.5 m. If the \( U/U_m = 0.2 \) as the end of the length of the energy dissipation region, the distance \( U/U_m \) decreases from 1 to 0.2 is called \( L_{tr} \). The \( L_{PC} \) can be described by:

\[
L_{ED} = L_{PC} + L_{tr}
\]

The \( L_{PC} = 6.60 \) m calculated by \( L_{PC} / d = 2100e^{-2(x_{exit}/d)} + 0.5 \). The \( L_{tr} = 39.53 \) m calculated by \( 0.2 = -0.096(x/d) + 1.465 \). As the result, the length of energy dissipation region is 43.13 m.

3.2. Vertical Velocity Spread

Figure 9 shows the flow field of the offset jet with different offset ratios. There is a large range of vortices formed near the jet flow, the location and size of the vortex on the streamwise section have notable differences. When OR = 1, in the range of \( x/d = 0–25 \), a large vortex was formed above the jet flow; When OR = 3, in the range of \( x/d = 0–25 \), a large vortex was formed below the jet flow. However, there is a smaller vortex above and below the jet flow in the range of \( x/d = 0–15 \).

<table>
<thead>
<tr>
<th>Decay Rate</th>
<th>( n ) (OR = 1)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fit Equation</td>
<td>Power Law</td>
</tr>
<tr>
<td>AR = 1</td>
<td>1.227</td>
</tr>
<tr>
<td>AR = 2</td>
<td>1.229</td>
</tr>
<tr>
<td>AR = 3</td>
<td>1.068</td>
</tr>
</tbody>
</table>

Table 3. The decay rate of the rectangular jet.

Figure 9. Velocity vectors of offset jet with different offset ratio: (a) OR = 1 (C-O1-E4); (b) OR = 2 (C-O2-E4); (c) OR = 3 (C-O3-E4).
Profiles of the streamwise mean velocities ($U$) extracted at $x/d = 1, 4, 9, 13$ and 17 are shown in Figure 10. It may be noted that to cover a range of ER = 4, Cases C-O1-E4, C-O2-E4, and C-O3-E4 were selected; otherwise, using the data of all Cases would make the plots clumsy. The velocity and length scale used was $U_m$ and $d$, respectively. Here, $z_c$ is the distance from the center of exit to the floor, that is, $z - z_c = 0$, where is the axis of the jet exits. Vertical profiles of $U$ are shown in Figure 10a for ER is 4. The effect of offset ratio (OR) on the vertical velocity spread was not evident within the region $x/d < 9$. It can be noted that the velocity distribution in the floor-normal direction conforms with the Gaussian distribution within the region of $5 \leq x/d \leq 9$. However, as the jet travels away from the jet exits ($x/d > 9$), the data of jets at different offset height are no longer overlapped. The location of the maximum of $U/U_m$ for OR = 2 is almost at the axis of the jet exits. The location of the maximum of $U/U_m$ is above and below the axis of the jet exits for OR = 3 and OR = 1, respectively. The results reveal offset height changes travel direction of the bulk of the jet.

Figure 10. Streamwise mean velocity distribution in symmetry ($x$–$z$) plane: (a) circular offset jets (ER = 4); (b) rectangular offset jets.

Figure 10b shows the development of the $U$ of the offset jet with rectangular exits. The results demonstrate that the bulk of the jet turns travel direction and then attaches to the floor within the region of $x/d < 13$. Further, the figure shows the spread rate of $U$ is larger as the aspect ratio increases, and the flow direction for AR = 3 was changed at $x/d = 17$.

The $U$ distribution in floor-normal direction in Case R-AR11 is different from those in other cases, the difference can be attributed to the jet exit of Case R-AR11 without sudden expand (ER = 1), there is an obviously lower pressure zone below the jet at the jet exit, then the main jet bends to the floor in short distance ($x/d < 2.5$). Thus, the profile is close to that of a wall jet.

Figure 11 shows contours of $U/U_m$ in the symmetry plane for the offset jets, and the lower and upper lines represent the loci of $z_{0.5}$ ($U = 0.5 \ U_m$, the inner separation line), and $z_{0.5}$ ($U = 0.5 \ U_m$, the outer separation line), respectively.
the outer separation line), respectively. The jet between $z_{0.5}^-$ and $z_{0.5}^+$ was considered as the main flow in the present paper. The $L_{20.5}^-$ is the distance from the exit to where the $z_{0.5}^-$ reaches the floor, and $L_{20.5}^+$ is the distance from the exit to where the $z_{0.5}^+$ reaches the water surface. For circular exits, the main flow for $OR = 1$ bends to the floor at $x/d = 12$ ($L_{20.5}^- < 12$ and $L_{20.5}^+ > 46$), then the flow spreads from floor to water surface (Figure 11a). The main flow for $OR = 2$ spreads evenly in the floor-normal direction at $x/d > 20$, the values of $L_{20.5}^-$ and $L_{20.5}^+$ are roughly equivalent (Figure 11b). Furthermore, the main flow for $OR = 3$ bends to the water surface, with the $L_{20.5}^- < 20$ and $L_{20.5}^+ > 42$, which means the flow in the pool is spreading from water surface to floor (Figure 11c). For rectangular exits (Figure 11d), the main flow for $AR = 1$ is identical to that of a circular jet. The main flow for $AR = 2$ spreads from floor to water surface. The main flow for $AR = 3$ bends sharply to water surface as the jet enters the pool, the reason is that jet is too thin to effectively maintain a stable flow pattern. As the expansion ratio increases to 11.48, the spread range of the main flow in floor-normal direction is small, and the high velocity region is close to the floor.

![Image of contour plots](https://example.com/contour_plots)

**Figure 11.** Contour of $U/U_m$ in symmetry ($x-z$) plane: (a) circular offset jets ($ER = 3$); (b) circular offset jets ($ER = 4$); (c) circular offset jets ($ER = 4.8$); (d) rectangular offset jets.

### 3.3. Lateral Velocity Spread

As observed in Figure 12, there is a negligible effect of the expansion ratio on the lateral velocity spread within the region $x/d < 9$. This observation reveals that the profiles of $U$ were independent
of the expansion ratios, the Gaussian distribution is overlapped on the present data plots within the region $5 \leq x/d \leq 9$. The results indicated that the offset height did not greatly alter the flow within early development regions of the offset jet. However, at $x/d = 13$ and $x/d = 17$, $U/U_m$ are lower for the expansion ratios, ER, are lower within the region $y/d > 0.5$. Figure 10 indicates that a more confining enclosure enhances the diffusion of the velocity than a less confining condition. The velocity profiles in the $x$-$y$ plane of the jet with rectangular exits are not obtained. The flow patterns are not stable as the expansion ratio was changed [37].

![Figure 12. Profiles of $U/U_m$ in (x–y) plane of circular jet.](image)

4. Conclusions

The present investigation sought to elucidate the velocity development of a submerged 3D offset jet flow occurred in the narrow and deep pool using the standard $k$-$\varepsilon$ model with VOF method. The flow field was studied for different offset ratio, expansion ratio, and jet exits. The numerical results showed that the solid boundaries of the narrow pool produce circulation in the surrounding fluid opposite the jet flow, which produces a rapid jet decay. The following conclusions can be drawn:

1. The development of the jet within the potential core zone was observed to be dependent on the circumference of jet exits. It was noted that the length of the potential core zone decreases with the circumference of exit.
2. The results showed that the development of the $U_m$ in the transition zone could be divided into two modes. That is, (a) the decay of $U_m$ could be estimated from power law fit with a decay rate $n$ of 1.089–1.451 as the offset ratio is lower (OR = 1). (b) A linear fit was used to estimate the decay rates for higher offset ratio jet (OR = 2 or 3). It was observed that $U_m$ decay is the fastest as the offset ratio (OR) is 2. Further, the results indicate that a more confining enclosure produces a more rapid jet decay than a less confining condition.
3. The spread rate of the circular jet is not affected by the expansion ratios and offset ratio in the early region of jet decay. The main flow for OR = 2 was traveled straightly, and the main flow was toward the floor and the water surface as the OR = 1 and OR = 3, respectively.
4. The absence of the sudden expansion coupled with the high aspect ratio of the exit contributed to form a unique flow pattern compared with other cases.

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**Conflicts of Interest:** The authors declare no conflict of interest.
Abbreviations

- $x$: Stream wise direction
- $y$: Lateral direction
- $z$: Floor direction
- $L_x$: Length of the jet pool in the streamwise direction (m)
- $L_y$: The width of the jet pool in the lateral direction (m)
- $L_z$: The height of the jet pool in the floor-normal direction (m)
- $d$: The diameter of circular jet exit (m) or equivalent diameter of rectangular exit (m)
- $a_0$: The height of the rectangular exit (m)
- $b_0$: Width of rectangular exit (m)
- $h_t$: The height of tailwater (m)
- $S$: Offset height of jet exit (m)
- $U$: Mean velocity in streamwise (m/s)
- $U_m$: Cross-Sectional streamwise maximum mean velocity (m/s)
- $U_j$: Velocity in jet exit (m/s)
- $L_{PC}$: Length of potential core
- $L_{exit}$: The circumference of jet exit
- $z_c$: Distance from center of exit to floor, $z_c = S + 0.5d$ or $z_c = S + 0.5a_0$
- $z_{0.5}^+$: The loci of where $U = 0.5 U_m$ above the jet
- $z_{0.5}^-$: The loci of where $U = 0.5 U_m$ below the jet
- $L_{z_{0.5}}^+$: Distance from the exit to where the $z_{0.5}$ reaches floor
- $L_{z_{0.5}}^-$: Distance from the exit to where the $z_{0.5}$ reaches water surface
- $n$: Decay rate used in power law
- $\kappa$: Decay rate used in the linear fit
- $R_0$: Reynolds number
- OR: Offset ratio of jet exit ($S/d$ or $S/a_0$)
- ER: The expansion ratio of jet exit ($L_y/d$ or $L_y/b_0$)
- AR: Aspect ratio of jet exit ($b_0/a_0$)

References


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